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SPECIFICATIONS FOR A GOOD ENGINEER.

"A good engineer must be of inflexible integrity, sober, truthful, accurate, resolute, discreet, of cool and sound judgment, must have command of his temper, must have courage to resist and repel attempts at intimidation, a firmness that is proof against solicitation, flattery or improper bias of any kind, must take an interest in his work, must be energetic, quick to decide, prompt to act, must be fair and impartial as a judge on the bench, must have experience in his work and in dealing with men, which implies some maturity of years, must have business habits and knowledge of accounts. Men who combine these qualities are not to be picked up every day. Still they can be found. But they are greatly in demand, and when found, they are worth their price; rather they are beyond price, and their value can not be estimated by dollars."-Chief Engineer Starling's Report to the Mississippi Levee Commissioners.

"Be sure you are right, and then go ahead."-D. Crockett.

CHAPTER I.

GENERAL INSTRUCTIONS.

FIELD WORK.

Habitual Correctness.—Habitual correctness is a duty. Error should be looked upon as *probable*, and every precaution taken to verify data and results. Unchecked work may always be regarded as doubtful. A discrepancy which is found by the maker in time to be corrected by him before any damage is done is not necessarily discreditable, provided the error is not repeated. However, *habitual error* is not only discreditable but dishonorable as well, and nothing except intentional dishonesty injures the reputation of the engineer more quickly or permanently.

Consistent Accuracy.—The degree of precision sought in the field measurements should be governed strictly by the dictates of common sense and experience. Due consideration of the purposes of the survey and of the time available will enable one to avoid extreme precision when ordinary care would suffice, or crudeness when exactness is required, or inconsistency between the degrees of precision observed in the several parts of the survey. It is a very common practice of beginners, and of many experienced engineers as well, to carry calculated results far beyond the consistent exactness.

Speed.—Cultivate the habit of doing the field work quickly as well as accurately. True skill involves both quantity and quality of results. However, while the habit of rapid work can and should be acquired, the speed attempted in any given problem should never be such as to cast doubt upon the results. Slowness due to laziness is intolerable.

Familiarity with Instructions.—The instructions for the day's work should be read over carefully, and preliminary steps, such as the preparation of field note forms, should be taken so as to save time and make the work in the field as effective as possible The ability and also the desire to understand and obey instructions are as essential as the skill to execute them.

Inferior Instruments.—Should a poor instrument or other equipment be assigned, a special effort should be made to secure excellent results. In actual practice, beginners often have to work with defective instruments, but they should never seek, nor are they permitted, to justify poor results by the character of the field equipment. The student should therefore welcome an occasional opportunity to secure practice with poor instruments.

Alternation of Duties.—The members of each party should alternate in discharging the several kinds of service involved in the field problems, unless otherwise instructed. Training in the subordinate positions is essential whether the beginner is to occupy them in actual practice or not, for intelligent direction of work demands thorough knowledge of all its details.

Field Practice Decorum.—The decorum of surveying field practice should conform reasonably to that observed in other laboratory work.

THE CARE OF FIELD EQUIPMENT.

RESPONSIBILITY.—The student is responsible for the proper use and safe return of all equipment. All cases of breakage, damage, loss or misplacement must be reported promptly. The equipment should be examined when assigned and a report made at once of any injury or deficiency found, so that responsibility may be properly fixed.

PRECAUTIONS.—Careful attention to the following practical suggestions will save needless wear to the equipment and reduce the danger of accidents to a minimum, besides adding to the quality and speed of the work.

Tripod.—Inspect the tripod legs and shoes. The leg is of the proper tightness if, when lifted to an elevated position, it sinks gradually of its own weight. The tripod shoes should be tight and have reasonably sharp points.

Setting Up Indoors.—In setting up the instrument indoors press the tripod shoes firmly into the floor, preferably with each point in a crack. Avoid disturbing other instruments in the room.

Instrument Case.—Handle the instrument gently in removing it from and returning it to the case. It is always best to place the hands beneath the leveling base in handling the detached instrument. Considerable patience is sometimes required to close the lid after returning the instrument; if properly placed the lid closes freely.

Mounting the Instrument.—See that the instrument is securely attached to the tripod before shouldering it. Undue haste in this particular sometimes results in costly accidents. When screwing the instrument on the tripod head, it should be turned in a reverse direction until a slight jar is felt, indicating that the threads are properly eugaged.

Sunshade.—Always attach the sunshade regardless of the kind of weather. The sunshade is a part of the telescope tube and the adjustment of a delicate instrument may sometimes be affected by its absence. In attaching or removing the sunshade or object glass cap, always hold the telescope tube firmly with one hand and with the other twist the shade or cap to the right to avoid unscrewing the object glass cell.

Carrying the Instrument.—Do not carry the instrument on the shoulder in passing through doors or in climbing fences. Before shouldering the instrument, the principal motions should be slightly clamped; with the transit, clamp the telescope on the line of centers; and with the level, when the telescope is hanging down. In passing through timber with low branches, give special attention to the instrument. Before climbing a fence, set the instrument on the opposite side with tripod legs well spread.

Setting Up in the Field.—When setting up in the field, bring the tripod legs to a firm bearing with the plates approximately level. Give the tripod legs additional spread in windy weather or in places where the instrument may be subject to vibration or other disturbance. On side-hill work place one leg up hill. With the level, place two tripod shoes in the general direction of the line of levels.

Exposure of Instrument.—Do not expose the instrument to rain or dampness. In threatening weather the water proof bag should be taken to the field. Should the instrument get wet, wipe it thoroughly dry before returning it to the case. Protect the instrument from dust and dirt, and avoid undue exposure to the burning action of the sun. Avoid subjecting it to sudden changes of temperature. In cold weather when bringing an instrument indoors cover the instrument with the hag or return it to the case immediately to protect the lenses and graduations from condensed moisture. Guarding the Instrument.—Never leave an instrument unguarded in exposed situations such as in pastures, near driveways, or where blasting is in progress. Never leave an instrument standing on its tripod over night in a room.

Manipulation of Instrument.—Cultivate from the very beginning the habit of delicate manipulation of the instrument. Many parts, when once impaired, can never he restored to their original condition. Rough and careless treatment of field instruments is characteristic of the unskilled observer. Should any screw or other part of the instrument work harshly, call immediate attention to it so that repairs may be made. Delay in such matters is very destructive to the instrument.

Foot Screws.—In leveling the instrument, the foot screws should be brought just to a snug bearing. If the screws are too loose, the instrument rocks, and accurate work can not be done; if too tight, the instrument is damaged, and the delicacy and accuracy of the observations are reduced. Much needless wear of the foot screws may be avoided if the plates are brought about level when the instrument is set up. With the level, a pair of foot screws should be shifted to the general direction of the back or fore sight before leveling up.

Eyepiece.—Before beginning the observations, focus the eyepiece perfectly on the cross-hairs. This is best done by holding the note book page, handkerchief, or other white object a foot or so in front of the object glass so as to illuminate the hairs; and then, by means of the eyepiece slide, focus the microscope on a speck of dust on the cross-hairs near the middle of the field. To have the focusing true for natural vision, the eye should be momentarily closed several times between observations in order to allow the lenses of the eye to assume their normal condition. The omission of this precaution strains the eye and is quite certain to cause parallax. After the eyepiece is focused on the cross-hairs, test for parallax by sighting at a well defined object and observing whether the cross-hairs seem to move as the eye is shifted slightly.

Clamps.—Do not overstrain the clamps. In a well designed instrument the ears of the clamp screw are purposely made small to prevent such abuse. Find by experiment just how tight to clamp the instrument in order to prevent slipping, and then clamp accordingly.

Tangent Screws.—Use the tangent screws for slight motions only. To secure even wear the screws should be used equally in all parts of their length. The use of the wrong tangent movement is a fruitful source of error with beginners.

Adjusting Screws.—Unless the instrument is assigned expressly for adjustment, do not disturb the adjusting screws.

Magnetic Needle.—Always lift the needle before shouldering the instrument. Do not permit tampering with the needle. If possible, avoid subjecting the needle to magnetic influence, such as may exist on a trolley car. Should the needle become reversed in its polarity or require remagnetization, it may be removed from the instrument and brought into the magnetic field of a dynamo or electric motor for several minutes, the needle being jarred slightly during the exposure; or a good horseshoe magnet may he used for the same purpose. The wire coil counterbalance on the needle will usually require shifting after the foregoing process.

Lenses.—Do not remove or rub the lenses of the telescope. Should it be *absolutely necessary* to clean a lens, use a very soft rag with caution to avoid scratching or marring the polished surface. Protect the lenses from flying sand and dust, which in time seriously affect the definition of the telescope.

Plumb Bob.—Do not abuse the point of the plumb bob and avoid needless knots in the plumb bob string.

Cleaning Tripod Shoes.—Remove the surplus soil from the tripod shoes before bringing the instrument indoors.

Leveling Rods.—Leveling rods and stadia hoards should not be leaned against trees or placed where they may fall. Avoid injury to the clamps, target and graduations. Do not mark the graduations with pencil or otherwise. Avoid needless exposure of the rod to moisture or to the sun.

Flag Poles.—Flag poles should not be unduly strained and their points should be properly protected.

Chains and Tapes.—Chains should not be jerked. Avoid kinks in steel tapes, especially during cool weather. When near driveways, in crowded streets, etc., use special care to protect the tape. Band tapes will be done up in 5-foot loops, figure 8 form, unless reels are provided. Etched tapes should be wiped clean and dry at the end of the day's work.

Axes and Hatchets.—Axes and hatchets will be employed for their legitimate purposes only. Their wanton use in clearing survey lines is forbidden, and their use at all. for such purpose, on private premises must be governed *strictly* by the rights of the owner.

Stakes.—The consumption of stakes should be controlled by reasonable cconomy, and surplus stakes returned to the general store. For the protection of mowing machines in meadows, etc., hub stakes should be driven flush with the surface of the ground, and other stakes should be left high enough to be visible. Whenever practicable, stakes which may endanger machines should be removed after serving the purpose for which they were set.

FIELD NOTES.

Scope of Field Notes.—The notes should be a complete record of each day's work in the field. In addition to the title of the problem and the record of the data observed, the field notes should include the date, weather, organization of party, equipment used, time devoted to the problem, and any other information which is at all likely to be of service in connection with the problem. No item properly belonging to the notes should be trusted to memory. Should the question arise as to the desirability of any item, it is always safe to include it. The habit of rigid self criticism of the field notes should be cultivated.

Character of Notes.—The field notes should have character and force. As a rule, the general character of the student's work can be judged with considerable certainty by the appearance of his field notes. A first-class page of field notes always commands respect, and tends to establish and stimulate confidence in the recorder. The notes should be arranged systematically.

Interpretation of Notes.—The field notes should have one and only one reasonable interpretation, and that the correct one. They should be perfectly legible and easily understood by anyone at all familiar with such matters.

Original Notes.—Each student must keep complete notes of each problem. Field notes must not be taken on loose slips or sheets of paper or in other note books, but the original record must be put in the prescribed field note book during the progress of the field work.

Field Note Book.—The field record must be kept in the prescribed field note book. For ease of identification the name of the owner will be printed in hold letters at the top of the front cover of the field note book. **Pencil.**—To insure permanency all notes will be kept with a hard pencil, preferably a 4H. The pencil should be kept well sharpened and used with sufficient pressure to indent the surface of the paper somewhat.

Title Page.—An appropriate title page will be printed on the first page of the field note book.

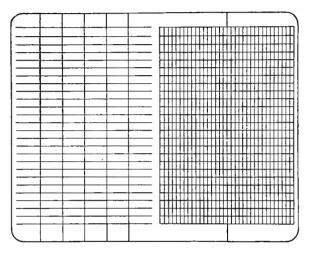
Indexing and Cross Referencing.—A systematic index of the field notes will be kept on the four pages following the title page. Related notes on different pages will be liberally and plainly cross referenced. The pages of the note book will be numbered to facilitate indexing.

Methods of Recording Field Notes.—There are three general methods of recording field notes, namely: (1) by sketch, (2) by description or narration, and (3) by tabulation. It is not uncommon to combine two or perhaps all three of these methods in the same problem or survey.

Form of Notes.—All field notes must be recorded in a field note book ruled as shown below, except where circumstances require modification. If no form is given, the student will devise one suited to the particular problem.

Lettering.-Field notes will be printed habitually in the "Engineering News" style of freehand lettering, as treated in Reinhardt's "Freehand Lettering." The body of the field notes will be recorded in the slanting letter and the headings will be made in the upright letter. The former slants to the right 1:2.5 and the so-called upright letter is made to slant to the left slightly, say 1:25. Lower case letters will be used in general, capitals being employed for initials and important words, as required. In the standard field note alphabet the height of lower case letters a, c, e, i, m, n, etc., is 340 inch, and the height of lower case b. d. f. g, h, etc., and of all capital letters and all numerals is 5_{40} (1/8) inch; lower case t is made four units (4/40) inch high. This standard accords with best current practice and is based upon correct economic principles. Sample pages of field notes with letters and figures drawn full size are given on page 9. The student is expected to make the most of this opportunity to secure a liberal amount of practice in freehand lettering.

Field Note Sketches.—Sketches will be used liberally in the notes and will be made in the field. If desired, a ruler may be used in drawing straight lines, but the student is urged to acquire skill at once in making good plain freehand sketches. The field sketches should be bold and clear, in fair proportion, and of liberal size so as to avoid confusion of detail. The exaggeration of certain details in a separate sketch sometimes adds greatly to the clearness of the notes. The sketches should be supplemented by descriptive statements when helpful, and important points of the sketch should be lettered for reference. The precise scaling of sketches in the field note book, while sometimes necessary is usually undesirable owing to the time consumed. It is also found that undue attention to the drafting of the sketch is very apt to occupy the mind and cause



omissions of important numerical data. Since recorded figures and not the size of the field sketch itself must usually be employed in the subsequent use of the notes, it is important to review the record before leaving the field to detect omissions or inconsistencies. Making sketches on loose sheets or in other books and subsequently copying them into the regular field book is very objectionable practice and will not be permitted in the class work. Copies of field notes or sketches are never as trustworthy as the original record made during the progress of the field work. In very rapid surveys where legibility of the original record must perhaps suffer somewhat, it is excellent practice to transcribe the notes at once to a neighboring page, thus preserving the original rough notes for future reference. The original has more weight as evidence, but the neat copy

FIELD NOTES.

ANGLES OF TRIANGLE 5-6-7 Station Value of Angle Ist Meas. 2nd Meas. Mean 88°51' 88°50' 88°50'30' 5 6 7 47°47' 47*°*47′ 47°47'00 13°23' 13°73' 43°73'00 180°00'30 (Difference in measurements not to exceed 1') (Error not to exceed 1) Left Hand Page. Observers, J. Doe & R. Roe. WITH ENGINEERS' TRANSIT. Nov. 15, 1914, (2 hours). Warm and quiet Used Hellar & Brightly Transit No. 10.

Right Hand Page.

9

made before the notes are "cold" is of great help in interpreting them.

Numerical Data.—The record of numerical data should be consistent with the precision of the survey. In observations of the same class a uniform number of decimal places should be recorded. When the fraction in a result is exactly one-half the smallest unit or decimal place to be observed, record the even unit. Careful attention should be given to the *legibility of numerals*. This is a matter in which the beginner is often very weak. This defect can be corrected best by giving studious attention and practice to both the form and vertical alinement of tabulated numerals.

Erasures.—Erasures in the field notes should be avoided. In case a figure is incorrectly recorded, it should be crossed out and the correct entry made near by. The neat cancellation of an item in the notes inspires confidence, but evidence of an erasnre or alteration casts doubt upon their genuineness. When a set of notes becomes so confused that erasure seems desirable, it should be transcribed, usually on another page. Rejection of a page of notes should be indicated by a neat cross mark, and cross reference should be made between the two places.

Office Copies.—Office copies of field notes will be submitted promptly, as required. These copies must be actual transcripts from the original record contained in the field note book of the individual submitting the copy. When office copies are made, a memorandum of the fact should be entered on the page of the field note book. When so specified, the office copies will be executed in india ink.

Criticism of Field Notes.—The field notes must be kept in shape for inspection at any time, and be submitted on call. All calculations and reductions must be kept up to date. The points to which chief attention should be directed in the criticism of the field notes are indicated in the following schedule. The student is expected to criticise his own notes and submit them in as perfect condition as possible. For simplicity the criticisms will be indicated by stamping on the note book page the reference letters and numbers shown in the schedule.

SCHEDULE OF POINTS FOR THE CRITICISM OF FIELD NOTE BOOKS.

A. SUBJECT MATTER.

(1) General:

- (a) Descriptive title of problem.
- (b) Date.
- (c) Weather.
- (d) Organization of party.
- (e) Equipment used.
- (f) Time devoted to the problem.
- (g) Indexing and cross referencing.
- (h) Page numbering.
- (i) Title page.
- (j) Identification of field note book.

(2) Record of Data:

- (a) Accuracy.
- (b) Completeness.
- (c) Consistency.
- (d) Arrangement.
- (e) Originality.

B. EXECUTION.

(1) Lettering:

(a) Style. ("Engineering News")

(b) Size. (a, c, e, i, etc., $\frac{3}{40}$ inch high; b, d, f, g, etc., A, B, C, etc., and 1, 2, 3, etc., $\frac{5}{40}$ ($\frac{1}{8}$) inch high; t, $\frac{4}{40}$ inch.)

(c) Slant. (In body of notes, "slanting," 1:2.5 right; in headings, "upright," about 1:25 to left.)

(d) Form. (See Reinhardt's "Freehand Lettering.")

(e) Spacing. (Of letters in words; of numerals; of words; balancing in column or across page.)

(f) Alinement. (Horizontal; vertical.)

(g) Permanency. (Use sharp hard pencil with pressure.) (2) Sketches.

- (a) To be bold, clear and neat.
- (b) To be ample in amount.
- (c) To be of liberal size.
- (d) To be in fair proportion.
- (e) To be made freehand.
- (f) To be made in the field.

OFFICE WORK.

Importance of Office Work.—Capable office men are comparatively rare. Skill in drafting and computing is within the reach of most men who will devote proper time and effort to the work. Men who are skillful in both field and office work have the largest opportunity for advancement.

Calculations.--All calculations and reductions of a permanent character must be shown in the field note book in the specified form. Cross references between field data and calculations should be shown. Consistency between the precision of computed results and that of the observed data should be maintained. Computed results should be verified habitually, and the verified results indicated by a check mark. Since most computers are prone to repeat the same error, it is desirable in checking calculations to employ independent methods and to follow a different order. A fruitful source of trouble is in the transcript of data, and this should be checked first when reviewing doubtful cal-Skilled computers give much attention to culations. methodical arrangement, and to contracted methods of computing and verifying results. Familiarity with the slide rule and other labor saving devices is important. (See Chapter X, Methods of Computing.)

Drafting Room Equipment.—The student is responsible for the proper use and care of drafting room furniture and equipment provided for his use.

Drafting.—The standard of drafting is that indicated in Reinhardt's "Technic of Mechanical Drafting."

Drafting Room Decorum.—The decorum of the student in the drafting room will conform to that observed in firstclass city drafting offices.

CHAPTER II.

THE CHAIN AND TAPE.

METHODS OF FIELD WORK.

Units of Measure.—In the United States the foot is used by civil engineers in field measurements. Fractions of a foot are expressed decimally, the nearest 0.1 being taken in ordinary surveys, and the nearest 0.01 foot (say $\frac{1}{8}$ inch) in more refined work.

In railroad and similar "line" surveys by which a station stake is set every 100 feet, the unit of measure is really 100 feet instead of the foot. The term "station" was originally applied only to the actual point indicated by the numbered stake, but it is now universal practice in this country to use the word station in referring to either the point or the 100-foot unit distance. A fractional station is called a "plus" for the reason that a plus sign is used to mark the decimal point for the 100-foot unit, the common decimal point being reserved for fractions of a foot. The initial or starting stake of such a survey is numbered 0.

The 100-foot chain is commonly called the "engineers' chain" to distinguish it from the 66-foot or 100-link chain which is termed the "surveyors' chain" because of its special value in land surveys involving acreage. The latter is also called the Gunter chain after its inventor, and is otherwise known as the four-rod or four-pole chain. British engineers use the Gunter chain for both line and land surveys. The "surveyors" or Gunter chain, while no longer used in actual surveying, is described in this book for the reason that the United States rectangular surveys were made throughout with the 66-foot chain.

In the Spanish-American countries the vara is generally used in land surveys. The Castilian vara is 32.8748 inches long, but the state of California has adopted 32.372 inches, and Texas 331₃ inches, as the legal length of the vara.

While the metric system is used exclusively, or in part, in

each of the several United States government surveys, except those for public lands, little or no progress has been made towards its introduction in other than government surveys.

Linear Measuring Instruments.—Two general types of linear measuring devices are used by surveyors, viz., the common chain and the tape. There are several kinds of each, according to the length, material, and method of graduation.



The common chain is made up of a series of links of wire having loops at the ends and connected by rings so as to afford flexibility. The engineers' chain is shown in (a), Fig. 1, the illustration being that of a 50-foot chain, or onehalf the length generally used. The surveyors' or Gunter chain is shown in (b), Fig. 1. In the common chain the end graduation is the center of the cross bar of the handle, and every tenth foot or link is marked by a notched brass tag. In the 100-foot or 100-link chain the number of points on the tag indicates the multiple of ten units from the nearer end, and a circular tag marks the middle of the chain. The chain is done up hour-glass shape, as shown in the cut.

Chaining pins made of steel wire are used in marking the end of the chain or tape in the usual process of linear measurement. A set of pins usually numbers eleven, as indicated at (c), Fig. 1. The pins are carried on a ring made of spring steel wire.

The flat steel band, shown in (d) and (e), Fig. 1, is the hest form of measuring device for most kinds of work. The band tape is usually 100 feet long. The end graduations of the band tape are usually indicated by brass shoulders, which should point in the same direction, as shown in (f), Fig. 1. The 100-foot band tape is commonly graduated every foot of its length, and the end foot to every 0.1 foot, every fifth foot being numbered on a brass sleeve. Brass rivets are most commonly used in graduating this tape. The band tape may be rolled up on a special reel, as indicated in (d) and (e), although some engineers dispense with the reel and do up the tape in the form of the figure 8 in loops of five feet or so.

The steel tapes shown in (g) and (h) have etched graduations. This style of tape is commonly graduated to 0.01 foot or $\frac{1}{6}$ inch. It is more fragile than the band tape and is commonly used on more refined work. The form of the case shown in (h) has the advantage of allowing the tape to dry if wound up while damp.

The "metallic" tape (i), Fig. 1, is a woven linen line having fine hrass wire in the warp.

The steel tape is superior to the common chain chiefly hecause of the permanency of its length. The smoothness and lightness of the steel tape are often important advantages, although the latter feature may be a serious drawhack at times. The tape is both easier to break and more difficult to mend than the common chain.

Tapes for measuring base lines with great precision have recently been made of Invar steel. Invar steel has a very small coefficient of expansion. Invar steel tapes are very expensive. Chaining.—In general, the horizontal distance is chained. Two persons, called head and rear chainmen, are required. The usual process is as follows:

The line to be chained is first marked with range poles. The head chainman casts the chain out to the rear, and after setting one marking pin at the starting point and checking up the remaining ten pins on his ring, steps hriskly to the front. The rear chainman allows the chain to pass through his hands to detect kinks and bent links. Just before the full length is drawn out, the rear chainman calls "halt." at which the head chainman turns, shakes out the chain and straightens it on the true line under the direction of the rear chainman. In order to allow a clear sight ahead, the front chainman should hold the chain handle with a pin in his right hand well away from his body, supporting the right elbow on the right knee, if desired. The rear chainman holds the handle in his left hand approximately at the starting point and motions with his right to the head chainman, his signals being distinct both as to direction and amount. Finally, when the straight and taut chain has been brought practically into the true line, the rear chainman, slipping the handle behind the pin at the starting point with his left hand, and steadying the top of the pin with his right, calls out "stick." The head chainman at this instant sets his pin in front of the chain handle and responds " stuck," at which signal and not before the rear chainman pulls the pin.

Both now proceed, the rear chainman giving the preliminary "halt" signal as he approaches the pin just set by the head chainman. The chain is lined up, stretched, the front pin set, and the rear pin pulled on signal, as described for the first chain length. This process is repeated until the head chainman has set his tenth pin, when he calls "out" or "tally," at which the rear chainman walks ahead, counting his pins as he goes and, if there are ten, transfers them to the head chainman who also checks them up and replaces them on his ring. A similar check in the pins may be made at any time by remembering that the sum, omitting the one in the ground, should be ten. This safeguard should be taken often to detect loss of pins. The count of tallies should be carefully kept.

When the end of the line is reached, the rear chainman steps ahead, and reads the fraction at the pin, noting the units with respect to the brass tags on the chain. The number of pins in the hand of the rear chainman indicates the number of applications of the chain since the starting or last tally point. A like method is used in case intermediate points are to be noted along the line.

On sloping ground the horizontal distance may be obtained either by leveling the chain and plumbing down from the elevated end, or by measuring on the slope and correcting for the inclination. In ordinary work the former is preferred, owing to its simplicity. In "breaking chain" up or down a steep slope, the head chainman first carries the full chain ahead and places it carefully on the true line. A plumb bob, range pole or loaded chaining pin should be used in plumbing the points up or down. The segments of the chain should be in multiples of ten units, as a rule, and the breaking points should be "thumbed" by both chainmen to avoid blunders. Likewise, special caution is required to avoid confusion in the count of pins during this process.

The general method of measuring with the band tape is much the same as with the common chain. The chief difference is due to the fact that the handle of the tape extends beyond the end graduation, so that it is more convenient for the head chainman to hold the handle in his left hand and rest his left elbow on his left knee, setting the pin with his right hand. Another difference is in the method of reading fractions. It is best to read the fraction *first by estimation*, as with the chain, making sure of the *feet*; then shifting the tape along one foot, getting an exact decimal record of the fraction by means of the end foot graduated to tenths; the nearest 0.01 foot is estimated, or in especially refined work, read by scale.

In railroad and similar line surveys, chaining pins are usually dispensed with and the ends of the chain are indicated by numbered stakes. The stake marked 0 corresponds to the pin at the starting point, and the station stakes are marked thence according to the number of 100-foot units laid off.

Perpendiculars.—Perpendiculars may be erected and let fall with the chain or tape by the following methods:

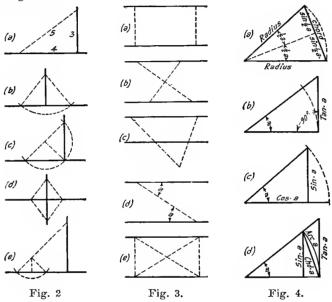
(a) By the 3:4:5 method, shown in (a), Fig. 2, in which a triangle having sides in the ratio stated, is constructed.

(b) By the chord bisection method, shown in (b), Fig. 2, in which a line is passed from the bisecting point of the chord to the center of the circle, or vice versa.

3

(c) By the semicircle method, shown in (c), Fig. 2, in which a semicircle is made to contain the required perpendicular.

The first method corresponds to the use of the triangle in drafting. Good intersections are essential in the second and third methods. Results may be verified either by using another process, or by repeating the same method with the measurements or position reversed, as indicated in (d), Fig. 2.



In locating a perpendicular from a remote point, the ratio method shown in (e), Fig. 2, may be used; or a careful trial perpendicular may be erected at a point estimated by placing the heels squarely on line and swinging the arms to the front, then proving by precise method.

Parallels.—Parallels may be laid off with the chain in varions ways, a few of the simpler of which are:

(a) By equal distances, as in (a), Fig. 3, in which two equal distances are laid off, usually at right angles to the given line.

(b) By similar triangles, as in (b) and (c), Fig. 3. The ratio may, of course, have any value.

(c) By alternate angles, as in (d), Fig. 3, in which two equal angles are laid off in alternation.

The first method is adapted to laying off a rectangle, as in staking out a building, in which case a good check is found in the equality of the diagonals. Precision of alinement is important, especially where a line is prolonged.

Angles.—Angles may be determined by linear measurements in the following ways:

(a) By the chord method, shown in (a), Fig. 4, in which the radius is laid off on the two lines forming the angle, and the chord measured.

(b) The tangent method, shown in (b), Fig. 4, in which a perpendicular is erected at one end of the radius, and the length of the perpendicular intercepted by the two lines measured.

(c) The sine-cosine method, (c), Fig. 4, which is better suited to constructing than to measuring angles.

The chord method is usually the most satisfactory. The tangent method may be applied to the bisected angle when its value approaches a right angle. Measurement of the supplementary angle affords an excellent check. A 100-foot radius is commonly used, although good results may be had with the 50-foot tape. Careful alinement is of the first importance in angular measurements.

It is sometimes necessary to determine angles, at least approximately, when no tables are at hand. Fair results may be had on smooth ground by measuring the actual arc struck off to a radius of 57.3 feet.

For very small angles, the sine, chord, arc and tangent, (d), Fig. 4, are practically equal. Thus, $\sin 1^{\circ}$ is .017452 and $\tan 1^{\circ}$, .017455, or either (say) .01745, or $1\frac{3}{4}$ per cent. Also, arc 1' is .000291, or (say) .0003 (three zeros three); and, arc 1" is .00000485, (say) .000005 (five zeros five).

Location of Points.—Points are located in surveying field practice in the following seven ways.

(a) By rectangular coordinates, that is, by measuring the perpendicular distance from the required point to a given line, and the distance thence along the line to a given point, as in (a), Fig. 5.

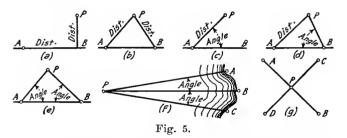
(h) By focal coordinates or tie lines, that is, by measuring the distances from the required point to two given points, as in (b), Fig. 5. (c) By polar coordinates, that is, by measuring the angle between a given line and a line drawn from any given point of it to the required point; and also the length of this latter line, as in (c), Fig. 5.

(d) By modified polar coordinates, that is, by a distance from one known point and a direction from another, as in (d), Fig. 5.

(e) By angular intersection, that is, by measuring the angles made with a given line by two other lines starting from given points upon it, and passing through the required point, as in (e), Fig. 5.

(f) By resection, that is, by measuring the angles made with each other by three lines of sight passing from the required point to three points, whose positions are known, as in (f), Fig. 5.

(g) By diagonal intersection, that is, by two lines joining two pairs of points so as to intersect in the required point, as in (g), Fig. 5.



In each of these methods, except (f), the point is determined by the intersection of either two right lines, or two circles, or a right line and a circle.

Methods (a) and (b) are best suited to chain surveys; (c) and (d) are used most in the location of railroad curves; (e) and (f) are employed chiefly in river and marine surveys for the location of soundings, the latter being commonly known as the "three-point problem"; the last method, (g), is much used for "referencing out" transit points in railroad and similar construction surveys.

Location of Objects.—The location of buildings and topographic objects usually involves one or more of the foregoing methods of locating a point. In Fig. 6, (a), (b), (c), and (d) suggest methods of locating a simple form, and (e) and (f) illustrate more complex cases.

Tie Line Surveys.—For many purposes tie line surveys, made with the chain or tape alone, are very satisfactory. The skeleton of such surveys is usually the triangle, the detail being filled in by the methods just outlined. Much time may be saved by carefully planning the survey. A few typical applications of the tie line method are shown in Fig. 7.

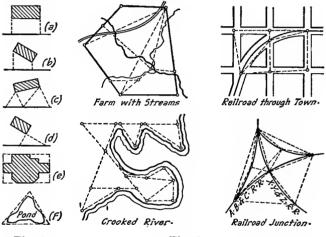


Fig. 6.

Fig. 7.

Ranging in Lines.—The range or flag pole is usually painted with alternate feet red and white, and the lower end is shod or spiked. A temporary form of range pole, called a picket, is sometimes cut from a straight sapling.

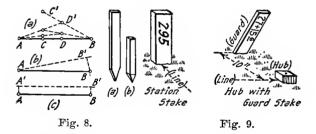
In flagging a point, the spike of the pole is placed on the tack and the pole plumbed by holding it symmetrically between the tips of the fingers of the two hands, the flagman being squarely behind the pole.

In hilly or timbered country the two land corners or other points between which it is desired to range in a line, are often invisible one from the other. In many cases two intermediate points C' and D', (a), Fig. 8, may be found, from which the end points B and A, respectively, are visible; so that after a few successive linings in, each by the other, the true points, C and D, are found.

Otherwise, as shown at (b), Fig. 8, a random line may be run from A towards B. The trial line is chained and marked, the perpendicular from B located, and points interpolated on the true line.

If the desired line is occupied by a hedge or other obstruction, an auxiliary parallel line may be established in the adjacent road or field, after one or two trials, as in (c), Fig. 8.

 $\overline{\Lambda}$ line may be prolonged past an obstacle by rectangular offsets or by equilateral triangles.



Signals.—There is little occasion for shouting in surveying field work if a proper system of sight signals is used. Each signal should have but one meaning and that a perfectly distinct one. Signals indicating motion should at once show clearly hoth the direction and amount of motion desired. Some of the signals in common use are as follows:

(a) "Right" or "left,"—the arm is extended distinctly in the desired direction and the motion of the forearm and hand is graduated to suit the lateral motion required.

(b) "Up" or "down,"—the arm is extended laterally and raised or lowered distinctly with motions to suit the magnitude of the movement desired. Some levelers use the left arm for the "up" signal and the right for "down."

(c) "Plumb the pole (or rod),"—If to the right, that arm is held vertically with hand extended and the entire body, arm included, is swung distinctly to the right, or vice versa.

(d) "All right,"-both arms are extended full length horizontally and waved vertically.

(e) "Turning point" or "transit point,"—the arm is swung slowly about the head.

(f) "Give line,"—the flagman extends both arms upward, holding the flag pole horizontally, ending with the pole in its vertical position. If a precise or tack point is meant, the signal is made quicker and sharper.

(g) Numerals are usually made by counted vertical swings with the arm extended laterally. A station number is given with the right hand and the plus, if any, with the left; or a rod reading in like manner. The successive counts are separated by a momentary pause, emphasized, if desired, by a slight swing with both hands.

Stakes and Stake Driving.—A flat stake is used to mark the stations in a line survey, and a square stake or hub to mark transit stations, (a) and (b), Fig. 9. The station stake is numbered on the rear face, and the hub is witnessed by a flat guard stake driven slanting 10 inches or so to the left, Fig. 9. The numerals should he hold and distinct, and made with keel or waterproof crayon, pressed into the surface of the wood.

Having located a point approximately with the flag pole, the stake should be driven truly plumb in order that the final point may fall near the center of its top. In driving a stake, the axeman should watch for signals. It is better to draw the stake by a slanting blow than to hammer the stake over after it is driven. Good stake drivers are scarce.

PROBLEMS WITH THE CHAIN AND TAPE.

General Statement.—Each problem is stated under the following heads:

(a) Equipment.—In which are specified the articles and instruments assigned or required for the proper performance of the problem. A copy of this manual and of the regulation field note book, with a hard pencil to keep the record, form part of the equipment for every problem assigned.

(b) *Problem.*—In which the problem is stated in general terms. The special assignments will be made by program.

(c) *Methods.*—In which the methods to be used in the assigned work are described more or less in detail. In some prohlems alternative methods are suggested, and in others the student is left to devise his own.

PROBLEM A1. LENGTH OF PACE.

(a) Equipment.—(No instrumental equipment required.)
(b) Problem.—Investigate the length of pace as follows:
(1) the natural pace; (2) an assumed pace of 3 feet; and
(3) the effect of speed on the length of the pace.

(c) Mcthods.—(1) On an assigned course of known length count the paces while walking at the natural rate. Observe the nearest 0.1 pace in the fraction at the end of the course. Secure ten consecutive results, with no rejections, varying not more than 2 per cent. (2) Repeat (1) for an assumed 3-foot pace. (3) Observe (in duplicate) time and paces for four or five rates from very slow to very fast, with paces to nearest 0.1 and time to nearest second. Record data and make reductions as in the form.

PROBLEM A2. DISTANCES BY PACING.

(a) Equipment.—(No instrumental equipment required.)

(b) Problem.-Pace the assigned distances.

(c) Methods.—(1) Standardize the pace in duplicate on measured base. (2) Pace each line in duplicate, results differing not more than 2 per cent. Record and reduce as in form.

PROBLEM A3. AXEMAN AND FLAGMAN PRACTICE.

(a) Equipment.—Flag pole, axe, 4 flat stakes, 1 hub, tacks.

(b) *Problem.*—Practice the correct routine duties of axeman and flagman.

(c) Methods.—(1) Number three station stakes to indicate representative cases and drive them properly. (2) Drive a hub flush with ground and tack it; number a witness stake and drive it properly. (3) Arrange program of signals with partner, separate 1.000 feet or so and practice same. (4) Signal say five station numbers to cach other and afterwards compare notes. Make concise record of the foregoing steps.

PROBLEM A4. RANGE POLE PRACTICE.

(a) Equipment.—4 flag poles.

(b) Problem.—Given two hubs approximately 1.000 feet apart, interpolate a flag pole say 100 feet from one hub.

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4	137.6				79	57	Slow	168.0		(6)		(6)
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6	139.0				77	,,	Natural	139.4		(0)		(0)
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remove the distant pole, prolong the line by successive 100foot sights and note the error at distant hub. Repeat process for 200-foot and 300-foot sights.

(c) Methods.—(1) Set distant flag pole precisely behind hub and hold spike of pole on tack of near hub; lying on ground back of near hub, line in pole 100 feet (paced) distant; remove pole from distant hub, and prolong by 100foot sights up to distant hub, noting error to nearest 0.01 foot. (2) Repeat in reverse direction, using 200-foot sights. (3) Repeat with 300-foot sights. Avoid all bias. Record data in suitable form, describing steps concisely.

PROBLEM A5. STANDARDIZING CHAIN OR TAPE.

(a) Equipment.—Chain or tape assigned in any problem where standard length of chain may be of value.

(b) *Problem.*—Determine the length of the assigned chain or tape by comparison with the official standard under the conditions of actual use.

(c) Mcthods.—In standardizing tape, reproduce the conditions of actual use as regards tension, support, etc., bring one end graduation of chain or tape to coincide with one standard mark, and observe fraction at the other end with a scale. As a general rule, observe one more decimal place than is taken in the actual chaining.

PROBLEM A6. DISTANCES WITH SURVEYORS' CHAIN.

(a) Equipment.—Surveyors' chain, set of chaining pins, 2 plumb bobs, 2 flag poles (unless instructed otherwise).

(b) *Problem.*—On an assigned chaining course about one mile long measure distances with the surveyors' chain to the nearest 0.1 link, and repeat the measurements in the opposite direction.

(c) Methods.—(1) Standardize the chain before and after, as prescribed in A5. (2) Chain along the assigned course, noting the distances from the starting point to the several intermediate points and to the end station. Observe fractions to the nearest 0.1 link by estimation. (3) Repeat the chaining in the opposite direction, noting the distances from the end point, as before. The difference between the totals in the two directions should not exceed 1:3,000. Retain the same party organization throughout the problem. Record the data as in the prescribed form.

		DIST	NCES	wit	н	SURVEYOR'S CHAIN
Line	Direction	Oberved	Diff- of	Ratio	Coef	Nead Chainman-J Doe; Rear Chainman, R Roe
	Chained	Length	Total	1:d	C	Sept 18, 14 (2 Hours) Clear and Cool
		Cĥ∙	Ch-		Lk ·	Used Gunter Chain Nº 210, Locker Nº35
Chain	BeFore				ĮĮ	Compared chain with official standard
"		1·0022				both before and after day's chaining.
A-B	E·	7-327				Chained along Chaining Course "A",
A-C	"	30.306				beginning at hub with tack, marked
A-D	"	60-357				A on guard stake, located at 5-odge
A-E	"	7 9 -838	h.			of W. brick walk on Green St; at E.
				ļ		curb line of Mathews Ave-, Urbana,
E-D	W.	19-479				III.; thence E'ly plong said 5 line of
E-C	"	49.53/				N. brick side walk, observing distanc-
E-B	"	72-506		1	1	es to nearest 0-1 lk· to tacked hubs
E-A	"		0.005	1:15970	0.06	marked B, C, D and E, the total distance
		*∠	<i>°E</i> =	CYL of	9=5-	From starting point A being noted
				N	1 7 3	Chained same course in the reverse
				15ee D.	iagram)	
		1.		L.		From Hub E.
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PROBLEM A7. DISTANCES WITH THE ENGINEERS' CHAIN.

(a) Equipment.—Engineers' chain, set of chaining pius, 2 plumb bobs, 2 flag poles (unless instructed otherwise).

(b) *Problem.*—On an assigned chaining course about one mile long measure distances with the engineers' chain to the nearest 0.1 foot, and repeat the measurements in the opposite direction.

(c) Methods.—(1) Standardize the chain before and after, as prescribed in A5. (2) Chain along the assigned course, noting the distances from the starting point to the several intermediate points and to the end station. Observe fractions to the nearest 0.1 foot by estimation. (3) Repeat the chaining in the opposite direction, noting the distances from the end point, as before. The difference between the totals in the two directions should not exceed 1:3,000. Retain the same party organization throughout the problem. Record the data as in the form.

PROBLEM A8. DISTANCE WITH 100-FOOT STEEL TAPE.

(a) Equipment.--100-foot steel band tape with end foot graduated to tenths, set of chaining pins, 2 plumb bobs, 2 flag poles (unless instructed otherwise).

(b) *Problem.*—On an assigned chaining course abont one mile long measure distances with the 100-foot steel band tape to the nearest 0.01 foot, and repeat the measurements in the opposite direction.

(c) Methods.—(1) Standardize before and after, as prescribed in A5. (2) Chain along the assigned course, noting the distances from the starting point to the several intermediate points and to the end station. In observing the fractions, first determine the foot units, then estimate the nearest 0.1 foot, then shift the tape along one foot and read the exact fraction on the end of the tape, estimating the nearest 0.01 foot. (3) Repeat the measurement in the opposite direction, noting the distances from the end point, as before. The difference between the totals in the two directions should not exceed 1:5,000. Retain the same party organization. Record data as in the form.

PROBLEM A9. HORIZONTAL DISTANCE ON SLOPE WITH STEEL TAPE.

(a) Equipment.—100-foot steel tape with etched graduations to 0.01 foot, set of chaining pins, 2 plumb bobs, 3 flag poles, axe, supply of pegs, engineers' level and rod (unless otherwise instructed).

(b) *Problem.*—Determine the horizontal distance between two assigned points on a steep slope, (1) by direct horizontal measurement, and (2) by measurement on the slope and reduction to the horizontal.

(c) Mcthods.—(1) Standardize the tape for each method, as prescribed in A5, both before and after the day's chaining. (2) In chaining down hill, *rcar chainman* lines in flag pole in hand of head chainman, then holds tape end to tack on hub; *flagman* stands 50 feet or more from line opposite middle of tape and directs head chainman in leveling front end, then supports middle point of tape under direction of head chainman; *head chainman*, with spring balance attached to tape and using pole as help to steady pull, brings tension to 12 pounds; *recorder* plumbs down front end, and sets pin slanting sidewise. After checking the pin, proceed

Line Chain " A-B A-C A-O A-E E-D E-C E-B E-A Note:	a 50b	Length Ft. 100, 10 100-12 484-0 2002-2 3987-5 5274-6 1286-9 3272-4 4790-2 5274-3 5274-3 5274-3 52-74-3	DIFF-oF Total Ft. <i>Ko.3</i> <i>K</i> <i>E=</i> <i>(See Diata will)</i> <i>f prob</i>	I:17580 CYI or ogram)-t t be us	0.04 0.04 11 C= YZ ed in discuss	Fractions of a foot were estimated A pocket rule was used to compare chain with standard W <> E A B C D P
						Hub of the of th
\geq	ι	1			,	
Line Tape	Chained	Observed Length Ft 100-01	Total Ft	WITI Ratio 1: d	CoeF C· Ft·	100 FT STEEL TAPE Rear Chain - P. Ree Sept-20, 14 - (2 hours) Clear, moderate- WU Ft Roe Steel Tape MS12, Lacker 35 Compared tape with of Ficial standard both Before and after day's choining- measuring fractlyn with engineer scale
A-B A-C A-D A-E	E- ""	48458 200379 3991-69 527948				Choined along Chaining Course 7%, previ- pusty chained with Gunter and 100 Et Chains, described on pp. of Field note book, observing cantinu-

	lenomico	congru	1.0101			WVIII KUE JIEEI IAPE II-JIZ, LUCKEI JJ
		Ft-	Ft.	í i	Ft.	Compared tape with of Ficial standard
Tape	Before	100-01				both before and after day's choining
	AFter	100.008				measuring Fraction with engineer's cale
A-B	E٠	48458				Choined along Chaining Course "A", previ-
A-C	.,	2003.79				pusty choined with Gunter and 100
A-D	, ,,	3991-69				Ft. Chains, described on pp. oF
A-E	"	527948				Field note book observing continu-
			1			ous distances to hubs B.C.D and
E-D	W.	1287.83	į –			E to neorest 0.01 Ft
E-C		3275.72	1			Chained course in reverse direction.
E-B	"	4794.96				Fractions of a foot were estimated
E-A	"	5279-57	0.09	1:58660	0.012	to nearest 0.01 Ft on the end foot
		L=	11		// _	of the tape which was graduated
		<i>52-7957</i>	E =	CVI or	E .	to tenths of a Foot-
			(5ee D	iogram	φ^{μ}	
]			- ·		₩·<- →E
Note:		above a				ABCDE
	ina	subseq	vent př	oblem	in	
	disc	ussing i	the pre	cision	oF	duh duh duh
	choi	ning				Hub Hub Hub
		-			1	
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with the next 100 feet. In chaining up hill, follow same general method, using plumb bob at rear end. In leveling the tape the tendency will be to get the down hill end too low. Chain the line in duplicate, retaining the same organization. (3) Chain the line again in duplicate, tape lying on the ground, pull 12 pounds, pins set plumb, fraction direct to nearest 0.01 foot. Set temporary pegs flush with ground every 100 feet and also at intermediate sudden changes of slope, for levels. Determine differences of elevation between successive pegs, unless the leveling data are supplied to the party. Record data and make reductions and comparisons as in the form.

PROBLEM A10. ANGLES OF A TRIANGLE WITH TAPE.

(a) Equipment.—100-foot steel tape, 50-foot metallic tape, set of chaining pins, 2 plumb bobs, 2 flag poles, five-place tables of trigonometric functions (each member of party to have tables).

(b) *Problem.*—Measure the angles of an assigned triangle with the steel tape and also with the metallic tape, the error of closure not to exceed 3 minutes.

(c) Methods.—(1) Measure each angle with the steel tape by both the chord and tangent methods, 100-foot radius, the difference in the two results not to exceed 2 minutes. If the angle is near 90°, the tangent method may be applied to the bisected angle. (2) After securing satisfactory check on an angle with the steel tape, make a rapid but careful measurement with the metallic tape, radius 50 feet. The results may be taken to the nearest half minute. (3) Measure at least one angle, preferably on smooth ground, by laying out an arc with radius of 57.3 feet, setting pins every few feet, and measuring the actual arc. Give close attention to alinement throughout. Record data and make reductions as in the form.

PROBLEM A11. SURVEY OF FIELD WITH STEEL TAPE.

(a) Equipment.—100-foot steel tape, set of chaining pins, 2 plumb bobs, 4 flag poles, five-place table of functions.

(b) Problem.—Make survey of an assigned field with tape, collecting all data required for plotting the field and calculating its area by the "perpendicular," "three-side," and "angle" methods.

PROBLEMS.

Har	701-7			A 14	A 17	Hd Chain, J-Doe Rr. Chain, R. Ros.
DOR	ZONTA		ANCE	△14 -	AI((STEEP SLOPE) WITH STEEL TAPE . Recorder, B.F. Keen. Flagman, G.W. Sure.
<u>A</u> ∙ <u>B</u> y No∙	<u>Direct</u>	Mass	ral Mea	SULEME		Sopt-21,'14. (3 Hours) Cloudy ; moderate.
110-	Observed		Cor For Standard			Used 100-Ft.K.&E. etched tape, Nº 416,
	Ft.	Ft.	Ft.		Ratio((:d)	
Tape 1	99.995	1.1.	гъ	11.	vario(1:0)	1st. Method: Standardized tape (before and
" 2		99.996			E=0.04	after), supported at ends and middle,
	761.45				c= 0-015	plumbing ends down, pull 12 pounds.
2		761.47	-0.03	761.44		Chained line in duplicate, leveling tape by
-		40000.0			(See. +	estimation, pull 12 lbs, plumbing down
		030			Diagram	
						leaning sidewise.
<u>B.</u>	By Me	surem	ent on	the Sla	pe and	Reduction to the Horizontal
No-	Observed	Mean	ent <u>on</u> Cor for	Reduced	Diff. (E)	2nd Method : Compared tape with standard
			Standard	Length		(before and after), supported Full length
1	Ff.	F Ť .	Ft.	Ft.	Ratio(1:d	
Tape 1	100-007		1			Chained line in duplicate, tape supported on
2	100.008	100.008	1		E=0.02	
1	76]-81		1		c=0.007	
2			+0.06		1:38590	
	ion For			-0.47		Ran levels over line with following results:
	Horizon				(diancam)	C B B ² d Fft Fft Fft Fft
	by First			761.44	1 ° N	Ft. Ft. Ft. 100 + 3-5 12-25 6-06 100 + 3-7 13-69 0-07
Differe	nce bet	ween Ke	sul ts	0.05		100 + 4.1 16.81 0.08
Mean	of Two	Results	1	761.42		100 + 3.3 10.39 0.05 With a smell, 100 + 4.5 20.25 0.10 1 3 ² (word)
]				1:15230	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
t I	1	1			1	$\frac{62}{762} + 1.6 \qquad 2.56 \qquad \frac{0.02}{-0.47} = \xi d$
-	L	L	1	1		
_						
			<u> </u>	[[
\bigcap			5 OF 1			5-6-8 with TAPE.
Station		unctions	Com	puted A	ngle	Surveyors, J.Doe and R.Roe.
	Name	unctions Value	Com Half	puted A Whole		Surveyors, J.Doe and R.Roe. Sept.22, 14. (2 Hours) Clear and warm-
6	Name 5in-± (6)	unctions Value 0-4050	Com Half 23 [°] 53'5	puted A Whole 47 [*] 47'	ngle Mean-	Surveyors, J-Doe and R-Roe. Sept-22,'14. (2 Hours) Cleer and Warm- Vised Roe 100-Ft-Steel Tape, No.362, and
6	Name 5in-±(6) Tan-(6)	unctions Value 0-4050 1-1023	Com Half 23 [°] 53'5	puted # Whole 47°47' 47°47'	ngle Mean <i>47°47</i> '	Surveyors, J-Doe and R-Ree- Sept 22, 14. (2 Hours) (Clear and warm- Used Roe 100-FF. Steel Tape, No.362, and Lurkin 50-FF. Metallic Tape, No.411, LKr:35-
6 " 8	Name 5in-±(6) Tan-(6) 5in-±(8)	Unctions Value 0-4050 1-1023 0-3696	Com Half <i>23[°]53'5</i> 2/°4/·5	puted A Whole 47 47 47 47 43 23	ngle Mean 47°47	Surveyors, J-Doe and R-Roe. Sept-22, '14- (2 Hours) (Jeer and warm- Used Roe 100-FF. Steel Tope, No-362, and Lufkin 50-FF. Metallic Tope, No-411, Lkr:35- Though not needed in problem, noted the
6 " 8 "	Name 5in-½(6) Tan-(6) 5in-½(8) Tan-(8)	unctions Value 0-4050 1-1023 0-3696 0-9450	Com Hal <i>F 23[°]53[:]5</i> 21 [°] 41 [:] 5	puted # Whole 47 47' 43 23' 43 25	ngle Mean 47°47' 43°23'	Surveyars, J-Doe and R-Ree- Sept.22, '14- (2 Hours) (lear and warm- Used Roe (00-FF. Steel Tape, No-362, and Lufkin 50-FF. MetalNc Tape, No-441, LK-35- Though nat needed in problem, nated the lengths of tapes by standard, 100-01
6 " 8 " 5	Name 5in-½(6) Tan-(6) 5in-½(8) Tan-(8) 5in-½(5)	Unctions Value 0-4050 1-1023 0-3696 0-9450 0-6995	Com Half 23 53'5 2/ 4/ 5 44 23'	puted # Whole 47°47' 43°23' 43°23' 43°25	ngle Mean 47°47' 43°23'	Surveyers, J-Doe and R-Roe- Sept.22, '14- (2 thours) (leer and warm- Used Roe 100-Ft-Steel Tape, No-362, and Lufkin 50-Ft-Metallic Tape, No-411, Lkr-35- Though not needed in problem, noted the lengths of Tapes by standard, 100-01 and 50-01 Ft-, respective/v-
6 " 8 " 5 "	Name Sin-±(6) Tan-(6) Sin-±(8) Sin-±(5) Tan-±(5) Tan-±(5)	Unctions Value 0-4050 1-1023 0-3696 0-9450 0-6995 0-9796	Com Half 23 53:5 21°41:5 44°23' 44°24'5	puted # Whole 47 47' 43 °23' 43 °23' 88 °46' 88 °46'	ngle Mean 47°47' 43°23'	Surveyers, J-Doe and R-Roe- Sept.22, '14- (2 thours) (leer and warm- Used Roe 100-Ft-Steel Tape, No-362, and Lufkin 50-Ft-Metallic Tape, No-411, Lkr-35- Though not needed in problem, noted the lengths of Tapes by standard, 100-01 and 50-01 Ft-, respective/v-
6 " 8 " 5	Name 5in-±(6) Tan-(6) 5in-±(8) 5in-±(5) Tan-±(5) 5in-±(5)	Unctions Value 0-4050 1-1023 0-3696 0-9450 0-6995 0-9796 0-6997	Com Half 23 53'5 21°41'5 44°23' 44°24'5 44°24'5	uted / Whole 47 47 47 43 23 88 46 88 46 88 48	ngle Mean 47°47 43°23'	Surveyers, J-Doe and R-Roe- Sept.22, '14- (2 Hours) (lear and warm- Viset Roe 100-FF. Steel Tape, No-362, and Lufkin 50-FF. Metallic Tape, No-362, and Lufkin 50-FF. Metallic Tape, No-411, Lkr:35- Though not needed in problem, nated the lengths of tapes by standard, 100-01 and 30-01 FF. respectively- Measured each angle by chord method and checked by tangent method, using radius of 100 FF with steel Tapestin measuring
6 " 8 " 5 "	Name 5in-±(6) Tan-(6) 5in-±(8) 5in-±(5) Tan-±(5) 5in-±(5)	Unctions Value 0-4050 1-1023 0-3696 0-9450 0-6995 0-9796	Com Half 23 53'5 21°41'5 44°23' 44°24'5 44°24'5	uted / Whole 47 47 47 43 23 88 46 88 46 88 48	ngle Mean 47°47' 43°23'	Surveyors, J-Doe and R-Roe- Sept.22, '14- (2 Hours) Clear and warm- Used Roe 100-FF-Steel Tape, No-362, and Lufkin SO-FF-Metallic Tape, No-362, and Lufkin SO-FF-Metallic Tape, No-411, Lkr-35- Though not needed in problem, noted the lengths of Tapes by standard, 100-01 and 50-01 FF, respectively- Measured each angle by chord method and checked by Tangent method, using radius of 100 FF with steel Tape- In measuring LS, (nearly S0") the tangent method was
6 " 8 " 5 "	Name 5in-±(6) Tan-(6) 5in-±(8) 5in-±(5) Tan-±(5) 5in-±(5)	Unctions Value 0-4050 1-1023 0-3696 0-9450 0-6995 0-9796 0-9796 0-9799	Com Half 23 [°] 53 [.] 5 2/ [°] 41 [.] 5 44[°]23['] 44 [°] 24 ['] 44 [°] 24 ['] 44 [°] 25 [']	outed A Whole 47'47' 43°23' 88°48' 88°48' 88°48' 88°50	ngle Maan- 47°47' 43°23' 88°49	Surveyars, J.Doe and R.Ree. Sept.22, '14. (2 Hours) (lear and warm. Used Roe (10-FF.Steel Tape, No-362, and Lufkin 50-FF. Metallic Tape, No-441, Lkr:35- Though nat needed in problem, nated the lengths of tapes by standard, 100-01 and 50-01 fF. respectively. 100-01 and 50-01 fF. respectively. Nord method and checked by tangent method, using reding of 100 fF. with steel tape. In mesuring LS, (nearly 80) the tangent method was applied to the bisceted angle - Each
6 " 8 " 5 "	Name 5in-±(6) Tan-(6) 5in-±(8) 5in-±(5) Tan-±(5) 5in-±(5)	unctions Value 0-4050 1-1023 0-3696 0-9450 0-9795 0-9796 0-9799 0-9799 Error	Com Half 23 53'5 21°41'5 44°23' 44°24'5 44°24'5	outed # Whole 47 47' 43° 73' 43° 73' 88° 43' 88° 48' 88° 48' 88° 50 0re =	ngle Mean. 47°47' 43°23' 88°49' 179°59' 01'	Surveyers, J-Dee and R-Ree- Seph22, 14- (2 Hours) (lear and warm- Vised Ree (NO-FF, Steel Type, No-S62, and Lufkin 50-FF. Metall's Tape, No-S62, and Lufkin 50-FF. Metall's Tape, No-S62, and lengths of tapes by standard, 100-01 and 50-01 FF, respectively- Measured each angle by chord method and checked by tangent method, using radius of 100 FF with steel tape - In measuring LS, (nearly S0) the tangent method was applied to the bisected angle - Each angle was verified before proceeding
6 " 8 " 5 "	Name 5in-±(6) Tan-(6) 5in-±(8) 5in-±(5) Tan-±(5) 5in-±(5)	unctions Value 0-4050 1-1023 0-3696 0-9450 0-9795 0-9796 0-9799 0-9799 Error	Com Half 23 53:5 21°41:5 44°23' 44°24'5 44°24'5 44°24' 44°25' 0F Clos	outed # Whole 47 47' 43° 73' 43° 73' 88° 43' 88° 48' 88° 48' 88° 50 0re =	ngle Mean. 47°47' 43°23' 88°49' 179°59' 01'	Surveyers, J-Dee and R-Ree- Sept.22, '14- (2 Hours) (lear and warm- Viset Ree (UO-FF, Steel Tape, No-362, and Lufkin 50-Ff. Netallic Tape, No-362, and Lufkin 50-Ff. Netallic Tape, No-411, Lkr:35- Though not needed in problem, nated the lengths of tapes by standard, 100-01 and 30-01 Ff., respectively- Measured each angle by chord method and checked by tangent method, using radius of 100 Ff with steed tape- In measuring LS, (nearly S0 ²) the tangent method was applied to the bisected angle · Each angle was verified before proceeding to nort, a difference of 2' being allow-
6 " 5 " "	Name 5in-±(6) Tan-(6) 5in-±(8) 5in-±(5) Tan-±(5) 5in-±(5)	Unctions Value 0-4050 1-1023 0-3696 0-9450 0-9450 0-9796 0-9796 0-9799 0-9799 Error Permi	Com Half 23 53:5 21°41:5 44°23' 44°24'5 44°24'5 44°24'5 5 5 Clos 5 Sable	outed 4 Whole 47 47' 43'23' 43'23' 43'25' 88'48' 88'48' 88'48' 88'50' 678 - Error	ngle Maan 47°47' 43°23' 179°33' 01' 03'	Surveyars, J. Doe and R. Ree. Sept.22, '14. (2 Hours) (lear and warm. Used Roe (10-FF. Steel Tape, No-362, and Lufkin 50-FF. Metallic Tape, No-441, LKr.35- Though nat needed in problem, nated the lengths of tapes by standard, 100-01 and 50-01 ff., respectively. Messured each angle by chord method and checked by tangent method, using redius of 100 ff. with steel tape. In messuring 2.5, (nearly 50') the tangent method was applied to the biscered angle - Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each.
6 " 5 " "	Name Sin-±(6) Tan-(6) Sin-±(8, Tan-(8) Sin-±(3, Tan-±(3, Tan-±(3,	unctions Value 0-4050 1-1023 0-3696 0-9450 0-9450 0-9796 0-9799 Error Permi 50 F	Com Half 23 ³ 33 ¹ 5 44 ² 24 ¹ 5 44 ² 25 ¹ 9F Clos 552 ble 552 ble C. <u>Meta</u>	outed 4 Whole 47 47' 43'23' 43'23' 43'25' 88'48' 88'48' 88'48' 88'50' 678 - Error	ngle Maan 47°47' 43°23' 179°33' 01' 03'	Surveyers, J-Dee and R-Ree- Seph22, '14- (2 Hours) (Ispe, No-Séc, and Lufkin 50-Ft. Netall's Tape, No-Séc, and Lufkin 50-Ft. Netall's Tape, No-Séc, and Lufkin 50-Ft. Netall's Tape, No-Séc, and lengths of tapes by skindard, 100-01 and 50-01 ft., respectively. Messured each angle by chord method and checked by tangent method, using redius of 100 ft. with steel tape • In measuring LS, (nearly S0) the tangent method was applied to the bisected angle • Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each.
6 " 8 " 5 " " "	Name Sin-±(6) Tan-(6) Sin-±(0) Sin-±(0) Sin-±(3) Tan-±(3) Tan-±(3) Tan-±(3) Cha	unctions Value 0-4050 1-1023 0-3696 0-9450 0-9450 0-9796 0-9799 0-9799 Error Permi 50 I 50 I 50 I	Com Half 23'53'5 44'23' 44'24'5 44'24'5 44'24'5 44'24'5 9F Clos ssable OF Clos ssable A. A.	outed 4 Whole 47°47' 43°23' 43°23' 43°23' 88°48' 88°48' 88°48' 88°50 0re - Error	ngle Maan 47°47' 43°23' 179°33' 01' 03'	Surveyers, J-Dee and R-Ree- Sept.22, '14- (2 Hours) (lear and warm- Viset Ree (UO-FF. Steel Tape, No-362, and Lufkin 50-Ff. Netall's Tape, No-362, and lufkin 50-Ff. Netall's Tape, No-362, and lengths of tapes by standard, 100-01 and 50-01 Ff. respectively- Measured each angle by chord method and checked by tangent method, using radius of 100 Ff with steel Kape In measuring LS, (nearly 50 ²) the tangent method was applied to the bisected angle Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each- After an angle was thus verified, a rapid but careful measurement was made
6 " 8 ", 5 ", ", ", ", ", ", ", ", ",	Name Sin ± (6) Tan - (6) Sin ± (8) Sin ± (8) Sin ± (3) Tan ± (3) Tan ± (3) Sin ± (3) Sin ± (3) Sin ± (3)	unctions Value 0-4050 1-1023 0-3696 0-9450 0-9450 0-9796 0-9799 0-9799 Error Permi 50 F \$20 F \$20 F \$20 F \$2134/5	Com Half 23 53:5 21°41:5 44°23' 44°24' 44°24' 44°25' 07 Clos 552 ble - Meta 5°46' 43°23'	outed 4 Whole 47'47' 43'23' 43'23' 43'25 58'45' 88'48' 88'48' 88'50 0re - Error	ngle Maan 47°47' 43°23' 179°33' 01' 03'	Surveyars, J. Doe and R. Ree. Sept.22, '14. (2 Hours) (lear and warm. Used Roe 100-FF. Steel Tape, No-362, and Lufkin 50-FF. Metallic Tape, No-441, LKr:35- Though nat needed in problem, nated the lengths of tapes by standard, 100-01 and 50-01 FF. respectively. Messured each angle by chord method and checked by tangent method, using redius of 100 FF with steel tape. In messuring 2.5, (nearly 50') the tangent method was applied to the bisected angle - Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each. After an angle was thus verified, a repid but careful messurement was made with metallic tape, by chord method with metallic tape, by chord method
6 " 8 " 5 " " " " " " " " " " " " " " " "	Name Sin ± (6) Tan - (6) Sin ± (8) Sin ± (8) Sin ± (3) Tan ± (3) Tan ± (3) Sin ± (3) Sin ± (3) Sin ± (3)	unctions Value 0-4050 1-1023 0-3696 0-9450 0-9450 0-9796 0-9799 0-9799 Error Permi 50 F \$20 F \$20 F \$20 F \$2134/5	Com Half 23 53'5 21"41'5 44"23' 44"24'5 44"24'5 44"24'5 44"25' 0F Clos 550 ble - Meta A7"45' 47"42' 47"42' 47"42''5 88"50'	uted 4 Whole 47 47' 43 23' 43 25 18 48' 88 48' 88 50 078 - Error	ngle Maan 47°47' 43°23' 179°33' 01' 03'	Surveyers, J-Dee and R-Ree- Seph22, 14-(2 Hours) (Isre and warm- Vised Ree (WO-FF. Steel Isre and Warm- Used Ree (WO-FF. Steel Isre and Warm- Lurkin 50-Ft. Metall's Tape, No-401, Lkr:35- Though not needed in problem, noted the lengths of tapes by skindard, 100-01 and 50-01 Ff., respectively. Measured each angle by chord method and checked by tangent method, using radius of 100 Ff with steel tape - In measuring LS, (nearly SU) the tangent method was applied to the bisected angle - Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each. After an angle was thus verified, a rapid but careful measurement was made with metallic tape, by chord method andy, using 50-FK, radius-
6 " 5 " " " " " " " " " " " " " " " " "	Name Sin ± (6) Tan (6) Sin ± (3) Sin ± (3) Tan ± (3) Tan ± (3) Sin ± A O 4051 O -3696 O 6999	unctions Value 0.4050 1.1023 0.3696 0.9450 0.6995 0.6997 0.6997 0.6997 0.6997 0.6997 0.6997 0.5097 Fermi 50 I 2.121 2.121 2.121 4.425	Cam Half 23 53:5 21°41:5 44°23' 44°24:5 44°24:5 44°24:5 44°25' 5F Clos 55 26/6 55 26/6 55 26/6 5 5 26/6 5 5 26/6 5 5 26/6 5 5 26/6 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	uted 4 Whole 47 47 47 43 23 43 25 88 48 88 48 88 50 0re - Error	ngle Maan- 47°47' 43°23' 88°49 179'59' 01' 03' ge	Surveyers, J. Dee and R. Ree. Sept.22, '14. (2 Hours) (lear and warm. Viset Rev (10-FF, Steel Tape, No-362, and Lufkin 50-FF. Netall's Tape, No-362, and lufkin 50-FF. Netall's Tape, No-361, kr:35- Though not needed in problem, noted the lengths of tapes by standard, 100-01 and 50-01 FF, respectively- Measured each angle by chord method and checked by tangent method, using radius of 100 FF with steel tape. In measuring LS, (nearly 50 ²) the tangent method was applied to the bisected angle. Each angle was verified before proceeding to next, a difference of 2 ¹ being allow- ed in each. After an angle was thus verified, a rapid but careful measurement was made with metallis tape, by chord method anly, using 50-Ft, radius- Used flagpeles For distant and pins for
6 " " 5 " " " " " " " " " " " " " " " "	Name Sin ± (6) Tan (6) Sin ± (3) Sin ± (3) Sin ± (3) Tan ± (3) Sin ± (3) Sin ± (4) Sin \pm (unctions Value 0-4050 0-9450 0-9450 0-9795 0-9799 Error Permi 23'54' 23'54' 21'41'5 44'25	Com Half 23 53:5 21°41:5 44°23' 44°24'5 44°24'5 44°24' 44°25' 55 2 b/c 55 2 b/c 55 2 b/c 47°48'' 43°23' 180°0/h 180°0/h 180°0/h	uted 4 Whole 47 47 47 43 23 43 28 88 48 88 50 ore - Error alic Ta	ngle Maan- 47°47' 43°23' 179°23' 179°39' 03' 88°49' 03' 03'	Surveyars, J. Doe and R. Ree. Sept.22, '14. (2 Hours) (lear and warm. Used Roe 100-FF. Steel Tape, No-362, and Lufkin 50-FF. Metallic Tape, No-441, LKr.35- Though nat needed in problem, nated the lengths of tapes by standard, 100-01 and 50-01 FF., respectively. Messured each angle by chord method and checked by tangent method, using radius of 100 FF with steel tape. In messuring 2.5, (nearly 50) the tangent method was applied to the biscered angle - Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each. After an angle was thus verified, a rapid but careful messurement was made with metallic tape, by chord method anly, using 50-FF. radius- Used Flagpoles for distant and pins for close targets.
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6 "" 5 "" "" "" "" "" "" "" "" "" "" "" "	Name Sin ± (6) Tan (6) Sin ± (3) Tan ± (3) Sin ± (3) Tan ± (3) Sin ± (3) Can ± (Unctions Value 0.4050 0.3696 0.9450 0.9796 0.9796 0.9799 Error Permi 50 I 2.73154 2.1315 44*25 (weight	Com Half 23 53:5 21°41:5 44°23' 44°24'5 44°24'5 44°24' 44°25' 55 2 b/c 55 2 b/c 55 2 b/c 47°48'' 43°23' 180°0/h 180°0/h 180°0/h	uted 4 Whole 47 47 47 43 23 43 28 88 48 88 50 ore - Error alic Ta	ngle Maan- 47°47' 43°23' 179°23' 179°39' 03' 88°49' 03' 03'	Surveyers, J. Dee and R. Ree. Sept.22, '14. (2 Hours) Clear and warm. Vised Rev (10-FF, Steel Tape, No.481, Lkr.35. Though not needed in problem, noted the lengths of tapes by standard, 100.01 and 50.01 Ft, respectively. Measured each angle by chord method and checked by tangent method, using radius of 100 Ft with steel tape. In measuring LS, (nearly 50) the tangent method was applied to the bisected angle. Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each. After an angle was thus verified, a rapid but careful measurement was made with metallic tape, by chord method anly, using 50-Ft, radius- Used Tlagpoles For Distant and pins for clease targets. Used 5-place
6 " " 5 " " " " " " " " " " " " " " " "	Name Sin ± (6) Tan.(6) Sin ± (8) Sin ± (8) Tan.± (3) Sin ± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) C.8096 O.80999 Tang equi Asy23/3	Unctions Value 0-4050 0-3696 0-9450 0-9796 0-9796 0-9799 0-9799 Error Permi 50 I 21%1/3 44°25 0 weighter most	Com Half 23 53:5 21°41:5 44°23' 44°24'5 44°24'5 44°24' 44°25' 55 2 b/c 55 2 b/c 55 2 b/c 47°48'' 43°23' 180°0/h 180°0/h 180°0/h	uted 4 Whole 47 47 47 43 23 43 28 88 48 88 50 ore - Error alic Ta	ngle Maan- 47°47' 43°23' 179°23' 179°39' 03' 88°49' 03' 03'	Surveyers, J. Dee and R. Ree. Seph.22, '14. (2 Hours) (lear and warm. Vised Ree (WO-FF. Steel Tape, No-362, and Lufkin 50-Ff. Metall's Tape, No-362, and Lufkin 50-Ff. Metall's Tape, No-362, and lengths of tapes by standard, 100-01 and 50-01 Ff., respectively. Measured each angle by chord method and checked by tangent method, using radius of 100 Ff with steel tape. In measuring LS, (nearly 50') the tangent method was applied to the bisected angle. Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each. Affor an angle was thus verified, a rapid but careful measurement was made with metallic tape, by chord method anly, using 50-Ff. radius- Used flagpoles for distant and pins for close targets.
6 "" 5 "" "" "" "" "" "" "" "" "" "" "" "	Name Sin-(4) Sin-(4	Unctions Value 0-4050 0-3696 0-9450 0-9796 0-9796 0-9799 0-9799 Error Permi 50 I 21%1/3 44°25 0 weighter most	Com Half 23 53:5 21°41:5 44°23' 44°24'5 44°24'5 44°24' 44°25' 55 2 b/c 55 2 b/c 55 2 b/c 47°48'' 43°23' 180°0/h 180°0/h 180°0/h	uted 4 Whole 47 47 47 43 23 43 28 88 48 88 50 ore - Error alic Ta	ngle Maan- 47°47' 43°23' 179°23' 179°39' 03' 88°49' 03' 03'	Surveyers, J. Dee and R. Ree. Sept.22, '14. (2 Hours) Clear and warm. Vised Ree WO-FF. Steel Tare and Warm. Used Ree WO-FF. Steel Tare and Warm. Used Ree WO-FF. Steel Tare and Warm. Lufkin 50-Ft. Metall's Tape, No-411, Lkr:35- Though nat needed in problem, nated the lengths of tapes by shandard, 100-01 and 50-01 Ft., respectively. Messured each angle by chord method and checked by tangent method was applied to the biscered angle. Each angle was verified before proceeding to naxh, a difference of 2' being allow- ed in each. After an angle was thus verified, a rapid bu: careful mesurement was made with metallic tape, by chord method andy, using 50-Ft. radius. Used Flagpeles For distant and pins for close targets. Used 5-place table.
6 "" 5 "" "" Angle 6 8 5 Assign stee Angle (1 8 5 5 8 1 1 8	Name Sin ± (6) Tan.(6) Sin ± (8) Sin ± (8) Tan.± (3) Sin ± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) Tan.± (3) C.8096 O.80999 Tang equi Asy23/3	Unctions Value 0-4050 0-3696 0-9450 0-9796 0-9796 0-9799 0-9799 Error Permi 50 I 21%1/3 44°25 0 weighter most	Com Half 23 53:5 21°41:5 44°23' 44°24'5 44°24'5 44°24' 44°25' 55 2 b/c 55 2 b/c 55 2 b/c 47°48'' 43°23' 180°0/h 180°0/h 180°0/h	uted 4 Whole 47 47 47 43 23 43 28 88 48 88 50 ore - Error alic Ta	ngle Maan- 47°47' 43°23' 179°23' 179°39' 03' 88°49' 03' 03'	Surveyers, J. Dee and R. Ree. Sept.22, '14. (2 Hours) Clear and warm. Vised Rev (10-FF, Steel Tape, No.481, Lkr.35. Though not needed in problem, noted the lengths of tapes by standard, 100.01 and 50.01 Ft, respectively. Measured each angle by chord method and checked by tangent method, using radius of 100 Ft with steel tape. In measuring LS, (nearly 50) the tangent method was applied to the bisected angle. Each angle was verified before proceeding to next, a difference of 2' being allow- ed in each. After an angle was thus verified, a rapid but careful measurement was made with metallic tape, by chord method anly, using 50-Ft, radius- Used Tlagpales For Distant and pins for clease targets. Used 5-place

(c) Methods.—(1) Standardize the tape once. (2) Examine the field carefully and plan the survey. (3) Measure the required angles with tape. (4) Locate the perpendiculars. (5) Chain all necessary lines, and also take distances to feet of perpendiculars. Follow the form.

PROBLEM A12. AREA OF FIELD BY PERPENDICULAR METHOD.

(a) Equipment.—Five-place logarithms.

(b) Problem.—Calculate the area of the assigned field by the perpendicular method, using the data collected in Problem A11.

(c) Methods.—(1) Prepare form for calculations; transcribe data, and carefully verify transcript. (2) Calculate double areas of the several triangles by contracted multiplication, perpendicular method, preserving a consistent degree of precision. (3) Make the same calculations with logarithms, as a check. (4) Combine the verified results, as shown in the form.

PROBLEM A13. AREA OF FIELD BY THREE-SIDE METHOD.

(a) Equipment.—Five-place logarithms.

(b) *Problem.*—Calculate the area of the assigned field by the three-side method, using data collected in A11.

(c) Methods.—(1) Prepare form for calculation; transcribe data, and carefully verify transcript. (2) Calculate the areas of the several triangles by logarithms, three-side method, preserving proper units in the results. (3) Carefully review the calculations, and combine the verified results, as in the form.

PROBLEM A14. AREA OF FIELD BY ANGLE METHOD.

(a) Equipment.—Five-place logarithms.

(b) *Problem.*—Calculate the area of the assigned field by the "two sides and included angle" method, using the data collected in A11.

(c) Methods.—(1) Prepare form, transcribe data, and verify copy. (2) Calculate the double areas of the several triangles by contracted multiplication, angle method, preserving consistent accuracy in results. (3) Make same cal-

		<u> </u>					
	SUR Angle ABE EBD DBC ABd	VEY 01 Sin ½ A -2968 -7/31 -5347 -0888	FIELD $\frac{1}{2} A$ 17%6' 45°29'5 32°19'5 5°06'	A 34*32* 90*59*	C-D-E Proof /90 ¹ 10' /80°00' /0°10	WITN	TAPE · (DATA FOR AREA AND PLAT.) Head Chainman, A. Rose. Rear Chainman, J. Doe. Sept 25, 1/4 · (3 Hours) Cloudy & Cool- Used Re 100 Ft Steel Tape N=361, Locker #30 Standardized tope before only. Let Fell perpendiculars Aa, Bb and Be by First estimation continues & a head
		Øbserv'd Length Ft∙					First estimating positions of a, b and c, then erecting precise perpendiculare and shifting as required - Set pegs at points a, b and c.
	Sept-25 Tape Sept-26	99·99Z					A points a, b and c. Measured angles ABE, EBD and DBC with tape by chord method, 100 ft-radius, and checked by measuring angle be-
	Таре AB	99·980 336·83 465·07	-0.07 -0.09	336·76 464 ·9 8			tween AB and Bd (line CB prolonged) Sept-26,99 (2thurs) Drizzling & Cold- Chained each line carefully once-
1	DE EA	483·82 616·65 241·89	-0-J0 -0-J2 -0-05	483·72 616·53 241·84		ł	Sketch shows reduced values.
	BD	425-93 438-70 190-69	-0.09 -0.09 -0.04	425-84 438-61 190-65			A 33676 B 3844
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ļ		38]-49 265-90	- 0-08 - 0-05	38]•4] 265 [.] 85			E 8 616 53 D
(Сомт	UTATI	N OF	AREA	OF FI	ELD	Sept-27, 14. Computer, J-Doe. A-B-GD-E, PERPENDICULAR METHOD.
	Triangie	Line	Base, b Ft•	Altitude,a Ft.		Logar- ithms	Double Areas Sq. Ft. $Area = \frac{1}{2} ab$.
	ABE	BE Aə	4 25 · 84	190-65	38326 256	2-62925 <u>2-28024</u> 4-90949 (81 190)	Data From pp. Transcript checked 81 190 (Result to nearest 10 5q. Ft.)
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				81 187	1		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
BDE	De Bb	616-53	302-10	0]-203 184959 1233 62	2-78995 2-48015 5-27010 (186 250)	186 250	., .	. ,, ,, ,, ,,
BĊD	CD Bc	483-72	381•41		(184 500)	184 500 2)451 940	,, (Result	, ,, ,, ,, ,, ,, to nearest 0-00/Ac-)
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Use l sho	ng điv. wn in i	ision o. the app	r one o Vication	F the h oppos	nethods ite		<u>305</u> 24 <u>26</u>	5.1876

culations by logarithms, as a check. (4) Combine the checked results. Follow the form.

PROBLEM A15. AREA OF FIELD FROM PLAT.

(a) Equipment.—Drafting instruments, paper, etc., planimeter (as assigned).

(b) *Problem.*—Determine the area of the assigned field directly from the plat.

(c) *Methods.*—(1) Make an accurate plat of the field from the notes secured in A11, using a prescribed scale. (2) Determine the area of the field by resolving the polygon into an equivalent triangle. (3) Determine the area from the plat by the polar planimeter and by one of the following "home-made" planimeters: "bird shot " planimeter, " jack knife" planimeter, cross-section paper, parallel strip, weighing, etc. (4) Prepare on the plat a tabulated comparison of results secured by the several methods. (5) Finish the plat, as required.

PROBLEM A16. SURVEY OF FIELD WITH CURVED BOUNDARY.

(a) Equipment.—100-foot tape, 50-foot metallic tape, set of chaining pins, 2 plumb bobs, 4 flag poles.

(b) *Problem.*—Make survey with tape of an assigned tract having a curved boundary, collecting all data required for plotting the field and calculating its area.

(c) Methods.—(1) Standardize the tape once to nearest 0.01 foot. (2) Examine the tract carefully and plan the survey so as to secure a simple layout of base lines designed to give short offsets to the curved boundaries. (3) Locate the perpendiculars, if any, and chain all lines; on the curved sides, take offsets so as to secure a definite location, and as a rule take equal intervals on the same line. Follow the form.

PROBLEM A17. AREA OF FIELD WITH CURVED BOUNDARY.

(a) Equipment.--(No instrumental equipment required).

(b) *Problem.*—Calculate the area of the assigned field with curved boundary by "Simpson's one-third rule," using the data collected in Problem A16.

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					_		14 Compute		
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(c) Methods.-(1) Prepare form for calculation; transcribe data in convenient form for calculation, and carefully check copy. (2) Calculate the area of the polygon formed by the base lines, preferably by the perpendicular method. (3) Calculate the areas of the curved figures by "Simpson's one-third rule," which is as follows: "Divide the base line into an eren number of equal parts and erect ordinates at the points of division: then add together the first and last ordinates, twice the sum of all the other odd ordinates, and four times the sum of all the even ordinates: multiply the sum by one-third of the common distance between ordinates." (The field notes might have been taken with special reference to the rule, but it is better to take from the notes the largest cren number of equal segments, assuming the remaining portion to be trapezoid or triangle.) (4) Give signs to the several results by reference to the field sketch. and combine them algebraically to get the net area, as shown in the accompanying form.

PROBLEM A18. AREA OF FIELD WITH CURVED BOUNDARY FROM PLAT.

(a) Equipment.—Drafting instruments, paper, etc., planimeter (as assigned).

(b) *Problems.*—Determine the area of the field with curved boundary directly from the plat.

(c) Methods.—(1) Make an accurate plat of the field from the notes obtained in A16, using a prescribed scale. (2) Determine its area directly from plat by two methods mentioned in (3) of A15, other than those used in that problem. (3) Prepare on the plat a tabulated comparison of the results by the several methods. (4) Finish the plat, as required.

PROBLEM A19. PASSING AN OBSTACLE WITH TAPE.

(a) *Equipment.*—100-foot steel tape, set of chaining pins, plumb bobs, 4 flag poles.

(b) *Problem.*—Prolong an assigned line through an assumed obstacle by one method and prove by another, finally checking on a precise point previously established.

(c) Methods.—Given two hubs, A and B, 200 feet apart prolong line and establish C 200 feet from B: (1) by constructing a 200-foot square in one direction; and (2) by lay-

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Part <i>abe</i>	Dəta	a For C <i>le, Base</i>	lalcula† <i>≥ 290-'0</i> ,	ion of . A/t = /	Areas 1 <i>45[:]3</i>	WITH CURVED BOUNDARY Indicated Calculations Data From pp- Transcript Chec 2(290-0 × 145-3)	(• +Areas <i>ked•</i> 21068	-Areas
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Part abe bce coe	Dəta <i>Triang</i> : "	For C	= 404'7	ion of A/t = 1 n = 1 $\frac{9}{5}$	Areas 45'3 199'3 Pson's Ruie Ruie	WITH CURVED BOUNDAR' Indicated Calculations Data From pp. Transcript Chec $\frac{1}{2}(290.0 \times 145.3)$ $\frac{1}{2}(410.4 \times 267.8)$ $\frac{1}{2}(410.4 \times 267.8)$ $\frac{1}{2}(40.47 \times 199.3)$ $\frac{49}{2}[(0 + 9.5)$ $+2(21).437.4 \pm 407.4 \times 32.4)$ $+4(10.8 \pm 30.1 \pm 403.4 \times 33.4 \times 24.8)$ $\frac{1}{2}(3.5 \times 18.4)$	(• +Areas <i>ked</i> • 21068 56024	
Part abe bce coe	Dəta <i>Triang</i> : "	For C	= 404'7	ion of A/t = 1 n = 1 $\frac{9}{5}$	Areas 45'3 199'3 Pson's Ruie Ruie	wiTH CURVED BOUNDAR: Indicated Calculations Data From pp- Transcript Cirec. $\frac{1}{2}(290.0 \times 145.3)$ $\frac{1}{2}(418.4 \times 267.8)$ $\frac{1}{2}(404.7 \times 199.3)$ $\frac{49}{2}[(0+9.5)]$ +2[(2)1+37.4+407+32.4) +4[108+301+403+393+246] $\frac{1}{2}(9.5 \times 18.4)$ $\frac{1}{2}(9.5 \times 18.4)$	(• +Areas <i>ked</i> • 21068 56024	11375
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Part abe bce coe	Data Triang. 801-24	For C le, Base	= 404'7	ion of A/t = 1 n = 1 $\frac{9}{5}$	Areas 45'3 199'3 Pson's Ruie Ruie	wiTH CURVED BOUNDAR: Indicated Calculations Data From pp- Transcript Cirec. $\frac{1}{2}(290.0 \times 145.3)$ $\frac{1}{2}(418.4 \times 267.8)$ $\frac{1}{2}(404.7 \times 199.3)$ $\frac{49}{2}[(0+9.5)]$ +2[(2)1+37.4+407+32.4) +4[108+301+403+393+246] $\frac{1}{2}(9.5 \times 18.4)$ $\frac{1}{2}(9.5 \times 18.4)$	(• +Areas <i>ked</i> • 21068 56024	11375 87 6831
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Part abe bce coe Line B	Data Triang """"""""""""""""""""""""""""""""""""	For C $\frac{1}{10}$ For C 1	= 290'0, 7 = 290'0,	ion of A/t : = 1 A/t: = 1 $S = \frac{1}{942}$ $S = \frac{1}{100}$ $S = \frac{1}{1000}$ $S = \frac{1}{10000}$ $S = \frac{1}{10000}$ $S = \frac{1}{10000000000000000000000000000000000$	Areas 45'3 257'8 199'3 Pson's Rule Rule Rule Rule	wiTH CURVED BOUNDAR' Indicated Calculations Data From pp- Transcript Chec. $\frac{1}{2}(2900 \times 145\cdot3)$ $\frac{1}{2}(4104 \times 267\cdot8)$ $\frac{1}{2}(4047 \times 199.3)$ $\frac{19}{2}(0+9.5)$ +2(21)+374+4407+32.4) +4(108+301+403+393+246) $\frac{1}{2}(9.5 \times 18\cdot4)$ $\frac{1}{2}(31\cdot8+39.0)$ $+2(31\cdot8+39.0)$ $+2(19.5 \times 18\cdot4)$ $\frac{1}{2}(0+15\cdot5)$ $\frac{1}{2}(19.5 \times 22.5)$ $\frac{1}{2}(10+15\cdot0)$ $+2(10-4+20\cdot8)$ $+4(105-4-20\cdot8)$ $+4(105-4-20\cdot8)$ +4(105-4-20-8) +4((• +Areas <i>ked</i> • 21068 56024	11375 87 6831 152 1961
Part abe bce cde Line B	Data Triang """"""""""""""""""""""""""""""""""""	$\begin{array}{c} For C \\ Base \\ \hline \\ $	= 290'0, 7 = 290'0,	ion of A/t : = 1 A/t: = 1 5/942 / $1/94son 5'1 / 1/947/16$ / $1/94$	Areas 45'3 257'8 199'3 Pson's Rule Rule Rule Rule	wiTH CURVED BOUNDAR' Indicated Calculations Data From pp- Transcript Chec. $\frac{1}{2}(2900 \times 145\cdot3)$ $\frac{1}{2}(4104 \times 267\cdot8)$ $\frac{1}{2}(4047 \times 199.3)$ $\frac{19}{2}(0+9.5)$ +2(21)+374+4407+32.4) +4(108+301+403+393+246) $\frac{1}{2}(9.5 \times 18\cdot4)$ $\frac{1}{2}(31\cdot8+39.0)$ $+2(31\cdot8+39.0)$ $+2(19.5 \times 18\cdot4)$ $\frac{1}{2}(0+15\cdot5)$ $\frac{1}{2}(19.5 \times 22.5)$ $\frac{1}{2}(10+15\cdot0)$ $+2(10-4+20\cdot8)$ $+4(105-4-20\cdot8)$ $+4(105-4-20\cdot8)$ +4(105-4-20-8) +4((• +Areas <i>ked</i> • 21068 56024	11375 87 6831 152 1961
Part abe bce cde Line B	Data Triang """"""""""""""""""""""""""""""""""""	For C $\frac{1}{10}$ For C 1	= 290'0, 0, 0 = 1 = 290'0, 0, 0 = 1 = 100'0, 0, 0 = 100'0, 0, 0 = 100'0, 0	ion of A/t = 1 A/t = 1 Sim O T = 0 Sim O	Areas 45'3 257'8 199'3 Pson's Rule Rule Rule Rule	$ \begin{array}{l} \text{WITH CURVED BOUNDAR:} \\ \text{Indicated Calculations} \\ \frac{1}{2} \left(280 - 0 \times 145 \cdot 3 \right) \\ \frac{1}{2} \left(418 + 4 \times 267 \cdot 8 \right) \\ \frac{1}{2} \left(280 - 0 \times 145 \cdot 3 \right) \\ $	/- +Areas <i>ked</i> : <i>21068</i> <i>56024</i> <i>40328</i>	11375 87 6831 152 1961
Part abe bce cde Line B	Data Triang """"""""""""""""""""""""""""""""""""	For C $\frac{1}{10}$ For C 1	$\begin{array}{c} \text{alculat} \\ \text{alculat} $	ion of $A/t = 1$ A/t = 1 n = 1	Areas 45'3 257'8 199'3 Pson's Rule Rule Rule Rule	$ \begin{array}{l} \text{WITH CURVED BOUNDAR:} \\ \text{Indicated Calculations} \\ \text{Data From pp- Transaript Chec.} \\ \frac{1}{2}(290.0 \times 145.3) \\ \frac{1}{4}(418.4 \times 257.8) \\ \frac{1}{2}(418.4 \times 257.8) \\ \frac{1}{2}(10+9.5) \\ +2[211+37.4+407+32.4] \\ +4[10.8+30.1+40.3+39.3+246] \\ \frac{1}{3}(19.5 \times 18.4) \\ +2[31.8 + 39.0] \\ +2(13.8 \times 22.5) \\ \frac{1}{3}(210,50,50) \\ +2(18.4 \times 20.8) \\ +4(10.5 + 20.2 + 19.7)] \\ \frac{1}{3}(20(50,57.2) + (7.2 \times 14.3)] \\ \frac{20}{3}(28.8 + 36.5) \\ +2(14.8 + 14.7) \\ +4(10.0 + 15.0 + 13.2)] \end{array} $	1. +Areas ked: 21068 56024 40328	11375 87 6831 152 1961
Part abe bce cde Line B	Data Triang """"""""""""""""""""""""""""""""""""	For C $\frac{1}{10}$ For C 1	= 290'0, 0, 0 = 1 = 290'0, 0, 0 = 1 = 100'0, 0, 0 = 100'0, 0, 0 = 100'0, 0	ion of A/t : = 1 A/t: = 1 5/942 / $1/94son 5'1 / 1/947/16$ / $1/94$	Areas 45'3 257'8 199'3 Pson's Rule Rule Rule Rule	WITH CURVED BOUNDAR' Indicated Calculations Deta Frim pp- Transcript Chec. $\frac{1}{2}(290.0 \times 145.3)$ $\frac{1}{2}(410.4 \times 267.8)$ $\frac{1}{2}(40.47 \times 199.3)$ $\frac{1}{2}(0 + 9.5)$ +2(21.1 + 37.4 + 40.7 + 32.4) +4(10.8 + 30.1 + 40.3 + 39.3 + 24.6) $\frac{1}{2}(0 + 13.5)$ $\frac{1}{2}(31.8 + 39.0)$ +2(31.8 + 39.0) +2(31.8 + 39.0) +2(10.5 + 29.4 + 30.3)] $\frac{1}{2}(10.5 \times 22.5)$ $\frac{1}{2}(10.5 \times 22.5)$ $\frac{1}{2}(10.5 \times 22.5)$ $\frac{1}{2}(20(15.0 + 72.2) + (7.2 \times 143.5)]$ $\frac{1}{2}(20(15.0 + 72.2) + (7.2 \times 143.5)]$ $\frac{1}{2}(10.6 + 15.2)$ $\frac{1}{2}(10.6 + 15.2)$ $\frac{1}{2}(10.6 + 15.2)$]	1. +Areas ked. 21068 56024 40328 40328	11375 87 6831 152 1961
Part abe bce cde Line B	Data Triang """"""""""""""""""""""""""""""""""""	For C ke, $BaseFVEVVE$	$\begin{aligned} z_{20} = \frac{1}{2} \frac$	ion of $A/t = 1$ A/t = 1 S = 1	Areas 45'3 267'8 199'3 Resons Res	$ \begin{array}{l} \text{WITH CURVED BOUNDAR:} \\ \text{Indicated Calculations} \\ \text{Data From pp- Transaript Chec.} \\ \frac{1}{2}(290.0 \times 145.3) \\ \frac{1}{4}(418.4 \times 257.8) \\ \frac{1}{2}(418.4 \times 257.8) \\ \frac{1}{2}(10+9.5) \\ +2[211+37.4+407+32.4] \\ +4[10.8+30.1+40.3+39.3+246] \\ \frac{1}{3}(19.5 \times 18.4) \\ +2[31.8 + 39.0] \\ +2(13.8 \times 22.5) \\ \frac{1}{3}(210,50,50) \\ +2(18.4 \times 20.8) \\ +4(10.5 + 20.2 + 19.7)] \\ \frac{1}{3}(20(50,57.2) + (7.2 \times 14.3)] \\ \frac{20}{3}(28.8 + 36.5) \\ +2(14.8 + 14.7) \\ +4(10.0 + 15.0 + 13.2)] \end{array} $	(- +Areas ked. 21068 56024 40328 10328	11375 87 6831 152 1961 273
Part a be bce cde Line B Line C Line C	Data ng. " Bol-X Bit "B AN " S Color	For C ke, $BaseFVEVVE$	$\begin{array}{c} \text{alculat} \\ \text{alculat} $	ion of $A/t = 1$ A/t = 1 S = 1	Areas 45'3 267'8 199'3 Resons Res	wiTH CURVED BOUNDAR' Indicated Calculations Data From pp- Transcript Chec. $\frac{1}{2}(2900 \times 145\cdot3)$ $\frac{1}{2}(4104 \times 267\cdot8)$ $\frac{1}{2}(4047 \times 199\cdot3)$ $\frac{1}{2}(0+9.5)$ +2/(21)+37.4+407+32.4) +4/(108+30)+403+393+244) $\frac{1}{2}(9.5 \times 18\cdot4)$ $\frac{1}{2}(9.5 \times 18\cdot4)$ $\frac{1}{2}(0+15\cdot5)$ $\frac{1}{2}(21,8+39\cdot4+30\cdot3)$ $+2/(18\cdot6+39\cdot4+30\cdot3)$ $+2/(18\cdot6+39\cdot4+30\cdot3)$ $+2/(18\cdot6+39\cdot4+30\cdot3)$ $+2/(18\cdot6+50)$ $+2/(18\cdot6+50)$ $+2/(18\cdot6+50)$ $+2/(28\cdot6+5)$ +2/(2	/- +Areas ked. 21068 56024 40328 40328 1487 8 8 8 8	11375 87 6831 152 1961
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ing off a 200-foot equilateral triangle on the opposite side using pins to mark points thus established. (3) Prolong the line by each method to the hub D, 200 feet from C, and record discrepancies in line. (4) Interpolate a point at Con true line between B and D, and note errors of prolongation at C. Record as in the form.

PROBLEM A20. OBSTRUCTED DISTANCE WITH TAPE.

(a) Equipment.—100-foot steel tape, set of chaining pins, 2 plumb bobs, 4 flag poles.

(b) *Problem.*—Determine the distance between two assigned points through an assumed obstruction to both vision and measurement, using two independent methods, and finally chain the actual distance.

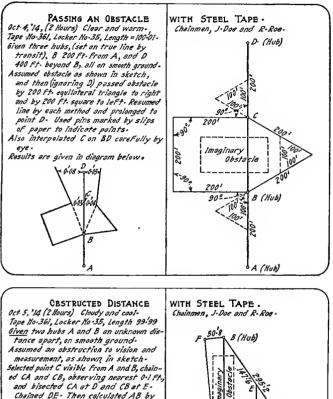
(c) Methods.—(1) Standardize the tape. (2) Determine the distance between the assigned points by constructing a line parallel to the given line, and equal or bearing a known relation to it. (3) Secure a second result by running a random line from one hub past the other so that a perpendicular less than 100 feet long may be let fall, measuring the two sides and calculating the hypothenuse. (4) After securing two results differing by not more than 1:1,000, chain the actual distance. Follow the form.

PROBLEM A21. RUNNING IN CURVE WITH TAPE.

(a) Equipment.—100-foot steel tape, 50-foot metallic tape, set of chaining pins, 2 plumb bobs, 3 hubs, 6 flat stakes, marking crayon, tacks, five-place table of functions.

(b) *Problem*.—Lay out two lines making an assigned angle with each other, and connect them with a prescribed curve by the "chord offset" method.

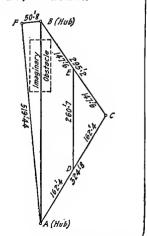
(c) Methods.—(1) Calculate the radius, R, for the given degree of curve, D. (2) Calculate the tangent distance, T, for the given radius, R, and angle of intersection, I. (3), Calculate the chord offset, d, and tangent offset, t, for the known radius, R, ehord, c and degree, D. (4) At the given point intersection (P. I.), A, lay off the given angle, I, by the chord method. (5) From the P. I. lay off T along the two tangent lines and locate point tangent (P. T.) and point curve (P. C.), setting hubs at P. C. and P. T., with guard stake at each hub. (6) Run in the curve, by chord offsets, beginning at P. C. and checking at P. T. Calling P.



doubling ED. 2607 x 2= 5214 Ren random line From A as close as practicable to obstruction so as to reduce BF to a minimum Let fall perpendicular BF from B on random line. Neasured BF and FA to nearast 0-1 Ft. Calculated hypothemuse AB^{-1}_{-1} $AB = \sqrt{50\sqrt{3} + 519} + 4^{-2} = 521^{10}_{-10}$

Finally, ofter securing the above results, chained the actual distance AB- The three results are sumarized below-

Method.	Obs-Dist-	Std-Cor-	Red Dist-
By similar triangles	521.4	-0-1	521-3
By right triangle	521.0	-0.1	520.9
By actual measurement	521·5	-0-1	521.4
Total range = 1	: 1040 .		



C. Station 0, establish Station 1 by laying off tangent offset, t, and chord, c Having one station on the curve, the next is located by prolonging the chord and forming an isosceles triangle having the chord offset as a base. Check on the P. T., noting the discrepancy of distance and line. Also establish the tangent again by tangent offset and observe the error of line. Follow the form.

PROBLEM A22. DISCUSSION OF ERRORS OF CHAINING

(a) Equipment.—(No instrumental equipment, unless further data are desired, in which case Problems A6, A7 and A8 may be assigned again).

(b) *Problem.*—Investigate the errors of linear measurement with the several kinds of chains and tape, with the view to determine practical working tests or coefficients of precision for actual use.

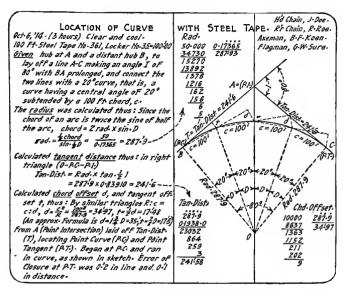
(c) Methods.—Assume that the conditions in Problems A6, A7 and A8 are practically constant in the same problem, and that the actual differences between observed lengths of the several segments when chained in opposite dirctions, represent the normal errors with the particular chain and chainmen; then tabulate: (1) the measured lengths of all possible segments of the chaining course, either from direct observation or by subtraction; (2) the actual errors or differences between the two results, giving signs; (3) the chaining ratios, l: d, and the decimal expressions of the same to six places; (4) the "coefficients of precision" for each case, calculated by formula, or more quickly, taken from the diagram in the chapter on errors of surveying; (5) the mean decimal chaining ratio and its equivalent; and (6) the mean coefficient of precision. Follow the form.

PROBLEM A23. TESTING (OR ESTABLISHING) AN OF-FICIAL STANDARD OF LENGTH.

(a) Equipment.—Standard tape (with certified length given), turnbuckle adjustments with holts, spring balance, standard steel rule graduated to 0.01 inch, 2 thermometers, 2 microscopes, strips of wood, a watch.

(b) *Problem.*—Make a series of ten observations with a standardized steel tape for the purpose of testing (or establishing) an official standard of length, observing the nearest 0.0001 foot. (The Bureau of Standards, Washington, D. C., will standardize a tape for a small fee.)

PROBLEMS.



						Oct-9,14 · Computer, J-Doe ·						
		Discu	5510N	OF ES	RORS							
Line	Direction	Observed	Differ-		Coef of							
	Chained	Length	ence, E		Precision							
		Ft.			(C), F†•							
A-B	Ĕ٠	484-58	E+ W	0.000052		Distances by Subtraction.						
B-A	W.		- 0.03	1:16150	0.014							
A-C		2003-7 9		0-000029		E-B 4794.96 E-C 3275.72 E-D 1287.83						
C-A	W-		- 0.06 1	1:33400	0.013	B-A 484.61 C-A 2003.85 D-A 3991.74						
A-D	E.	399/ 69		0.000012								
D-A			- 0.05	1:79830	0.008							
A-E	E٠	5279-48		0-000017		A-B 484-58 E-C 3275-72 A-B 484-50						
E-A	W.	<i>5279</i> •57		1:58660	0.012	B-C 1519-21 C-B 1519-24 B-D 3507-11						
B-C	E.	15/9-21		0.000019								
С-В	ψ.		- 0.03	1:50640	0.008							
B-D	Ë.	3507-11		0-000006		E-D 1287.83 A-B 484.58 A-C 2003.79						
D-B	W.	3507-13		1:175350	0.003	D-B 3507-13 B-E 4794-90 C-D 1987-90						
8-E	E.	4794·90		0-00001Z								
E-B		47 94 -96		1:78250	0.009	B-C 3275.72 A-E 5278.48 A-E 5279.4						
C-D	E.	1987-90		0-000005		E-D 1287-83 A-C 2003-79 A-D 3991-6						
D-C	W-	1987-89		1:198790	0.002	D-C 1987-89 C-E 3279-69 D-E 1287-75						
C-E	E.	3275-69		0.000009								
E-C	w.	3275-72		1:109190	0.005	Designating E + and W- (4th Column) it is						
D-E	<i>E</i> •	1287-79	1 1	0-000030		seen that the returning results (except						
E-D	w.	1287-73		1:32920		(-D) are greater. This is explained by						
		(L· in		0-060202 -0000202								
		100-Pt-	Meen = 1	1:49500	0.008							
		units)	E=cVI	ar. (C =	ħ	gradually decreased in length, causing						
			(See Dieg	in a	12	greater observed lengths.						

(c) Methods.—(If a new official standard is being established, one standard mark may be made permanent, and the precise distance taken to an approximate temporary point on the other bolt, the exact correction being applied after a sufficient number of results have been obtained. If the sun is shining, the tape should be protected by a wooden box or other covering throughout its length. Cloudy days or night time give best results. The observations should be made briskly so as to have slight range of temperature.

~													
/	Ŧ		Oct. 10, 14	4. Cloud	ly and	Cool.	Party: J.Doe, R.Roe, B.F.Keen, G.W. Sure.						
	LE	ST O	F 100-	-FT-S	TAND	ARD	UNIVERSITY .						
										period of			
1	Used .	Standal	rd Tape	No.41	7, marke	ed "U•5·W	XM.215,"	certifi	ed leng	th = 99.95	767 F:	ŕ.,	
1	at	62° F - и	vith 12	lb pull	, tape :	supporte	l, coeffic	ient of	expan.	sion ≈ 0·00	00061	•	
		r 2 "Bo	lt -7.	urnbucklø	#Hook	n' ATape	-East	Bolt	Turnbuck	le-			
2 COLERS COL													
۴	* Tot in * Wasping Spring Balance 100 Standard + Zero * Sast Bolt in Gasping												
P										tape supp			
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Ì.	the.	rmomete	ers plac	ed one	each a	t 33' and i	67'• Relea	sed pi	ill bet	ween obse	rvatio.	ns.	
-		_					_				<u> </u>	-	
No			emper			Temp.Cor.				Standard			
Ι.			At 67'				Ft.	ln.			9(0001)	95	
1	2:23		53.0	52°5	i <i>9.</i> 5	0.0058	99-9909			100.0006	/		
2		52.0	53.0	52.5	9.5	0.0058	99.9909			100-0007	0	0	
	:32	52.0	53.0	52.5	9.5	0.0058	99 <i>.9909</i>			100.0006		1	
4		52.0	53.0	52.5	9.5	0.0058	99.9909			100-0007	0	0	
5		52.0	52.5	52.2	9.8	0.0060	99 <i>•99</i> 07			100.0008	1		
6		52.0	52.5	52.2	9.8	0.0060	99•9907			100.0007	0	0	
7		52.5	57.5	52.5	9.5	0.0058	99·9909			100-0008	1	1	
8		52.5	52.0	52-2	9.8	0.0060	<i>99-99</i> 07	·122		100-0009	2	4	
	3:04	52.0	52.0	52.0	10.0	0.0061	99·9906			100.0007	0	0	
10	:08	52.0	52.0	52.0	10.0	0.0061	99.9906			100.0008		1	
^،	E,=0-6	$T_1 / \frac{\Sigma d^2}{2} = 0$	0-000057	En=	'== 0·00	0021	Mean = 100·0007 Σd2= 9 Length of Standard = 100·0007±0·00002 Ft.						
~		11-1		Ĭr.	2		Length of	standa	erd = 10	0.0007±0	.00002	Ft.	

If isolated standard monuments are used, their foundation should go below frost line, and the monuments should be located so as to suffer as little as possible from heaving. If the standard marks are indoors, the conditions are less difficult to control.)

(1) Arrange "bncksaw" or turnbuckle adjustments, each held firmly by a bolt dropped into a piece of gaspipe driven flush with surface of ground, with spring balance and tape lined up, as shown in sketch in accompanying form; place the two thermometers at the one-third points as nearly as possible under the actual conditions of the tape. (2) With four men in party, No. 1 sets end graduation precisely at one standard mark by means of screw adjustments and microscope; No. 2 sets balance at 12 pounds; No. 3 observes fraction at other standard mark by means of steel scale graduated to 0.01 inch, estimating to nearest 0.001 inch (say 0.0001 foot) by microscope; and No. 4 records all data, observes time to nearest minute, and temperature to nearest 0.1 degree. Nos. 1, 2 and 3 should lie flat. Release the tension between observations. Record and reduce as in the form.

PROBLEM A24. DETERMINATION OF CONSTANTS OF A STEEL TAPE.

(a) Equipment.—Steel tape and other articles named in preceding problem.

(b) *Problem.*—Determine coefficients of expansion and stretch of the assigned tape.

(c) Methods.--(See Problem E9.)

PROBLEM A25. MAKING A STANDARD WIRE TAPE.

(a) Equipment — Spring balance, thermometer, etc., as in A23, and a piece of piano or other suitable steel wire.

(b) Problem.—Make a 100-foot or other standard tape by graduating the wire with reference to the official standard.
 (c) Methods.—(To be devised by the student.)

PROBLEM A26. COMPARISON OF DIFFERENT MAKES AND TYPES OF CHAINS AND TAPES.

(a) Equipment.—Department equipment and collection of catalogs of representative instrument makers.

(b) *Problem.*—Make a critical comparison of the several types of chains and tapes made by different makers.

(c) Methods.—Study the different catalogs and prepare a systematic and concise report.

CHAPTER III.

THE COMPASS.

Description.—The magnetic compass consists of a line of sight attached to a graduated circular box, at the center of which is a magnetic needle supported on a steel pivot. The compass box is attached to a tripod or jacob staff by a ball and socket joint, and is leveled by means of the plate levels. The needle should be strongly magnetized and have an agate cap to receive the point of the hardened steel pivot. The dip of the needle is counter-balanced by a small coil of wire, which can be shifted as desired. The E and W points are reversed.

In Fig 10 are shown the usual types of magnetic compasses: (a) the vermer compass; (b) the plain compass;

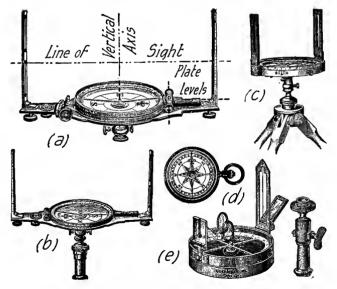
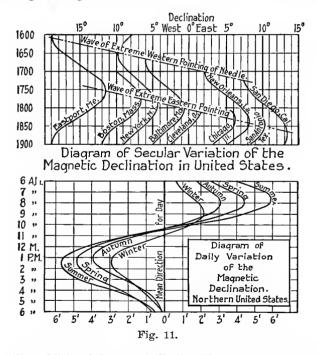


Fig. 10.-Types of Magnetic Compasses.

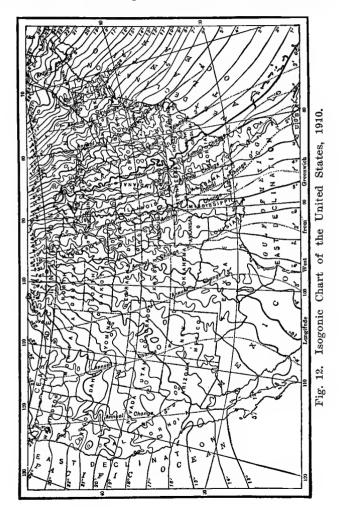
(c) the vernier pocket compass with folding sights; (d) the ordinary pocket compass; (e) the prismatic compass.

Declination of the Needle.—If the needle is allowed to swing freely, its magnetic axis will come to rest in the magnetic meridian. The horizontal angle between the magnetic meridian and the true meridian at any point is called the magnetic declination for that point. Imaginary lines joining points on the earth's surface having the same declination are called *isogonic lines*. The isogonic line joining the points of zero declination is called the *agonic line*. Fig. 12 is an isogonic chart of the United States. Of the three agonic lines on the earth's surface, one passes through Michigan, Ohio, etc.



(For additional data see bulletin of Department of Commerce, U. S. Coast and Geodetic Survey, entitled "Principal Facts of the Earth's Magnetism.")

Variation of the Declination.—The declination of the needle is not a constant at any place. The change or fluctuation is called the *variation* of the declination. The variations of the magnetic needle are of several kinds:



secular, daily, annual, lunar, and irregular variations que to The most important of these is the magnetic storms. secular variation which is illustrated in the upper diagram of Fig. 11 for a series of representative points in the United This diagram shows that the extreme range or States. swing of the needle is roughly 6° or 7°, and that the period of time between extreme positions is about a century and a half. Also that the wave of magnetic influence progresses across the continent alike in successive cycles. In 1900 the needle was at its extreme western position at Eastport, Me., and at its extreme eastern position at San Diego, Cal. The 3° East isogonic line passed through western Indiana, and was moving westward at the rate of about 4' per year. This rate of change was general throughout the central part of the United States, and is represented by the straight sections of the curve in the upper diagram of Fig. 11.

The daily variation of the magnetic declination is shown graphically in the lower part of Fig. 11, the scale being greatly magnified laterally. It is seen that the needle undergoes each day a vibration similar in a general way to the grand swing of three centuries or so shown in the upper diagram. The magnitude of the daily movement in northern United States ranges from 5' in winter to nearly 12' in summer time. The needle is in its mean daily position between 10 and 11 a. m. for all seasons. The diagram repneares the normal magnetic day, of which there are perhaps five or six per month.

Local Attraction.—The pointing of the needle is affected by the close proximity of magnetic substances, such

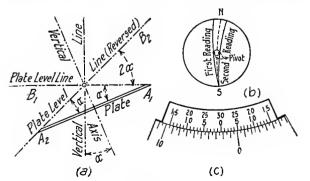


Fig. 13.

as iron ore, wire fences, railroad rails, etc. However, local attraction does not prevent correct work, provided back and fore sights are taken without change of magnetic conditions. It is therefore especially important to avoid disturbances of the needle by the chain, axe, passing vehicles, electric wires, etc., or by articles on the person of the observer, such as keys, knife, spectacle frame, wire in the hat rim, reading glass case, etc. Also the glass cover may become electrified by friction and attract the needle, in which case it may be discharged with the moistened finger, or by breathing on it.

The Vernier.—The vernier is an auxiliary scale used to read fractional parts of the divisions of the main scale or limb. Verniers are retrograde or direct, according as the divisions on the vernier are larger or smaller than those on the limb. The vernier used on compasses for the setting off of the declination is direct, and is usually of the type shown in (c) of Fig. 13. In reading a vernier of any kind, blunders may be avoided by first estimating the fraction by eye before noting the matched lines on the two scales.

USE OF THE COMPASS.

Use.—The compass is used: (1) to determine the bearings of lines; (2) to measure the angle formed by two lines; (3) to retrace old lines. The bearing of a line is the horizontal angle between the line and a meridian through one end of it. Bearings are measured from the north or south point 90° each way. The angle between two lines is the difference in their directions as indicated by the bearings. Having the true bearings of one side of a polygon, the true bearings of the others may be obtained by algebraic addition of the angles; or by using the declination vernier so as to read the true bearing direct on the fore sights.

Practical Hints.—Point the north end of the compass box along the line and read the north end of the needle. Protect the pivot from needless wear by turning the needle in about the proper direction before releasing it. Always lift the needle before disturbing the compass. Habitually obtain duplicate needle readings on each sighting. Read the needle by estimation to the nearest five minutes, that is, to the one-sixth part of one-half degree, which is the usual subdivision of the compass box. Care should be taken to avoid parallax in reading the needle.

ADJUSTMENTS AND TESTS.

Elementary Lines.—The *clementary lines* of the compass, shown in (a) of Fig. 10, are: (1) the line of sight; (2) the vertical axis; (3) the plate level lines.

The maker should see: (1) that the needle is strongly magnetized; (2) that the magnetic axis corresponds with the line joining the two ends; (3) that the metal in the compass box is non-magnetic; (4) that the line of sights passes through the center of graduation; (5) that the plates are perpendicular to the vertical axis; (6) that the zero of the vernier coincides with the line of sights.

The needle may be magnetized with a bar magnet or by putting it into the magnetic field of a dynamo. The metal of the compass box may be tested by reading the needle, then moving the vernier and noting if the needle has moved the same amount, this process being repeated at intervals around the full circle.

The Principle of Reversion.—In adjusting surveying instruments, the presence, direction and amount of the error are made evident by the *method of reversions* which doubles the apparent error. If there is no difference after reversion, there is no error.

Plate Levels.—To make the plane of the plate level lines perpendicular to the rectical axis.—Level up the instrument by means of the plate levels and reverse the compass box in azimuth, that is, turn it through a horizontal angle of 180°. Correct one-half the error, if any, by means of the adjusting screws at the end of the level tube, and bring the bubble to the center by the ball and socket joint. The reasons for this process are shown in (a) of Fig. 13.

Sights.—To make the plane of sights normal to the plane of the plate level lines.—With one sight removed and the instrument leveled, range in with the remaining sight two points as far apart vertically as possible, say on the side of a building. Reverse in azimuth and bring the bottom of the sight in range with the lower point; if the upper point is then in range, the sight is in adjustment. If not, correct one-half the error by putting paper under one side, or by filing off the other side. Repeat process for the other sight.

The Pivot.—To adjust the pirot to the center of the graduated circle.—Set the south end of the needle to read zero, and read the north end of the needle; reverse the compass box in azimuth, repeat the observations, and correct onehalf the difference between the two readings of the north end of the needle by bending the pivot, using the special wrench for the purpose. Turn the compass box 90° and repeat. See (b), Fig. 13.

The Needle.—To straighten the needle.—Having adjusted the pivot, set the north end of the needle to read zero and bend the needle so that the south end reads zero also. Turn the compass box and test for other graduations.

PROBLEMS WITH THE COMPASS.

PROBLEM B1. DECLINATION OF THE MAGNETIC NEEDLE.

(a) Equipment.—Surveyors' compass, flag pole, reading glass.

(b) *Problem.*—At a point on the true meridian determine the mean magnetic declination with the surveyors' compass.

(c) Methods.—(1) Set the compass over one point and a flag pole at another on the true meridian. (2) Lower the needle and sight at the flag pole carefully with the north end of the compass box to the front. (3) When the vibra-

1 2 3 4 M 5 6 7 M 8 M	Needle Mean Reading 1330/5 1330/5 1330/5 14330/5 14330/5 14330/5 14330/5 14330/5 14330/5	Time Mean P-M- 2:05 2:11 2:22 2:22 2:27 2:31 2:35 2:42	Och 12,14. (2 Hours) (slear and Cool- Used Gurley Compass M°26. (Need) e recently remagnetized), and Watch Set compass on true meridian with dec- linetion vernier set to read zero- Sighted at Flag pale set on meridian at a distance of 200 Ft, and read needle by estimation to 5 minutes (one sixth part of one-half degree), carefully avoiding parallax and
1 2 4 2 3 4 M 5 6 7 M 8 M	H330E H330E H330E H330E H335E H335E H335E H335E H335E	2:05 2:11 2:15 2:22 2:21 2:31 2:35 2:42	recently remagnetized), and Watch Set compass on true meridian with dec- lination vernier set to read zero- Sighted at Flag pole set an meridian at a distance of 200 Fr. and read needle by estimation to 5 minutes (one sixth part of ane-half degree),
2 3 4 M 5 6 M 8 M	N3355 N330/5 N330/5 N3355 N3355 N3355 N3355 N33575 N33575	2:11 2:15 2:22 2:21 2:31 2:35 2:42	Set compass on true meridian with dec- lination vernier set to read zero Sighted at Flag poleset on meridian at a distance of 200 Fr. and read needle by estimation to 5 minutes (one sixth part of ane-half degree),
3 / / / / / / / / / / / / / / / / / / /	N330/F N330/F N335/F N335/F N335/F N335/F N330/F	2:15 2:22 2:21 2:31 2:35 2:42	lination vernier set to raad zero- Sighted at Flag poleset on meridian at a distance of 200 Ft-, and read needle by estimation to 5 minutes (one sixth part of one-half degree),
4 1. 5 1. 6 1. 8 1.	4330'E 4335'E 4335'E 4335'E 4335'E 4330'E	2:22 2:27 2:31 2:35 2:42	Sighted at Flag pole set an meridian at a distance of 200 ft, and read needle by estimation to 5 minutes (one sixth part of ane-half degree),
5 M 6 M 7 M	H-335'E. H335'E. H335'E. H330'E.	2:21 2:31 2:35 2:42	a distance of 200 ft+, and read needle by estimation to 5 minutes (one sixth part of one-half degree),
6 /. 7 /. 8 /	N335'E N335'E- N330'E-	2:31 2:35 2:42	needle by estimation to 5 minutes (one sixth part of one-half degree),
7 1	4335'E- 1.330'E-	2:35 2:42	(one sixth part of one-half degree),
8 1	1.330'E.	2:42	
			carefully avoiding parallax and
9 1	W. 3"25'E		
	10.00 20	2:48	magnetic disturbances Observed
10 1	H335'E H333'E	2:54 2:30	time to nearest minute.
			Disturbed needle by lifting it from
			pivot and verified sighting; then
Yote:	Assuming that	the magnetic	
	ditions are no	mal for the	day, recread the needle.
	the correction	For daily var.	stion Continued the process until ten consec
	by Diagram of	Daily Variation	is utive readings, having a maximum
	3 minutes Wes	, which added	to range of not more than ten min-
	the mean give	N.3'36'E as	the sites, were obtained.
	most probable		
	nation For thi	particular in	stru-
	ment.		

tions of the needle have ceased, move the vernier by means of the tangent screw so that the north end of the needle reads zero, and check the sighting of the compass. (4) Read the declination on the vernier to the nearest minute. (5) Lift the needle, verify the zero needle reading and the sighting, read the vernier and record; repeat the process until ten satisfactory consecutive values of the declination are obtained. Observe the time of each reading to the nearcst minute. (6) Correct the mean of the ten values for daily variation by reference to the diagram, Fig. 11, using the mean time. Record and reduce the data as in the form. (Note that the values in the form were obtained by estimating the nearest five minutes. Which is better? Try both if time allows.)

PROBLEM B2. ANGLES OF TRIANGLE WITH COMPASS.

(a) Equipment.—Surveyors' compass, two flag poles, reading glass.

(b) *Problem.*—Measure the angles of a given triangle with the surveyors' compass.

(c) Methods.—(1) Set the compass over one of the vertices of the triangle and a flag pole behind each of the other two. (2) Lower the needle and sight at one of the flag poles carefully, with the north end of the box to the front. (3) When the vibrations have ceased, read the north end of the needle to the nearest five minutes by estimation. (4) Lift the needle, verify the sighting and also the reading. (5) Turn the compass box to the other point and determine the bearing, as before. The required angle is the difference between the two hearings. (6) Measure the other two angles in like manner. The error of closure must not exceed 5 minutes. Follow the form.

PROBLEM B3. TRAVERSE OF FIELD WITH COMPASS.

(a) Equipment.—Surveyors' compass, 2 flag poles, engineers' chain, set of chaining pins.

(b) *Problem.*—Determine the bearings of the sides of an assigned field with the surveyors' compass and measure the lengths of the sides with an engineers' chain.

(c) Methods.—(1) Set the compass over one of the corners of the field which is free from local attraction, and set off the declination with the vernier. (2) Take back sight on the last point to the left and fore sight to the next point

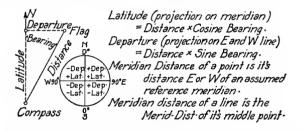
		OF TI		E 5-6	-8	WITH SURVEYORS	COMPASS
Station 5	5-6	Observed Bearing <i>5:83 15W</i>	Angle			Observers, R·Roe Oct·13,14·(2Hours, Used Gurley Comp	ass, Locker Nº 26.
" 8	5-8 8-5	5-540'H N-540'E	77°35'			Each bearing wa	s observed in eedle being dis-
"	8-6	H-49°05W	54°45'			turbed and the	sighting verified
6,,		H49°00'E H83°15'E	470451			between readi	95.
			180°05'			(Discrepency not t	o exceed 5 minutes.)
						6 4	A S S
	3						854 455 8
		·	·		L	L	
Station		RSE O Observed				WITH COMPASS AN	D CHAIN .
Station	Líne	Observed Bearing	Interior Angle	Adjusted		Observers : J.Doe a Oct.16,'14 · (3 Hours)	R. Roe. Clear & Windy
Station A	Líne <i>A-E</i>	Observed Bearing <i>5-60 301</i>	Interior Angle <i>93°15'</i>	Adjusted Bearing	Distance Ft•	Observers : J·Doe d Oct·I6,'I4 • (3 Hours) Used Gurley Compa	R•Roe∙ Clear & Windy ss. Locker Nº24•
	Líne <i>A-E</i> <i>A-B</i> <i>B-A</i>	0bserved Bearing 5-60 [°] 30W 5-32 [°] 45/F N-33 [°] 05 W	Interior Angle <i>93°15'</i> <i>190°20'</i>	Adjusted Bearing <i>5:32%45E</i>	Distance Ft• <i>336•5</i>	Observers : J-Doe d Oct-16,'14+ (3 Hours) Used Gurley Compa Made needle read d true north by se.	R.Roe Clear & Windy ss, Locker Nº24 ero when pointing tting off declination
A B	Líne <i>A-F</i> <i>A-B</i> <i>B-A</i> <i>B-C</i>	0bserved Bearing 5-60 [°] 30W 5-32 [°] 45/E N-33 [°] 05 [°] W N-43 [°] 25/E	Interior Angle <i>93°15'</i> <i>190°20'</i>	Adjusted Bearing	Distance Ft• <i>336•5</i>	Observers : J+Doe d Oct-16, ¹ /4+ (3 Hours) Used Gurley Compa Made needle read true north by se with vernier on d	R·Roe. Clear Æ Windy ss, Locker №24 tero when pointing
A B C	Line <i>A-F</i> <i>A-B</i> <i>B-A</i> <i>B-C</i> <i>C-B</i> <i>C-D</i>	Observed Bearing 5-60°30M 5-32°45/E N33°05W N 43°25/E N 43°25/E N 43°27/W 5-81°35′W	Interior Angle 93°15' 190°20' 55°05'	Adjusted Bearing <i>5:32%45E</i>	Distance Ft• <i>336•5</i> <i>464•6</i>	0bservers : J-Dae a Oct-16,14 - (3 Hours) Used Gurley Compa Made needle reed 2 true north by se, with vernier on a M3436/E- Read bearings wi	R.Roe. Clear & Windy ss, Locker Nº24. tero when pointing tring off declination eclimation arc of th N. End of Compass.
A B	Line <i>A-F</i> <i>A-B</i> <i>B-A</i> <i>B-C</i> <i>C-B</i> <i>C-D</i> <i>D-C</i>	Observed Bearing 5-60°30W 5-32°45/E N33°05 W N43°25/E N43°25/W 581°35′W N81°35′E	Interior Angle 93°15' 190°20' 55°05' 103°55'	Adjusted Bearing <i>5:32*45E</i> <i>5:43*05*E</i> 5:81*50*W	Distance Ft• <i>336·5</i> <i>464·6</i> <i>483·3</i>	Observers : J-Doe a Oct-16, '14 - (31 Auros) Used Gurley Compa Made needle read : true north by se with vernier on a 1: 3*36/E- Read bearings wi toward the forw	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C	Line <i>A-F</i> <i>A-B</i> <i>B-A</i> <i>B-C</i> <i>C-B</i> <i>C-D</i> <i>D-C</i> <i>D-E</i> <i>E-D</i>	Observed Bearing 5-60 30M 5-32 45E N 43 25E N 43 25E N 43 25E N 43 25E N 43 25E N 22 20M 5-22 20M 5-22 20M	Interior Angle 93°15' 190°20' 55°05' 103°55'	Adjusted Bearing 5:32 ^{:4} 355 5:43 [:] 855'5 5:81 [:] 50'W N:22 [:] 05'W	Distance Ft• <i>336·5</i> <i>464·6</i> <i>483·3</i> <i>616·0</i>	0bservers : J-Dae a Oct-16,14 - (3 Hours) Used Gurley Compa Made needle reed 2 true north by se, with vernier on a M3436/E- Read bearings wi	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C D	Line <i>A-F</i> <i>A-B</i> <i>B-A</i> <i>B-C</i> <i>C-B</i> <i>C-D</i> <i>D-C</i> <i>D-E</i>	Observed Bearing 5-60 30M 5-32 45 7 N 43 25 N 43 25 N 43 20 M 5 81 35 W N 81 35 F N 22 20 M	Interior Angle 93°15' 190°20' 55°05' 103°55'	Adjusted Bearing <i>5:32*45E</i> 5:43*05 [*] E 5:81*50 [*] W	Distance Ft• <i>336·5</i> <i>464·6</i> <i>483·3</i> <i>616·0</i>	Observers : J. Doe a Oct-IG'14. (3 Hours) Used Gurley Comps Nade needle read J true north by se with vernier on o N:3°36'E- Read bearings wi toward the Forw read N- End of N	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C D E	Line <i>A-F</i> <i>A-B</i> <i>B-A</i> <i>B-C</i> <i>C-B</i> <i>C-D</i> <i>D-C</i> <i>D-C</i> <i>D-C</i> <i>D-E</i> <i>E-D</i> <i>E-A</i>	0bserved Bearing 5-60 ³ 014 5-32 ⁴ 55 173 ⁵ 25 1743 ² 25 1743 ² 25 1743 ² 5 175 175 175 175 175 175 175 175 175 17	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05'	Adjusted Bearing 532455 543055 5-8145014 5-8145014 8-2240514 14604255	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Observers : J-Doe a Oct-16, '14 - (31 Auros) Used Gurley Compa Made needle read : true north by se with vernier on a 1: 3*36/E- Read bearings wi toward the forw	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C D E See ca on	Line A-F A-B B-A B-C C-B C-D D-C D-C E-D E-A Iculation PP	0bserved Bearing 5-60 30M 5-32 45E N33 65 M 143 252 N43 20 M 5-81 35 M N-81 35 E N-22 70M 5-82 70E N-60 90E	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05' itudes	Adjusted Bearing 532455 543°05'5 5-81°50'W K22°05'W K60°25'5 9nd' depa	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Observers : J. Doe a Oct-IG'14. (3 Hours) Used Gurley Comps Nade needle read J true north by se with vernier on o N:3°36'E- Read bearings wi toward the Forw read N- End of N	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C D E See ca on	Line A-F A-B B-A B-C C-B C-D D-C D-C E-D E-A Iculation PP	0bserved Bearing 5-60 ³ 014 5-32 ⁴ 55 173 ⁵ 25 1743 ² 25 1743 ² 25 1743 ² 5 175 175 175 175 175 175 175 175 175 17	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05' itudes	Adjusted Bearing 532455 543°05'5 5-81°50'W K22°05'W K60°25'5 9nd' depa	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Observers : J. Doe a Oct-IG'14. (3 Hours) Used Gurley Comps Nade needle read J true north by se with vernier on o N:3°36'E- Read bearings wi toward the Forw read N- End of N	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C D E See ca on	Line A-F A-B B-A B-C C-B C-D D-C D-C E-D E-A Iculation PP	0bserved Bearing 5-60 30M 5-32 45E N33 65 M 143 252 N43 20 M 5-81 35 M N-81 35 E N-22 70M 5-82 70E N-60 90E	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05' itudes	Adjusted Bearing 532455 543°05'5 5-81°50'W K22°05'W K60°25'5 9nd' depa	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Observers : J. Doe a Oct-IG'14. (3 Hours) Used Gurley Comps Nade needle read J true north by se with vernier on o N:3°36'E- Read bearings wi toward the Forw read N- End of N	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C D E See ca on	Line A-F A-B B-A B-C C-B C-D D-C D-C E-D E-A Iculation PP	0bserved Bearing 5-60 30M 5-32 45E N33 65 M 143 252 N43 20 M 5-81 35 M N-81 35 E N-22 70M 5-82 70E N-60 90E	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05' itudes	Adjusted Bearing 532455 543°05'5 5-81°50'W K22°05'W K60°25'5 9nd' depa	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Observers : J. Doe a Oct-IG'14. (3 Hours) Used Gurley Comps Nade needle read J true north by se with vernier on o N:3°36'E- Read bearings wi toward the Forw read N- End of N	R.R.a. Clear & Windy ss, Lacker Nº24. tring off declination eclination arc of th N. End of Compass erd station and
A B C D E See ca on	Line A-F A-B B-A B-C C-B C-D D-C D-C E-D E-A Iculation PP	0bserved Bearing 5-60 30M 5-32 45E N33 65 M 143 252 N43 20 M 5-81 35 M N-81 35 E N-22 70M 5-82 70E N-60 90E	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05' itudes	Adjusted Bearing 532455 543°05'5 5-81°50'W K22°05'W K60°25'5 9nd' depa	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Observers : J. Joe a Oct-IG, VA-IS Hours, Used Guriey Comps Nade needle read J true north by se with vernier on o H. 3°36/E- Read bearings wi toward the forw read H- End off	R.Roe. Clear & Windy ss, Locker Nº24. tero when pointing ting off declination eclination arc of th N. End of Compass ard station and Needla. N S N S N S N S N S N S N S N S N S N S N S N S
A B C D E See ca on	Line A-F A-B B-A B-C C-B C-D D-C D-C E-D E-A Iculation PP	0bserved Bearing 5-60 30M 5-32 45E N33 65 M 143 252 N43 20 M 5-81 35 M N-81 35 E N-22 70M 5-82 70E N-60 90E	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05' itudes	Adjusted Bearing 532455 543°05'5 5-81°50'W K22°05'W K60°25'5 9nd' depa	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Allowable error of	R. Roe. Glear & Windy ss, Lacker Nº24. tero when pointing ting off declination eclination arc of th N. End of Compass erd station and Needla. N S Closure = 0°101.
A B C D E See ca on	Line A-F A-B B-A B-C C-B C-D D-C D-C E-D E-A Iculation PP	0bserved Bearing 5-60 30M 5-32 45E N33 65 M 143 252 N43 20 M 5-81 35 M N-81 35 E N-22 70M 5-82 70E N-60 90E	Interior Angle 93°15' 190°20' 55°05' 103°55' 97°30' 540°05' itudes	Adjusted Bearing 532455 543°05'5 5-81°50'W K22°05'W K60°25'5 9nd' depa	Distance Ft• 336•5 464•6 483•3 6/6•0 24/.6	Observers : J. Joe a Oct-IG'14. (3Hours) Used Gurley Compa Nade needle read 1 true north by se. with vernier on o N.3'36'E. Read bearings with toward the Forw read II. End of Allowable error of Chained each line	R.Roe. Clear & Windy ss, Locker Nº24. tero when pointing ting off declination eclination arc of th N. End of Compass ard station and Needla. N S N S N S N S N S N S N S N S N S N S N S N S

to the right, following the methods used in Problem B2. (3) Repeat this process for the remaining corners of the polygon taken in succession to the right. (4) Chain the sides of the field to the nearest 0.1 foot by estimation. (5) Compare the chain with standard. (6) From the observed bearings compute the interior angles of the field, and the true bearings of the sides. The angular error of closure must not exceed 10 minutes for a five-sided field. Record and reduce data as in the form.

PROBLEM B4. AREA OF FIELD WITH COMPASS.

(a) Equipment.—Five-place logarithms.

(b) *Problem.*—Compute the area of the assigned field by means of latitudes and departures.



(c) Methods.-(1) Prepare forms for calculations; transcribe data, and carefully verify copy. (2) Compute latitudes and departures by contracted multiplication, preserving results to the nearest 0.1 foot. (3) Make the same calculations by logarithms, as a check. (4) Determine the actual linear error of closure. (5) Determine the permissible error of closure (see chapter on errors of surveying). (6)If consistent, distribute the errors in proportion to the several latitudes and departures, respectively, repeating the additions as a check. (7) Transcribe field notes and adjusted latitudes and departures, and verify transcript. (8) Calculate the meridian distances of the several stations and (9) Calculate the latitude coordinates. lines. (10) Calculate the partial trapezoidal areas by multiplying the meridian distances of the lines by the respective latitudes, preserving consistent accuracy, and observing algebraic signs. (11) Determine the area by taking the algebraic sum of the partial areas. Reduce to acres, and correct for standard.

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\frown						Oct-17, 14 Data Fro	4 Computer, J.Doe. Im pp. Transcript O.K.
COMF	ASS TI	AVERS	EOF	FIELD	A-B-C-D		UDES AND DEPARTURES
Line	Adjusted	Observed	Compu	tation	oF Lati	tudes.	Computation of Departures.
	Bearing	Distance	Multipli-	Logar-	Computed	Lat Adjusted	Muitipli- Logar- Computed Dep Adjusted
		Ft-	cation (Lat=Dist				cation ithms Departure Cor Departure (Dep=DistX Sin Bq.) Ft. Ft. Ft.
AB	5.32 45 E		336.5	2.52698		-0.2 5.2828	
			26920	<u>9-92481</u>			16825 9-73318
			283.01	2.45180			30 2.26016 182-03 (182-04)
				(283.01)			(182-04)
BC	543°05'E	464.6			5.339.3	-0.2 5.339.1	
			32522 1334 14	<u>9-86353</u> 2-53061			27876 3717 139 7.50154
			339.32	(339.32)			3/7.35 (3/7.35)
60	58150W	483-3	483.3 5024/-0		5.68.6	0.0 5. 68.6	
			1833 1933	9.15245			43497 3866 9.99557
]	97	2.83667			+35 39 2.67979
	.,		68-65	(68-65)			+78.40 (478.40)
DE	H-22 05W	616.0	6/6.0 <u>+6629.0</u> 55440		N 570-8	+0.3 N.571.1	59573-0 2.78958 W-231.6 -0.1 W.231.5
	1		1232	9.96691			18480 4312 306 236472
1		i .	37	2·75649 (570·81)			305 35 2-36472
EA	N.60 25'F	241.6	570-81 241-6 563940		N. 119.3	+0.1 N. 119.4	
		2142.0	963940 9664		1.690.1		19320 9.93934 E.709.5 +02 E.709.7
	ibution el	Error	72	2.07655	5.690.9	-44 5-690.5	217 2.32244 W.710.0 -0.3 W.709.7
Líne AB	Lat. 3 102	210-0	119:21			0.8 0.0	
	3 0.2	3 0-1	1		OFC		See Diagram) Jap
DE	6 0.3	5 02				YLZ+DZ	Permissable Error = $\frac{3ap}{10.000}$ = $\frac{3 \times 5 \times 2142}{5}$ = 3.2 Ft.
5	14 0.8	72 03	I	= 1.9	+0.5" =	0.9 FF.	= 10000 = 3.2 Ft.

$\ $	- 1						Oct. 17.1	4. 0	omputer	J-Doe.		-
								om pp.		nscript		
						LD A-E						
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Follow the form. (12) Make plat of field, using total rectangular coordinates, and checking by polar planimeter.

PROBLEM B5. ADJUSTMENT OF THE COMPASS.

(a) Equipment.—Surveyors' compass, adjusting pin, small screw driver.

(b) *Problem.*—Make the necessary tests and adjustments of the surveyors' compass.

(c) Methods.—Observe the following program: (1) test the magnetism of the needle; (2) test the metal of the compass box; (3) test and adjust the plate levels; (4) test the sights; (5) test the pivot; (6) test the needle.

PROBLEM B6. COMPARISON OF DIFFERENT MAKES AND TYPES OF COMPASSES.

(a) Equipment.—Department equipment, catalogs of representative makers of compasses.

(b) *Problem.*—Make a critical comparison of the several types of compasses.

(c) Methods.—Examine the department equipment and study the several catalogs carefully, noting the characteristic features, prices, etc. The following items, at least, should be included in the tabulated report: name of instrument, length of needle, length of alidade, vernier, tripod, weight, price, etc.

CHAPTER IV.

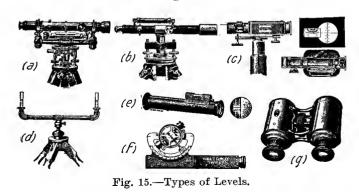
THE LEVEL.

Description.—The engineers' level consists of a line of sight attached to a bubble vial and a vertical axis. Two types of level, the wye and dumpy, Fig. 14, are used by engineers. In the former the telescope rests in Y-shaped supports, from which it may be removed. In the dumpy level the telescope is fixed. The dumpy is a favorite with British



Engineers' Wye Level. Fig. 14.

Dumpy Level.



57

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and the wye level with American engineers. (The dumpy level with erecting eye-piece has been adopted as standard by the Division of Valuation, Interstate Commerce Commission.) The two types differ chiefly in the methods of adjustment. A third type, not shown in the cuts, is called the level of precision because of its use solely for work of extreme refinement.

In Fig. 15 are shown: (a) an architects' or builders' level of the wye type; (b) a road builders' level of the dumpy type; (c) a reconnaissance level with a decimal scale for reading horizontal distances direct; (d) a water level sometimes used in locating contours; (e) a Locke hand level; (f) a clinometer; (g) a binocular hand level.

THE TELESCOPE.

Principles.—The telescope used in the engineers' level and transit, shown in section in Figs. 16 and 22, consists of an objective or object glass which collects the light and forms an image in the plane of the cross-hairs, and an ocular or eyepiece which magnifies the image and cross-hairs. The cross-hairs are thus at the common focus of the oujective and eyepiece. The principle of this type of telescope, both optically and mechanically, may be illustrated by the photographic camera if cross lines be ruled on the ground glass focusing plate and a microscope be used in viewing the image formed by the lens. Telescopes of the above class are called measuring telescopes, while those of the opera glass type are termed secing telescopes. The latter have no real image formed between the object glass and eyepiece.

Line of Collimation.—The telescope of the level or transit may be represented by a line, called the *line of collimation*, which joins the optical center of the objective and the intersection of the cross-hairs. The optical center is a point such that a ray of light passing through it emerges from the lens parallel to its original direction. The line of collimation is independent of the eyepiece.

Objective.—The objective is a double convex or planoconvex lens. In all good telescopes the objective is compound, that is, made up of two lenses, with the view to correct two serious optical defects to which a simple lens is subject. These defects are called *chromatic aberration* and *spherical aberration*.

Chromatic aberration is the separation, by the objective, of white light into its component colors. A lens which is

Optical Center Intersection of of Objective Cross Hairs Line of Collimation Tangent Line of Level Tube Evepiecei Object Glass (Magnifies image (a) (Forms image in plane and cross-hairs) of cross-hairs) ···> Vertical Axis Vertical Axise Clip Ring Clip~. + Ring Line of Collimation Tanaent to Bubble Wvez AWVP Azimuth Screws ···> Wve Nuts Level Bar Altitude Screws *(b)* Foot Screws -Rings Unequal Rings Equal-Line of Collimation (Axis of Cone) Line of Collimation (Axis of Cylinder) Element of Rings Bottom Bottomy Element of Rings <u>Tangent</u> to Bubble Tangent to Buhhle (d) (C) True Line of Collimation True Line of Collimation Fake Line of Col False Line of Col Bubble Line. True Level Line From Target to Target (Base of Cone) to Length of Fore Sight -Length of Back Sight equal True Level Line Through Top of Peg. (e) Correct Levels by Equal Sights. TrueLine of Collimation True Line of Collimation False Line of Collimation Erroi False Line of Collimation fod True Level Line Rod True Level Line Rod-S Peq Peq Peg Say 400' Sav 400 6av AO Ist Method. 2nd Method.

free from this defect is called achromatic. A telescope is tested for the chromatic defect by focusing on a bright object, such as a piece of paper with the sun shining on it, and noting the colors on the edge of the object and especially at the edge of the field of view as the focus is slightly deranged. Yellow and purple are the characteristic colors indicating good qualities in the lens.

Spherical aberration is a defect which prevails to a serions extent in a simple lens having spherical surfaces. It is due to a difference in the focal distance for different concentric or annular spaces of the objective, so that the plane of focus for rays passing through the outer edges of the lens is different from that of the middle portion. A telescope is tested for this defect by focusing on a well defined object, such as a printed page, with the rays of light cut off alternately from the middle and the edge of the lens. This is best done by means of a circular piece of paper with a small round hole in it.

As a rule, the object glass in good levels and transits consists of a double convex lens of crown glass fitted to a concavo-convex or a plano-concave lens of flint glass, the former to the front. The defects described above are avoided through the different dispersive and refractive powers of the two kinds of glass, and by grinding the surfaces of the two lenses to the proper curvatures.

Eyepiece.—As in the camera, the image formed by the objective is inverted, so that if a simple microscope be used as an eyepiece, the observer sees objects inverted. Such an eyepiece is commonly used on the dumpy level, as shown in Fig. 14. This form of eyepiece consists of two planoconvex lenses with their convex sides facing each other. The form of eyepiece most used in American instruments is the erecting eyepiece in which two plano-convex lenses replace each of the two in the simpler form. The erecting eyepiece is much longer than the simple one, as may be seen at a glance in Fig. 14. While the simple eyepiece causes a little confusion at first, owing to the inversion of objects, it is much superior to the erecting eyepiece in the matter of clearness and illumination.

The chief inherent defect in the eyepiece is a *lack of flatness* of the field. A single lens usually causes a distortion or curving of straight lines in the image, especially towards the edge of the field. A telescope is tested for this defect by observing a series of parallel right lines, preferably a series of concentric squares, which fill the entire field of view.

In the best achromatic eyepieces, one or more of the separate lenses may be compounded, the curvatures being such as to eliminate the color defect and give rectilinear qualities to the lens or combination of lenses.

Definition.—The definition of a telescope depends upon the finish and also the accuracy of the grinding of the curved surfaces of the lenses. It may be tested by reading the time on a watch or a finely printed page at some distance from the instrument.

Illumination.—Illumination and definition are apt to be confused. Poor definition causes indefinite details, while poor illumination causes faintness in the image. The latter may be tested about dusk, or in a room which can be gradually darkened, and can be best appreciated if two telescopes of different illuminating qualities be compared.

Aperture of Objective.—The aperture or effective diameter of the objective is determined by moving the end of a pencil slowly into the field and noting the point where it first appears to the eye when held say 8 or 10 inches back from the eyepiece. The process should be repeated in the reverse order. The annular space is deducted from the actual diameter to obtain the real aperture.

Size of Field.—The field of the telescope is determined by noting the angle between the extreme rays of light which enter the effective aperture of the objective. With the transit telescope, the limiting points may be marked on the side of a building and the angle measured directly with the plates; or with either level or transit the angle may be calculated from the measured spread in a given distance. For simplicity, a distance of 57.3 feet may be taken, and the result reduced to minutes.

Magnifying Power.—The magnifying power of a telescope is expressed in diameters, or as the multiplication of linear dimension. It is determined most readily by making an observation with both eyes open, one looking through the telescope and the other by natural vision. The comparison may be made by means of a leveling rod, or the courses of brick or weather-boarding on the side of a honse may be used in like manner.

Parallax.—Parallax is the apparent movement of the cross-hairs on the object with a slight movement of the eye, and is due to imperfect focusing of the eyepiece on the cross-hairs before focusing the objective. The eyepiece

should be focused with the eye normal, the cross-hairs being illuminated by holding the note book page or other white object a few inches in front of the objective.

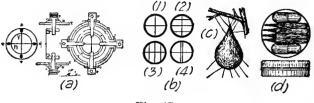


Fig. 17.

Cross-Hairs.—The cross-hairs are attached to a ring or reticule which is held by two pairs of capstan headed screws. The hairs usually consist of spider lines, although some makers use platinum wires for the purpose. To remove the reticule the eyepiece is taken out, one pair of screws is removed and a sharpened stick is inserted in a screw hole. The hest spider lines are obtained from the spider's egg nest.

In Fig. 17, (a) shows the usual arrangement of the crosshair ring and the method of attaching the hairs; (h) shows the number and positions of hairs used, (1) being the most common. (2) the form for stadia work with the transit and also for estimating the lengths of sights with the level, (3) a form used by some makers with the level, and (4) a style found in English levels; (c) shows the egg pod or case of the large brown spider (about half size) which yields the best lines for engineering instruments; (d) illustrates a convenient vest pocket outfit for replacing cross-hairs in the field, consisting of a supply of spider lines and some adhesive paper (hank note repair paper) each in a capsule or tin tube, and several sharpened sticks for stretching the hairs. Cross-hairs stretched in this manner may last indefinitely, or they may be fastened on permanently with shellac at the first opportunity.

THE BUBBLE VIAL.

Principle.—The spirit level consists of a sealed glass tube nearly filled with ether or other liquid, and bent or ground so that the action of gravity on the liquid may indicate a level line by means of the bubble. The delicacy of the buble depends upon the radius of the curvature in a vertical plane, the greater the radius the more delicate the level. Thus, for example, a perfectly straight tube could not be used as a level.

Curvature of Bubble Vials.—Good bubble vials are now made by grinding or polishing the interior surface of a selected glass tube by revolution, as indicated in exaggerated form at (a) Fig. 18. As a general rule, only one side of the vial is actually used, it being customary to encase it in

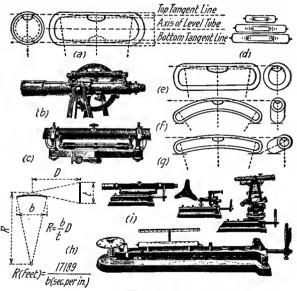


Fig. 18.

a brass tube having a slot or race on one side. However, both sides of the vial may be utilized, as in (b) and (c), Fig. 18, which show the *reversion level* adapted to the transit and wye level, respectively. Bubble vials of several sizes are shown in (d), Fig. 18. It was formerly customary to grind out only a portion of the upper side of the glass tube, as shown at (e). The cheap vial, consisting merely of a bent tube, used mostly in carpenters' and masons' levels, is shown at (f); and a method of increasing the precision of the bent tube by tilting it is indicated at (g), Fig. 18.

Delicacy.—The delicacy of the bubble vial is designated either by the radins, usually in feet, or by the central angle in seconds corresponding to one division or one inch of the bubble scale. Two methods are employed to determine the delicacy of level vials, (1) by the optical method, as at (h), Fig. 18, where the radius is calculated from an observed target movement at a given distance for an observed bubble movement, the two triangles being similar; and (2) by the level tester, as at (i), by means of which the angular movement of the bubble. The engineer usually employs the radial designation, while the maker expresses the delicacy in angular units. As shown at (h) and (i), Fig. 18, the radius in feet is equal to 17,189 divided by seconds per inch of bubble.

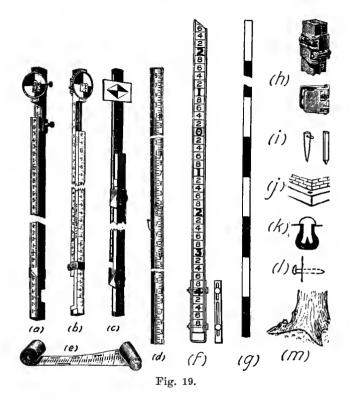
Bubble Line.—The relations of the bubble to the other parts of the instrument are best understood by representing the vial by a line. This line may be either the axis of the surface of revolution in (a), Fig. 18, or to provide for either of the three forms of vial shown, it may be taken as the tangent line at the middle or top point. This tangent line will be meant hereafter in referring to the bubble line.

LEVELING RODS.

Types.—There are two classes or types of leveling rods; (1) *target* rods, having a sliding target which is brought into the line of sight by signals from the leveler; and (2) *sclf-reading* or speaking rods which are read directly by the leveler.

In Fig. 19, (a) is the Philadelphia rod; (b) the New York rod; and (c) the Boston rod. The first is either a target or self-reading rod; the second is a target rod, but may be read from the instrument when the rod is "short"; the Boston rod is strictly a target rod. The Philadelphia rod is perhaps the favorite for most purposes, and the Boston rod is used least. A folding self-reading rod is shown at (d), Fig. 19; (e) is a woven pocket device which may be tacked to a strip of wood and used as a leveling rod; (f) is a railroad contouring rod with an adjustable base; (g) is a plain rod graduated to feet, for use with the water level.

Targets.—The targets shown on the Philadelphia and New York rods, (a) and (b), Fig. 19, are called quadrant targets. That on the Boston rod, (c), is a modified form of



the diamond target. A special form, called the corner target, is bent to fit two sides of the rod to assist in plumbing it, and another target has two parallel planes for the same purpose. A detachable rod level is shown at (h). The target on rod (b), with the zero of the vernier 0.09 foot below the center of the target, frequently causes blunders.

USE OF THE LEVEL.

Use.—The engineers' level is used: (1) to determine differences of elevation; (2) to make profile surveys; (3) to locate contours; (4) to establish grade lines; (5) to cross section; (6) to run lines.

Differential Leveling .-- Differential leveling consists of finding the difference of elevation between two or more points. In the simplest case the difference of elevation between two points may be found from a single setting of the level, the leveling rod being used to determine the vertical distance from the plane of the instrument to each of the two points, and the difference between the rod readings taken. When the distance between the two points is too great, either vertically or horizontally, or both, to admit of this simple process, two or more settings of the level are taken so as to secure a connected series of rod readings. the algebraic sum of which gives the desired difference of elevation. This difference may be expressed either by the numerical result of the algebraic sum of the rod readings, or by assuming an elevation for the beginning point and calculating the elevation of the closing point by means of the observed rod readings.

A back sight is a rod reading taken to determine the height of the instrument. A fore sight is a rod reading taken to determine the height of a point. A bench mark is a point selected or established for permanent reference in leveling operations. A turning point is a temporary reference point used in moving the instrument ahead to a new setting. The same point is often both a turning point and bench mark. The datum is the plane or surface of reference from which the elevations are reckoned; it may be sea level, or an arbitrary local datum. A level line is a line parallel to the surface of a smooth body of water. A horizontal line is tangent to a level line at any point. The curvature varies as the square of the distance from the point of tangency, and is 0.001 foot in 204 feet, or 8 inches in one mile.

In Fig. 19, (i) shows a metal and also a wooden peg commonly used for turning points. Several forms of bench marks are shown in Fig. 19; (j) is a mark on the corner of a stone water-table; (k) a rivet leaded into a hole drilled in a stone slab; (l) a railroad spike driven into a wooden post or telegraph pole; (m) a projection cut on the root of a tree, preferably with a spike driven vertically into the top of the bench, and usually with a blaze above marked "B. M. No.-..." All bench marks and also turning points should be clearly described in the notes.

Fig. 19a shows the essential details of differential leveling. In practice the calculations are made mentally.

Two chief essentials in correct differential leveling are: (1) that the bubble be in exactly the same position (usually the middle) on both back and fore sight; and (2) that the length of back sight and fore sight, horizontally, shall be balanced. It is seen at (e), Fig. 16, that with the bubble always in the middle, the line of collimation generates a horizontal plane when in perfect adjustment, but a cone with axis vertical when out of adjustment; so that in taking equal distances in the opposite directions, the base of the cone is used, this base being parallel to the true colli-

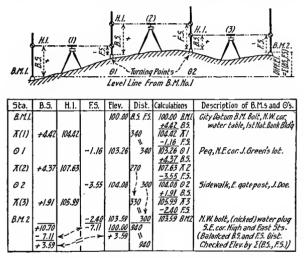


Fig. 19a.-Details of Differential Leveling.

mation plane. In the best leveling practice the instrument is adjusted as perfectly as possible and then used so that the residual errors balance each other.

The three common styles of leveling rods may be read to 0.001 foot by vernier or by estimation on a scale to 0.005 foot. However, for most kinds of leveling, it is an absurd refinement to read the rod closer than 0.01 foot, especially with the usual maximum length of sight of 350 to 400 feet, and with the more or less sluggish bubbles supplied in the general run of leveling instruments. Furthermore, the horizontal hair usually covers 0.01 foot or so of the target at the maximum length of sight, that is, the target can move that amount without being noticed by the observer.

Profile Leveling .- Profile leveling consists of finding the relative elevations of a series of representative points along a surveyed line, for the purpose of constructing a profile or vertical section. The skeleton of profile leveling, that is, the precise bench marks and turning points with the successive heights of instrument, is identical with differential leveling, already described. Having determined the height of instrument by taking a back sight on a bench mark of known or assumed elevation, rod readings are taken at proper intervals along the measured and staked line. These readings are fore sights, but they are usually termed intermediate sights to distinguish them from the more precise rod readings taken on turning points and bench marks. On railroad surveys intermediate sights are taken usually to the nearest 0.1 foot on the ground; but in other cases, such as tile and sewer surveys, intermediates are often read to the nearest 0.01 foot on small pegs driven heside the station stakes flush with the surface of the ground. In railroad work, the benches, turning points, and intermediates of special importance are commonly read to 0.01 foot, although some engineers persist in the questionable practice of taking the nearest 0.001. In drainage surveys the nearest 0.01 foot is usually taken on bench marks, although more carefully than on the intermediate peg points, and the nearest 0.1 foot is read on ground points.

The errors of profile leveling are balanced on turning points by equal back and fore sights, as in differential leveling. If the instrument is seriously out of adjustment, an error is made in the case of odd bench marks with unbalanced sights, and also on all intermediate sights. However, the error is usually unimportant when ground readings are taken to the nearest 0.1 foot. In important leveling, such as canal and drainage work, it is customary to run a line of check levels to prove benches, before construction begins.

The profile is plotted to an exaggerated scale vertically on a special paper, called profile paper. Three kinds, known as plates A, B and C, are in general use. The most common is plate A, which is ruled in $\frac{1}{4}$ -inch squares with a further subdivision to $\frac{1}{20}$ inch vertically. In railroad profiles the scales most used are 400 feet to the inch horizontally and 20 feet vertically. A still greater exaggeration is generally used in drainage profiles.

Reciprocal Leveling.—The application of differential leveling to the determination of the difference of elevation between two bench marks separated by a wide river or gorge is termed reciprocal leveling. A setting of the level is taken on each side of the river, and the mean of the two results is taken. The necessary unbalancing of distances in one setting is balanced up in the other. Each back or fore sight should be the mean of a series of careful observations. In best practice, simultaneous readings are taken with two levels.

Contour Leveling.—Contour leveling is an application of the methods of profile leveling to the location of contour lines, that is, lines having the same elevation. Two methods are employed: either (1) actually establishing points on the adopted contour planes on the ground and then locating these points; or (2) taking random elevations at representative points and interpolating the contour lines from the plotted data. The latter is the more common. The chief purpose of contour leveling is to make a contour map, and the process is essentially a part of topographic surveying, where it will be more fully considered.

Grade Lines .- The establishment of grade lines is usually the concluding part of profile leveling. After making the profile, the grade line is established by stretching a fine thread through the ruling points, taking into account the controlling conditions, such as maximum gradient or earthwork quantities on a railroad profile, the carrying capacity or the scour in the case of a ditch, etc. After laying the grade line on the profile, notes are made of the data, and the actual grade line is established. Two methods are used : (1) the height of instrument is determined as usual. and stakes are driven at measured intervals with their tops to match calculated rod readings; and (2) a limited number of ruling points are established by the first method or otherwise, and the remaining stakes are "shot in" by constructing a line parallel to the ruling line used. The latter is more rapid, since a constant rod reading is used; however, the method is unreliable unless the foresight he checked frequently on a fixed target.

Cross-Sectioning.—Cross-sectioning consists of staking out the limits of the transverse section of an excavation or emhankment for the purpose of construction, and usually includes the collection of data for the calculation of the quantities. This may be done either with the engineers' level, rod and tape line, or with special rods called crosssection rods. The notes are taken as rectangular coordinates, usually with reference to the center of the finished roadbed. The slope stakes are set where the side slope lines pierce the surface of the ground.

Running Lines.—Lines are sometimes run with the engineers' level, provision being made in most good levels for the attachment of a plumb bob. A line may be prolonged by sighting in two points ahead. A clamp and tangent movement are necessary. Some builders' levels have a needle and also a roughly divided horizontal circle for use in staking out buildings.

Practical Hints.—The following practical suggestions apply more or less directly to all kinds of leveling, and also in a general sense to transit work.

Speed.—Cultivate the habit of briskness in all the details of the work. While undue haste lowers the standard of the results, an effort should be made to gain speed steadily without sacrificing precision. Gain time for the more important details by moving rapidly from point to point. On rapid surveys both leveler and rodman often move in a trot. Neither rodman nor leveler should delay the other needlessly.

Care of Instruments.—Do not carry the level on the shoulder in climbing fences. Clamp the telescope slightly when hanging down Keep the tripod legs at the proper tightness, and avoid looseness in the tripod shoes. Avoid undue exposure to the elements, and guard the level from injury. Do not leave the instrument standing on the tripod in a room over night.

Setting Up—In choosing a place to set the level up, consider visibility and elevation of back point and probable fore sight. Set up with plates about level. On side-bill ground place one leg up hill. In general, place two tripod shoes parallel to the general line of the levels.

Leveling Up.—A pair of foot screws should be shifted to the general direction of the back or fore sight before leveling up. Set the foot screws up just to a snug bearing and no tighter. If either pair of screws binds, loosen the other pair a little The bubble moves with the left thumb. Level up more precisely in the direction of the sight than transverse to it, but do not neglect the latter. Inspect the bubble squarely to avoid parallax, and also to prevent such blunders as reading the bubble five spaces off center.

Observations.—Adjust the eyepiece for parallax with the eye unstrained. It is much easier on the eye to observe with both eyes open. Read at the intersection of the crosshairs, since the horizontal hair may be inclined. Set the target approximately, check the bubble, and repeat the process several times before approving the sight. Be certain that the bubble is exactly in the middle at the instant of approving the target. If the level has horizontal stadia lines, beware of reading the wrong hair (the reticule may be rotated one-quarter so as to have the extra hairs vertical, or a filament may be attached to the middle horizontal hair to assist in identifying it). Avoid disturbance of the tripod by stepping about the instrument. Assist the rodman in plumbing the rod. Let signals be perfectly definite both as to direction and amount, using the left hand for "np" and the right for "down," or vice versa.

The leveler can work much more intelligently if he knows the space covered on the rod by one division of the bubble scale at the maximum length of sight, and also the space on the rod hidden by the cross hair.

Adjustments.—Keep the instrument in good adjustment and then use it as though it were out of adjustment.

Balancing Sights.—Balance the length of back sight and fore sight, and record the approximate distances. The distances in the two directions may be made equal roughly by equality of focus, but it is better on careful work to pace the distances or determine them by means of the stadia lines in the level. If necessary to unbalance the sights, they should be balanced up at the first opportunity, and in general they should he in balance when closing on important benches. When leveling up or down steep slopes, follow a zigzag course to avoid short sights. Take no sights longer than 350 or 400 feet.

Leveling Rod.—The rod should be carefully plumbed, to accomplish which the rodman should stand squarely behind the rod and support it symmetrically between the tips of the extended fingers of the two hands. In precise work wave the rod to and fro towards the observer and take the minimum reading of the target. With "short" rods avoid the somewhat common blunder of 0.09 foot when the vernier slot is below the center of the target. With "long" rods, see that the target has not slipped from its true setting before reading the rod. Read the rod at least twice, and avoid blunders of 1 foot, 0.1 foot, etc. Careless rodmen sometimes invert the rod. Each rod reading on turning points and bench marks should, when practicable, be read independently by both rodman and leveler.

Bench Marks and Turning Points.-Wooden pegs or other substantial points should be used to turn the instrument on. Select bench marks with reference to ease of identification, the balancing of sights, freedom from disturbance, etc. As a rule, each bench mark should he used as a turning point so that the final closure of the circuit may prove the bench. Mark the benches and turning points and describe them in the notes so plainly that a stranger may readily find them. Green rodmen sometimes hammer at turning point pegs with the rod. When leveling near a still body of water, its surface may be used to save time and check the work.

Record and Calculations.—Describe bench marks and turning points clearly. It is good practice to apply algebraic signs to the back and fore sight rod readings. The elevations should be calculated as fast as the rod readings are taken, and calculations on turning points should be made independently by leveler and rodman, and results compared at each point. The rodman may keep turning point notes in the form of a single column. The calculations should be further verified by adding up the columns of back sights and fore sights for each circuit, or page, or day's work, and the algebraic sum of the two compared with the difference between the initial and last calculated elevation.

Error of Closurc.—A circuit of levels run with a good level by careful men, observing all the foregoing precautions, should check within 0.05 foot into the square root of the length of the circuit in miles (equivalent to 0.007 foot into the square root of the length of the circuit in 100-foot stations). In closing a circuit, the error should be carefully determined, as above indicated, and the value of the coefficient of precision found. (See discussion of errors of leveling and precision diagrams in Chapter IX, Errors of Surveying.)

ADJUSTMENT OF THE WYE LEVEL.

Elementary Lines.—The principal elementary lines of the wye level, as shown in Fig. 16, are: (1) the line of collimation; (2) the bubble line; (3) the vertical axis. For the purpose of adjustment there should be added to these: (4) the axis of the rings; (5) the bottom element of the rings. The following relations should exist between these lines; (a) the line of collimation and bubble line should be parallel; (b) the bubble line should be perpendicular to the vertical axis. The first of these relations involves two steps, viz., (1) to make the bubble line parallel to the bottom element of the rings, and (2) to make the line of collimation coincide with the axis of the rings. The other relation involves the wye adjustment, and is similar to the plate level adjustment described in the chapter on the compass.

Bubble.—To make the bubble line parallel to the bottom element of the rings.—Two steps are involved, (a) to place the bubble line in the same plane with the bottom element, and (b) to make the two lines parallel.

Azimuth Screws.—To make the bubble line in the same plane with the bottom element of the rings.—Clamp the level over a pair of foot screws, loosen the wye clips, and level up; rotate the telescope through a small angle, and if the bubble moves away from the middle, bring it back by means of the *azimuth* adjusting screws. Test by rotating in the opposite direction. Leave the screws snug.

Altitude Screws.—To make the bubble line and the bottom element of the rings parallel.—Make the element level with the foot screws and bring the bubble to the middle by means of the altitude adjusting screws. The element is made level by the method of reversions as follows: With the level clamped over a pair of foot screws, as above, lift the clips and level up precisely; cautiously lift the telescope out of the wyes, turn it end for end, and very gently replace it in the wyes; if the bubble moves, bring it half way back by means of the foot screws. Before disturbing adjusting screws make several reversals, and conclude the adjustment with screws snug. This end for end reversal is similar to that made with the carpenter's level, the straight edge of the level corresponding to the element of the rings. The lines involved are shown in Fig. 16.

Line of Collimation.—To make the line of collimation coincide with the axis of the rings.—Loosen clips, sight on a point, say a nail head or the level target, more distant than the longest sight used in leveling; rotate the telescope half way and note the movement of the hair, if any. The line of collimation generates a cone, the axis of which is that of the rings, and the apex of which is at the optical center of the objective. Correct one-half the observed error by means of the capstan headed screws which hold the crosshair ring. Gradually perfect the adjustment until the intersection of the cross-hairs remains fixed on the same point when reversed by rotation with reference to either hair. The adjustment should be concluded with the screws at a snug bearing. After collimating the instrument for a long distance, the adjustment should be checked for a short distance, say 50 or 100 feet, so as to test the motion of the optical center of the objective.

Rings.—The theory of the wye level demands perfect equality of the rings, that is, the parallelism of the axis and element, as in (c), Fig 16. Should the rings be unequal, either from poor workmanship or uneven wear in service, they form a cone instead of a culinder, and the axis is not parallel to the element, as in (d), Fig. 16. Under the latter conditions, the principle of the wye level fails, and an independent test is demanded. This is known as the two-peg test, the details of which are shown in (e) and (f). Fig. 16, and described in the adjustments of the dumpy level. If, after making the wye level adjustments above described, the two-peg test shows that the line of collimation and bubble line are not parallel, the rings are probably unequal and the instrument should thereafter be adjusted as a dumpy level. However, hasty conclusions should be guarded. against.

In case the instrument has a reversion level, shown at (c), Fig. 18, the equality of the rings may be tested by first adjusting the top tangent line of the bubble vial parallel to the bottom element of the rings, and then after rotating the telescope half way round in the wyes, compare the bottom (now above) tangent line of the vial with the top (now below) element of the rings, all by the end for end reversion. However, the exact parallelism of the top and hottom tangent lines of the reversion level should first be proven by the two-peg method.

 $\hat{\mathbf{W}}$ yes.—To make bubble line perpendicular to the vertical axis.—Make the vertical axis vertical and bring the bubble to the middle by means of the wye nuts. The vertical axis is made vertical hy reversion thus: With clips pinned, level up; reverse over the same pair of screws, and bring the bubble half way back with the foot screws. When adjusted, the bubble will remain in the middle during a complete revolution. This adjustment is identical in principle with the plate level adjustment of the compass and transit, illustrated in (a), Fig. 13. The wye adjustment should follow the adjustment of the bubble line parallel to the element of the rings. The wye adjustment is a convenience, not a necessity.

Centering the Eyepiece.—After collimating the level, the cross-hairs should appear in the center of the field.

The eyepiece is centered by moving its ring held by four screws. This adjustment is desirable, but not essential.

ADJUSTMENT OF THE DUMPY LEVEL.

Elementary Lines.—The principal elementary lines of the dumpy level are identical with those of the wye level (1) the line of collimation; (2) the bubble line; (3) the vertical axis. As in the wye level, the bubble line should be (1) perpendicular to the vertical axis, and (2) parallel to the line of collimation. However, owing to the difference in the construction of the two types of instrument, the auxiliary elementary lines are not recognized in the dumpy level. The transit with its attached level is identical in principle with the dumpy level.

Bubble.—To make the bubble line perpendicular to the vertical axis.—Make the vertical axis vertical by the method of reversions, and adjust the bubble to the middle. This adjustment is identical in principle with the plate level adjustment, shown in (a), Fig. 13. The bubble should remain in the middle through a complete revolution.

Line of Collimation.—To make the line of collimation parallel to the bubble line.—Construct a level line, and adjust the cross-hairs to agree with it. The level line is determined either by using the surface of a pond of water, or by driving two pegs at equal distances in opposite directions from the instrument, and taking careful rod readings on them with the bubble precisely in the middle, as shown at (e), Fig. 16. For simplicity, the two pegs may be driven to the same level, or two spikes may be driven at the same level in the sides of two fence posts, say 400 feet apart. Otherwise, determine the precise difference of elevation, as indicated in (e), Fig. 16. Then set the level almost over one of the pegs, level up, and as in the first method of (f), Fig. 16, set the target of the leveling rod at the line of collimation, as indicated by the center of the object glass or eyepiece (this can be done more precisely than most levels will set the target at 400 feet distance); now with the rod on the other peg, sight at the target (shifted to allow for the difference if the two pegs are not on the same level): adjust the cross-hair to the level line so constructed. If preferred. the second method shown in (f), Fig. 16, may be used; the level is set back of one peg, rod readings are taken on both pegs, allowance made for the difference in level of the two pegs, if any, the inclination of the line of

collimation determined, correction made for the small triangle from the level to the first peg, and finally the level line constructed by means of the calculated rod readings. The second method is simplified and made practically equivalent to the first by setting the level at minimum focusing distance from the first peg. The small corrective triangle is thus practically eliminated. Strictly speaking the rod readings should be corrected for the earth's curvature (0.001 foot in about 200 feet, or say 0.004 foot in 400 feet distance). However, the effect of curvature is reduced by atmospheric refraction; and with errors of observation, sluggishness of bubble, etc., to contend with, the curvature correction should be ignored, especially when the rod is read to the nearest 0.01 foot.

(The foregoing process is known as the "two-peg adjustment." Although exceedingly simple, this adjustment is commouly regarded as a "bug-bear" by many American engineers. But for it, the dumpy level would have the extended use in this country which it merits. It is said that "the wye level is easy to adjust and usually needs adjustment." Many good levelers employ the "two-peg test" to prove the wye level adjustments. Time may be saved by establishing an adjusting base. The adjustments of a good dumpy level are very stable.)

Uprights.—Iu some dumpy levels the uprights which connect the telescope with the level bar are adjustable, similar to the wyes of the wye level. This adjustment is designed to bring the bubble line perpendicular to the vertical axis in case the bubble is first adjusted parallel to the line of collimation. However, the best order is that already described, viz., first adjust the bubble line perpendicular to the vertical axis, and then the line of collimation parallel to the bubble line, in which case the adjustable uprights are unnecessary.

PROBLEMS WITH THE LEVEL.

PROBLEM C1. DIFFERENTIAL LEVELING WITH THE HAND LEVEL (OR WATER LEVEL).

(a) Equipment.—Hand level (or water level), rod graduated to feet.

(b) *Problem.*—Run an assigned level circuit with the hand level (or water level), observing the nearest 0.1 foot by estimation, and closing back on the starting point.

(c) Methods.—(1) Determine the correct position of the bubble of the hand level by sighting along a water table, or sill course of a building, or by the principles of the twopeg test. (If the water level is used, fill the tube so as to have a good exposure of the colored water in the glass uprights.) (2) Take sights of 100 feet or so (paced), estimating the rod reading to the nearest 0.1 foot; balance back and fore sights; assume the elevation of the starting point, and keep the notes in a single column by addition and subtraction, as in the 7th column, Fig. 19a. (3) Check back on the first point. Determine coefficient of precision. (The error of closure in feet should not exceed 0.5 $\sqrt{\text{distance in}}$ miles.)

PROBLEM C2. DIFFERENTIAL LEVELING WITH EN-GINEERS' LEVEL (OR TRANSIT WITH ATTACHED LEVEL).

(a) Equipment.—Engineers' level (or transit with attached level), leveling rod, hatchet, pegs, spikes.

(b) Problem.—Run the assigned level circuit, observing the nearest 0.01 foot, and closing back on the initial point.

(c) Methods.—Follow the practical suggestions given at the conclusion of the "Use of the Level," giving special attention to the following points: (1) eliminate parallax of the eyepiece; (2) balance back and fore sight distances; (3) have the bubble precisely in the middle at the instant of sighting; (4) both rodman and leveler read each rod and also make the calculations independently; (5) calculate elevations as rapidly as rod readings are obtained; (6) plumb the rod; (7) avoid blunders; (8) determine coefficient of precision; (9) no sights longer than 350 or 400 feet. Follow the first form shown to begin with,—the other after several circuits have been run.

PROBLEM C3. PROFILE LEVELING FOR A DRAIN.

(a) Equipment.—Engineers' leveling instrument, leveling rod, 100-foot steel tape, stakes, pegs, axe.

(b) *Problem.*—Make a survey, plat and profile, with estimate of cuts and quantities for a drain under assigned conditions.

(c) Methods.—(1) Examine the ground, determine the head and outlet of the drain, and select the general route. (2) Stake out the line, set stakes every 50 feet, or oftener if required to get a good profile, and drive a ground peg flush, say 2 feet to the right (or left) of each stake; record data for mapping the line. (3) Starting with the assigned datum or bench mark, run levels over the line of the proposed drain, observing the nearest 0.01 foot both on turning points and ground pegs, the former somewhat more carefully; take rough ground levels, as required, to the nearest 0.1 foot; locate and determine the depth of intersecting drains or pipe lines, or other objects which may influence the grade line of the drain, and secure full data for placing the same on the profile; observe due care with the back and

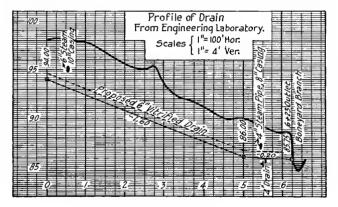
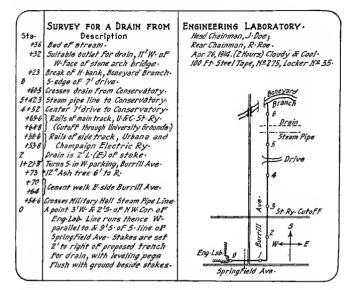


Fig. 19b.

fore sights, as in differential leveling, and conclude the leveling work with a line of check levels back to the initial bench mark; a permanent bench mark should be established at each end of the drain, and if the length is considerable, at one or more intermediate points as well. (4) Make plat and profile of the drain line; lay the grade line, taking into account all ruling points; calculate the cuts, both to the nearest 0.01 foot, and also to the nearest $\frac{1}{4}$ -inch; mark the latter on the stakes for the information of the ditcher, using waterproof keel and plain numerals; make estimate of the quantity of drain pipe, and of the cost of the job. Follow the form and the profile in Fig. 19b.

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02 03 04 05 06 07 08 09 010 011 8:M2 0 12 013 014 015	5.95 5.70 4.93 4.23 4.24 4.73 4.44 5.18 4.54 4.54 4.62 4.10 3.65	694-02 696-30 698-18 699-75 699-04 699-33 699-61 699-86 699-86 698-86 698-86 698-86 698-00 596-13	3.67 3.82 4.37 4.95 4.46 5.40 5.40 5.55 4.08 5.55 4.08 5.59 5.59 5.59 5.59 5.59 5.59 5.59 5.5	689.82 690.35 692.48 693.81 694.80 694.80 694.80 694.80 695.17 694.82 693.32 693.31 694.04 693.30 693.90 693.90 692.48 692.48 690.21 686.82	855 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 300	Nor23 '4. (budy, Cool & & B. Dumpy Level. Pama & & B. M, M. R. Z. J. drivan reii (levels Pag- direct Fram tide gage at " Sandy Heak, M.Y.) " (South along Monon R.R) " " " " " " " " " " " " "
02 03 04 05 06 07 08 09 010 011 8:M-2: 013 014 015 8:M-3	5.95 5.70 4.93 4.23 4.24 4.73 4.44 5.18 4.54 4.54 4.54 4.81 4.82 4.10 3.65 2.71 3.21	694-02 696-30 698-18 699-74 699-74 699-94 699-93 699-64 699-33 699-64 699-39 697-86 698-86 698-86 698-80 698-00 698-13 692-92 690-03	- 3.67 3.82 4.37 4.46 4.55 4.55 4.55 4.55 4.55 4.55 5.59 2.25 5.59 3.55 5.59 3.55 5.59 3.55 5.59 3.55 5.59	639.82 690.35 692.48 693.51 694.80 694.80 694.60 694.60 694.60 694.60 693.32 693.32 693.32 693.32 693.32 693.32 693.32 693.32 693.42 693.32 693.42 69	155 F.5. 165 240 240 240 240 240 240 240 240 240 240 240 240 240 300 300 300 300 300 300 300 300 300 300 360 360 360 300 360 300	Nor 23 VA. Clevidy, Cool. 8 & B. Dumpy Level. Panna F. B. M. N. P. 27, driven reil (levels Peg. direct From tide gage at " Sandy Hook, M.Y.] " (South along Monon R.R.) " (South along Monon R.R.) " " opposite Cathollc Church, Reynalds- " F side tr'k, between tel poles 2289-90. " " J F side tr'k, between tel poles 2296-97. BH on ask, tel pole 2300. " " " 2313, F side track. HF-cor. parapet wall, Bridge H2 97.4
02 03 04 05 06 07 08 09 010 011 8:M2 012 012 012 013 014 015 8:M3 016	5.95 5.70 4.93 4.23 4.24 4.73 4.44 5.18 4.54 4.58 4.58 4.82 4.82 4.10 3.65 2.71	694-02 696-30 698-18 698-74 699-75 699-04 699-33 699-61 699-33 699-61 699-39 697-86 698-12 698-86 698-13 692-92	- 3:67 37 22 55 44 46 47 75 58 86 75 95 95 95 95 95 95 95 95 95 95 95 95 95	689-82 690-35 692-48 693-81 694-80 694-80 694-80 694-80 694-80 694-80 694-80 694-80 694-80 694-80 694-80 694-80 692-88 690-21 6886-88 686-88 686-18	155 240 165 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 300	Nor 23 VA. Clevidy, Cool. 8 & B. Dumpy Level. Panna F. B. M. N. P. 27, driven reil (levels Peg. direct From tide gage at " Sandy Hook, M.Y.] " (South along Monon R.R.) " (South along Monon R.R.) " " opposite Cathollc Church, Reynalds- " F side tr'k, between tel poles 2289-90. " " J F side tr'k, between tel poles 2296-97. BH on ask, tel pole 2300. " " " 2313, F side track. HF-cor. parapet wall, Bridge H2 97.4
02 03 04 05 06 07 08 09 07 01 01 01 01 01 01 01 01 01 01 01 01 01	5.95 5.70 4.93 4.24 4.73 4.44 5.18 4.54 4.54 4.81 4.82 4.10 3.65 2.71 3.21 4.65	694-02 698-30 698-18 699-75 699-04 699-33 699-61 699-33 699-61 699-85 698-12 698-86 698-13 692-92 690-83 690-83	- 3:67 3:827 4:3:25 4:44 4:40 4:55 4:55 5:592 5:55 5:592 5:55 5:592 5:55 5:592 5:55 5:592 5:55 5:592 5:55 5:592 5:55 5:55	639-82 692-35 692-48 693-81 695-52 694-80 694-60 694-60 694-60 694-60 694-60 694-60 694-60 694-60 694-04 693-32 693-31 693-31 693-32 693-31 693-32 692-48 692-48 692-48 692-48 692-54 686-55	155 240 165 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 300	Nor23 Va. Clevity, Cool. 8 & B. Dumpy Level. Pama & & B.M., M. R. 27, driven reii (levels Pag. direct From tide gage at " Sandy Heak, M.Y.] " (South along Nonon R.R.) " " " " " " " " " " " " "
02 03 04 05 06 07 08 07 01 01 01 01 01 01 01 01 01 01 01 01 01	5:95 5:70 4:93 4:24 4:24 4:24 4:73 4:44 5:18 4:54 4:48 4:51 3:65 2:71 3:21 4:65 4:51	694-02 696-30 698-34 699-75 699-04 699-33 699-39 699-39 697-86 698-12 698-86 698-13 692-92 690-83 690-83 690-83	- 3:67 3:827 3:43:25 4:45 4:55 6:455 8:66 4:55 4:55 5:59 2:0 1:55 2:59 2:59 2:59 2:59 2:59 2:59 2:59 2	639-82 692-35 692-48 693-81 695-52 694-80 695-57 694-80 695-57 694-82 693-32 693-32 693-32 693-31 693-32 693-31 693-34 693-32 693-31 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-48 693-58 693-48 693-58 693-58 693-58 693-58 693-58 693-58 693-58 693-59 695-59 695-59 695-595-595-595-595-595-595-595-595-595-	153 F5. 165 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 300 300 300 300 300 300 300 300 300 300 360	Nor 23 VA. Clevidy, Cool. 8 & B. Dumpy Level. Panna F. B. M. N. P. 27, driven reil (levels Peg. direct From tide gage at " Sandy Hook, M.Y.] " (South along Monon R.R.) " (South along Monon R.R.) " " opposite Cathollc Church, Reynalds- " F side tr'k, between tel poles 2289-90. " " J F side tr'k, between tel poles 2296-97. BH on ask, tel pole 2300. " " " 2313, F side track. HF-cor. parapet wall, Bridge H2 97.4
02 03 04 05 06 07 08 07 08 07 012 012 012 012 014 015 8-M-3 016 8-M-3 016 8-M-3 016 9-17 018	5.95 5.70 4.93 4.24 4.73 4.44 5.18 4.54 4.54 4.81 4.82 4.10 3.65 2.71 3.21 4.65	694-02 698-30 698-18 699-75 699-04 699-33 699-61 699-33 699-61 699-85 698-12 698-86 698-13 692-92 690-83 690-83	- 3:67 3:437 4:45 4:46 4:558 4:558 4:558 4:558 5:552 5:55 5:5	689-82 690-35 692-84 693-81 695-52 694-80 694-80 695-52 695-52 693-32 693-32 693-32 693-90 692-48 690-21 686-82 686-82 686-82 686-82 686-82 686-82 686-82 686-82	#5 F-5- 165 240 165 240 240 165 240 165 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 300 300 300 300 360 360 360 360 360 360 360 360 360 360 360 360 360 360 360	Nor 23 (4. Cloudy, Cool. B & B. Dumpy Level. Panna-F.B. M. N. P. 21, driven roll (levels Peg. direct From tide gage at " Sandy Nock, M.Y.) " (South along Monon R.R) " " " " " " " " " " " " "
02 03 04 05 06 07 08 07 01 01 01 01 01 01 01 01 01 01 01 01 01	5:95 5:70 4:92 4:24 4:24 4:73 4:44 5:18 4:54 4:54 4:54 4:54 4:55 2:71 3:65 2:71 3:65 2:71 3:65 2:71 3:65 2:71 3:65	694-02 696-30 698-34 699-75 699-04 699-33 699-39 699-39 697-86 698-12 698-86 698-13 692-92 690-83 690-83 690-83	- 333432554461075586662220595893003	689-82 690-35 692-84 695-52 694-80 695-57 694-80 695-57 694-82 693-32 693-90 693-90 692-81 690-21 688-82 688-81 688-81 688-81 688-81 688-21 688-21 688-21 688-21	423 165 240 240 240 240 240 240 240 240	Nor23 Va. Clevity, Cool. 8 & B. Dumpy Level. Pama & & B.M., M. R. 27, driven reii (levels Pag. direct From tide gage at " Sandy Heak, M.Y.] " (South along Nonon R.R.) " " " " " " " " " " " " "
02 03 04 05 06 07 08 07 08 07 012 012 012 012 014 015 8-M-3 016 8-M-3 016 8-M-3 016 9-17 018	5:95 5:70 4:93 4:24 4:24 4:24 4:73 4:44 5:18 4:54 4:48 4:51 3:65 2:71 3:21 4:65 4:51	694-02 696-30 698-34 699-75 699-04 699-33 699-39 699-39 697-86 698-12 698-86 698-13 692-92 690-83 690-83 690-83	- 3.67 3.437 4.954 4.96 4.958 6.075 4.9662 4.962 4.9662 4.962 4.964 5.92 9.95 1.955 4.93 5.73 4.93 4.95 4.9	689-82 690-35 692-84 695-52 694-80 695-57 694-80 695-57 694-80 695-57 694-82 695-10 692-84 692-82 692-82 692-82 686-82 68	#5 F-5- 165 240 165 240 240 165 240 165 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 240 300 300 300 300 360 360 360 360 360 360 360 360 360 360 360 360 360 360 360	Nor 23, Va. Chardy, Charl. B.K. B. Dumpy Level. Panna-F.B. B.M., N.P. 21, driven reil (levels Peg. direct Fram tide gage at " Sandy Nock, N.Y.) " (South along Monon R.R) " " " " " " " " " " " " "
02 03 04 05 06 07 08 07 08 07 012 012 012 012 014 015 8-M-3 016 8-M-3 016 8-M-3 016 9-17 018	5:95 5:70 4:92 4:24 4:24 4:73 4:44 5:18 4:54 4:54 4:54 4:54 4:55 2:71 3:65 2:71 3:65 2:71 3:65 2:71 3:65 2:71 3:65	694-02 696-30 698-34 699-75 699-04 699-33 699-39 699-39 697-86 698-12 698-86 698-13 692-92 690-83 690-83 690-83	- 3:67.27.25.44.64.77.55.88.78.46.22.20.91.55.27.30.23.44.4.64.77.86.22.20.91.55.27.30.23.44.55.86.27.86.27.20.23.45.55.88.85.78.85.55.60.23.25.27.88.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.778.85.7788.7788.85.7888.85.7788.77888.778888.778888.778888.778888.77888888	689-82 690-35 692-84 692-84 694-80 694-80 694-80 694-80 694-80 694-80 694-80 694-80 694-80 693-32 693-32 693-32 693-32 693-32 693-82 69	423 165 240 240 240 240 240 240 240 240	Nor 23, Va. Chardy, Charl. B.K. B. Dumpy Level. Panna-F.B. B.M., N.P. 21, driven reil (levels Peg. direct Fram tide gage at " Sandy Nock, N.Y.) " (South along Monon R.R) " " " " " " " " " " " " "
02 03 04 05 06 07 08 07 08 01 012 012 013 014 015 8-M3 016 8-M3 016 4-017 018	5:95 5:70 4:92 4:24 4:24 4:73 4:44 5:18 4:54 4:54 4:54 4:54 4:55 2:71 3:65 2:71 3:65 2:71 3:65 2:71 3:65 2:71 3:65	694-02 696-30 698-34 699-75 699-04 699-33 699-39 699-39 697-86 698-12 698-86 698-13 692-92 690-83 690-83 690-83	- 3.67 3.437 4.954 4.96 4.958 6.075 4.9662 4.962 4.9662 4.962 4.964 5.92 9.95 1.955 4.93 5.73 4.93 4.95 4.9	689-82 690-35 692-84 695-52 694-80 695-57 694-80 695-57 694-80 695-57 694-82 695-10 692-84 692-82 692-82 692-82 686-82 68	423 165 240 240 240 240 240 240 240 240	Nor 23 (4. Cloudy, Cool. B.A. B. Dumpy Level- Panna-F.B. B.M., N.P. 21, driven rail (Levels Peg. direct From tide gage at " Sandy Nock, N.Y.) " (South along Monon R.R.) " " " " " " " " " " " " "

THE LEVEL.



\frown						Leveler, R. Roe- Rodman, J. Dos.
La	VEL 1	IOTES	FOR	A D	RAIN	FROM ENGINEERING LABORATORY.
Sta-	B-5-	H-1-	F- 5-	Elev.	Grade	Cut Oct 23, 14. (2 hrs) Clear and Cool.
				100-00		S.End stone sill, W. door, Eng. Lab.
π	+1-23	101-23				Station stakes are 2 R proposed trench.
0			3.05	98.18	94.00	4 18 Peg driven flush with ground beside stake.
+50			3.22	98.01	93.20	481 12
+546			3-2	98.0	93-13	4.9 Ground, 6"Steam Pipe, 10"cesing, top 2.6 deep.
+66			3.23	98.00	92.94	5.06 Cament welk, E-side BurrIII Ave-
1			3-38	97-85	92:40	5.45 Peg-
+21.5			3.72	97.51	92.06	545 Drain turns 5-in W-parking Burrill Ave-
+50			4.65	96.58	91.60	4.98 Feq
2			5.71	95.52	90.80	4.72 11
+50			6.31	94.92	90 00	4 92 "
0+59			-5.85	95.38	89.86	5.52 (Jurning Point) N.Rail, Main Track, U.&C. Ry.
π	+ 0-13	95.51				
3			2.08	93.43	89.20	4-23 Peg
+50			3.45	92.06	88.40	3.66 17 Fauth Wye Level.
4			4.34	91.17	87.60	3 57 17 Phile Rod, Lkr. 20.
+50			5.50	90.01	86.80	3.21 11
5			5 52	89 99		3.99 11
+423			6-1	89.4	85.91	3.5 Ground, 4"Steam Pipe, 8"Casing, top 2.10 deep.
+50			6.26	89.25	85·90	3-35 Pag.
+60.5			6.4	89.1	85.88	3.2 Ground, 4"vitriFied drain, top 3.4 deep.
6		I '	7.11	88.40	85.80	2.60 Peg.
+23			.7.0	88.5	85·75	2.7 Break of N bank, Boneyard Branch.
+36			10.9	84 6		Bed of Stream, water 10"deep.
						, ,

PROBLEMS.

PROBLEM C4. RAILROAD PROFILE LEVELING.

(a) Equipment.—Engineers' leveling instrument, leveling rod, 100-foot steel tape, stakes, axe.

(b) *Problem.*—Run levels over a short section of line staked out after the manner of railroad surveys, for the purpose of constructing a profile.

(c) Methods.-Follow the general process outlined in the preceding problem, taking rod readings to the nearest 0.01 foot on turning points and bench marks, and also on important profiling points, when consistent; but take ground rod readings only to the nearest 0.1 foot. In calculating elevations, preserve the same degree of exactness in the result as observed in the rod reading, that is, when the rod readings are taken to the nearest 0.1 foot, use only the nearest 0.1 foot in the height of instrument to determine the elevations. When a hub or station stake is to be used as a turning point, the notes should show the ground rod and elevation to the nearest 0.1 foot on the line preceding the precise turning point record. Bench marks should be selected with reference to their freedom from disturbance during construction, and they should be located not more than 1500 or 2000 feet apart along the line. Check levels by the same parties should not differ more than 0.05 foot into the square root of the length of circuit in miles. Back and fore sights should be balanced, and no sight longer than 350 or 400 feet should be taken. In order to secure a representative profile, ground rods should be taken not only at every station stake, but also at every important change of slope hetween station points. Pluses may be determined either by pacing, or when short, by means of the leveling The rodman should keep a record of the turning rod. The notes should be checked and the other safepoints. guards taken, as outlined in the practical hints under the "Use of the Level." Bottoms of deep gullies may be taken by means of the hand level, or with the engineers' level used like the hand level; or a "long" rod of 17 feet or more may be obtained by holding the 12-foot rod 5 feet or more from the ground.

The profile is best plotted by having another person read off the data. The horizontal scale on railroad profiles is usually 400 feet to the inch and the vertical scale 20 feet to the inch. Gradients are expressed to the nearest 0.01 per

\square	(Da				GROUND	ELEVATIONS TO 0.1 FOOT.
			VEC N		GROUND E-	LLEVATIONS TO OT TOUTY
5.	÷	Π 3	-	R. 5.0	7/3.3	In Brown St. (Unimproved)
209		718-33			713.6	
210				4.7		n n
2/1 0		9		3.9	714.4	Water Plug, N. bolt, N.W. Cor., Brown-Curtis.
B-M-26	6.79	723-87	1.25	7.0	(<u>717-08</u>) 716-3	
2/2			1	7.6	717.5	Ground, Brown 5t.
213			1	5.4		11 IT
214				5.9	718.0	n n
+50				4.0	719.2	
215				6-1	7/7-8	1) <i>11</i>
216				8.0	7/5.9	" <i>"</i>
217		ł		8.5	715.4	17 67
218		1		10-3	7/3-6	11 11
219		6	11.45	12.2	7/1.7	In Corn Field
e Stake	9.22	721-64	11.45		(712.42)	
220				8.6	713-0	Corn Field.
221			1	4.4	7/7-2	"
222				2.7	718-9	"
223				2.9	718.7	25
224			1	2.3	719.3	"
225				3.4	718.2	Timber Pasture
+90		l I		12.4	709.2	6ully•
226				11.2	710.4	
+35		5		6.0	715.6	Break of bank, Plum River.
B-M-27	2.04	713.52	10.16		7/1-48	B.M., root, 24" elm, 72" R., 5ta. 226+65-
+80		718.33	-22.86	6.0	707-5	Column (S= Station - = Fore Sight.
	+18.05	- 4.81	+18.05			Column + . Back Sight R- Rod (Intermediate) Headings A . Height Inst. E. Elevation.
	L,	ن ــــــــــــــــــــــــــــــــــــ	* - 4·81	Check	I	- (the many in misite E & Energy in the

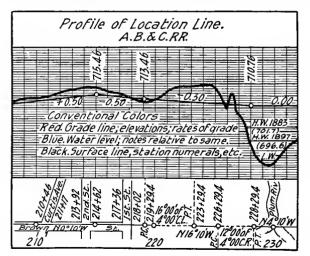


Fig. 19c.

cent. It is usual to give the alinement notes and prominent topography, as shown in Fig. 19c.

(The complete series of steps involved in railroad and similar leveling for location and construction purposes is: (1) setting the station stakes; (2) running the levels; (3) making the profile; (4) laying the grade line on profile; (5) calculating vertical curves; (6) cross-sectioning for earthwork; (7) calculating earthwork quantities; (8) setting grade stakes.)

PROBLEM C5. VERTICAL CURVE.

(a) Equipment.-Drafting instruments, profile paper.

(b) Problem.—Connect two grade lines by a parabolic curve, as assigned.

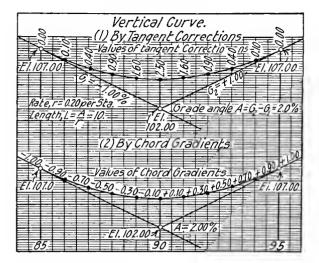
(c) Methods.—(1) Plot the given grade lines, station numbers, etc., on a sheet of profile paper. (2) Find the grade angle, i. e. the algebraic difference of the two rates of grade. (3) Determine the length of the vertical curve by dividing the grade angle by the assigned or adopted change of grade per station (notice the analogy to simple circular curves). (4) Calculate the apex correction. (5) Determine the corrections at the several stations or fractional stations (as assigned), and tabulate the stations and elevations.
(6) Plot the vertical curve from the data so determined, as in Fig. 19d. (7) Also compute and plot the same curve by the method of chord gradients.

PROBLEM C6. ESTABLISHING A GRADE LINE.

(a) Equipment.—Leveling instrument, leveling rod, flag pole, 100-foot steel tape, stakes, axe.

(b) *Problem.*—Establish an assigned grade line, (1) by measured distances and calculate rod readings, and (2) by "shooting in" the same line, for comparison.

(c) Methods.--(1) Stake off the distance between ruling points, and drive stakes to the required grade, or if desirable, parallel to it, by dividing up the fall in proportion to the distance. (2) Set the level over one ruling point and determine the height from the point to the line of collimation by means of the leveling rod; set the flag pole behind the other ruling point and establish a target, consisting of a rubber band holding a strip of paper wrapped about the



COMPARISON OF RESULTS										
Station	Elevation of Grade Tangent .	By Tangen Tangent Correction.		Chord Gra	ients. Curve Elevation.					
	Ft.	Ft.	Ft.	Per Cent.	Per Cent.	Ft.				
84 85(P,C) 86 87 88 90 (Apex) 91 92 93 93 95(P,T,) 96	108.00 107.00 105.00 103.00 103.00 103.00 104.00 105.00 106.00 107.00 108.00	+0.00 +0.10 +0.40 +0.90 +1.60 +2.50 +1.60 +0.40 +0.40 +0.10 \$0.00	107.00 106.10 105.40 104.90 104.60 104.50 104.60 104.90 105.40 106.10 107,00	+0.10 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20 +0.20	(+1.00) -0.90 -0.50 -0.50 -0.30 +0.10 +0.50 +0.50 +0.50 +0.70 +0.90 (+1.00)	107.00 106.10 105.40 104.90 104.60 104.60 104.60 104.90 105.40 105.40				

Fig. 19d.

pole at a height equal to the rod reading; having thus constructed a line parallel to the desired grade line, direct the telescope on the fore sight target, and with the same rod reading, "shoot in" the same stakes. Make careful record of data and comparative results.

PROBLEMS.

PROBLEM C7. SETTING SLOPE STAKES.

(a) Equipment.—Leveling instrument, self-reading leveling rod, 50-foot metallic tape, stakes, axe, marking crayon. (Or, instead of levelling instrument and rod, use special cross-sectioning rods, if assigned.)

(b) *Problem.*—Set slope stakes for the construction of a railroad, canal, etc., as assigned.

(c) Methods.—(Follow the methods described in Chapter VIII, "Railroad Surverying," under the head of "Cross-Sectioning.")

PROBLEM C8. CALCULATION OF QUANTITIES.

(a) Equipment.—(No instrumental equipment unless planimeter is assigned.)

(b) *Problem.*—Compute the quantity of earthwork for an assigned set of cross-section notes.

(c) Methods.—(1) Transcribe the notes and carefully verify the copy. (2) Calculate the sectional area for each station and intermediate in the notes, and prove the results. (3) Calculate the volume by the "average end area" method, results to nearest 0.1 cubic yard, and check the same. (4) If so instructed, plot the notes on cross-section paper and determine the areas by means of the planimeter as a check. Record the results.

PROBLEM C9. STAKING OUT A BORROW PIT.

(a) Equipment.—Engineers' level or transit with attached bubble, leveling rod tape, stakes, axe.

(b) *Problem.*—Stake out a borrow pit and take notes required for calculation of earthwork quantities.

(c) Methods.—(1) Select a base line, preferably outside the limits of the proposed borrow pit, set substantial station stakes say 50 or 100 feet apart along this base; designate these stakes A, B, C, etc. (2) Establish auxiliary reference lines by erecting perpendiculars to the base line at the several stakes, driving temporary stakes for pegs at suitable distances on these lines. (3) Establish a permanent bench mark and run levels, as in profile leveling, along lines starting at A, B, C, etc., noting elevations both at pegs and at marked intermediate changes of slope. (4) In

THE LEVEL.

case actual construction is undertaken, repeat the levels along the same auxiliary lines from time to time and calculate the quantities. (5) Record complete data.

LEVE	LS FOR	PROF	ILE AN	D QUA	NTITIE	5 FOR	. Pav	EMEN	TON	WRIG	NT 5	Ţ.	
Station	B- 5-	H-1-	F-5	T. P.	B•M•	Levele	r; J.Doo	. Rodma	n, R·Ro	e. Chaini	nen, 8·F·	Keen	
ł .								VEL5				9.W-Swift	
												R. Prop.	
						L 40 FT	L• 37 F f	10 20 17.	i i	K. LUFT	K-21 L2-	R·43Ft.	
+43	North F	roperty	Line, h	aaly 5t		<u>707•4</u> 4•7	<u>707-9</u> 4-2	<u>707.3</u> 4.8	<u>707:4</u> 4:7	<u>707-4</u> 4.7	707-2 4-9	<u>707.9</u> 5-2	
4+06	Center	Line, h	eely 51			<u>708.0</u> 4.1	<u>708.0</u> 4.1	<u>707-8</u> 4-3	708-2 3-9	<u>707-2</u> 4-9	<u>7072</u> 51	<u>706.7</u> 5.4	
+76	South A	ropert	y Line,	Hesiy S	×.	<u>707-5</u> 4-6	<u>707.5</u> 4.6		<u>708.6</u> 3.5		1	<u>706-6</u> 5-5	
3 7	Horth E	nd of B. 712.08	ridge ov	er Boney.	ard Creek	<u>705.8</u> 6.3	707-2 4-9	<u>708-6</u> 3-5	<u>708-8</u> 3-3	707:5 4.6	<u>705-1</u> 7•0	<u>706-7</u> 5-9	
;	212	112.00	7-89	708.95									
+62	South Er	d oF Bri	dge over	Baneya	d Creek	<u>705:4</u> 11:4	<u>707-0</u> 9-8	<u>707-3</u> 9-5	7.8	<u>706•3</u> 10•5	10.7	<u>706-3</u> 10-5	
2						<u>707-8</u> 9-0	<u>708-4</u> 8-4	<u>708-2</u> 8-6	<u>709.5</u> 7.3	<u>708-6</u> 8-2	<u>708-2</u> 8-6	<u>708-2</u> 8-6	
<i>i</i>						<u>7/1•1</u> 5·7	<u>711-0</u> 5-8	710-8	<u>711.3</u> 5.5	<u>711-1</u> • 5•7	<u>711.9</u> 4.9	<u>711-9</u> 4-9	
0	North Pi		Line, Gr	een St.		<u>7/3.9</u> 2.9	<u>714.0</u> 2.8	<u>713-6</u> 3-2	<u>714-0</u> 2.8	<u>713-9</u> 2-9	<u>714-9</u> 1-9	<u>714-2</u> 2-6	
π	0.88	716-84		au				•	1	1	4	•	
$\frac{1}{\pi}$	1.07	720-16	4.20	715.96		Maria	7 1011 /	the work			11:00		
	1.01	12010	3.94	719.09		May 7, 1914 (3 hours) Warm and Windy- Used Buff & Berger Dumpy Level, Locker Nº 15-							
	3.03	723-03	2.24	112.00		Chained down center of street, lining in							
2.1.0.M	- /•				720.00								

PROBLEM C10. LEVELS FOR PROFILE AND QUANTI-TIES FOR PAVING A STREET.

(a) Equipment.—Level, level rod, 3 flag poles, 100-foot steel tape, chaining pins, 50-foot metallic tape, hubs, axe.

(b) *Problem.*—Take level rod readings on the center line, right and left curb lines, right and left sidewalk lines, and right and left property lines to determine profiles and quantities for paving street. Plot profiles on Plate A profile paper to a scale of 100 feet to 1 inch horizontal and 10 feet to 1 inch vertical. Estimate the quantities of cut and fill, and paving materials.

(c) Methods.—(1) Locate the center line of the street and set flag poles on line about 400 feet apart by ranging in with the eye. (2) Drive a hub at one end of the street and call this point station zero. (3) Run a line of differential levels from the Standard B. M. to the zero end of the line.

						J.Doe, Leveler. R.Roe, Rodman.
	LEVE	.5 FO	r Coi	TOUR	5 ON	PROPOSED PARK SITE .
5.	+	π	-	R	E۰	Oct 16, 14. Clear, Warm. B.& B.Wye Level, Phila. Rod.
B·M·	6.67	106-67			100.00	Boulder, Sta. A1+45, 46'R. on knoll.
40				11.4	95.3	Ground- (All levels From single setting.)
A7				8.4	98.3	
A1+45				8.3	98.4	.0 1 2 3 4 +50
	(46'R)			6.9	99.8	
A2				9.7	97.0	is / Lovel &
A3				5.6	101-1	2 / 1 / 2
A3+50	Ridge 3			3.7	103.0	100
14				2.4	104.3	In the second se
A4+50				0.5	106-2	
80				10.5	96-2	
80+75	Ridge I			8-9	97.8	W-FE
81	Gully I			8.9	97.8	
	Ridge 2			8.1	98.6	0 1 2 3 4 $+50$
82	Gully 2			9.7	97.0	Dotted lines show ridges.
	Ridge 3			8.2	98.5	
B 2+70	Gully 3			8.8	97.9	
8.3			1	8.0	98.7	Set stakes only at Ste.0 and 4+50
84				5.3	101.4	on each line for future refer-
84+50				3.8	102.9	ence. Used chaining pins for
co				<i>]</i>]•7	95.0	intermediate points.
C 0+60	Ridge I			11-2	95.5	
CO+ 8 5	Gully 1			11.9	94.8	
c1			•	11-3	95.4	
	(Cont	nued on	Pollowi	ng page	e)	
	•					1

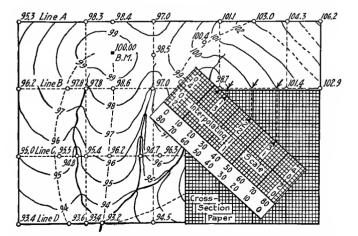


Fig. 19e.—Contour Plat and Device for the Rapid Interpolation of Contours.

Read the rod to 0.01 foot. (4) Read the level rod to 0.1 foot on the ground at center hub. (5) Measure the distance out to the right curb line, right sidewalk and right property lines with the metallic tape and read the rod to 0.1 foot on the ground at station zero. (5) Measure the distance out to the center line to station 1. (8) Measure to the right and left from the chaining pin the required distances with the metallic tape and take rod readings as at station zero. (9) Repeat the process at each station and at abrupt changes intermediate. (10) Check the level circuit. (11) Make profile on Plate A paper, scales 100 feet to the inch horizontal and 10 feet vertical, indicating the several lines by conventional lines or colors. (12) Lay grade line as directed. (13) Show plat at bottom of profile. (14)Plot sections to a scale of 20 feet to the inch and determine areas. (15) Compute quantities of earthwork, paving, etc. Follow the form.

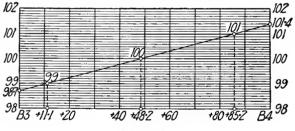


Fig. 19f.

PROBLEM C11. CONTOUR LEVELING.

(a) Equipment.—Engineers' leveling instrument, leveling rod, 100-foot steel tape, stakes, axe.

(b) *Problem.*—Make a rapid contour survey of an assigned tract of ground with the level and chain.

(c) Methods.—(1) Examine the tract and plan the system of reference lines for locating the points at which levels are to be taken; if the ground is comparatively regular, a simple subdivision into squares of 100 feet may suffice; but if much broken, special lines along gullies and ridges should be included in the survey plan. (2) Stake off the tract according to the plan, and make a record of the same. (3) Starting from an assigned bench, determine the elevations of the ground at the various stakes and at such other points as may be required to give a correct basis for accurate contouring. (4) Plot the data, and interpolate contours at a specified interval, employing both numerical calculations and geometrical methods, Fig. 19e. (5) Finish the plat, as required.

PROBLEM C12. USE OF CONTOUR MAP.

(a) Equipment.—Contour map, drafting instruments, etc.

(b) Problem.—From the given contour map: (1) construct profiles on the assigned lines; (2) project a line of specified grade through assigned points on the contour map; make profile, lay grade line and estimate earthwork quantities approximately; (3) calculate the earthwork quantities from the map for given grade planes and limitations of area. (The third step may, perhaps, best he taken with a different map from the first two.)

(c) Methods.—(1) Use profile paper for the profiles. (2) To project the line on the map, set the dividers at the horizontal distance in which the specified gradient will surmount the vertical interval between successive contour planes, Fig. 19f; then beginning at a specified point, locate points on the successive contour lines up or down on the given gradient, as required; sketch in the ronte roughly, and project a series of connected curved and tangent lines approximating to it; construct a profile along the new line; lay the required grade line on the profile, and estimate approximate earthwork quantities for specified dimensions and slopes of roadbed. (3) By means of end area method calculate the earthwork quantities required to establish the specified grade planes on the designated contoured area.

PROBLEM C13. RECIPROCAL LEVELING.

(a) Equipment.-Engineers' level, 2 leveling rods.

(b) *Problem.*—Determine the difference of elevation between two bench marks on opposite sides of a river (or wide ravine) by reciprocal leveling.

(c) Methods.—(1) Set the level up so that a rod reading may be taken on both henches at one setting. Station a rodman at each hench. (2) Take a back sight consisting of a series of say 5 or 10 careful consecutive rod readings. (3) Without delay take a like series of readings for a foresight. (4) Set the instrument on the opposite side of the river or ravine and repeat the above process. (5) Determine a difference of elevation by taking the difference between the mean back sight and fore sight for each setting, and finally take the mean of the two results. Observe rigid care in all details of the problem.

						10	os & R. Roe. Obs	TUATE.
(Dett	CACY	OF BU	-	/141		B. WYE LEV	
1.4			Level		, me,	0		With Telescope
No-	<u>Method</u> Microm		Scale*		rences	Length		I I
110-			B End		B End.			
. 1	Reading			A cuo	<u>B</u> C110.	DUDDIE	+	t= target
1	7	9.8	51.8		4:6	61.4	1	movement
2	17	14.2	47.2	4·4 4·3		61.2		Y I
3	27	18.5	42.7		4.5		\ ! /	
4	37	23.0	38.5	4.5	4.2	61.5	 <i>j</i>	0
5	47	27.0	34.4	4.0	4.1	61.4	$ \{\lambda \mid i\} $	
6	57	31.5	30.0	4.5	4.4	61.5		
7	67	35.8	25.7	4.3	4.3	61.5		R:D=b:t
8	77	40-2	21.0	4.4	4.7	61.2	RI	$R = \frac{b}{t}D \cdot$
							[i \]	
8	77	40.0	21.2			61.2	$ \wedge $	Target Movement (t)
7	67	35.5	25.5	4.5	4.3	61.0		<u>at 100 ft</u> . (<u>D</u>)
6	57	31.1	30.2	4.4	4.7	61.3	11 - 11	for Bubble Movement
5	47	26.7	34.6	4.4	4.4	61.3	Li Vi	(b) of 1 inch (0.083 Ft)
4	37	22.3	38-8	4.4	4.2	61.1	¥	No- Rods (Ft.) b (Ft.)
3	27	18.2	42.8	4.1	4.0	61.0	60	1 4.631 4.588 0.043
2	17	14.0	47.1	4.2	4.3	61-1	$R = \frac{bD}{E}$	2 4.586 4.546 0-040
	7	9.5	51.5	4.5	4.4	61.0	= -083 × 100	3 4.547 4.591 0.044
	el scala			60.9	61.1		0-042	4 4.593 4.634 0.041
ed	te 20th	inch)	Mean =	<u>4-36</u> 20ths	nch.		= 198 Ft.	. Mean = 0.042
Ten di	visions d	f micro	neter se	rew co	rrespon	d to 19	2 seconds of an	c, so that one division
								enths of an inch)
= 8	8 secon						•	
	s in Feer	ŀ <u>-</u>	17182	L 1 17	182 =	195 Fe	et.	
\mathbf{V}	1	\$005	per inc	7	88 -			L /

PROBLEM C14. TEST OF DELICACY OF BUBBLE VIAL.

(a) Equipment.—Engineers' leveling instrument, leveling rod, tape, level tester.

(b) *Problem.*—Determine the radius of curvature of the assigned bubble vial. (1) by means of the optical test, and (2) by the level tester.

(c) Methods.—(1) Measure off a base line say 100 feet long, set level at one end and hold rod on a peg driven at the other end; note the target movement corresponding to a given bubble movement, both in the same linear unit; calculate the radius by the method shown at (h), Fig. 18. (2) Set the level tester on a solid base and place the instrument on it, as indicated at (i), Fig. 18; by means of the micrometer head and known relations of the level tester, determine the angular equivalent in seconds for one division and also one inch movement of the bubble, from which calculate the radius of curvature of the vial in feet. Follow the form.

PROBLEM C15. COMPARISON OF LEVEL TELESCOPES.

(a) Equipment.—Five (or other specified number) engineers' levels (both wye and dumpy), leveling rod, metallic tape.

(b) *Problem.*—Make a critical examination and comparison of the telescopes of the assigned instruments.

(c) Methods.—Carefully read the discussion of the telescope in the text. Then compare the telescopes with reference to: (1) magnifying power; (2) chromatic aberration; (3) spherical aberration; (4) definition; (5) illumination; (6) flatness of fields; (7) angular width of field; (8) effective aperture of objective. Make tabulated record of comparisons, giving in separate columns; (a) locker number; (b) kind of level; (c) name of maker; (d) magnifying power, and so on for the other points examined.

PROBLEM C16. TESTS OF THE WYE LEVEL.

(a) Equipment.-Wye level, feveling rod, tape.

(b) Problem.—Test the essential relations and adjustments of the wye level.

(c) Methods.—Carefully note the construction of the assigned level and the positions of the elementary lines. Then following the methods outlined in the text, test the following adjustments (but do not disturb the adjusting screws): (1) The bubble, both as to the azimuth and altitude movements; find the position of the bubble when parallel to the element of the rings. (2) The line of collimation; its deviation from the axis in 400 feet. (3) The wyes; finding the position of the bubble when the vertical axis is vertical. Keep a neat and systematic tabulated record of observed numerical data, with explanation of the several adjustments.

PROBLEM C17. ADJUSTMENT OF THE WYE LEVEL.

(a) Equipment.—Wye level (reserved expressly for adjustment), leveling rod, tape, adjusting pin.

(b) *Problem.*—Make the full series of adjustments of the wye level.

(c) Methods.—Follow the methods detailed in the text according to the following program: (1) Adjust the bubble line (a) into the same plane with the bottom element of the rings, and (b) parallel to that element. (2) Adjust the line of collimation to coincide with the axis of the rings, first on a long distance; and then, to test the object glass slide, try it for a short distance; if necessary, shift the reticule in rotation to make the horizontal hair horizontal. and also center the eveniece. (3) Adjust the bubble line perpendicular to the vertical axis by means of the wve nuts. (4) Test the rings of the wye level by the two-peg test; if the level has a reversion bubble, first test the parallelism of the top and bottom tangent lines, and then test the rings. Keep a clear and systematic record. In each case, state (a) the desired relation, (b) the test, and (c) the adjustment.

PROBLEM C18. SKETCHING THE WYE LEVEL.

(a) Equipment.—Wye level.

(b) *Problem.*—Make a first-class freehand sketch of the assigned wye level.

(c) *Methods.*—The sketch should be correct in proportion and clear in detail. The essential parts should be designated in neat and draftsmanlike form, and the elementary lines clearly indicated.

PROBLEM C19. TESTS OF THE DUMPY LEVEL.

(a) Equipment.—Dumpy level, leveling rod, tape.

(b) *Problem.*—Test the essential relations and adjustments of the dumpy level.

(c) Methods.—Carefully note the construction of the assigned level and the position of the elementary lines. Then, following the methods outlined in the text, test the following adjustments: (1) the bubble line, whether perpendicular to the vertical axis; and if not, what is the angular inclination of the vertical axis when the bubble is in the

PROBLEMS.

middle? (3) The line of collimation, whether parallel to the bubble line. Record the errors and observations systematically.

PROBLEM C20. ADJUSTMENT OF THE DUMPY LEVEL.

(a) Equipment.—Dumpy level (reserved expressly for adjustment), leveling rod, tape, pegs, axe, adjusting pin.

(b) Problem.—Make the essential adjustments of the assigned dumpy level.

(c) Methods.—(1) Adjust the bubble line perpendicular to the vertical axis. (2) Adjust the line of collimation parallel to the bubble line by the two-peg method. In describing the adjustments, the record should state (a) the desired relation, (b) the test, and (c) the adjustment.

PROBLEM C21. SKETCHING THE DUMPY LEVEL.

(See Problem C18.)

PROBLEM C22. STRETCHING CROSS-HAIRS.

(a) Equipment.—Engineers' level or transit (or crosshair reticule), pocket cross-hair outfit, reading glass.

(b) *Problem.*—Renew the cross-hairs in a level or transit instrument by a method applicable to field use.

(c) Methods.—(If instrument is provided, follow the complete program outlined below; otherwise, merely stretch the lines on the reticule and test same.) (1) Remove the eyepiece, carefully preserving the screws from loss. (2)Remove one pair of the capstan headed reticule screws; turn the ring edgewise and insert a sharpened stick in the exposed screw hole, take out the other two screws and remove reticule from telescope tube. (3) Clean the cross-hair graduations, and support the reticule on a sharpened stick, or (if a transit) place it on the object glass with a piece of paper interposed to protect the lens. (4) Select from the capsule (see (d), Fig. 17) two spider lines 2 inches or more long, and fasten a stick to either end of each hair by means of glue from the adhesive paper. (5) Put the bairs in place, (with the bits of wood hanging loose), shifting them as desired with a pin point or knife blade. (6) Apply a bit of the moistened adhesive paper to the reticule over each hair.

and after a few minutes cut or break the sticks loose. (7) Test the hairs by blowing on them full force. (8) If they stand this test, replace the reticule, and adjust the instrument. Make a record of the process.

PROBLEM C23. ERROR OF SETTING A LEVEL TARGET.

(a) Equipment.—Engineers' leveling instrument, leveling rod (preferably a New York or Boston rod), tape, pegs.

(b) *Problem.*—Determine the probable error of setting the level target at distances of 100 and 300 feet (or such other distances as may be assigned).

(Leveler, R.Roe.	Young Level.
		Rodman, J. Doe.	Boston Rod, Lr. 12.
ERROR OF S	ETTING	Level Target.	
Distance 100 Feet. Distan	ce 300 Feet.	Nov. 1, 1914, (2 hours).	laudy.cool.breezy.
Reading d d d ² Reading		Distances with 50-F	
No.I Ft. Ft. Nal Ft.	FE.	<i>processes men se y</i>	
1 3.169 0.000 0.000000 1 4.843	0.006 0.000036	Setinstrument in s	heltered place, measured
2 3.170 .001 .000001 2 4.835	.002 .000004		peg. Same at 300 Ft.
3 3.170 .001 .000001 3 4.836	.001 .000001	Placed pair of foot s	
4 3.170 .001 .000001 4 4.837	.000 .000000		up, leaving screws just
5 3.169 .000 .000000 5 4.834	.003 .000009	snuq.	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
6 3.168 .001 .000001 6 4.834	.003 .000009		crosshairs very care-
7 3.171 .002 .000004 7 4.837	.000 .000000		normal condition.
8 3.168 .001 .000001 8 4.839	.00Z .000004	Set target ten time:	
9 3.169 .000 .000000 9 4.838	.001 .000001		the position of the
10 3.168 .001 .000001 10 4.835	.002 .000004	bubble each time be	fore approving sight.
n 3.169 0.0008 0.000010 n 4.837	0.002 0.000068	Determined maanif	ving power of telescope
			on rod natural size
Mean Mean=F Sum=E Mean	Mean=f Sum=2		agnified by telescope
			nd Mag.Power to be
Prob.Error Single Obs.		28 diameters.	
	010	Found radius of cur	vature of bubble
$E_{r} = 0.67 \frac{1}{10-1} = 0.00070 E_{r} = 0.00070$	010	$R = \frac{b}{D} = \frac{0.07}{x} \times 100$	
Approx. Prob. Single Error		F 0.078	
	rox.)=0.0017	Diam. hor. hair, h==	<u> </u>
			400
Prob.Error of Mean		=0.00002 Ft.=0.0	0024 in. rod
$E_m = \frac{E_1}{\sqrt{n}} = 0.00022$ $E_m = 0.00022$	0005	¥	11-1
4m Vn - V.00022 [2m = 0.	0003	h 🛛 🗠 🚬	
		¥	· · · · · · · · · · · · · · · · · · ·
		f	D
		<u> </u>	

(c) Methods.—(1) Determine the magnifying power of the telescope. .(2) Determine the radius of curvature of the level vial by the field method. (3) Determine the space on the rod covered by the diameter of the hair. (4) Drive a peg at 100 feet from the level, level up, and secure ten satisfactory consecutive rod readings with rod held truly plumb on the peg; shift the target several inches between readings, and reset without bias; reject no readings; watch the bubble closely, but work briskly. (4) Repeat the series at 300 feet. (5) Determine for each distance the mean rod, the probable error of a single reading, and of the mean, as indicated in the form.

PROBLEM C24. MAKING A LEVELING ROD.

(a) Equipment.—Piece of straight dressed clear white pine of proper dimensions, steel tape graduated to 0.01 foot, carpenter's tri-square, paint, etc.

(b) Problem.-Make a self-reading leveling rod.

(c) Methods.—(To be devised by the student. See Fig. 27 for suggested graduations.)

PROBLEM C25. COMPARISON OF DIFFERENT MAKES AND TYPES OF ENGINEERS' LEVELS.

(a) Equipment.—Department equipment, catalogs of representative engineering instrument makers.

(b) *Problem.*—Make a critical comparison of the several types and makes of engineers' levels.

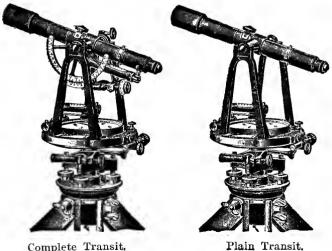
(c) Methods.—Examine the department equipment and study the several catalogs carefully, noting the usual and special features, prices, etc., and prepare a systematic summary or digest of the same. Prepare brief specifications for a leveling instrument, and also suggest the preferred make.

CHAPTER V.

THE TRANSIT.

Description.-The engineers' transit consists of an alidade, carrying the line of sight, attached to an inner vertical spindle (or upper motion) which turns in an outer annular spindle (or lower motion). The latter carries the horizontal graduated circle or limb, and is supported by the tripod head. The alidade includes the telescope, magnetic needle with its graduated circle, and the vernier; it may be revolved while the graduated limb remains stationary. The horizontal limb is graduated to degrees and half degrees and sometimes to twenty minutes, and is numbered preferably from zero to 360° in both directions.

The complete transit differs from the plain transit, Fig. 20, in having a vertical arc and level bubble attached to the telescope.



Plain Transit.

Fig. 20, 97

THE TRANSIT.

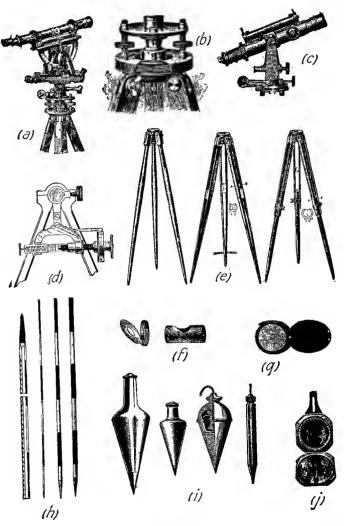


Fig. 21.

In Fig. 21 are shown: (a) the English theodolite; (b) the shifting plates and foot screws of a transit; (c) the Saegmuller solar attachment to the transit; (d) the gradienter; (e) tripods; (f) reflectors; (g) reading glass; (h) flag poles; (i) plumb bobs; (j) the Brunton pocket transit.

The Vernier.—The vernier is an auxiliary scale used to read fractional parts of the main graduated scale or limb. The *least count* of a direct vernier is found by dividing the value of one division of the limb by the number of divisions on the vernier. With a limb graduated to half degrees and a direct vernier reading to single minutes 30 divisions on the vernier cover 29 divisions on the limb.

In *reading* a direct vernier observe the following rule: Read from the zero of the limb to the zero of the vernier, then along on the vernier until coincident lines are found. Add the reading of the vernier to the reading of the limb.

In setting the vernier to a given reading, as for example a zero reading for measuring an angle, the tangent movement should be given a quick short motion to secure the last refinement, since a slow movement is not noticed by the eye. Notice adjacent and end graduations.

In Fig. 23, (c) is a vernier reading to single minutes, (d) to half minutes (30''), and (e) to thirds of minutes (20''). The slant in the numerals on the limb corresponds with that on the vernier.

USE OF THE TRANSIT.

Use.—The complete transit is used: (1) to prolong lines; (2) to measure horizontal angles; (3) to measure vertical angles; (4) to run levels; (5) to establish grade lines. The plain transit is confined to the first two uses, unless it has a vertical clamp and tangent movement, when it may be used to "shoot in" grade lines.

Prolongation of Lines.—If the instrument is in adjustment a line can be prolonged by sighting at the rear station and reversing the telescope in altitude. It is, however, not safe to depend on the adjustments of the transit, and important lines should always be prolonged by the method of "double sights," as given in Problem D2. Lines may be prolonged with the plates by sighting at the rear station with the A vernier reading 180°, reversing the alidade in azimuth and locating stations ahead with the A vernier reading zero. A third method employs two points ahead of the instrument.

Measurement of Horizontal Angles.—Horizontal angles are measured as described in Problem D1. If greater accuracy is required, angles may be measured by series or by repetition.

By Series.—In measuring an angle by series all the angles around the point are read to the right, both verniers being read to eliminate eccentricity. The instrument is then reversed in altitude and azimuth and all the angles around the point are read to the left. The readings are checked by sighting back on the first point in each case. These observations constitute one "set." The vernier is shifted between sets 360° divided by the number of sets. The arithmetical mean of the observed values is taken as the true value.

By Repetition.—Angles are measured by repetition as described in Problem D13. This method is especially suited to the accurate measurement of angles with an ordinary transit, and is to be preferred to the series method, which is a favorite where precise instruments are used. In the repetition method all the instrumental errors are eliminated and the error of reading is very much reduced. It is doubtful if it is ever consistent to make more than 5 or 6 repetitions.

Azimuth.—The azimuth of a line is the horizontal angle which it makes with a line of reference through one of its ends, the angles being measured to the right from 0° to 360° , as in (f) Fig. 23. It is usual to assume that the true meridian is the line of reference, the south point being taken as zero in common surveying.

Deflection.—The deflection of a line is the angle that it makes with the preceding line produced, and is called deflection right or left depending upon whether the angle is on the right or left side of the line produced, as in (h), Fig. 23.

Vertical Angles.—Vertical angles are referred to the horizon determined by the plane of the level under the telescope, and are angles of depression or elevation relative to that plane. In measuring vertical angles the instrument should be leveled by means of the level under the telescope and correction should be made for index error of the vernier. With a transit having a complete vertical circle, the true vertical angle may be obtained by measuring the angle with the telescope normal and reversed and taking the mean.

Traversing.-A traverse is a series of lines whose

lengths and relative directions are known. Traverses are used in determining areas, locating highways, railroads, etc.

Azimuth Traverse.-In an azimuth traverse the azimuths of the lines are determined, usually passing around the field to the right. In orienting the transit at any station the A vernier is set to read the azimuth of the preceding course, the telescope is reversed, directed towards the preceding station and the lower motion clamped; the telescope is then reversed in altitude. The reading of the A vernier with telescope normal will then give the azimuth of any line sighted on. If there is any error in collimation the transit may be oriented by sighting back with the A vernier reading the back azimuth of the preceding course. In a closed traverse the last front azimuth should agree with the first back azimuth. The azimuth traverse is especially adapted to stadia and railroad work. Azimuths can be easily changed to hearings, if desired.

Deflection Traverse.—In a deflection traverse the deflection of each line is determined, usually passing around the field to the right. To avoid discrepancies due to error in collimation, the transit may be oriented by sighting at the preceding station with the A vernier set at 180°, the telescope being in its normal position, and the lower motion clamped. The reading of the A vernier will then give the deflection of any line sighted on.

Compass Bearings.—Compass bearings should always be read on an extended traverse as a check against such errors as using the wrong motion or an erroneous reading of the vernier. To guard against errors due to local attraction, back and front bearings should always be read, and the angle thus determined compared with the transit angle.

Leveling with the Transit.—The transit with an attached level is the complete equivalent for the engineers' level. The instrument is leveled up with the plate levels first, after which the position of the attached bubble is controlled by means of the vertical tangent movement.

Grade Lines.—Grade lines may be established with the transit either by means of known distances and calculated rod readings, or by "shooting in" a parallel line by means of the inclined telescope, as described under the use of the engineers' level. For the latter purpose the transit is rather more convenient than the level.

Setting up the Transit.—To set the transit over a point, spread the legs so that they will make an angle of about 30°, place them symmetrically about the point with two legs down hill. Bring one plate level parallel to two of the legs, force these legs firmly into the ground and bring the plumb bob over the point and the plates approximately level with the third leg, changing the position of the plumb bob with a radial motion and leveling the plates with a circular motion of the leg. Finish the centering with the shifting plates. In leveling up, the bubbles move with the left thumb. Use care to bring the foot screws to a proper bearing.

Parallax.—Before beginning the observations the eyepiece should be carefully focused on the cross-hairs so as to prevent parallax.

Back Sight With Transit.—Always check the back sight before moving the transit to see that the instrument has not been disturbed or that a wrong motion has not been used.

Instrumental Errors.—The transit should be kept in as perfect adjustment as possible, and should be used habitually as though it were out of adjustment, that is, so that the instrumental errors will balance. No opportunity should be lost to test adjustments.

ADJUSTMENTS OF THE TRANSIT.

Elementary Lines.—Fig. 22 shows the elementary lines of the transit, viz., (1) line of collimation; (2) horizontal axis; (3) vertical axis; (4) plate level lines; (5) attached level lines. These lines should have the following relations: (a) the plate levels should be perpendicular to the vertical axis; (b) the line of collimation should be perpendicular to the horizontal axis; (c) the horizontal axis should be perpendicular to the vertical axis; (d) the attached level line should be parallel to the line of collimation. The following additional relations should exist: (e) the vertical axes of the upper and lower motions should be coincident; (f) the optical center of the objective should be projected in the line of collimation; (g) the center of the graduated circle should be the center of rotation, i. e., there should be no eccentricity.

Plate Levels.—To make the plate levels perpendicular to the vertical axis.—Make the vertical axis vertical and adjust the bubbles to the middle of their race. The vertical axis is made vertical by leveling up, reversing in azimuth, and if the bubbles move, bring them half way back with the foot screws. The adjustment is the same as for the compass, and the reasons are shown in (a), Fig. 13. After adjusting the plate levels with reference to say the upper motion, test them with the lower motion to prove the coincidence of the vertical axes.

(a) Optical Center Intersection of Cross-Hairs Line of Collimation Line of Collimation Attached Level Line (C) Plate Level Line Plate Level Line (b)

Line of Collimation.—To make the line of collimation perpendicular to the horizontal axis.—Construct a straight line and adjust the vertical hair so that the instrument will reverse in altitude on it The straight line may be established either by prolongation beyond a point in front, or

Fig. 22.

preferably by the methods of double sighting, described in Problem D2. One-fourth the apparent error is corrected in second case as shown in (a), Fig. 23. In deciding which way to move the hair, notice that the optical center is the fulerum. The transit should be collimated first for equal back and fore sights, say 100 feet or so, and then checked for a distant point in one direction and perhaps 50 feet in the other, so as to test the motion of the optical center of the objective. The points should all be as definite as possible. Chaining pins may be used, or V-marks may be made on the side of a stake driven securely. Each altitude reversal should be checked back and forth to make sure of the prolongations, and the telescope should be handled very carefully. If the cross-hair reticule is removed from the instrument or should be much disturbed, the foregoing adjustment is made approximately and the hair is made vertical by sighting on a plumb line, such as the corner of a building, or by noting whether the hair continuously covers the same point as the telescope is moved in altitude; the collimation adjustment is then made precisely.

Horizontal Axis.—To make the horizontal axis perpendicular to the vertical axis.—Adjust the horizontal axis so that the line of collimation will follow a plumb line. An actual plumb line may be used; or preferably a vertical line may be constructed by first sighting on a high point, then depressing the telescope and marking a low point; then reversing in altitude and azimuth (turning the horizontal axis end for end), sighting at the high point again and marking a second low point beside the first one. The mean of the two low points is vertically beneath the upper one. The transverse plate level is especially important in this process. One end of the horizontal axis is changed, as in (b), Fig. 23.

Attached Level.—To make the attached level and the line of collimation parallel to each other.—Construct a level line and adjust the instrument to agree with it. The level line may be obtained either by using the surface of a still body of water, as of a pond, or it may be constructed by equal back and fore sights, as indicated in (e), Fig. 16. Either the horizontal hair may be changed to bring the line of collimation parallel to the bubble line, or vice versa. The method is the same as nsed for the dumpy level.

If the bubble vial is a reversion level, as shown at (b), Fig. 18, the adjustment is much simpler. However, the two-peg test should be applied at least once to the reversion level to prove the parallelism of the top and bottom tangent lines of the bubble vial.

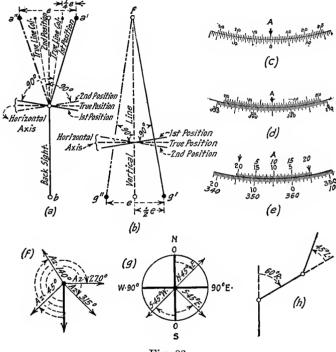


Fig. 23.

Vertical Arc.—After the last preceding adjustment, the vernier of the vertical circle should be made to read zero when the bubble is at the center of the tube. Bring the bubble to the center and shift the vernier to read zero. If the vernier is fixed, an index correction may be applied to all vertical angles; or the bubble may be made to agree with the vernier and the horizontal hair then adjusted by the two-peg method.

Eccentricity.—Read the two verniers at intervals around the circle; if the verniers have changed the same amount in each case the circle is well centered. If the two verniers have not changed the same amount, the mean of the angles passed over by the verniers is the actual angle through which the instrument has turned. The error cannot be adjusted.

Centering the Eyepiece.—If the intersection of the cross-hairs is not in the center of the field of view, move the inner ring of the eyepiece slide by means of the screws which hold it.

PROBLEMS WITH THE TRANSIT.

PROBLEM D1. ANGLES OF A TRIANGLE WITH TRANSIT.

(a) Equipment.—Transit, 2 flag poles, reading-glass.

(b) Problem.—Measure the angles of a given triangle with the transit.

(c) Methods.—(1) Set the transit over one of the vertices of the triangle and plumb a transit pole over each of the other two. (2) Set the A vernier to read zero, sight at the left hand point approximately, clamp the lower motion and make an exact bisection with the lower tangent movement. (3) Unclamp the upper motion, sight at the right hand point approximately and make an exact bisection with the upper tangent movement. (4) Read the A vernier to the nearest single minute. This reading is the angle sought. (5) With the A vernier set to read zero repeat the measurement, sighting first at the right hand station and then at the left. The recorded value of the angle is to be the mean of these two determinations which must not differ by more than one minute. (6) Measure the other angles in like manner. The error of closure must not exceed one minute. Follow the prescribed form.

PROBLEM D2. PROLONGATION OF A LINE WITH TRANSIT.

(a) Equipment.—Transit, 2 flag poles, axe, 6 hubs, 6 flat stakes, tacks.

(b) *Problem.*—Prolong a 300-foot base line successively with the transit by the method of "double sights" about 1500 feet, and check on a hub previously established.

(c) Methods.—(1) Drive two hubs, A and F, about 1500 feet apart. (2) Set the transit over tack in hub A, sight at

PROBLEMS.

Observers, J. Doe & R. Roe. ANGLES OF TRIANGLE WITH ENGINEERS' TRANSIT. 5-6-8 Station Value of Angle. Nov 15, 1914, (2 hours). Warm and quiet. Used Hellar & Brightly Transit No 10 5 88°50' 88°51' 88°50'30 The 1st measurement was made by sighting 6 498491 47850 on Sta-8 with the lower motion, the 47 47 47 47 47°47'00 ... plates clamped at zero; then sighting 43°23' 43°23'0 43 23 on Sta 6 with the upper motion, and 180 00'30 reading the plates. The second measurement was made by sighting on 5ta-6 and then on Sta-8-Used transit poles at targets, plumbing tham very carefully over the monu-(Difference between to exceed I') measurements not (Erra r not to exceed 1') ments. Sketch shows observed angles. J.Doe 11-16-14. (3 hrs.) Cool. Cloudy. Observers R.Rog Used K.S.E. Transit Nº4. "DOUBLE SIGHTINGS" TRANSIT WITH ENGINEERS PROLONGATION OF LINE-INTERPOLATION OF POINT. (Set up at E "double Bisected pp' at P. Set (5) sighted to F. New up at A and checked P; error, 0:02 to right. tack F is 0.01 left check on each altitude telescope Reversed in azimuth; of original tack. (Allowable error is shifted transit so it è, (4) 0.01 VNo-Sightings would again plunge pue For 300' sights) Set up at D, "double sighted" to E. exactly on A and B b plunge Drove hub p" to bob. 0:13 SDEGG o'13 (Set up and shifted Set up at C, ^Gdouble transit laterally N/Y sighted" to D. \$ until it would with last. (3) Set up at B. "double plunge exactly 888 Paces important on A and B. (See Note) sighted to Cy as observations Forth . Drove hub p' to plumb bob. Follows; (See Note-+) 18/¥ Set Flags on tacks at (a) Backsighted on A (b) Plunged to C' A and B, and determined Bces 13 and Ά (c) Rotated to A (2) point P. by lining in two exceeding the poles successively by eye. (See p.22.) *<100 F (d) Plunged to c" beck Drove temporary peg (Drove hubs A and B about 600' apart, Take (e) Bisected c'c" to check locate tack C ello Paces delicately reversal. 1. ALWAYS chec Set up at A; sighted (1) assumed to have hill between them, <u>ي</u>. both visible from desired hub P. on Fleg at F; drove hub 1 B; removed Flag F. μÌ NOTE. Watched plate levels closely, Orove hubs A and F 20X (l)especially transverse bubble. 1500' apart (about)

flag pole plumbed over tack in hub F, drive hub B about 300 feet from the transit and locate a tack in line very carefully. Remove the flag pole from hub F. (3) Set the transit over hub B, back sight on hub A and clamp the vertical axis. (4) Reverse the telescope, drive hub \hat{C} at a distance of about 300 feet and mark line very carefully with a pencil. (5) Reverse the transit in azimuth, sight on hub A; reverse the telescope and locate a second point on hub C. Drive a tack midway between these two points. (6) Set the transit over the mean point on hub C. back sight on hub B, prolong 300 feet and set hub D by double sights. (7) Set over hub D, back sight on hub C, prolong, 300 feet and set hub E, as before. (8) Finally prolong from hub E, with back sight on D, and establish mean tack at terminal hub F. Record the collimation errors at C, D, E, and the final error at F. Follow the form.

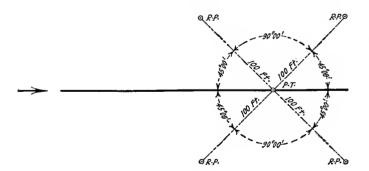
PROBLEM D3. INTERSECTION OF LINES BY TRANSIT.

(a) Equipment.—Transit, 2 flag poles, plumb bob string, axe, 6 hubs, 6 flat stakes, tacks, marking crayon.

(b) *Problem.*—Determine the intersection of the bisecting lines of two angles of a triangle and check by bisecting the third angle.

(c) Methods.—(1) Drive and tack three hubs so as to form a triangle approximately equilateral and having sides about 400 feet long; properly witness the hubs with guard stakes. (2) Set the transit over one of the vertices of the triangle, and measure the angle as in Problem D1. (3) Set two hubs on the bisecting line, about 6 feet apart, so that the point of intersection of the bisecting lines will come between them, and mark the line by stretching a string between the hubs. Check by measuring each half angle independently. (4) Set the transit over one of the other vertices of the triangle, measure the angle and determine the bisecting line as at the first point. (5) Drive a hub at the intersection of the two bisecting lines and mark the exact point with a tack; check by measuring each half angle independently. (6) Set the transit over the third vertex and determine the angular and linear error of intersection. (7) As a final check measure the angles around the point of intersection of the bisectors. The angular error of closure of any triangle should not exceed one minute. Follow the form.

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PROBLEM D4. REFERENCING OUT A POINT.

(a) Equipment.—Transit, 2 flag poles, 100-foot steel tape, axe, 6 hubs, 6 flat stakes, marking crayon, tacks.

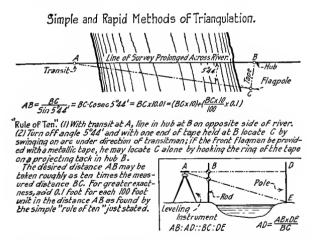
(b) Problem.—Reference out a point with a transit and tape.

(c) Methods.--(1) Drive two hubs about 500 feet apart and mark them with guard stakes. (2) Set the transit over one of the hubs and reference it out as shown in the diagram. All hubs should be driven flush with the ground, and the exact points should be marked by means of tacks driven into the tops of the hubs. Record in proper form.

PROBLEM D5. TRIANGULATION ACROSS RIVER.

(a) Equipment.—Transit, 2 flag poles, 100-foot steel tape, axe, 4 hubs, 4 flat stakes, tacks.

(b) *Problem.*—Determine the distance across an imaginary river by triangulating with the transit and check by direct measurement.



(c) *Methods.*—(To be devised by the student. Use this and the next problem to learn the relative merits of several good methods. The "rule of ten" method in the sketch below is very rapid and also quite accurate.)

PROBLEM D6. PASSING OBSTACLE WITH TRANSIT.

(a) Equipment.—Transit, 100-feet steel tape, 2 flag poles, axe, hubs, flat stakes, tacks.

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	Distance F] . "Equ	An Iateral	gle Value Triang	Error a Dist Ft	Closura Line Ft	Observers : J-Doe Nov I7, 1914 , (2 Ho Used Gurley Trans	& R·Roe urs) Warm & cloudy- it, Locker Nº5, and
A	Distance F†· ¹⁴ Equ 200·00	An lateral <i>N-A-E</i>	gle Value Triang <i>60°00</i> 7	Error a Dist Ft	Closura Line Ft	Observers : J.Doe Nov. 17, 1914, (2 Ho Used Gurley Trans chaining Locke	& R•Roe vrs) Warm & cloudy- it, Locker Nº5, and r Nº32•
A E	Distance F†- ¹⁴ Equ 200-00 200-00	An lateral <i>N-A-E</i> <i>A-E-D</i>	gle Value Triang <i>60°00'</i> <i>60°00'</i>	Error a Dist Ft	Closura Line Ft	Observers : J. Doe Nov 17, 1914 , (2 Ho Used Gurley Trans chaining Locke With the transit o	& R. Roe yrs) Warm & claudy. it, Locker Nº5, and r Nº32. yer M, set hubs at A
A E D	Distance F†- ¹⁴ Equ 200-00 200-00 301-03	An lateral <i>N-A-E</i> <i>A-E-D</i>	gle Value Triang <i>60°00</i> 7	Error a Dist Ft- e Met	Closur <i>e</i> Line Ft had"	Observers : J-Doe Nov 17, 1914, (2 Ho Used Gurley Trans chaining Locke With the transit o and N, in the line	& R. Roe yrs) Warm & Claudy. it, Locker Nº5, and r Nº32 ver M, set hubs at A MN. Set transit at A
A E	Distance F†- ¹⁴ Equ 200-00 200-00	An lateral <i>N-A-E</i> <i>A-E-D</i>	gle Value Triang <i>60°00'</i> <i>60°00'</i>	Error a Dist Ft- e Met	Closura Line Ft	Observers : J-Doe How 17, 1914 , (2 Ho Used Gurley Trans chaining Locke With the transit o and N, in the line and prolonged th	& R.Roe urs) Warm & cloudy- it, Locker Nº5, and r Nº32- ver M, set hubs at A MN-Set transit at A e line MA by the "Eqi-
A E D	Distance Ft. ''Equ 200-00 301-03 199-93	An lateral <i>N-A-E</i> <i>A-E-D</i> <i>e-D-N</i>	g le Value Triang 60°00' 50°00' 59°59'	Error a Dist: Ft- e Met -0-07	Closure Line Ft. hod" <i>0.09 R</i> -	Observers : J-Doe Nov 17, 1914, (2 Ma Used Gurley Trans chaining Locke With the transit o and N, in the line and prolonged th Isteral Triangle	& R.Ros urs) Warm & cloudy- it, Locker Nº5, and r Nº32- ver M, set hubs at A MM- Set transit at A e line MA by the "Eqi- Method" the "Right
A E D	Distance Ft. ''Equ 200-00 301-03 199-93	An lateral <i>N-A-E</i> <i>A-E-D</i> <i>e-D-N</i>	g le Value Triang 60°00' 59°59' 1e Offs	Error a Dist: Ft- e Met -0-07	Closure Line Ft. hod" <i>0.09 R</i> -	Observers : J-Doe Nov 17, JUA, (2 Nd Used Gurley Trans chaining Locke With the transito and N, in the line and prolonged th lateral Triangle Angle OFFset	& R.Roe. Urs) Warm & cloudy. It, Locker NS-5, and. r N-32. ver M, set hubs at A MN. Set transit at A e line MA by the "Raight Method" and the
A E D	Distance Ft- '' Equ 200-00 200-00 301-03 199-93 '' Ric	An lateral <i>N-A-E</i> <i>A-E-D</i> <i>e-D-N</i>	gle Value Triang <i>60°00'</i> <i>60°00'</i>	Error a Dist: Ft- e Met -0-07	Closure Line Ft. hod" <i>0.09 R</i> -	Observers : J-Doe Nov 17, 1914 , (2 No Used Gurley Trans chaining Locke With the transit o and H, in the line and prolonged th Isteral Triangle Angle Offset J "Deflection No	& R.Roe Vrs) Warm & cloudy- it, Locker Nº5, and r Nº32 ver M, set hubs at A MN. Set transit at A e line MA by the "Right Method" and the thad
A E D A-D	Distance Ft- '' Equ 200-00 200-00 301-03 199-93 '' Ric 20-00	An lateral <i>N-A-E</i> <i>A-E-D</i> <i>e-D-N</i> ht Ang	g le Value Triang 60°00' 59°59' 1e Offs	Error a Dist: Ft- e Met -0-07	Closure Line Ft. hod" <i>0.09 R</i> -	Observers : J-Doe Nov 17, 1914 , (2 No Used Gurley Trans chaining Locke With the transit o and H, in the line and prolonged th Isteral Triangle Angle Offset J "Deflection No	& R.Roe Vrs) Warm & cloudy- it, Locker Nº5, and r Nº32 ver M, set hubs at A MN. Set transit at A e line MA by the "Right Method" and the thad
A E D A-D A B	Distance Ft- '' Equ 200-00 301-03 199-93 '' Ric 20-00 200-00	An lateral <i>N-A-E</i> <i>A-E-D</i> <i>e-D-N</i> ht Ang <i>N-A-B</i> <i>A-B-C</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00'	Error a Dist: Ft- e Met -0-07	Closure Line Ft. hod" <i>0.09 R</i> -	Observers : J-Doe Nov 17, 1914 , (2 No Used Gurley Trans chaining Locke With the transit o and H, in the line and prolonged th Isteral Triangle Angle Offset J "Deflection No	& R.Roe Vr3) Warm & cloudy- it, Locker Nº 5, and r Nº 32 ver M, set hubs at A MH. Set transit at A eline MA by the 'Eqi- Method', the "Right Method' and the thod a, Length of tepe
А Е D A-D А В С	Distance Ft- ¹¹ Equ 200-00 301-03 199-93 ¹¹ Ric 20-00 200-00 20-00 20-00	An Iateral <i>KA-E</i> <i>A-E-D</i> <i>e-D-N</i> <i>ht Ang</i> <i>N-A-B</i> <i>A-B-C</i> <i>B-C-D</i>	gle Value Triang 60°00' 59°59' 90°59' 1e Offs 90°00' 90°00' 90°00'	Error o Dist: Ft: e Met - <i>0-07</i> et Met)	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers : J-Doo Nov I7, 1914, (2 Ho Used Gurley Trans chaining Locké With the Transit o and N, in the line and prolonged th Isteral Triangle Angle OFFset , "Deflection No en f	AF R. Roe. UTS) Warm AF Cloudy. UTS) Warm AF Cloudy. If Locker NS-5, and. T MS Set hubs at A Min. Set transit at A Min. Set transit at A Min. MA by the "Right Method" and the Method" and the Set Length of tape = 100-01 Ft.
A E O A-D A-D A B C O	Distance Ft- ⁶¹ Equ 200-00 200-00 301-03 199-93 ⁶¹ Ric 20-00 200-00 20-00 20-00 300-88	An lateral <i>N-A-E</i> <i>A-E-D</i> <i>e-D-N</i> ht Ang <i>N-A-B</i> <i>A-B-C</i>	gle Value Triang 60°00' 59°59' 90°59' 1e Offs 90°00' 90°00' 90°00'	Error a Dist: Ft- e Met -0-07	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers: 1-Doe Now 17, 1914, (2 Ho Used Gurley Trans chaining Locké With the Transit o and N, in the line and prolonged th lateral Triangle Angle OFFset. "Deflection No "Jeflection No	& R.Roe. UT3) Warm & Cloudy. If Locker NS5, and. r NS22. ver M, set hubs at A Mill. Set transit at A e line MA by the "Rgint Method" and the thad. Length of tepe = 100.01 Ft. Observed measure- ment concred.
А Е D Д-D Д В С	Distance Ft- ¹¹ Equ 200-00 301-03 199-93 ¹¹ Ric 20-00 200-00 20-00 20-00	An Iateral <i>KA-E</i> <i>A-E-D</i> <i>e-D-N</i> <i>ht Ang</i> <i>N-A-B</i> <i>A-B-C</i> <i>B-C-D</i>	gle Value Triang 60°00' 59°59' 90°59' 1e Offs 90°00' 90°00' 90°00'	Error o Dist: Ft: e Met - <i>0-07</i> et Met)	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers: 1-Doe Now 17, 1914, (2 Ho Used Gurley Trans chaining Locké With the Transit o and N, in the line and prolonged th lateral Triangle Angle OFFset. "Deflection No "Jeflection No	& R.Roe. UT3) Warm & Cloudy. If Locker NS5, and. r NS22. ver M, set hubs at A Mill. Set transit at A e line MA by the "Rgint Method" and the thad. Length of tepe = 100.01 Ft. Observed measure- ment concred.
A E O A-D A-D A B C O	Distance Ft- '' Equ 200-00 200-00 301-03 199-93 " Ric 20-00 200-00 200-00 200-08 200-08	An Ilateral <i>N-A-E</i> <i>A-E-D</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C</i> <i>B-C-D</i> <i>C-B-N</i>	gle Value Triang 60'00' 59'59' 59'59' 90'00' 90'00' 90'00' 90'00'	Error a Dist. Ft. e Met - <i>0-07</i> et Met) <i>+0-08</i>	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers: 1-Doe Now 17, 1914, (2 Ho Used Gurley Trans chaining Locké With the Transit o and N, in the line and prolonged th lateral Triangle Angle OFFset. "Deflection No "Jeflection No	AF R.Rog. UTS) Warm & Cloudy. IF Locker NSS, and. T NSST hubs at A Will. Sat transit at A Will. Sat transit at A e Vine MA by the "Eqi- Nethod" and the thad. Length of tape =00-01 FF. Observed messure-
A E D A-D A B C D A-D	Distance Ft- "Equ 200-00 301-03 301-03 300-00 200-00 2000 2000 2000 2000 20	An Iateral <i>NA-E</i> <i>A-E-D</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C</i> <i>B-C-D</i> <i>C-B-N</i> Flectic	gle Value Triang 60°00' 50°00' 59°59' 90°00' 90°00' 90°00' 90°00' 90°00'	Error a Dist. Ft. e Met - <i>0-07</i> et Met) <i>+0-08</i>	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Transft o and H, in the Irransft o and prolonged th Isteral Triangle Angle Offset . "Deflection He off	& R.Roe. UT3) Warm & Cloudy. If Locker NS5, and. r NS22. ver M, set hubs at A Mill. Set transit at A e line MA by the "Rgint Method" and the thad. Length of tepe = 100.01 Ft. Observed measure- ment concred.
A E D A-D A B C O A-D A	Distance Ft- "Equ 200-00 301-03 199-93 "Ric 20-00 20-00 20-00 20-00 20-00 20-00 20-00 20-00 20-00	An Iateral <i>HA-E</i> <i>A-E-D</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C</i> <i>B-C-D</i> <i>C-B-N</i> Flectic <i>N-A-F</i>	gie Value Triang 60°00' 50°00' 59°59' 90°00' 90°00' 90°00' 90°00' 90°00' 90°00' 90°00'	Error a Dist. Ft. e Met - <i>0-07</i> et Met) <i>+0-08</i>	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers: 1-Doe Now 17, 1914, (2 Ho Used Gurley Trans chaining Locké With the Transit o and N, in the line and prolonged th lateral Triangle Angle OFFset. "Deflection No "Jeflection No	& R.Roe. UT3) Warm & Cloudy. If Locker NS5, and. r NS22. ver M, set hubs at A Mill. Set transit at A e line MA by the "Rgint Method" and the thad. Length of tepe = 100.01 Ft. Observed measure- ment concred.
A E D A-D A-D A-D A-D A-F	Distance Ft- I' Equ 200-00 301-03 199-93 " Ric 20-00 20-00 20-00 20-00 300-88 200-08 200-00 120-00 120-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met - <i>0-07</i> et Met) <i>+0-08</i>	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Transft o and H, in the Irransft o and prolonged th Isteral Triangle Angle Offset . "Deflection He off	& R.Roe. UT3) Warm & Cloudy. If Locker NS5, and. r NS22. ver M, set hubs at A Mill. Set transit at A e line MA by the "Rgint Method" and the thad. Length of tepe = 100.01 Ft. Observed measure- ment concred.
A E D A-D A-D A B C O D A-D A F G	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>HA-E</i> <i>A-E-D</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C</i> <i>B-C-D</i> <i>C-B-N</i> Flectic <i>N-A-F</i>	gie Value Triang 60°00' 50°00' 59°59' 90°00' 90°00' 90°00' 90°00' 90°00' 90°00' 90°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Transft o and H, in the Irransft o and prolonged th Isteral Triangle Angle Offset . "Deflection He off	AF R. Rog. UTS) Warm & Cloudy. If Locker NS5, and. T N222- Ver N, set hubs et A Wil. Set transit et A Wil. Set transit et A ver NA by the "Eqi- Nethod" and the thad. S. Length of tape = 100-01 FF. Observed messure- ments recorded. S. Solo S. Solo S
A E D A-D A-D A-D A-D A-F	Distance Ft- I' Equ 200-00 301-03 199-93 " Ric 20-00 20-00 20-00 20-00 300-88 200-08 200-00 120-00 120-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met - <i>0-07</i> et Met) <i>+0-08</i>	Closura Line Ft. had" <i>0.09 R</i> - had"	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Transft o and H, in the Irransft o and prolonged th Isteral Triangle Angle Offset . "Deflection He off	& R.Roe. UT3) Warm & Cloudy. If Locker NS5, and. r NS22. ver M, set hubs at A Mill. Set transit at A e line MA by the "Rgint Method" and the thad. Length of tepe = 100.01 Ft. Observed measure- ment concred.
A E D A-D A-D A B C O D A-D A F G	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers: 1-Doe Nov 17, 1914, (2 Ho Used Gurley Trans chaining Locké With the Transit o and M, in the line and probaged th lateral Triangle Angle Offset - "Deflection Ne " " Deflection Ne " " " Deflection Ne" " "	AF R. Rog. UTS) Warm & Cloudy. If Locker NS5, and. r N322. Ver M, sat hubs at A Mil. Sat transit at A Will Sat transit at A the line MA by the "Eqi- Method" and the thod. Second the same construction of tape 100-01 Ft. Observed measure- ments recorded. Second to the Second t
A E D A-D A-D A B C O D A-D A F G	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Transft o and H, in the Irransft o and prolonged th Isteral Triangle Angle Offset . "Deflection He off	AF R. Rog. UTS) Warm & Cloudy. If Locker NS5, and. r N322. Ver M, sat hubs at A Mil. Sat transit at A Will Sat transit at A the line MA by the "Eqi- Method" and the thod. Second the same construction of tape 100-01 Ft. Observed measure- ments recorded. Second to the Second t
A E D A-D A-D A B C O D A-D A F G	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers: 1-Doe Nov 17, 1914, (2 Ho Used Gurley Trans chaining Locké With the Transit o and M, in the line and probaged th lateral Triangle Angle Offset - "Deflection Ne " " Deflection Ne " " " Deflection Ne" " "	AF R. Rog. UTS) Warm & Cloudy. If Locker NS5, and. r N322. Ver M, sat hubs at A Mil. Sat transit at A Will Sat transit at A the line MA by the "Eqi- Method" and the thod. Second the same construction of tape 100-01 Ft. Observed measure- ments recorded. Second to the Second t
A E D A-D A-D A B C O D A-D A F G	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers: J-Doo Nov 17, 1914, (2 Ho Used Gurley Transft on and prolonged th Isteral Triangle Angle OffSet, "Deflection Na B B B B B B B C C C C C C C C C C C C	AF R. Rog. UTS) Warm & Cloudy. If Locker NS5, and. r N322. Ver M, sat hubs at A Mil. Sat transit at A Wil. Sat transit at A the line NA by the "Eqi- Nethod" and the thod. Second of tape 100.01 Ft. Observed measure- ments recorded. Second Second Second Second S
A E D A-D A-D A B C O D A-D A F G	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-F-G</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Translt o and prolonged th Isteral Triangle Angle OFFset . "Deflection Ne Burley of G Deflection Ne Stationary Stat	AF R. Roe UTS) Warm & Cloudy. It Locker Nº 5, and. T Nº 32. Ver M. set hubs et A MIN - Set transit et A MIN - Set transit et A e line MA by the "Eqi- Method" the "Right Method" and the Hodd" and the = 100-01 Ft. Observed measure- ments recorded. -90° -50°
A E D A-D A-D A-D A-D A-F F	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-F-G</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Translt o and prolonged th Isteral Triangle Angle OFFset . "Deflection Ne Burley of G Deflection Ne Stationary Stat	AF R. Rog. UTS) Warm & Cloudy. If Locker NS5, and. r N322. Ver M, sat hubs at A Mil. Sat transit at A Will Sat transit at A the line MA by the "Eqi- Method" and the thod. Second the same construction of tape 100-01 Ft. Observed measure- ments recorded. Second to the Second t
A E D A-D A-D A-D A-D A-F F	Distance Ft- Ft- 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00 200-00	An Iateral <i>NA-E</i> <i>A-E-O</i> <i>e-D-N</i> <i>ht</i> Ang <i>N-A-B</i> <i>A-B-C-D</i> <i>G-B-N</i> <i>Flectic</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-A-F</i> <i>J-F-G</i>	gle Value Triang 60°00' 59°59' Ie Offs 90°00' 90°00' 90°00' 90°00' 90°00' 10°00'	Error a Dist. Ft. e Met -0.07 et Met) +0.08 hod "	Closura Line Ft. pod'' <i>0-09 R</i> - nod'' <i>0-10 L</i> -	Observers : J-Doo Nov 17, 1914, (2 Ho Used Burley Translt o and prolonged th Isteral Triangle Angle OFFset . "Deflection Ne Burley of G Deflection Ne Stationary Stat	AF R. Roe UTS) Warm & Cloudy. It Locker Nº 5, and. T Nº 32. Ver M. set hubs et A MIN - Set transit et A MIN - Set transit et A e line MA by the "Eqi- Method" the "Right Method" and the Hodd" and the = 100-01 Ft. Observed measure- ments recorded. -90° -50°

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(b) Problem.—Prolong a line beyond an imaginary obstacle by three methods and check by direct measurement.
(c) Methods.—(To be devised by the student.)

PROBLEM D7. TRAVERSE OF FIELD WITH TRANSIT.

(a) Equipment.—Transit, 2 flag poles, 100-foot steel tape.

(b) *Problem.*—Determine the deflections of the sides of an assigned field with the transit, check angles by observing the magnetic bearings, and measure the lengths of the sides with a steel tape.

(c) Methods.—(1) Set the transit over one corner of the field, set the A vernier to read 180°, and sight at a flag pole plumbed over the point to the left with the telescope normal. Read and record the magnetic bearing. (2) Keep the telescope normal and sight at the next point to the right. The reading of the A vernier will be the deflection of the second line. (3) Read and record the magnetic bearing and compare the transit and magnetic deflections. (4) Repeat this process for the remaining corners of the polygon taken in succession to the right. Deflections will be based on duplicate readings agreeing within one minute. (5)Measure the sides to the nearest 0.01 foot with the tape. Compare the tape with the standard at the beginning and conclusion of the chaining. (6) From the observed deflections determine the bearings of the field assuming one side as a true meridian. The angular error of closure must not exceed one minuté. Record and reduce data as in the prescribed form. Should a side of the field be obstructed, use one or more auxiliary points (see (c) of D8).

(Most engineers prefer "plunge reversals" to the above method of "plate reversals." To avoid the collimation error involved in a single plunge reversal, the principles of "double sights" must be used and the mean angle taken. To save time, some engineers try to keep the transit always in first-class adjustment, so as to omit one altitude reversal in the "plunge" method, and some turn the transit "end for end" (reverse in azimuth) every setting or so.)

PROBLEM D8. AREA OF FIELD WITH TRANSIT.

(a) Equipment.—Five-place table of logarithms.

(b) Problem.—Compute the area of the assigned field by means of latitudes and departures.

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Error of Closure

Actual 0.55 Ft. Permissible 0.6 Ft. (See Diagrams)

P= 2143.12

Line AB BC CD DE EA

(c) Methods.—(Follow the instructions in the corresponding problem with the compass, Problem B4, preserving the same degree of precision in the computed latitudes and departures as in the field measurements. In case auxiliary stations are used on an obstructed side of the field, calculate the latitudes and departures of the polygon actually traversed in the field, and then to find the area drop the false corners in calculating the meridian distance and the latitude of the real side of the field.)

PROBLEM D9. STAKING OUT A BUILDING.

(a) Equipment.—Transit, 100-foot steel tape, 2 flag poles, axe, hubs, tacks, plan of building

(b) *Problem.*—On an assigned plot of ground stake out the assigned building.

(c) Methods.—(1) Orient one side of the enclosing rectangle with reference to a true meridian or a street line. (2) Locate and check up the corners of the rectangle by setting over each corner in turn, passing around to the right, back-sighting on the corner to the left, turning off 90° and locating the corner to the right. (3) Locate the corners of the building by setting stakes on the side lines of the building produced, using the rectangle as a base line. (4) Check all stakes by additional measurements. The rectangle should close to the nearest minute, the linear error should not exceed 1: 50,000. Follow the form.

PROBLEM D10. HEIGHT OF TOWER WITH TRANSIT.

(a) Equipment.—Complete transit, 2 flag poles, leveling rod, 100-foot steel tape, axe, hubs, tacks.

(b) Problem.—Determine the height of an assigned tower with the transit and steel tape.

(c) Methods.—(1) Set the transit over a hub located a little further from the base than the height of the tower.
(2) Level the instrument very carefully with the attached level and determine the index error of the vertical circle.
(3) Bring the bubble of the attached level to the center and read a level rod held on the base of the tower (4) Sight at the top of the tower, read the vertical angle, correct for index error and record. (5) Reverse the telescope and locate a second point at least as far from the first as the height of the tower, check by "double sights." (6) Set

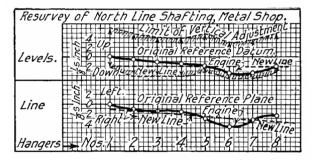
ass. tion Locat. A b Thence Set t Set t The	of tay uned a uned a of the of hub blished y obsain struct part of and ter and ter and ter and set and ine transit checke angle for line for line remain located	te = 100 s stance s build A to Fi a truct vation ted a c follows over h nporar Measur over h tempo over c, d temp and dis s Fr der of with	ub A an	s tape - the c te, ano lan th. laris- recta- d set listance ghted ub C; s d on B hub D error mce. ubs wise	being ponstuc- then rough ngle hub B hub s fwice. st A et hub sof for g for g	Surveyors, John Doe & Richard Roe. WITH ENGINEERS' TRANSIT. Nov 28,1914. (3 hours). Cool and clear. Usad Gurlay Transit, Locker No. 6 and Locker No.30. Hubs are set on line 5' from corners. D (90° D (10°) C (10°
Station A B	Vertical Angle 20°/6' 46°24'	Ft. 150-00	F·5· (Levels) <i>4·50=</i> <i>3·82=</i>	hi he		Observers, J-Doe & R. Ros. WITH ENGINEERS' TRANSIT. Nov 28,194, (2 hours)- Warm & Cloudy- Used Gurley Transit, Locker No.5, and Chaining Locker No.35. Set transit over A and measured the vertical angle M, having first determin- ed the index error of vertical circle-
(1) (2) (3) (4) (5) (6)	$D_{I} = H$ $D_{2} = H$ $H = H_{I}$ $H_{I} = H$ $in (I) = D_{2}$	Eot M Cot N +h, =h - (h,- nd sub = Hz(Co		bstitut g (2) Fi ·N)-(h,	om (I) 3 -hz)Cot·M	Read level rad on base of tower. (h,) Set B in line with A and top of tower and measured Dr-D2 as base line- Set transit over B and Found Nand hz- Length of tape = 99-92 Ft. Reduced measurements recorded.
Subs.	rituting H ₂ =	, <u>150 + (</u> 60 86.47	(4:50-3 t:20°16 Ft: z = 86.	- <u>82) Cot</u> '-Cot·46	<u>20°16</u> r 1024'	A Hub Hub A Base - D

the transit over the second hub, sight at the top of the tower and read the vertical angle, as before. (7) Read the level rod on the base of the tower as before. Each angle and rod reading is to be based on duplicate readings. Follow the form.

PROBLEM D11. SURVEY OF LINE SHAFTING.

(a) Equipment.—Engineers' transit with attached bubble, leveling rod (or instead of these engineers' instruments, a 16-foot metal-bound straight-edge with an adjustable bubble of say 20-foot radius, a long braided fishing line, and 3 long metal suspenders made exactly alike, from which to suspend straight-edge from line of shafting), 2 good plumb bobs, 50-foot etched steel tape, copper tacks, hatchet.

(b) *Problem*—Make a survey of a line of shafting in a machine shop, and establish a true alinement for it, both vertically and transversely.



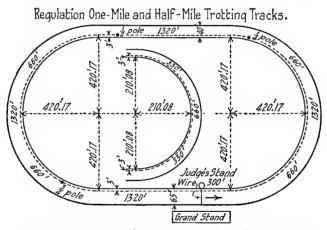
(c) Mcthods.—(1) Establish a reference line for lateral deviations and carefully mark the same. (2) Select a suitable permanent bench mark to which the levels may be referred. (3) Determine the horizontal distance from the vertical reference plane to the line shafting at selected points, say at each hanger. (4) Determine the elevations of the same points by the methods of profile leveling. (5) Plot the data as suggested in the diagram. (6) Note the ruling points and permissible change both laterally and vertically at each hanger, and record the data. (7) Lay grade lines, and prepare data to shift the line shafting to a true position. (8) Make complete record of results.

PROBLEM D12. SURVEY OF RACE TRACK.

(a) Equipment.—Outfit for transit party (instrument assigned, a long wire, say No. 20, spring balance, thermometer, etc.).

(b) Problem.—Make the survey for a race track, as instructed.

(c) Methods.—(1) Standardize steel tape, noting temperature and pull. (2) Make a careful examination of the tract of land with a view to secure the best location for the race



The standard distance is measured on a line 3 feet from the hub-board. The inner edge of the track is thus $2\pi \cdot 3 = 18.85$ feet shorter than the standard distance. The track is "banked" on curves from 1:12 to 1:15, and, to provide drainage, should be sloped one foot on the straight stretches. The ends of curves are sometimes flattened.

track as regards visibility, drainage, economy of construction and maintenance, etc. (3) After fixing the ruling points, establish the principal axis of the track by locating the centers of the two semi-circles and the intersections of the axis with the curves; also establish the ends of the curves, preferably on the true measured line (3 feet from the hub plank for a sulky track, and 18 inches from the inner edge for a bicycle track). (4) Run in each quadrant, either by the deflection angle method, or, if trees or other obstructions do not prevent, by using the wire as a radius with observed pull; set points 16 feet apart unless instructed otherwise. (5) After locating the true line, check up the total distance very carefully. (6) Make plat and complete record of survey.

PROBLEM D13. ANGLES OF TRIANGLE BY REPETITION.

(a) Equipment.—Transit, reading glass, 2 chaining pins, 2 tripods with plumb bobs (if necessary).

(b) Problem.—Measure the angles of a prescribed triangle with transit by repetition.

							Observers	: John Doe d	Richard R	08.
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		1	∆5		2274700					gle
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					264 12 40			88°50'32'		5 Reps.
	U	12	A 6	180 00 00'		00'00"		00 00 02		2 neps
	•	-	AB	268 30 20			88'50'20"			Single
		1	20	26412 20		" 12'20"		88°50'28"	AR'50'30"	5 Reps.
								to exceed 15		, -
		1								

(c) Methods.—(1) Set the transit over one of the vertices of the triangle and set chaining pins in the tops of the monuments at the other two. (2) Set the A vernier to read zero. (3) Sight at the left hand station with the bubble down, and clamp the lower motion. (4) Unclamp the upper motion, sight at the right hand station, read both verniers and record. (5) Unclamp the lower motion, sight at the

left hand station, and check the verniers to see that they have not moved. (6) Unclamp the upper motion and sight at the right hand station but do not read verniers. Repeat until five repetitions of the angle are secured, and read both verniers to eliminate errors of eccentricity. (7) Divide the arithmetical mean of the two vernier readings by five and compare with the value obtained by single measurement. (8) Reverse the instrument in altitude, and set the A vernier to read zero. (9) Sight at the right hand station with the bubble up, and clamp the lower motion. (10) Unclamp the upper motion, sight at the left hand station, read both verniers and record. (11) Unclamp the lower motion, sight at the right hand station, and check the verniers to see that they have not moved. (12) Unclamp the upper motion and sight at the left hand station, but do not read the verniers. Repeat until five repetitions of the angle are secured, and read both verniers to eliminate errors of eccentricity. (13) Divide the mean of the two vernier readings by five and compare with the value obtained by single measurement. (14) Take the mean of the two sets as the most probable value. (15) Measure the other angles in the same manner. The angular error of closure should not exceed 15". Follow the form.

PROBLEM D14. DETERMINATION OF TRUE MERIDIAN BY OBSERVATION ON POLARIS AT ELONGATION.

(a) Equipment.—Complete transit, reading glass, hub, 2 flat stakes, board 2''x 4''x 3', 4 8d nails, axe, 2 lanterns, good watch set and regulated to keep railroad time.

(b) *Problem.*—Determine a true meridian by an observation on Polaris at elongation.

(c) Methods.—(1) Calculate the time of elongation of Polaris, and regulate and set a good reliable watch to keep railroad time (mean solar time). Calculate the time of elongation of Polaris from Table II.

Set the transit over a hub about 40 minutes before the time of elongation. Level the instrument very carefully, and set the vernier of the vertical circle to read the latitude of the place. (2) Focus the objective on a bright star; sight at Polaris which will be found by following the pointers of the Great Dipper, at an elevation equal to the latitude of the place. (3) With a reflector or a piece of white paper reflect light into the telescope so that the cross-hairs and the image of Polaris will be visible at the same time. (4) Depress the telescope and establish a target at a distance of about 500 feet; place the plank on the ground and nail it firmly to flat stakes, driving one at each end. (5) Level up again and follow Polaris with the telescope by means of the tangent movement; at elongation it will appear to traverse the vertical hair for several minutes. (6) Depress the tele-

(Observers, J.Doe & R	-Roe.
DET	ERMINA	HOIT	bf Tru	ie Mei	NAIDIS	BY QB'S ON POLARI	5 AT ELONGATION.
No- Bub-	RRTime	Azim	th of i	olaris	Error	Dec.7, 1915 (2 Hours)	, Clear and warm.
					Azimuth	Buff & Berger Transi.	t No•9, 2 Lanterns,
1 Дожп	2"17"	1º28-4	0°0.0	1°28.4	-0:7	hubs, 2 flat stake	s, plank 18"×4"×2", 4
2 "	2 30	1º 28.9	0°0.1	1°29.0	-0-1	8 d nails, axe, wat	ch set to keep Railroad
3 Up	2 40	1°29.9	00:5	1°30.4	+1'3	time.	
	2 48				+1.8	Şet transit over hu	b at 1:40 A.M., sighted
· ·			Мегл	1º29.8	+ 0.7	at Polaris, depres	sed the telescope and
		[A]	pwable	error =	1:0)	established targe	et about 500 Ft. From
['						instrument The	plank was placed at
Calcu	lation of	F Railroa	ið Tíme o	F Elong	ation.	right angles to I	ine and nailed to
Latit	ude 40°	06', Long	gitude 8	8°15'	6 00.	a stake driven a	rteach end
	on Time				3 ^h 50.8 ^{m.}	Made First observat	ion at western elongation
	ction Fo				- 23.6	Reversed instrument	t in altitude and
	n Time				8 27.2	azimuth between	2nd and 3rd readings
	action f				- 7.0	Reduced observations	
	Time U-0				8 20-2	2,3&4 by the	K Polaris
	ction Fo			stion+.	5 55.0	Fallowing Formula:	-Pole
	road Tin				2"15.0"	<i>4•M• corr•"= 0•058 †</i> ²	
	lation o				Elong'n	where t = time	
	uth Pola				1°29:9	From elongation	`@./
	ection f				- 0.8	in minutes; the	pipper
	with Polar				1°29:1	correction be-	A PART & Sea
	of Elor				-	ing seconds of arc.	erest + + 13
	Vestern					(For Latitude 40°,	° ¥
	U·C·Pola				ation	30 min. From	Polaris at
subt.	ract 5'	'55 ^m f	from the	ne U·C·		elongation).	Upper Culmination

scope, sight at a pencil held on the target and mark the point very carefully. (7) As a check make three observations within half an hour after elongation, noting the time of sighting on the star. Reverse the instrument in altitude and azimnth after the first check observation. (8) Reduce the check observations to observations at elongation by the following rule: Multiply the square of the time since elongation in minutes by 0.058, and the product will be the correction to the azimuth of Polaris in seconds of arc, for latitude 40°. (9) The next morning lay off the azimuth of Polaris for each observation to the cast or west, depending upon whether the observation was made at western or eastern elongation. (10) Check the observed mcridian with the standard meridian. The error of the mean of the four observations should not exceed one minute. Record and reduce the data as in the form.

PROBLEM D15. DETERMINATION OF TRUE MERIDIAN BY OBSERVATION ON POLARIS AT ANY TIME.

(a) Equipment.—The same as in Problem D14.

(b) *Problem.*—Determine a true meridian by observing Polaris at any time.

(c) Methods.—Make the observations as described in Problem D14, noting the time of observation to the nearest minute, and reversing the instrument in altitude and azimuth between the 3rd and 4th observations. The transit should be leveled up very carefully with the attached bubble, particular attention being given to the horizontal plate level at right angles to the line of sight. (2) Reduce the observations by means of the tables.

A star comes to the meridian 4 minutes (nearly) earlier each day than it did the preceding day. The sideral day is therefore shorter than the solar day, the time from upper culmination to upper culmination being 23 hours 56.1 minutes mean solar time. The time from Upper Culmination to Lower Culmination is 11 hours 58 minutes.

Astronomical time, or Local Mean Solar time, is the time that would be kept by the mean sun and is obtained from Standard, or railroad time, by adding or subtracting 4 minutes for each degree of longitude that the place of observation is east or west of the Standard Meridian. The Astronomical day begins at noon of the civil day of the same date, and is reckoned from zero to 24 hours.

The Hour Angle of Polaris is found by subtracting the correct Local Mean Solar time of Upper Culmination, Table II, from the Local Mean Solar time of observation.

The Time Argument used in entering Table IV is the Hour Angle of Polaris, or 23 hours 56.1 minutes minus the Hour Angle of Polaris. Table IV is used as follows: Find the "hours and minutes" of the time argument in the left hand column of either page of Table IV. On the horizontal line with the "time before or after upper culmination" (time argument), the azimuth of Polaris for a declination of Polaris of 88° 51' will be found in the column under the given latitude. The correction to the azimuth for each

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TABLE I.

AZIMUTH OF POLARIS AT ELONGATION FOR ANY YEAR BETWEEN 1915 AND 1924.

Latitude	1915	1916	1917	1918	1919	1920	1921	1922	1923	1924
30	1°19.6	1°19.2	1°18.8	1°18.5	1°18.1	1°17.́8	1°17.4	1°17.0	1°16.7	1°16.4
31	20.4	20.0	19.7	19.3	18.9	18.6	18.2	17.9	17.5	17.2
32	21.2	20.9	20.5	20.1	19.8	19.4	19.1	18.7	18.3	18.0
33	22.1	21.8	21.4	21.0	20.7	20.3	19.9	19.6	19.2	18.8
34	23.1	22.7	22.4	22.0	21.6	21.2	20.9	20.5	20.1	19.8
35	1 24.1	1 23.7	123.3	123.0	1 22.6	122.2	1 21.8	121.5	121.1	1 20.7
36	25.2	24.8	24.4	24.0	23.6	23.3	22.9	22.5	22.1	21.7
37	26.3	25.9	25.3	25.1	24.7	24.3	24.0	23.6	23.2	22.8
38	27.4			26.2	25.9	25.5	25.1	24.7	24.3	23.9
39	28.6	28.2	27.8	27.5	27.1	26.7	26.3	25.8	25.5	25.1
40	1 29.9	1 29.5	1 29.1	1 28.7	128.3	127.9	1 27.5	1 27.1	126.7	1 26.3
41	31.3	30.9					28.8		28.0	27.6
42	32.7	32.3	31.9	31.5	31.0	30.6	30.2	29.8	29.4	29.0
43	34.2	33.8	33.4	32.9	32.5	32.1	31.8	31.2	30.8	30.4
44	35.8	35.3	34.9	34.5	34.1	33.6	33.2	32.8	32.4	31.9
45	1 37.4	1 37.0	136.6	1 36.1	1 35.7	1 35.3	134.8	1 34.4	1 34.0	$1 \ 33.5$
46	39.2	38.7	38.3	37.8	37.4	37.0	36.5	36.1	35.6	35.2
47	41.0	40.6		39.7	39.2	38.8		37.9	37.4	37.0
48	43.0			41.6	41.1	40.7		39.8	39.3	38.8
49	45.0	44.5	44.1	43.6	43.1	42.7	42.2	41.7	41.3	40.8
50	1 47.2	146.7	1 46.2	1 45.7	$1 \ 45.3$	144.8	1 44.3	1 43.8	1 43.4	1 42.9

Correction For Above Table

The above table was computed with the mean declination of Polaris for each year. A more accurate result will be bad by applying to the tabular values the following corrections, which depend on the difference of the mean and the apparent place of the star. The deduced azimuth will, in general, be correct within 0'.3.

For middle of	Correction in minutes	For middle of	Correction in minutes
January	$-0.5 \\ -0.4 \\ -0.3 \\ 0.0 \\ +0.1 \\ +0.2$	July.	+0.2
February		August	+0.1
March		September .	-0.1
April		October	-0.4
May		November .	-0.6
June		December	-0.8

minute of change in Declination of Polaris are given in the last two columns on each page. The changes for latitudes between 30° and 40° and between 40° and 50° may be interpolated. The Declination of Polaris at any date may be

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TABLE II.

LOCAL MEAN (ASTRONOMICAL) TIME OF THE CULMINATION AND ELONGATION OF POLARIS IN THE YEAR 1915.

(Computed for latitude 40° and longitude 90° or 6^h west of Greenwich.)

Date	East elongation	Upper culmination	West elongation	Lower culmination
1915 January 1 15 February 1 15 I5 April 1 15 March 1 15 April 1 15 Jupril 1 15 June 1 15 July 1 15 August 1 15 September 1 15 November 1 15 December 1 15	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	Correctio	on For Years	After 1915	
1916 subtract 1917 subtract 1918 add 1919 add 1920 add subtract	1.6 up to Mar 2.3 on and aft 0.7 0.9 2.5 4.0 up to Mar 0.1 on and aft March 1 1.6	er 1923 1924 1925 1926 1926 1926 1926 1927 1928	add 4.5 { add 5.9 up to { add 2.0 on and add 3.3 add 4.6 add 5.9 { add 7.2 up to	i after March 1

found from Table III. For example the azimuth of Polaris with a time argument of 9 hours and 15 minutes in latitude 40°, on April 21, 1915, was as follows: From Table III the declination of Polaris on April 21 was very closely 88° 51.25'. From Table IV for declination 88° 51' the azimuth of Polaris was 58.65'; the correction for 0.25' was $0.83 \times 0.25 = 0.21'$, and the azimuth was 58.65' - 0.21 = 58.44'. If the exact time argument is not found in the table, the azimuth may be found with sufficient accuracy by direct inter-

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polation. Azimuths for latitudes between values given in Table IV may be found by direct interpolation. The nearest whole degree of latitude is usually sufficiently ac-

TABLE III.

DECLINATION	OF	POLARIS	FOR	1915.	
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Date	Declination	Date	Declination	
Jan. 1	88° 51′.54	July 1	88° 51'.05	
15	51.58	15	5105	
Feb. 1	51.57	August 1	51.09	
15	51.54	15	51.13	
March 1	51.49	Sept. 1	51.21	
15	51.43	15	51.28	
April 1	51.35	Oct. 1	51.38	
15	51.27	15	51.47	
May 1	51.20	Nov. 1	51.58	
15	51.14	15	51.67	
June 1	51.08	Dec. 1	51.75	
15	51.06	15	51.81	

10 obtain the declination for the corresponding time for years after 1915, add 0.34 min. for each year to the corresponding declination for 1915.

No Bub- Nos ble 1 Bown 2 m 3 n 4 Up 5 n 6 n 4 Up 5 n 6 n 4 Up 5 n 6 n 1 Mean Atrono Reduct Astrono Time Hour A 0 f 0 U-C-	h. m. 8 26 8 41 8 56 9 11 9 18 9 26 Solar Tom Time tion to A nomical 0 C-Poo ngle of Bos+24 Polaris	Mean So- lar Time of Obs- h. m. 8 33 8 48 9 03 9 18 9 25 9 33 Calcu D'06' Time Up U.C.Pol pr. 21,= (Locol M. Varis, Ag Polaris, Agentis, Agentis, Agentis, Agentis, Agentis, Calcu U.C.Pol Polaris, Agentis, Calcu U.C.Pol Polaris, Agentis, Calcu U.C.Pol Polaris, Calcu U.C.Pol Polaris, Calcu U.C.Pol Polaris, Calcu (23 *	Hour An- gle of Polaris h. m. 9 9 00 9 15 9 15 9 25 10 00 0 455 9 52 10 00 0 455 0 br>10 10 10 10 10 10 10 10 10 10 10 10 1	Azimuth of Pol's Wof N- o <i>1° 02.7</i> <i>58.4</i> <i>53.9</i> <i>49.2</i> <i>49.5</i> <i>44.2</i> <i>Error</i> <i>Error</i> <i>vola 88</i> minatio <i>r.J.5 1/5</i> <i>5</i> <i>50lar</i> <i>iolar Tii</i>	Error of 0bs. 	nt	April 22,1115 (21115) Reduced obsera- tions using Azi- muth Tables- Laid off Azimuth to the East and	e er & Warm 7, 2 lanterns K 36"4" × 2", k keep Rail- axo- 15 P.N-, ssed teles- ssed teles- ssed teles- tesch gnd t each gnd t each gnd isescope
0F 0 U·C·	65.+24	h ₀₀ m_ (23 h	Mean 5 26 ¶)	iolar Tii	ne,		Laid off Azimuth to the East and measured angle	Dipper
(or 2 Astron is re	23 ^h 56 Iomice ckoned ivil Day	t ^m – Hou I Time (From I	ir Angi Local M 2 oʻcloo	le) lean 50 :k Noor	isr) a an		with the True Meridian	

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curate. The time used in making observations should be correct to the nearest minute, if accuracy is desired.

Table II was compiled from "Ephemeris for the Sun and Polaris and Tables of Azimuth of Polaris for the year 1915," published by the Department of Interior, General Land Office. Tables I, II and IV were compiled from "Principal Facts of the Earth's Magnetism," published by the U. S. Coast and Geodetic Survey, 1914.

The observations should be made as near elongation as possible, for the reason that Polaris is moving most rapidly in azimuth near culmination and errors in observing the time and using the table are then a maximum.

With careful work the range of 6 reduced observations should in no case exceed 1' of arc. Record the data and make the calculations as in the form.

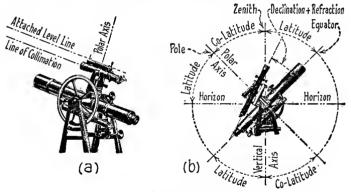


Fig. 23a.

PROBLEM D16. DETERMINATION OF TRUE MERIDIAN WITH SOLAR TRANSIT.

(a) Equipment.—Complete transit with solar attachment, reading glass, solar ephemeris, axe, hubs, tacks.

(b) Problem.—Determine a true meridian with a solar transit.

(c) Methods.—(There are various forms of solar attachments, to transits, among which are the Saegmuller, (a), and the Buff and Berger, (b), Fig. 23a; the former is the best known. The theory of all solar attachments in geueral use is the same, and is as follows: In order to bring

TABLE	1V. A	ZIMUT	HS OF	FOLA	RIS AT	ANY	HOUR	ANGLE.		
Hour Angle before c after	r	Azimuths of Polaris computed for Declination 88° 51′ Azimuths given in minutes Azimuths given in minutes								
upper cu minatio	n Lat. 30°	Lat. 32°	Lat. 34°	Lat. 36°	Lat. 38°	Lat. 40°	Lat. 30°	Lat. 40°		
$ \begin{array}{ccc} h & m \\ 0 & 15 \\ 0 & 30 \\ 0 & 45 \end{array} $	$05'28 \\ 10.52 \\ 15.73$	$05.38 \\ 10.75 \\ 16.07$	$05.52 \\ 11.02 \\ 16.45$	$05.67 \\ 11.30 \\ 16.88$	$05.82 \\ 11.62 \\ 17.35$	06.00 11.95 17.87	-0'08 -0.15 0.23	-0.08 -0.17 -0.27		
$ \begin{array}{r} 1 & 00 \\ 1 & 15 \\ 1 & 30 \\ 1 & 45 \end{array} $	$20.85 \\ 25.90 \\ 30.82 \\ 35.62$	$\begin{array}{c} 21.32 \\ 26.47 \\ 31.50 \\ 36.40 \end{array}$	21.83 27.10 32.25 37.27	22.40 27.80 33.08 38.23	$23.02 \\ 28.57 \\ 34.00 \\ 39.28$	$23.70 \\ 29.43 \\ 35.02 \\ 40.45$	-0.30 -0.38 -0.45 -0.52	$\begin{array}{c c} -0.35 \\ -0.43 \\ -0.52 \\ -0.60 \end{array}$		
$egin{array}{ccc} 2 & 00 \ 2 & 15 \ 2 & 30 \ 2 & 45 \ \end{array}$	$\begin{array}{r} 40.25 \\ 44.70 \\ 48.95 \\ 53.00 \end{array}$	$\begin{array}{r} 41.13 \\ 45.68 \\ 50.03 \\ 54.17 \end{array}$	$\begin{array}{r} 42.12 \\ 46.77 \\ 51.22 \\ 55.45 \end{array}$	43.20 47.97 52.53 56.87	$\begin{array}{r} 44.38 \\ 49.30 \\ 53.98 \\ 58.42 \end{array}$	$\begin{array}{r} 45.70 \\ 50.75 \\ 55.58 \\ 60.15 \end{array}$	-0.58 -0.65 -0.72 -0.77	-0.67 -0.75 -0.82 -0.88		
$\begin{array}{cccc} 3 & 00 \\ 3 & 15 \\ 3 & 30 \\ 3 & 45 \end{array}$	$\begin{array}{c} 56.80 \\ 60.37 \\ 63.67 \\ 66.68 \end{array}$	$58.05 \\ 61.68 \\ 65.05 \\ 68.13$	$59.42 \\ 63.13 \\ 66.58 \\ 69.73$	$\begin{array}{c} 60.93 \\ 64.75 \\ 68.27 \\ 71.50 \end{array}$	$\begin{array}{c} 62.62 \\ 66.52 \\ 70.13 \\ 73.45 \end{array}$	$\begin{array}{c} 64.47 \\ 68.48 \\ 72.20 \\ 75.60 \end{array}$	-0.83 -0.88 -0.93 -0.97	-0.95 -1.00 -1.05 -1.10		
$egin{array}{ccc} 4 & 00 \ 4 & 15 \ 4 & 30 \ 4 & 45 \end{array}$	69.40 71.82 73.93 75.73	70.90 73.38 75.53 77.35	72.57 75.10 77.30 79.15	74.40 76.98 79.23 81.13	76.43 79.08 81.38 83.33	78.67 81.38 83.75 85.75	$-1.02 \\ -1.05 \\ -1.07 \\ -1.10$	-1.15 -1.20 -1.23 -1.25		
$egin{array}{cccc} 5 & 00 \ 5 & 15 \ 5 & 30 \ 5 & 45 \end{array}$	77.1878.3279.1279.57	$78.85 \\ 79.98 \\ 80.80 \\ 81.25$	80.67 81.83 82.67 83.12	82.68 83.88 84.72 85.18	$\begin{array}{r} 84.92 \\ 86.13 \\ 86.98 \\ 87.45 \end{array}$	87.38 88.63 89.50 89.97	-1.13 -1.15 -1.15 -1.15	-1.27 -1.28 -1.30 -1.30		
$egin{array}{ccc} 6 & 00 \ 6 & 15 \ 6 & 30 \ 6 & 45 \end{array}$	79.68 79.43 78.87 77 97	$81.37 \\ 81.12 \\ 80.53 \\ 79.60$	83.22 82.97 82.37 81.42	85.28 85.02 84.40 83.40	$8755 \\ 87.28 \\ 86.63 \\ 85.62$	90 07 89.77 89.10 88.05	-1.17 -1.15 -1.13 -1.12	-1.30 -1.30 -1.28 -1.27		
$egin{array}{ccc} 7 & 00 \ 7 & 15 \ 7 & 30 \ 7 & 45 \end{array}$	76.73 75.17 73.28 71.10	78.33 76.73 74.82 72.57	$80.10 \\ 78.47 \\ 76.50 \\ 74.20$	82.07 80.38 78.35 76.00	84.23 82.50 80.42 77.98	86.62 84.83 82 68 80.18	-1.10 -1.08 -1.07 -1.03	-125 -1.22 -1.20 -1.15		
$egin{array}{ccc} 8 & 00 \ 8 & 15 \ 8 & 30 \ 8 & 45 \ \end{array}$	$\begin{array}{c} 68.60 \\ 65.82 \\ 62.77 \\ 59.45 \end{array}$	$70.02 \\ 67.18 \\ 64.07 \\ 60.67$	$71.60 \\ 68.68 \\ 65.48 \\ 62.02$	73.33 70.35 67.07 63.52	75 23 72.18 68.82 65 17	77.35 74.20 70.73 66.98	-1.00 -0.95 -0.90 -0.85	-1.10 -1.07 -1.02 -0.97		
$egin{array}{ccc} 9 & 00 \ 9 & 15 \ 9 & 30 \ 9 & 45 \end{array}$	55.88 52.08 48.07 43.85	57.03 53.15 49.05 44.73	$58.30 \\ 54.33 \\ 50.13 \\ 45.73$	59.72 55.63 51.33 46.82	$61.23 \\ 57.07 \\ 52.65 \\ 48.02$	$\begin{array}{c} 62.95 \\ 58.65 \\ 54.12 \\ 49.35 \end{array}$	-0.80 -0.75 -0.70 -0.63	-0.90 -0.83 -0.77 -0.70		
$\begin{array}{cccc} 10 & 00 \\ 10 & 15 \\ 10 & 30 \\ 10 & 45 \end{array}$	39.45 34.88 30.17 25.33	$\begin{array}{r} 40.25\\ 35.58\\ 30.78\\ 25.85\end{array}$	$\begin{array}{r} 41.13 \\ 36.37 \\ 31.47 \\ 26.42 \end{array}$	$\begin{array}{c} 42.12 \\ 37.23 \\ 32.20 \\ 27.05 \end{array}$	43.20 38.20 33.03 27.73	$\begin{array}{r} 44.40\\ 39.25\\ 33.95\\ 28.50\end{array}$	-0.57 -0.50 -0.43 -0.37	-0.63 -0.57 -0.48 -0.40		
$\begin{array}{cccc} 11 & 00 \\ 11 & 15 \\ 11 & 30 \\ 11 & 45 \end{array}$	$\begin{array}{r} 20.40 \\ 15.37 \\ 10.28 \\ 05.15 \end{array}$	$20.82 \\ 15.68 \\ 10.48 \\ 05.25$	$21.27 \\ 16.03 \\ 10.72 \\ 05.37$	21.77 16.40 10.97 05.50	$22.33 \\ 16.83 \\ 11 \ 25 \\ 05.63$	$22.95 \\ 17\ 28 \\ 11.57 \\ 05.78$	-0.30 -0.22 -0.15 -0.07	-0.33 -0.25 -0.17 -0.08		
Elongatic Azimutl Hour Ang	1 19.68 debm s	hm s'	1 23.23 h m s 5 56 54	hmel	1°27.57	1°30.08	$-1.15 + 2^{s}$	-1'.30 +3		

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Hour Angle before or after	Azimu	ths of P Azim	Correction for 1' increase in declination of Polaris					
upper cul- mination	Lat. 40°	Lat. 42°	Lat. 44°	Lat. 46°	Lat. 48°	Lat. 50°	Lat. 40°	Lat. 50°
h m 0 15 0 30 0 45	06.00 11.95 17.87	06.18 12.35 18.45	06.40 12.77 19.08	06.63 13.23 19.78	06.90 13.77 20.57	$07.20 \\ 14.35 \\ 21.45$	-0.08 -0.17 -0.27	-0.10 -0.22 -0.32
$egin{array}{cccc} 1 & 00 \ 1 & 15 \ 1 & 30 \ 1 & 45 \end{array}$	$23.70 \\ 29.43 \\ 35.02 \\ 40.45$	$\begin{array}{r} 24.47 \\ 30.37 \\ 36.13 \\ 41.75 \end{array}$	$25.30 \\ 31.42 \\ 37.38 \\ 43.18$	26.23 32.57 38.77 44.77	$27.28 \\ 33.87 \\ 40.30 \\ 46.55$	$\begin{array}{r} 28.45 \\ 35.30 \\ 42.02 \\ 48.52 \end{array}$	-0.35 -0.43 -0.52 -0.60	-0.42 -0.53 -0.63 -0.72
$\begin{array}{cccc} 2 & 00 \\ 2 & 15 \\ 2 & 30 \\ 2 & 45 \end{array}$	$\begin{array}{r} 45.70 \\ 50.75 \\ 55.58 \\ 60.15 \end{array}$	47 17 52.37 57.35 62.07	$\begin{array}{r} 48.78 \\ 54.17 \\ 59.30 \\ 64.18 \end{array}$	$50.58 \\ 56.15 \\ 61.48 \\ 66.53$	52.58 58.37 63.90 69.15	$54.82 \\ 60.85 \\ 66.62 \\ 72.07$	-0.67 -0.75 -0.82 -0.88	-0.82 -0.90 -0.98 -1.07
$\begin{array}{cccc} 3 & 00 \\ 3 & 15 \\ 3 & 30 \\ 3 & 45 \end{array}$	$\begin{array}{c} 64.47 \\ 68.48 \\ 72.20 \\ 75.60 \end{array}$	66.50 70.65 74.48 77 98	68.77 73.05 77.00 80.62	71.28 75.72 79.82 83.55	74.08 78.68 82.93 86.82	77.20 82.00 86.42 90.45	-0.95 -1.00 -1.05 -1.10	-1.13 -1.20 -1.27 -1.33
$\begin{array}{rrrr} 4 & 00 \\ 4 & 15 \\ 4 & 30 \\ 4 & 45 \end{array}$	78.67 81.38 83.75 85.75	81.13 83.93 86.37 88.43	83.88 86.77 89.27 91.38	86.90 89.90 92.50 94.68	90.30 93.40 96.10 98.33	94.08 97.28 100.07 102.42	-1.15 -1.20 -1.23 -1.25	$-1.38 \\ -1.43 \\ -1.47 \\ -1.50$
$egin{array}{cccc} 5 & 00 \ 5 & 15 \ 5 & 30 \ 5 & 45 \end{array}$	87.38 88.63 89.50 89.97	90.10 91.38 92.27 92.75	93.10 94.42 95.33 95.83	96.45 97.80 98.73 99.23	$\begin{array}{c} 100.17 \\ 101.57 \\ 102.52 \\ 103.03 \end{array}$	$\begin{array}{c} 104.32 \\ 105.75 \\ 106.73 \\ 107.27 \end{array}$	-1.27 -1.28 -1.30 -1.30	$-1.52 \\ -1.53 \\ -1.55 \\ -1.57$
$egin{array}{ccc} 6 & 00 \ 6 & 15 \ 6 & 30 \ 6 & 45 \end{array}$	90.07 89.77 89.10 88.05	92.83 92.53 91.83 90.73	95.92 95 58 94.85 93.72	99.32 98.97 98.20 97.02	103.10 102.73 101.93 100 68	$\begin{array}{c} 107.32 \\ 106.93 \\ 106.07 \\ 104.77 \end{array}$	$-1.30 \\ -1.30 \\ -1.28 \\ -1.27$	-1.55 -1.55 -1.53 -1.52
$egin{array}{ccc} 7 & 00 \ 7 & 15 \ 7 & 30 \ 7 & 45 \end{array}$	86.62 84.83 82.68 80.18	89.25 87.40 85.18 82.60	92.18 90.27 87.97 85.28	95 42 93.42 91.03 88.27	99.02 96.93 94.45 91.57	$\begin{array}{c} 103.03 \\ 100.85 \\ 98.27 \\ 95.25 \end{array}$	-125 -122 -1.20 -1.15	-1.48 -1.45 -1.42 -1.37
	77.35 74.20 70.73 66.98	79.68 76.43 72.87 68.98	82.27 78.90 75.20 71.20	85.13 81.65 77.82 73.67	88.32 84.68 80.72 76.40	91.85 88.08 83.93 79.45	$-1.10 \\ -1.07 \\ -1.02 \\ -0.97$	$-1.32 \\ -1.27 \\ -1.20 \\ -1.13$
9 00 9 15 9 30 9 45	62.95 58.65 54.12 49.35	$\begin{array}{c} 64.83 \\ 60.40 \\ 55.73 \\ 50.82 \end{array}$	$\begin{array}{c} 66.92 \\ 62.33 \\ 57.52 \\ 52.45 \end{array}$	$69.22 \\ 64.48 \\ 59.48 \\ 54.25$	$\begin{array}{c} 71.78 \\ 66.87 \\ 61.68 \\ 56.25 \end{array}$	$74.63 \\ 69.53 \\ 64.13 \\ 58.48$	-0.90 -0.83 -0.77 -0.70	-1.07 -0.98 -0.92 -0.83
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	44.40 39.25 33.95 28.50	$\begin{array}{r} 45.72 \\ 40.42 \\ 34.95 \\ 29.35 \end{array}$	47.17 41.70 36.07 30.28	48.78 43.13 37.30 31.32	50.58 44.72 38.67 32.47	$52.58 \\ 46.48 \\ 40.20 \\ 33.75$	-0.63 -0.57 -0.48 -0.40	-0.75 -0.67 -0.57 -0.48
$\begin{array}{rrrr} 11 & 00 \\ 11 & 15 \\ 11 & 30 \\ 11 & 45 \end{array}$	$\begin{array}{r} 22.95 \\ 17.28 \\ 11.57 \\ 05.78 \end{array}$	$\begin{array}{r} 23.62 \\ 17.80 \\ 11.90 \\ 05.97 \end{array}$	$24.37 \\ 18.37 \\ 12.28 \\ 06.15$	$\begin{array}{r} 25.20 \\ 19.00 \\ 12.70 \\ 06.37 \end{array}$	26.13 19.70 13.17 06.60	27.15 20.47 13.72 06.85	-0.33 -0.25 -0.17 -0.08	0.38 0.30 0.20 0.10
Elongation Azimuth Hour Angle	1 30.08 h m s 5 56 08	hmg	1 35.93 h m s 5 55 33	hms	1 [°] 43.13 h m s 5 54 53	1°47.35 h m s 5 54 31	-1.30 +3	-1^{55}_{8} +3

the image of the sun into the center of the solar telescope when the line of collimation of the solar telescope makes an angle with the line of collimation of the main telescope equal to the sun's declination corrected for refraction, and the line of collimation of the main telescope is elevated at an angle equal to the co-latitude of the place of observation, it is rigidly necessary that the line of collimation of the main telescope lie in a true meridian as shown in (b), Fig. 23a.

The elementary lines of a solar attachment are: (1) The polar axis; (2) the line of collimation of the solar telescope; (3) the attached level line. These lines should have

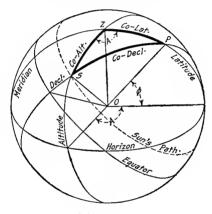


Fig. 23b.

the following relations: (1) The polar axis should be perpendicular to the line of collimation of the solar telescope and the horizontal axis of the main telescope; (2) the line of collimation of the solar telescope and the attached level line should be parallel. The methods of making these adjustments are obvious.

The declination of the sun (see Fig. 23b for explanation of astronomical terms) for the place of observation is found by adding, algebraically, the hourly change multiplied by the number of hours since Greenwich mean noon (6 A. M., 90th Meridian) to the declination of the sun, as given in the solar ephemeris for Greenwich mean noon for the given date. The setting (apparent declination) is found by taking the algebraic sum of the refraction correction and the declination of the sun obtained as above. The refraction is always plus; the declination is plus when the sun is north and minus when south of the celestial equator; and the hourly change in declination is plus when the sun is moving north and minus when moving south.

The "Pocket Solar Ephemeris and Refraction Tables for Use with Saegmuller's Solar Attachment," is given in "Handbook for Engineers" by George N. Saegmuller, published by Bausch & Lomb Optical Co., Rochester, N. Y. An "Ephemeris of the Sun and Polaris, and Tables of Azimuths of Polaris" is published by the General Land Office for each year. This Ephemeris may be obtained by addressing the Department of Interior, General Land Office, Washington, D. C., or may be purchased at a price of 5 cents per copy from the Government Printing Office, Washington, D. C. The true local mean solar time should always be used, and may be obtained from standard or railroad time by adding or subtracting four minutes for each degree that the place of observation is east or west of the standard meridian. The mean refraction of the sun for different altitudes is given in Table V.)

TABLE V.

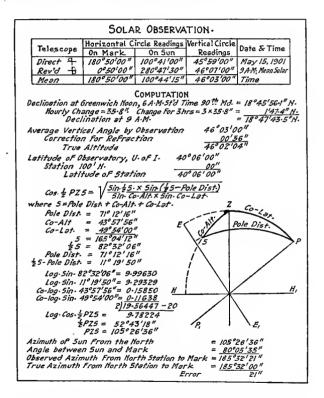
MEAN REFRACTION OF THE SUN.

BAROMETER 30 INCHES, TEMPERATURE 50° FAHE. (Refraction makes observed altitude too large.)

Altitude,	Refraction,	Altitude,	Refraction,	Altitude,	Refraction,
Degrees	Minutes	Degrees	Minutes	Degrees	Minutes
$ \begin{array}{r} 10 \\ 12 \\ 14 \\ 16 \\ 18 \\ 20 \\ 22 \\ \end{array} $	5.10 4 25 3.62 3 17 2 80 2 48 2.22	$24 \\ 26 \\ 28 \\ 30 \\ 35 \\ 40 \\ 45$	$\begin{array}{c} 2.02 \\ 1 83 \\ 1.67 \\ 1.53 \\ 1.25 \\ 1.03 \\ 0.85 \end{array}$	50 55 60 65 70 80 90	$\begin{array}{c} 0.70 \\ 0.58 \\ 0.48 \\ 0.38 \\ 0.30 \\ 0.13 \\ 0.00 \end{array}$

(1) Calculate the apparent declination (setting) of the sun for several different times, varying by 15 minutes, between 8 and 10 o'clock A. M. and 2 and 4 o'clock P. M. (2) Set the transit over the hub, level up very carefully with the attached bubble, and very carefully adjust the main transit and solar attachment. Determine the index error of the vertical circle, and either correct it or apply it to all vertical angles with its proper sign. (3) Level the transit

very carefully with the attached hubble. Bring the line of collimation of the main telescope and the line of collimation of the solar telescope parallel by sighting on a distant point, and point the main telescope south. (4) Set off the apparent declination (setting) with opposite sign on the vertical circle, i. e., dip the telescope when the declination is plus (north), and elevate the telescope when the declination is minus (south). (5) Level the solar telescope by means of its attached bubble. (6) Set off a plus vertical angle on the vertical circle equal to the co-latitude of the place. (7) Set the A vernier at zero and sight at a point on the true meridian. (8) Unclamp the upper motion, turn the main telescope about its upper motion and the solar telescope about its polar axis until the image of the sun is brought to the center of the cross lines in the solar telescope at the time for which the declination was computed. and clamp the upper motion. The line of collimation of the main telescope will then be in the meridian. (9) Read the horizontal plates. The reading will be the azimuth of the line first sighted on. (10) Repeat, using the setting corresponding to the time of observation, until ten values are obtained. If possible make five determinations in the A. M., and five in the P. M., about the same time from noon. The mean of these observations will eliminate instrumental errors. The most favorable time for making observations with a solar transit is from 8 to 10 A. M. and from 2 to 4 P. M. (11) Determine the true azimuth of the given line. The error of the determination of the meridian should not exceed one minute. Record as in the form.



PROBLEM D17. DETERMINATION OF TRUE MERIDIAN BY DIRECT OBSERVATION ON THE SUN.

(a) Equipment.—Complete transit, reading glass, hub, axe, colored eyepiece or colored shade to fit over objective, good watch set to keep standard time, solar ephemeris.

(b) *Problem.*—Determine a true meridian by a direct observation on the sun with a transit.

(c) Methods.—(1) Set the transit over a hub and level up very carefully with the attached hubble. (2) Test the adjustments of the transit very carefully, and determine the index error of the vertical circle. (3) Sight on a horizontal mark and read the horizontal plates. (4) Sight at the sun directly, by the aid of the colored eyepiece or colored glass shade, and bring his image tangent to the horizontal and vertical wires. (5) Read vertical circle and horizontal plates. (6) Reverse the telescope and make a second observation the same as the first except that the sun should he in the opposite quarter of the field of view. (7) The mean of the vertical and horizontal circle readings will give the apparent altitude and plate reading of the sun's center. (8) Observe the standard time of the observation and reduce to mean solar time by adding or subtracting 4 minutes for each degree that the place of observation and reduce to mean solar time by adding or subtracting 4 minutes for each degree that the place of observation is east or west of the standard meridian. (9) Calculate the angle PZS in the PZS triangle as shown in the accompanying form. Refraction makes the sun appear too high and it should therefore be subtracted. (10) Determine the azimuth of the line from the hub to the mark and check the observed azimuth. (The data for this problem may be obtained from Saegmuller's "Solar Ephemeris and Refraction Tables," or from the "Ephemeris of the Sun and Polaris, and Tables of Azimuths of Polaris," by the General Land Office, mentioned in Problem D16. Mean refraction of the sun for different altitudes is given in Table V.) (11) Where considerable accuracy is desired, make a second observation when the sun is about the same distance on the opposite side of the meridian. The error of the determination should not exceed 1 minute.

PROBLEM D18. COMPARISON OF TRANSIT TELESCOPES.

(a) Equipment.—Five engineers' transits.

(b) *Problem.*—Make a critical comparison of the telescopes of five engineers' transits.

(c) Methods.—Follow the methods outlined in the comparison of level telescopes.

PROBLEM D19. TEST OF A TRANSIT.

(a) Equipment.—Transit, reading glass, leveling rod, chaining pins, foot rule.

(b) *Problem.*—Test the following adjustments of an assigned transit: (1) Test the graduation for eccentricity. (2) Test the plate levels to see if they are perpendicular to the vertical axis. (3) Test the line of collimation to see if it is perpendicular to the horizontal axis. (4) Test the horizontal axis to see if it is perpendicular to the vertical axis. (5) Test the level under the telescope to see if the tangent to the tube at the center is parallel to the line of collimation. (6) Test the vertical circle to see if the vernier reads zero when the line of sight is horizontal.

(c) Methods.—Make the tests as described in the first part of this chapter but do not make any of the adjustments or tamper with any of the parts of the instrument. Check each test. Make a careful record of the methods and errors, including a statement of the manner of doing correct work with each adjustment out.

PROBLEM D20. ADJUSTMENT OF A TRANSIT.

(a) Equipment.—Transit, reading glass, leveling rod, chaining pins, adjusting pin, small screw driver.

(c) Methods.—Make the following tests and adjustments of an assigned transit that has been thrown out of adjustment by the instructor: (1) Test the graduation for eccentricity. (2) Adjust the plate levels perpendicular to the vertical axis. (3) Adjust the line of collimation perpendicular to the horizontal axis. (4) Adjust the horizontal axis perpendicular to the vertical axis. (5) Adjust the level under the telescope parallel to the line of collimation. (6) Adjust the zero of the vertical circle to read zero when the line of sight is horizontal. (7) Center the eyepiece.

(c) Methods.—Make the tests and adjustments as described in the first part of this chapter. Use extreme care in manipulating the screws and if any of the parts stick or work harshly, call the instructor's attention before proceeding. Repeat the tests and adjustments. Make a careful record of methods and errors.

PROBLEM D21. SKETCHING A TRANSIT.

(a) Equipment.-Engineers' transit.

(b) Problem.—Make a first-class sketch of an engineers' transit.

(c) Methods.—(See similar problem with the level.)

THE TRANSIT.

PROBLEM D22. ERROR OF SETTING FLAG POLE WITH TRANSIT.

(a) Equipment.—Transit, iron flag pole, flat stake 1"x 2"x 15", foot rule.

(b) *Problem.*—Determine the probable error of setting a flag pole with the transit at a distance of 300 feet. Repeat for 600 feet.

	r			1	· · · · · · · · · · · · · · · · · · ·	
1 _	· ·	_			L	Observers, J. Doe & R. Roe
	OR OF		ING	LAG	POLE	WITH ENGINEERS' TRANSIT.
Distance	No. of	Distance	d	dz		Dec. 6, 1914. (2 hours) Cool and Quiet.
Ft.	Setting	ln•	ln-			Used Buff & Berger Transit, Locker No 9,
300	1	1.18	0.18	0-0324	1	flat stake, I"x 2 x15," and iron Flag pole-
	2	1.38	·02	.0004	1	Sighted at iron Flag pole set on stake
	3	1.30	·06	·0036		which had been placed on ground at
	4	1.53	•17	·0289		about 300 Ft. From the Transit, and
	5	1.32	·04	· 0016		clamped both plates; then measured
	6	1.38	-02	· 0004		the distance in Inches From a line
í í	7	1.29	.07	· 0049		drawn across the board.
	8	1.46	•10	·0100-		With both plates clamped, lined in the
	9	1.46	-10	.0100		rod 10 times in all, the Flagman not-
	10	1.30	-06	·0036		ing the distance From the line.
	Mean	1.36		0-0958	= 2d2	The pole was shifted each time.
						Repeated test for 600 Ft.
600	1	1.14	0.25	0.0625		Probable Error for 300 Ft.
[]	2	1.56	•17	-0289		$E_1 = 0.6745 \sqrt{\frac{\sum d^2}{2}} = 0.6745 \sqrt{\frac{0.958}{9}} = 0.103$ in
	3	1.14	-25	.0625		2,-00145 1-1 200145 9 -0105 11
	4	1.22	•17	·0289		E .= E. 0.103 1032 := - 20027 EL
	5	1.76	·37	.1369		$E_m = \frac{E_1}{Vn} = \frac{0.103}{VN} = 0.032 \text{ in} = 0.0027 \text{ Ft.}$
	6	1.55	•16	·0256		$E_m(Angle) = \tan^{-1} \frac{0.0027}{3.00} = 1.8$.
	7	1.23	·16	·0256		Probable Error For 600 Ft.
	8	1.10	·29	-084-1		$E_{1} = 0.6745 \frac{5472}{9} = 0.247 \text{ in.}$
	9	1.55	·16	.0256		21-0-0173 1 9 - 0-241 11.
	10	1-65	·26	.0676		$E_m = \frac{0.247}{V_{10}} = 0.078 in = 0.0065 Ft.$
	Mean	1.39		0.5472	= E d ² .	
	Ì					$E_m (Angle) = tan^{-1} \frac{0.0065}{600} = 2.2$
						600

(c) Methods.—(1) Set the transit up and sight at the flag pole plumbed near the middle of the stake at a distance of about 300 feet. (2) Measure the distance from the point of the flag pole to a mark on the stake. (3) Keep the vertical axis clamped, and move the pole to one side. (4) Set the pole with the transit, and measure the distance from the first line. (5) Repeat until at least ten consecutive satisfactory results are obtained. (6) Compute the probable error of a single observation and of the mean of all the observations (see chapter on errors of surveying), and reduce the mean error to its angular value. (7) Repeat for 600 feet. Determine distances by pacing. Follow the form.

PROBLEMS.

PROBLEM D23. REPORT ON DIFFERENT MAKES AND TYPES OF TRANSITS.

(a) Equipment.—Department equipment, catalogs of the principal makers of engineers' transits.

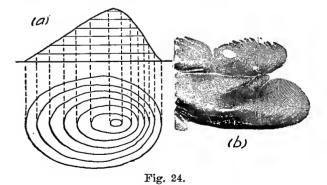
(b) *Problem.*—Make a critical comparison of the several types of transits made by the different makers.

(c) Methods.—(See similar problem with the level.)

CHAPTER VI.

TOPOGRAPHIC SURVEYING.

Topographic Map.—A topographic map is one which shows with practical accuracy all the drainage, culture, and relief features that the scale of the map will permit. These features may be grouped under three heads as follows: (1) the culture, or features constructed by man, as cities, villages, roads; (2) the hypsography, or relief of surface forms, as hills, valleys, plains; (3) the hydrography, or water features, as ponds, streams, lakes. The culture is usually represented by conventional symbols. The surface forms are shown by contours (lines of equal height), (a), Fig. 24, or hachures, (b), Fig. 24. The water features are shown by soundings, conventional signs for bars, etc.



Topographic maps may be divided into two classes depending upon the scale of the map. Small scale topographic maps are made by the U. S. Coast and Geodetic Survey and the U. S. Geological Survey, and are drawn to a scale of 1:62,500, 1:125,000 or 1:250,000 with corresponding contour intervals of 5 to 50, 10 to 100, and 200 to 250 feet. These maps show the streams, highways, railroads, canals, etc., in ontline but do not show any features of a temporary character. For topographic symbols, see Chapter XI.

Large scale topographic maps are drawn to a scale of 400 feet to 1 inch (1.4800), or greater, with contour intervals from 1 to 10 feet depending upon whether the ground is flat or hilly Roads, streets, dwellings, streams, etc., are drawn to scale. Features too small to be properly represented when drawn to scale are drawn out of proportion to the scale of the map.

Topographic Survey.—The object of a topographic survey is the production of a topographic map, and hence neither time nor money should be wastefully expended in obtaining field data more refined than the needs of the mapping demand. A topographic survey may be divided into three parts: (1) the reconnaissance; (2) the skeleton of the survey; (3) filling in the details.

Reconnaissance.—The reconnaissance is a rapid preliminary survey to determine the best methods to use in making the survey and the location of the principal points of control. A careful reconnaissance enables the topographer to choose methods that are certain to result in a better map and a distinct saving of time.

Skeleton.—There are three general methods of locating the skeleton of a topographic survey: (1) tie line survey with chain only, (2) traverse method with transit or compass; (3) triangulation system, (f), Fig. 30. The first method is used for the survey of small tracts. The second method, in which the distances are measured with the chain, tape, or stadia, is used on railroad and similar surveys. The third method, in which triangulation stations are connected with each other and with a carefully measned base line and base of verification, is used on surveys for small scale maps and on detailed or special surveys, such as surveys of cities and reservoir sites.

Filling in Details.—There are three general methods employed for filling in the details: (1) with transit or compass and chain; (2) with transit and stadia; (3) with plane table and stadia. The transit and stadia are used by the Mississippi and Missouri River Commissions. The plane table and stadia are used by the U. S. Coast and Geodetic and the U. S. Geological Surveys.

Topographic City Survey.—A topographic city survey is one of the best examples of a survey for a large scale map. It is usually based on a system of triangulation executed with precision and connected with carefully measured base lines. The details of the survey are usually taken up in the following order: (1) reconnaissance and location of triangulation stations; (2) measurement of base line and base of verification; (3) measurement of angles by repetition; (4) establishment of bench marks by running duplicate levels; (5) adjustment of angles of triangulation system; (6) computation of sides, azimuths and coordinates; (7) filling in details, usually with transit and stadia; (8) plotting of triangulation and other important points on the map by rectangular coordinates; (9) plotting the details and completing the map. The instructions given on the succeeding pages are for a survey of this type.

Hydrographic Survey.—Hydrographic surveying is divided into river and marine. The first includes the location of bars and obstructions to navigation, and the determination of the areas of cross-section, the amount of sediment carried, etc. The second includes the making of soundings, location of bars, ledges, buoys, etc. The depth of the water is determined by making soundings with a lead or rod, and the velocity is gaged by means of floats or a current meter, (d), Fig. 31.

Soundings are located: (1) by two angles read simultaneously from both ends of a line on the shore, (f), Fig. 31; (2) by keeping the boat in line with two flags on shore, and determining the position on the line by means of an angle read on the shore, or by a time interval; (3) by intersecting ranges, (g), Fig. 31; (4) by stretching a rope or wire across. the stream; (5) by measuring with a sextant in the boat at the instant that the sounding is taken two angles to three known points on the shore, (c), Fig. 31; the point is located by solving the three point problem graphically with the three arm protractor, (e), Fig. 31; (6) by locating the position of the boat at the instant that the soundings are taken with transit and stadia. The first three methods are used on small river or lake surveys. The fourth method is used where soundings are taken at frequent intervals. The fifth method has been used almost exclusively in locating soundings in harbors, lakes, and large rivers. The sixth method is rapidly coming into general use and promises to be the favorite method.

THE STADIA.

Description.—The stadia is a device for measuring distances by reading an intercept on a graduated rod. The stadia-hairs, shown in (g), Fig. 27, are carried on the same reticule as the cross-hairs and are placed equidistant from the horizontal hair. The stadia-hairs are sometimes placed on a separate reticule and made adjustable. It is, however, considered better practice by most engineers to have the stadia-hairs fixed and use an interval factor, rather than try to space the hairs to suit a rod or to graduate a rod to suit an interval factor.

Stadia Rods.—Stadia rods are always of the self reading type. In Fig. 27, (a) and (b) are the kind used on the U. S. Coast Survey; (c) on the U. S. Lake Survey; (d) and (c) by the U. S. Engineers. A target for marking on the rod the height of the horizontal axis of the transit above the station occupied is shown in (f), Fig. 27.

Theory of the Stadia.—In Fig. 25, by the principles of optics, rays of light passing from points A and B on the rod through the objective so as to emerge parallel and pass through the stadia-hairs a and b, respectively, must inter-

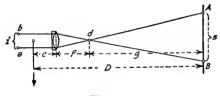


Fig. 25.

sect at the principal focal point d in front of the objective; therefore the rod intercept, s is proportional to the distance, g from the principal focal point in front of the objective.

Stadia Formula For Horizontal Line of Sight and Vertical Rod.—In Fig. 25, from similar triangles we have

$$s:g::i:f$$
 (1)

$$g = \frac{f}{i} s = k. s \tag{2}$$

From which

and

$$\mathbf{D} = \mathbf{k} \cdot \mathbf{s} + (\mathbf{c} + \mathbf{f}) \tag{3}$$

Stadia Formula For Inclined Line of Sight and Vertical Rod.—In Fig. 26 we have

THE STADIA.

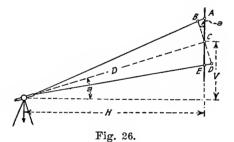
$$BD = AE. \cos a$$
 (approx.) (4)

and
$$D = k. s. \cos a + (c + f)$$
 (5)

but
$$H = D$$
. cos a
k. s. cos² a + (c + f) cos a (7)
= k. s - k. s. sin² a + (c + f) cos a (8)

also
$$V = D$$
. sin a (9)

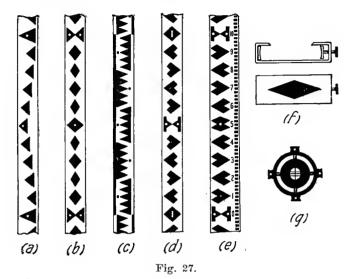
$$=\frac{1}{2}$$
 k. s. sin 2 a + (c + f) sin a (11)



Use of the Stadia.—The transit is set up over a station of known elevation and with a given direction or azimuth to another visible station; the height of the line of collimation above the top of the station is determined either by holding the rod beside the instrument and setting the target, or preferably by graduating one leg of the tripod and using the plumb bob; then with the transit oriented on a given line, "shots" are taken to representative points, and record made of the rod intercept, vertical angle and azimuth. In reading the intercept the middle hair is first set roughly on the target, then one stadia-hair is set at the nearest foot-mark on the rod and the intercept read with the other stadia-hair, after which the precise vertical angle is taken, and the azimuth is read.

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Reducing the Notes.—The notes may be reduced by means of tables, diagrams, or a special slide rule. The slide rule is the most rapid. There are several forms of stadia slide rule that are very accurate and are convenient for field use.

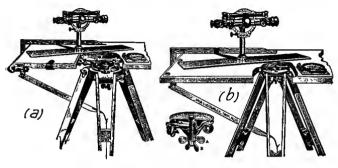


THE PLANE TABLE.

Description.—The plane table consists of an alidade, carrying a line of sight and a ruler with a fiducial edge. The alidade is free to move on a drawing board mounted on a tripod. The drawing board is leveled by means of plate levels. The line of sight should make a fixed horizontal angle with the fiducial edge of the ruler. The complete plane table is a transit in which the horizontal limb has been replaced by a drawing board.

There are three general types of plane tables: (1) the Coast Survey plane table, (a), Fig. 28; (2) the Johnson plane table, (b), Fig. 28; (3) the Gannet plane table, (d), Fig. 29.

Use of the Plane Table.—In making a survey with the plane table the angles are measured graphically and the lines and points are plotted in the field. The principal methods of making a survey with a plane table are: (1) radiation; (2) traversing; (3) intersection; (4) resection. *Radiation.*—In this method a convenient point on the



Complete Plane Tables. Fig. 28.

paper is set over a selected point in the field, and the table clamped. The line of sight is then directed towards each point to be located in turn and a line is drawn along the

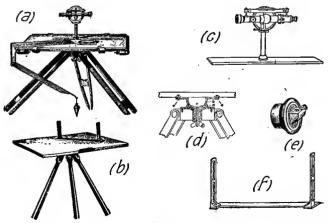
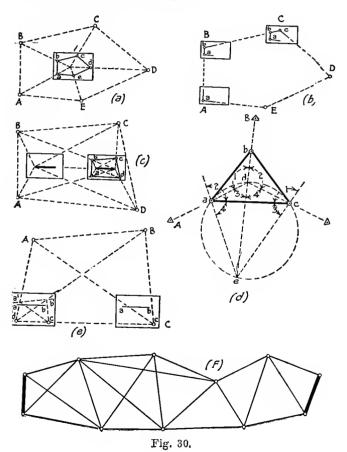


Fig. 29.

fiducial edge of the ruler. The distances, which may be determined by measuring with chain, tape or stadia, are plotted to a convenient scale, (a), Fig. 30.

Traversing.—This method is practically the same as traversing with a transit, (b), Fig. 30. Care should be used in orienting the plane table to get the point on the paper over the corresponding point on the ground as nearly as the character of the work requires.



Intersection.—In this method the points are located by intersecting lines drawn from the ends of a measured base line, (c), Fig. 30.

Resection.—In the resection method the plane table is set up at a random point and oriented with respect to either three or two given points, which gives rise to two methods known respectively as the three-point and two-point problems.

Three Point Problem.—Where three points are located on the map and are visible but inaccessible, the plane table is oriented by solving the "three point problem." There are several solutions, the best known of which are: (1) the mechanical solution; (2) the Coast Survey solution; (3) Bessel's solution; (4) algebraic solution. The problem is indeterminate if a circle can be passed through the four points.

In the mechanical solution the two angles subtended by the three points are plotted graphically on a piece of tracing paper, and the point is located by placing the tracing paper over the plotted points.

In Bessell's solution, (d), Fig. 30, a, b, c are three points on the map corresponding to the three points, A, B, C on the ground, and D is the random point at the instrument whose location, d, it is desired to find on the map. Construct the angle 1 with vertex at point c as follows: Sight along the line ca at the point A, and clamp the vertical axis. Then center the alidade on c and sight at B by moving the alidade, and draw a line along the edge of the ruler. Construct the angle 2 with vertex at a in the same manner. The line joining b and e will pass through the point d required. Orient the board by sighting at B with the line of sight along the line e b, and locate d by resection.

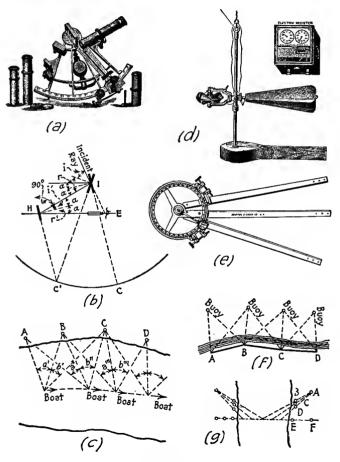
Two Point Problem.—To orient the board when only two points are plotted, proceed as follows: Select a fourth point, c, that is visible, and with these two points as the ends of a base line, (e), Fig. 30, laid off to a convenient scale, locate two points a' and b' on the map by intersection. The error of orienting the board will be the angle hetween the lines a-b and a'-b'. The table can now be oriented and the desired point located on the board by resection.

Adjustments.—The adjustments of the plane table are: (1) the plate levels; (2) the line of collimation; (3) the horizontal axis; (4) the attached level. These adjustments are practically the same as those for the transit.

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THE SEXTANT.

Description.—The sextant consists of an arc of 60° , with each half degree numbered as a whole degree, (a), Fig. 31, combined with mirrors so arranged that angles can be measured to 120° .



Theory.—The principle upon which the sextant is constructed is that if a ray of light is reflected successively between two plane mirrors, the angle between the first and last direction of the ray is twice the angle of the mirrors.

In (b), Fig. 31, the angles of incidence and reflection are equal,

$$i = r \text{ and } i' = r', \text{ and}$$

 $E = (i + r) - (i' + r') = 2(r - r')$
 $C' = (90^{\circ} - i') - (90^{\circ} - r) = (r - r')$
exceptore $E = 2 C'$

and therefore E = 2 C'

hut

C' = angle CIC', by geometry, since the

mirrors are parallel for a zero reading.

Use of the Sextant.—To measure an angle between two objects with a sextant, bring its plane into the plane of the two objects; sight at the fainter object with the telescope and bring the two images into coincidence. The reading is the angle sought. The angle will not be the true horizontal angle between the objects unless the objects are in the same level with the observer. Since the true vertex of the measured angle shifts for different angles, the sextant should not be used for measuring small angles between objects near at hand.

Adjustments, Index Glass.—To make the index glass, I, perpendicular to the plane of the limb, bring the vernier to about the middle of the arc and examine the arc and its image in the index glass. If the glass is perpendicular to the plane of the limb, the image of the reflected and direct portions will form a continuous curve. Adjust the glass by means of the screws at the base.

Horizon Glass.—To make the horizon glass, H, parallel to the index glass, I, for a zero reading. With the vernier set to read zero, sight at a star and note if the two images are in exact coincidence. If not, adjust the horizon glass until they are. If the horizon glass cannot be adjusted, bring the images into coincidence by moving the arm and read the vernier. This reading is the index error which must be applied with its proper sign to all the angles measured.

Line of Collimation.—To make the line of collimation parallel to the limb. Place the sextant on a plane surface and sight at a point about 20 feet away. Place two objects of equal height on the extreme ends of the limb, and note whether both lines of sight are parallel. If not, adjust the telescope by means of the screws in the ring that carries it.

PROBLEMS IN TOPOGRAPHIC SURVEYING.

PROBLEM E1. DETERMINATION OF STADIA CON-STANTS OF TRANSIT WITH FIXED STADIA-HAIRS.

(a) Equipment.—Complete transit, stadia rod, steel tape, set chaining pins, foot rule.

(b) Problem.—Determine the stadia constants c, f and k for an assigned transit.

(c) Methods.—(1) Set up the transit and set ten chaining pins in line about 100 feet apart on level ground. (2)Plumb the stadia rod by the side of the first pin. (3) Set the lower hair on an even foot or half foot mark keeping the telescope nearly level, and read the upper stadia-hair. (4) Record the intercept. (5) Read the intercept on the rod at the remaining pins. (6) Measure the distance from the center of the transit to each pin with the steel tape. (7)Focus the objective on a distant object, measure f (the distance from the plane of the cross-hairs to the center of the objective), and c (the distance from the center of the objective to the center of the instrument). (8) Calculate the value of the stadia ratio, k, for each distance by substituting in the fundamental stadia formula. (9) Take the arithmetical mcan of the ten determinations as the true value. (10) Compute the probable error of a single observation and of the mean of all the observations. The interval factor should be determined by the instrument man under the conditions of actual work. The determination should be checked at frequent intervals during the progress of the field work. Follow the prescribed form.

PROBLEM E2. STADIA REDUCTION TABLE.

(a) Equipment.—(No instrumental equipment required.)
(b) Problem.—Compute a stadia reduction table giving the horizontal distances from a point in front of the objective equal to the principal focal distance for the stadia intervals from 0.01 feet to 10 feet, for the transit used in Problem E1.

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(D	TEDM	NATIO	NAT	5tadi.	h con	STANTS - FIXED HAIRS -
No.	5		D-(c+f)	k	d d	d^2	
	Ft.		(c+f=}17)	Ft.	6	a-	Observers, J. Doe & R. Roe.
	1.81	180-41	179.24	99.02	0.02	00004	Dec 14, 14. (2 Hours) Cool & Cloudy
r	2.70		267.23	38.96	0.02	0.0064	Used Buff & Berger Transit, Locker 12 and Chaining Locker Nº 38.
33			354.15	98.92	0.12	0.0144	Set 10 chaining pins in line about 100 1
	1.05		399.72	98.72	0.32	0.1024	apart on level ground.
	1.86		481.63	99.11	0.07	0.0049	With telescope of transit nearly
	-61	556.30		99.20	0.16	0.0256	level and determined intercept
	5.50	643.58	642.41	98.84	0.20	0.0400	"s" at each pin by setting lower
8 1	1.90	786.93	785.76	99.47	0.43	0.1849	hair on a foot or haif foot mark
99	1.15	914.40	913-23	98.91	0.13	0.0169	and reading upper hair.
10 10	2.31	1024.71	1023-54	99.26	0.22	0.0484	
	1		Mean	99.04	202=	0.4443	
		-/			L-,		transit to each pin with steel tape to nearest 0.01 Ft.
1	- - -	1.67 Y 20	$\frac{1}{1} = 0.6$	7 Y 0.44.	<u>*</u> 2 =	0.15 Ft	With object glass Focused on a distan.
			ſ		4		object, determined c and F by
Ľ	<i>m=</i>		= 0.6:	1/20], ≏	0.05 Ft	
1					7	ł	of objective to center of the
			0.47 F			1	horizontal exis and the plane
		/* =					of the cross-wires respectively.
		C+F=	1-17 F	7.			Determined the different values
					1	i .	of k by substituting in the
						ļ	formula D=k5+c+F•
]	i i		
			l				
~			L	L	I	l	L
1				r			
(47114	тн Т	AVES			Observers, J. Doe & R. Roe.
5+-	+100	Azimuth				ITH	TRANSIT AND STADIA. Dec. 15, 1914, (3 hours) Clear and Warm.
	0bj-	AZIINUTI		Ft.		Elevation Ft.	Vec-13, 1914, (5 Nours) Clear and Warm-
A	1.00.		Bearing	FT.	Angle	718.00	Used Buff & Berger Transit, Locker No.12 and Stadia Board No.6.
17	F	000	N.4°00'W.	432	+ 0 20'	110.00	Stadia Constants : c+F=1.17 ft., k=100.00
	8		5-12°10'W		- 040'	(-7.2)	Sighted at target set at H.I., for Vert.
В	۳		1	0.10	1 44	710.8	Angle.
1	A	16°13'	N.12%0'E.	624	+ 0°38'		Oriented the transit by Azimuth reversals
ł	C		5.43°15 W.		+ 0.50'	(+7.3)	
C	T			1		718-1	
	B	47°16'	N-43°10'E.	499	-0.50'		$\mathcal{E} \left(\begin{array}{c} \mathcal{E} \\ \mathcal{F} \end{array} \right) $
1	0	0°03'	N.4°05'W.	758	- 1º10'	(-15.4)	
0			1			702.7	
	C	180°03'		756	+ 1º12'		
	E	6°14'	N.2°20'E.	618	+ 0°56'	(+10-1)	E+W)
E				1		712.8	$ \downarrow \rangle \downarrow $
		186° 14'		618	~0°56'		
	F	89°46'	N•85°15'E.	473	+0°54'	(+7.4)	<i>р</i> а ; н , -
F					-0-1	720.2	
	E		5-85°15'W.		-0°54'	(
	A	180"01"	5.4°05 E	434	-0°20'	(-2.5)	
A		180°00				7/7.7	ز هفر
1		180-00		[I	718.0	

718.0

с

Error = 0.3

Allowable Error 0.5 Ft.

.

180°00 Error = 0°01

Allowable error 2'

(c) Methods.—(1) Prepare form for calculation. (2) Compute the horizontal distances by substituting the different values of s in the stadia formula. Compute D' for values of s varying from 0.01 foot to 0.1 foot varying by 0.01 foot; from 0.1 foot to 1 foot varying by 0.1 foot; and from 1 foot to 10 feet varying by 1 foot.

STADIA REDUCTION TABLE									
(c+F) = 1.20 feet. $k = 115.75$ $D=kS+(c+F) = D'+(c+F)$									
Stadia Reading S	Distance D'=kS	Stadia Reading S	Distance D'= k5	Stadia Reading S	Distance D'=k5				
0.01 .02 .03 .04 .05 .06 .07 .08 .09 .10	0.01 1.2 .02 2.3 .03 3.5 .04 4.6 .05 5.8 .06 6.9 .07 8.1 .08 9.3 .09 10.4		11.6 23.2 34.7 46.3 57.9 69.4 81.0 92.6 104.2 115.8	1.0 2 3 4 5 6 7 8 9 10	115.8 231.5 347-2 463.0 578.8 694.5 810-2 926.0 1041.8 1157-5				

(To use the table, take the sum of the values of D' corresponding to the units, tenths and hundredths of s as given in the table. To the value of D' thus obtained add c plus f.)

PROBLEM E3. AZIMUTH TRAVERSE WITH TRANSIT AND STADIA.

(a) Equipment.—Complete transit, stadia rod, steel pocket tape.

(b) *Problem.*—Make a traverse of the perimeter of an assigned field with a transit and stadia.

(c) Methods.—(1) Set the transit over one corner of the field and set the A vernier to read the back azimuth of the preceding course. (2) Sight at a stadia rod held edgewise on the last station to the left with the telescope normal, and clamp the lower motion. (3) Read the intercept on the rod to the nearest 0.01 foot. (4) Sight at the target set at height of first station and read the vertical angle to the nearest minute. (The observer should measure the height of the horizontal axis above the station with the steel pocket tape, or one tripod leg may be graduated and the instrument height determined by swinging the plumb bob out against

the leg.) (5) Unclamp the upper motion, sight at the next station to the right and clamp the upper motion. (6) Read the A vernier. (this will be the azimuth of the course). (7)Read the intercept on the rod. (8) Measure the vertical angle by sighting at the target set at the height of the horizontal axis as before. (9) Set the transit over the next station to the right and determine the intercepts and vertical angles as at the first station. (10) Determine the stadia intercepts and vertical angles at the remaining stations, passing around the field to the right. (11) Reduce the intercepts to horizontal distances before recording. (12) Compute the vertical differences in elevation using mean distances and vertical angles. (13) Compute latitudes and departures to the nearest foot using a traverse diagram or traverse table. Follow form B4, (14) Compute the permissible error of closure of the traverse by means of Baker's formula (see Chapter IX "Errors of Surveying"); using "a" equals one minute times square root of number of sides, and "b" equal 1:500. If consistent, distribute the errors in proportion to the several latitudes and departures. respectively. (15) Compute the area by means of latitudes and departures, and reduce to acres.

PROBLEM E4. SURVEY OF FIELD WITH PLANE TABLE BY RADIATION.

(a) Equipment.—Plane table, stadia rod, 2 flag poles, engineers' divided scale, drawing paper, 6H pencil.

(b) *Problem.*—Make a survey of an assigned field by radiation with the plane table.

(c) Methods.—(1) Set the plane table up at some convenient point in the field and select a point on the drawing board that will allow the entire field to be plotted on the paper. (2) Sight at one of the stations with the ruler centered on the point on the paper. (3) Draw a line along the fiducial edge of the ruler towards the point. (4) Measure the distance to the point with the stadia. (5) Lay off the distance on the paper to the prescribed scale. (6) Locate the remaining points in the same manner. (7) Complete the map in pencil. The map should have a neat title, scale, meridian, etc. (8) Trace the map on tracing linen. (9) Compute the area by the perpendicular method, scaling the dimensions from the map.

PROBLEM E5. SURVEY OF A FIELD WITH PLANE TABLE BY TRAVERSING.

(a) Equipment.—Plane table, stadia rod, 2 flag poles, engineers' divided scale, drawing paper, 6H pencil.

(b) Problem.—Make a survey of an assigned field by traversing with the plane table.

(c) *Methods.*—Follow the same general methods as those given for traversing with the transit. Adjust the plane table before beginning the problem. Complete the map and compute the area as in Problem E4.

PROBLEM E6. SURVEY OF FIELD WITH PLANE TABLE BY INTERSECTION.

(a) Equipment.—Plane table, 2 flag poles, engineers' divided scale, drawing paper, 6H pencil.

(b) *Problem.*—Make a survey of an assigned field with the plane table by intersection.

(c) Methods.—(1) Select and measure a base line having both ends visible from all the stations in the field. (2) Set the plane table over one end of the base line, sight at the other end of the base line and at each one of the stations of the field. (3) Set the plane table over the other end of the base line, orient the instrument by sighting at the station first occupied and sight at all the stations in the field. (4) Complete map and compute area as in E4.

PROBLEM E7. THREE POINT PROBLEM WITH PLANE TABLE.

(a) Equipment.—Plane table, 2 flag poles, engineers' divided scale, 6H pencil.

(b) *Problem*.—Having three points plotted on the map, required to locate a fourth point on the map by solving the "three point problem" with the plane table.

(c) Methods. (1) Use Bessell's solution. (2) Check by using the mechanical solution.

PROBLEM E8. ANGLES OF TRIANGLES WITH SEXTANT.

(a) Equipment.-Sextant, 2 flag poles.

(b) Problem.—Measure the angles of an assigned triangle with the sextant.

(c) Methods.-(To determine index error, sight at a dis-

			1			· · · · · · · · · · · · · · · · · · ·	
		Angle	5 OF	TRIAN	SLE Å	-G-N WITH SEXTANT	
Station	Sextant	Observed	Index	Corrected	Mean	Observers: J.Doe & R.Roe.	
		Angle		Angie	Angle	Mch-28, 1914 (2 Hours) Cool &	
	28°34'30"			32 10'30		To desermine index error, s	ighted
	28°33'30"				32 10 00'	at flag staff I mile away	
	65°10'00'			68 46'00'		made reflected image coil	ncide
	65°09'30"				684545	with direct image The re	
	75'26'00"			79°02'00'		of the vernier gave an in	dex
	75°76'30″	Inverted	17		79°02'15"	error of +3°36'.	
					179 38'00		
	Actual e				02'	Held sextant over 6, sight	
	Allowabi	le error	of clos	ure	03'	and moved sextant arm	
		}				images of Flag poles at k	and N
	Í	}	1	1	1	coincided.	
			1		1	Inverted sextant, sighted a	
						moved sextent orm to me coincide •	ke images
		1				Repeated at other stations	
						Used Sextant Nº 75.	
			t i	1			
		1	1	i			
			ł			Langit	
			1			L=79 0L	
		1	ł			1500	
1	1	ł	ł	1			G
		1		1	1	K √ * *	<u> </u>
			1	1			

tant object and bring the direct and reflected images into coincidence. The reading of the vernier will give the index error, which, with proper sign, must be applied to all angles measured.) (1) Set the flag poles behind the monuments at two of the vertices of the triangle and stand on the monument at the third. (2) Hold the plane of the sextant horizontal, sight at one flag pole directly with the telescope and bring the image of the other flag pole into coincidence by moving the arm. (3) Read the vernier, and correct the angle for index error. (4) Repeat the measurement with the sextant inverted. Take the mean of the two readings, which should not differ more than 2', as the true value of the angle. (5) Measure the other angles in the same manner. The error of closure should not exceed 3'. Record the data in the form.

PROBLEM E9. DETERMINATION OF COEFFICIENTS OF A TAPE.

(a) Equipment.—Steel tape, spring balance, 2 thermometers, steel rule, 2 stout stakes, axe, 2 pieces sheet zinc 2 by 2 inches. (b) *Problem.*—Determine the coefficients of expansion, stretch, and sag of an assigned tape. Make three determinations of each, and take the arithmetical mean as the true value.

(Standard Tapes.—In laying off a standard or measuring a base line where a high degree of precision is required it is important that all measurements be referred to the same standard. The Bureau of Standards, Washington, D. C., will compare a tape with the government standard for a small fee. The tape tested is certified to be of a given length for a given temperature and pull. For example the standard tape marked "U. S. W. & M. 215" used in laying off the 100-ft. standard in Problem A23, was certified to be 99.9967 feet long at a temperature of 62° F. and a pull of 12 pounds, when tested on a plane surface. The coefficient of expansion of this tape was 0.0000061 per degree F. Tapes for measuring base lines with great precision have recently been made of Iuvar Steel.)

(c) Methods.—(1) Correction for Expansion.—Measure the length of the tape on a plane surface at two different temperatures but with a constant pull determined by a spring balance. Then substitute the lengths, l and L, and temperatures, t and T, in the formula

$$l - L \equiv e(t - T)l$$

where e is the coefficient of expansion. Repeat the test and obtain three values of the coefficient e. As large a range of temperatures as possible should be secured. Take the arithmetical mean of the three determinations as the true value.

(2) Correction for Stretch.—Measure the length of the tape on a plane surface with two different pulls but at a constant temperature. Determine the pull with a spring balance. Then substitute the lengths, l and L, and the pulls p and P, in the formula

$$l-L = s(p-P)l$$

where s is the coefficient of stretch. Repeat the test and obtain three values of the coefficient s. The pulls should range from 10 to 40 pounds. Take the arithmetical mean of the three determinations as the true value.

(3) Correction for Sag.—Remove the handles from the tape and determine its weight very carefully. Divide the weight by the length to obtain the weight per foot, w.

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Drive two stout hubs a little less than 100 feet apart and fasten a piece of sheet zinc with a line ruled at right angles to the line on the top of each stake. With a pull of 10 pounds, as determined by the spring balance, measure the distance between the stakes. Calculate the correction for sag by substituting the lengths, l and L, pull p, and weight per foot w, in the formula.

$$l - L = \frac{l}{24} \left(\frac{w \cdot l}{p} \right)^2$$

Repeat the measurements using a pull of 20 and 30 pounds, respectively. Add the corrections for sag to each measurement and compare the results. The temperature should remain constant during the tests. To remove the possibility of an error due to temperature, observe the temperature at the time of each observation and correct the observed length for e pansion before substituting in the formula.

Report the methods, data, computations and results on a suitable form.

PROBLEM E10. MEASUREMENT OF BASE LINE.

(a) Equipment.—Standard tape, transit or level, stakes (number and size to be specified by instructor), axe, spring balance, 2 thermometers, lath stakes, 8-d nails, steel rule, pieces sheet zinc 2 by 2 inches.

(b) Problem.—Measure an assigned base line with a standard tape.

(c) Methods.—(1) Set the transit over one end of the base line, sight at the other end and determine the difference in elevation and grade. (2) Drive stout square stakes to grade, by "shooting" them in with the instrument in true line, a little less than a full tape length apart. The top of the lowest stake should not be less than 6 inches above the ground. (3) Fasten a piece of sheet zinc, with a fine line ruled at right angles to the direction of the base line, on the top of each stake. (4) Drive lath stakes in line about 20 feet apart. (5) Drive an 8-d nail through each lath stake at grade to support the tape. (6) Measure from stake to stake, the men working as follows: No. 1 plumbs up from the rear monument or holds the zero on the mark on the rear stake; No. 2 takes the spring balance and puts a pull of 16 pounds on the tape; No. 3 reads the tape and measures the fraction of a tenth with a steel rule to 0.001

fect; No. 4 records the reading of the tape and reads the two thermometers placed at the quarter points of the tape. (7) Obtain at least three determinations of the length of the base line. (8) Correct each measurement of the base for standard, expansion, sag, stretch, and slope (see problem on coefficients of a tape). The three measurements should not differ more than 1:100,000. Report methods, computations and results on a suitable form.

PROBLEM E11. CALCULATION OF TRIANGULATION SYSTEM.

(a) Equipment.--Seven-place table of logarithms.

(b) *Problem.*—Adjust and calculate an assigned triangulation system and plot the skeleton.

(c) Methods.—Observe the following program: (1) prepare forms for calculations and transcribe data; (2) adjust the angles of the triangulation system (see chapter on crrors of surveying); (3) calculate the front and back azimuths of each line; (4) beginning with the base line compute the sides, to the nearest 0.001 foot; (5) calculate the latitudes and departures to the nearest 0.001 foot (6) calculate the coordinates of the triangulation stations to the nearest 0.001 foot. In computing the coordinates of the stations take the mean of the values found by taking the different routes from the base line as the true value. (7) Plot the skeleton of the triangulation system to the prescribed scale by means of the coordinates of the points. Check by lengths of sides. Use a steel straight edge.

PROBLEM E12. SKETCHING TOPOGRAPHY.

(a) Equipment.---Small drawing board or plane table, plat of assigned field, 4H pencil.

(b) *Problem.*—Sketch in the roads, walks, buildings and five-foot contours on the plat of the assigned field by eye having given the elevations of the ruling points.

(c) Methods.—(1) Transfer from the level notes to the plat the elevations of the ruling points of the field. (2) Locate the roads, buildings, etc., on the map as nearly as possible in their relative positions (the topographers' estimate of distance should be frequently checked by pacing).
(3) Estimate the slopes and locate the contour points between the points of known elevation. (4) Join these points by smooth curved lines. (5) Finish the map in pencil, put-

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ting on a neat title, the scale of the map and a meridian. (6) Compare the finished map with a contour map furnished by the instructor.

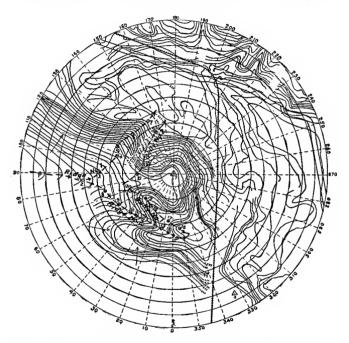
PROBLEM E13. FILLING IN DETAILS WITH TRANSIT AND STADIA.

(a) Equipment.—Complete transit, 2 stadia rods, pocket tape.

(b) *Problem.*—Locate the topographic details of an assigned area with the transit and stadia.

						Obcarua	r, 0.B.Q	nek	<u> </u>	C	I. Doe.
						Recorde	r, A.M.SL	ire	5ta	adiamen 🕻	Roe.
		(Top	OGRAP	HY BY	TRAN	SIT-S	TADIA	Мет	HOD.) `	
Sta.	Ver, A.	Ver. B.	Obs Dist.	Cor Dist	Vert Ang	DIFF EI.	Elev.	Des	tripti	on of Po	int.
1	AT ∆7	. Elev	A7=63	3:5, H·I	= 5-1	(A.S.B.)	ransit,	k= 100	00) 1	1-6-14	clear.
A5		332 51'	523.2	523.2	- 0°11'	- 1.6	631.9	No. E	1.05	= 631·8 (C	heck)
Shot No I	89°25'		524	520	+ 5°13'	+ 47.3	680.8	1 6	idge	Noll	•
2	85° 18'		355	353	+ 548'	+ 35.5	669.0	2.3	17	17	
3	90°06'		293	Z90	+ 5°27	+ 27.6	661.1		"	"	
	106'35'		235	235	+ /23'	+ 5.8	639.3	4	"	"	
5	114°50'		245	245	+ 0°33'	+ 2.3	635-8	5	22	"	
6	132°33'		223	220	~ 7°52	- 30.4	603.1	6	"	19	
7	152°57'		228	202	- 18°55'	- 69.2	564.3	7	111	"	
8	75°04'		277	273	+ 5°20'	+ 25.5	659.0		¢idge .	No-Z	
9	60°40'	[245	245	+ 4°06'	+ 17.6	651.1	9	11	"	
10	46°55'	1	226	226	+ 1º32	+ 6.0	639.5	10	"	"	
]/	41°51'	ł	218	218	+ 0°44	+ 2.7	636-2	11	"	17	
12	34°00'		214	214	- 1º20'		628-5	12	,11	11	
13	11°58'		217	Z10	- 9°20'			/3	"	"	
14	4°10'		228	221	- 9'34	- 37.5	596.0	14	27	**	
15	355°48'		250	238	- 1145	- 45.9	587.6	15	, , ,	**	
16	352°40'		212	196	- 15°12	- 53.5			īųIIy ,	No·1	
17	5°06		185	177	- 11°58	- 37.4		17	"	**	
18	33°28'		158	153	- 11°00	- 29.7		18	"	**	
19	47°15'		146	142	- 8º21		612.5	19	27	**	
20	67°58'		182	182	+ 1º10		637·Z	20	"	"	
21	88°41'		145	145	+ 037				ially N	6.2	
22	104"55'		124	119	- 1202		608.4	22	"	#	
23	155°52'	1	180	153	- 22 55	- 69.2	564.3	23	17	"	
			1	I	<u> </u>	i					

(c) Methods.—(1) Set transit up over assigned triangulation or other point. (2) Orient instrument, i. e., set plates to given azimuth and sight at given back sight. (3) Measure height of axis above station hub with tape or by graduations on tripod leg, and set target to correspond. (4) Take shot on given back sight and reduce results as a check before proceeding. (The program for each shot is: (a) set middle hair roughly on target, then set one stadia hair on nearest foot-mark and read intercept; (b) set middle hair precisely on target and signal rodman "all right"; (c) read vertical angle; (d) read azimuth.) (5) Take side shots to representative points, keeping in mind the scale of the proposed map. Select points according to a systematic plan, following along ridges, gullies, etc. Contour points should be taken with reference to change of



slope. (6) Reduce and plot the notes, and interpolate the contours, as in the accompanying diagram. (This toporaphy sheet should be carefully preserved for use in Problem E15.) (7) After completing the survey at the assigned station, move the instrument ahead to a new stadia station, taking both fore and back sights. (8) Lose no opportunity to take check sights at other triangulation stations, traverse points, etc.

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PROBLEM E14. FILLING IN DETAILS WITH PLANE TABLE AND STADIA.

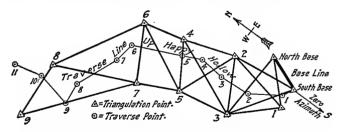
(a) Equipment.—Complete plane table (preferably with prismatic eyepiece), 2 stadia rods, engineers' divided scale, drawing paper, 6H pencil, pocket tape.

(b) *Problem.*—Locate the topographic details of an assigned area with the plane table and stadia.

(c) Methods.—Follow the same methods as in Problem E13 except that the notes are to be plotted on the drawing paper in place of being recorded in the field book. Mark the points by number and write the elevation of each point under the number in the form of a fraction. Locate the contour points by interpolation on the map and connect the points by smooth curves. Complete the map in pencil and make a tracing if required.

PROBLEM E15. TOPOGRAPHIC SURVEY.

(a) Equipment.—Complete transit, 2 stadia rods, stakes, hubs, spring balance, pocket tape, stadia slide rule, sevenplace logarithm table, (extra tripods, stadia reduction table, stadia reduction diagrams, etc., as required).



(b) *Problem.*—Make a complete topographic survey of an assigned area and make a topographic map.

(c) Methods.—(1) Make a reconnaissance and locate the triangulation stations. Care should be used to select the triangulation stations so that the sights will be clear and the triangles well formed. A system composed of quadrilaterals or more complicated figures will give more conditions and checks than a simple string of triangles. A system composed of simple triangles is sufficient for this survey. (2) Mark the triangulation stations with gas pipe monuments about 4 feet long, the exact point being marked by a hole drilled in a bolt screwed into a cap on the top of the gas pipe. (3) Measure the base line and base of verification as described in Problem E10. (4) Measure the angles by repetition as described in Problem D13. (5) Calculate the skeleton as described in Problem E11. (6) Establish permanent bench marks and determine their elevations and the elevation of the stations of the triangulation system by running duplicate levels with the engineers' level, reading the rod to 0 001 foot. (7) Fill in the details with either the transit and stadia or the plane table and stadia, or both, as described in Problems E13 and E14. (8) Complete the map in pencil on manila paper, and after it has been approved by the instructor trace it on tracing linen. The title, meridian, seale, lettering and border should receive careful attention.

CHAPTER VII.

LAND SURVEYING.

Kinds of Surveys.—Surveys of land are of two kinds: (a) original surveys; (b) resurveys.

Original Surveys.—An original survey is made for the purpose of establishing monuments, corners, lines, boundaries, dividing land, etc. The survey of a townsite and the government survey of a section are examples of original surveys.

Resurveys.—A resurvey is made for the purpose of identifying and locating corners, monuments, lines and boundaries that have been previously established. The resurvey of a city block, or a survey to relocate a section corner are examples of resurveys.

Functions of a Surveyor.—In an original survey it is the function of the surveyor to make a perfect survey, establish permanent monuments and true markings, and make a correct record of his work in the form of field notes and a plat.

In a resurvey it is the function of the surveyor to find where the monuments, courses, lines and boundaries originally were, and not where they ought to have been. Failing in this it is his business to reestablish them as nearly as possible in the place they were originally placed. No reestablished monument, no matter how carefully relocated, will have the same weight as the original monument if the latter can be found. In making resurveys the surveyor has no official power to decide disputed points. He can act only as an expert witness. If the interested parties do not agree to accept his decision the question must be settled in the courts.

Also see Problem F6, "Resurvey of a City Block."

Responsibility of the Surveyor for the Correctness of His Survey.—An engineer in the discharge of his professional duties requiring an exercise of judgment can be held liable only for failure to exercise reasonable care and skill, or for negligence or fraud. A surveyor is liable not only for negligence or fraud but for want of skill. A surveyor agrees to not only do his work carefully, honestly, diligently, but skillfully as well. The precision required in making any particular survey in order to satisfy the requirement for skill will depend upon the conditions; greater accuracy being required for making a survey of an expensive city lot than for a survey of a farm. Surveying is a trade and the precision required in any particular case to show proper skill is a matter to be decided by the court after evidence has been submitted.

Ownership of Surveyors' Notes .- Survey notes, data, maps, plats and records obtained by a surveyor while in the employ of a city, state, railroad or other corporation, or of a consulting or independent engineer belong to the employer. A city engineer or a county surveyor has no ownership rights in the notes, data, maps, plats and records which he prepares or obtains, or are prepared or obtained by him or by his assistants, in the exercise of the duties of his office as city engineer or county surveyor. Survey notes. data, maps, plats and records obtained by a consulting or independent engineer in preparing a report or plans for a client, belong to the consulting or independent engineer. The client, whether it be an individual, city, state, or corporation, is entitled only to the finished report or plans, and is not entitled to the notes and data used in the preparation of the report or the plans.

Rules for Resurveys.—The following rules may be safely observed in making resurveys.

(1) The description of boundaries in a deed are to be taken as most strongly against the grantor.

(2) A deed is to be construed so as to make it effectual rather than void.

(3) The certain parts of a description are to prevail over the uncertain.

(4) A conveyance by metes and bounds will convey all the land included within.

(5) Monuments determine boundaries and transfer all the land included.

(6) When a survey and a map disagree the survey prevails.

(7) Marked lines and courses control courses and distances.

(8) The usual order of calls in a deed is; natural objects, artificial objects, course, distance, quantity.

(9) A long established fence line is better evidence of

actual boundaries than any survey made after the monuments of the original survey have disappeared.

(10) A resurvey made after the monuments have disappeared is to determine where the monuments were and not where they should have been.

(11) All distances measured between known monuments are to be pro rata or proportional distances.

If the above rules do not cover the case in question special court decisions on that particular point should be consulted.

THE UNITED STATES RECTANGULAR SYSTEM OF PUBLIC LAND SURVEYS.

Historical.—The United States rectangular system of subdividing lands was adopted by congress May 20, 1785. The first public land surveys were made in the eastern part of the present state of Ohio under the direction of Capt. Thomas Hutchins,* Geographer of the United States, and were known as the "Seven Ranges." The townships were six miles square, and were laid out in ranges extending northward from the Ohio river; the townships were numbered from south to north, the ranges from east to west. In these initial surveys only the exterior lines of the townships were run, but mile corners were established on the township lines, and sections one mile square were marked on the plat and numbered from 1 to 36, commencing with section 1 in the southeast corner and running from south to north in each tier to 36 in the northwest section.

The act of congress approved May 18, 1796, provided for the appointment of a surveyor general and changed the law relating to the surveys of public lands. Under this law the townships were subdivided into sections by running parallel lines two miles apart each way and setting a corner at the end of each mile. This law also provided that the sections be numbered beginning with section 1 in the northeast corner of the township, thence west and east alternately to 36 in the southeast corner. This is the method of numbering still in use, shown in Figs. 33 and 34.

* The earliest published reference to the rectangular system of land surveys is found in an appendix to "Bouquet's March," published in Philadelphia, 1764. Hutchins was engineer with this expedition to the forks of the Muskingum river, and wrote the appendix. (See reprint by Robt. Clarke, Cincinnati.) The act of congress approved May 10, 1800, required that townships be subdivided by running parallel lines through the same from east to west and from south to north at a distance of one mile from each other. Section corners and half section corners on the lines running from east to west were required to be set. The excess or deficiency was to be thrown into the north and west tiers of sections in the townships.

1	FIRST S	FIRST STANDARD PARALLEL NORTH .										
N	T∙4N•, R∙IE∙	T-4 N., R-2 E-	T∙4 N•, R•3 E•	T∙4 N•, R∙4 E∙	Ŀ							
AL MERIDIAN	T·3N-, R·1E-	T·3N•, R·2E•	T: 3 N, R: 3 E.	T-3 N- R-4 E-	MAN EAST							
ed Principal.		T·2N•, R·2E·	T·2N·, R·3E·	T· 2 N•, R· 4 E-	GUIDE MERIDIAN							
Тнікр	T•1N-, R•1E•	T• 1 N•, R• 2 E•	T· I N·, R· 3 E•	T- N-, R- 4 E-	FIRST 6							
înitial Point		BASE	LINE		·							
Louit												

Fig. 32.

The act of congress approved February 11, 1805, required that interior section lines be run every mile; that corners be established every half mile on both township and section lines; that discrepancies be thrown on the north and west sides of the township. This act of congress further provided "that all corners marked in the original surveys shall be established as the proper corners of sections, or subdivisions of sections; and that corners of half and quarter sections not marked shall be placed as nearly as possible 'equidistant' from those two corners which stand on the same line. The boundary lines actually run and marked shall be established as the proper boundary lines of the sections or subdivisions for which they were intended; and the length of such lines as returned by the surveyor shall be held and considered as the true length thereof, and the boundary lines which shall not have been actually run and marked as aforesaid shall be ascertained by running straight lines from the established corners to the opposite corresponding corners." Under this law, which is still the established rule of procedure, each reported distance between established monuments is an independent unit of measure.

The revised instructions issued in 1855 required that the sections be subdivided as shown in Fig. 33. The full lines representing "true" lines, are parallel to the east exterior line of the township, and the dotted lines, representing "random" lines, close on corners previously established. The order of the survey of the interior section lines is indicated by the small numerals. Double corners on the north and west township lines, which were common in the earlier surveys, were thus avoided in the revised practice.

Laws Inconsistent.—It is obviously impossible to preserve a true rectangular system on a spherical surface, owing to the convergency of meridians.* To harmonize the methods of making surveys, the General Land Office has issued instructions for the survey of public lands from time to time.

DETAILS OF SURVEY.—The details of the survey are taken up in the following order: (1) selection of initial points; (2) establishment of the base line; (3) establishment of the principal meridian; (4) running standard parallels; (5) running the guide meridians; (6) running the township exteriors; (7) subdividing the township; (8) meandering lakes, rivers, streams, etc. See Figs. 32 and 33.

Initial Points.—Initial points from which to start the survey are established whenever necessary under special instructions prescribed by the Commissioner of the General Land Office.

Base Line.—The base line is extended east and west from the initial point on a parallel of latitude. The proper township, section and quarter corners are established and meander corners at the intersection of the line with all meanderable streams, lakes, or bayous. Two sets of chain-

* The angular convergency, a, of two meridians is m. sin L, where m is the angular difference of longitude of meridians and L is the mean latitude of the two positions. The linear convergency, c, for a length. t, is t. sin a. Latitude 40°, the difference between the north and south sides of a township is 0.60 chains.

LAND SURVEYING.

men are employed and the mean of the two measurements is taken as the true value. When the transit is used, the base line—which is a small circle parallel to the equator is run by making offsets from a tangent or secant line, the direction of the line being frequently checked hy an observation of Polaris.

Fig. 33.

Principal Meridian.—The principal meridian is extended either north or south, or in both directions from the initial point on a true meridian. The same precautions are observed as in the measurement of the base line.

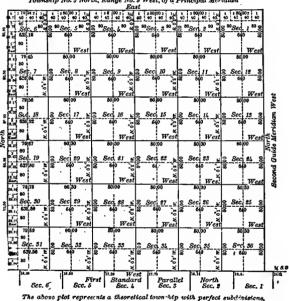
Standard Parallels.—Standard parallels, which are also called correction lines, are extended east and west from the principal meridian, at intervals of 24 miles north and south of the base line. They are surveyed like the base line.

Guide Meridians.—Guide meridians are extended north from the base line, and standard parallels, at intervals of 24 miles east and west from the principal meridian, in the

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manner prescribed for running the principal meridian. When existing conditions require that guide meridians shall be run south from the base or correction lines, they are initiated at properly established closing corners on such lines.

Township Exteriors.—The township exteriors in a tract 24 miles square, bounded by standard lines, are surveyed successively through the block, beginning with the south-

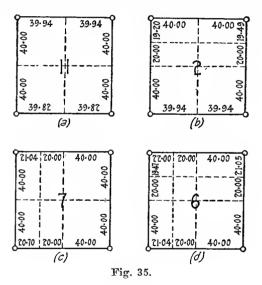


Township No. 5 North, Range No. 9 West, of a Principal Meridian

The above plot represents a theoretical town "htp with perfect subdivisions, contiguous to the north side of a Standard Parallel; in common Latter 20 15/N. ad Lon Sides 20000° W. of Gr. Arcs 2508.16 A

Fig. 34.

western township. The meridional boundaries are run first from south to north on true meridians with permanent corners at lawful distances; the latitudinal boundaries are run from east to west on random or trial lines and corrected back on true lines. Allowance for the convergency of meridians is made whenever necessary. Township Subdivisions.—A true meridian is established at the southeast corner of the township and the east and south boundaries of section 36 are retraced. Then beginning at the corner to sections 35 and 36 on the southern boundary, a line is run north parallel to the township line, corners are established at a distance of 40 and 80 chains; from the last named corner a random line is run eastward, parallel to the south boundary line of section 36, to its intersection with the east boundary of the township. A temporary corner is set at a distance of 40 chains, and a permanent corner is afterwards established midway be-



tween the two permanent corners. The other corners are located in a similar manner, as shown in Fig. 33. The lines closing on the north and west boundary lines of the township are made to close on the section corners already established. A theoretical township with perfect subdivisions is shown in Fig. 34.

Meandering.—Navigable rivers and other streams having a width of three chains and upwards are meandered on both banks, at the ordinary high water line by taking the general course and distances of their sinuosities. The meanders of all lakes, navigable bayous, and deep ponds of the area of twenty-five acres and upwards are surveyed as directed for navigable streams. Meander corners are established where meander lines cross base lines, township lines, or section lines.

Subdivision of Sections.—In Fig. 35, (a) gives the subdivision of an interior section, (b) of section.2 on the north side, (c) of section 7 in the west tier, and (d) of section 6 in the northwest corner.

10 Ac. 	YW# Ac	NE 4 160 Ac. 1.8.
W 1 5W4 80Ac	64(E½ SW4 80Ac.) Ac• 5E4 160 Ac•

Fig. 36.

Description of Land.—Land is described in the rectangular system by giving its location in a civil township; for example, in Fig. 36, the northeast quarter, containing 160 acres, would be described as: $N \ge \frac{1}{4}$, Sec. 8, T 19 N, R 9 E, 3 P. M. The ten acre lot indicated in the northwest quarter would be described as: $S \ge \frac{1}{4}$, N W $\frac{1}{4}$, N W $\frac{1}{4}$, Sec. 8, T 19 N, R 9 E, 3 P. M.

Corners.—The corner monuments may be as follows: (a) stone with pits and earthen mound; (b) stone with mound of stone; (c) stone with bearing trees; (e) post in mound of earth; (f) post in mound of stone; (g) post with bearing trees; (h) simple mount of earth or stone; (i) tree without bearing trees; (j) tree with bearing trees; (k) rock in place, etc. The trees on line are required to be blazed. The size, markings and proper corners to be used in any particular case and all other details are given in the "Manual of Surveying Instructions for the Survey of Public Lands of the United States," issued by the General Land Office, Washington, D. C.

The last edition of the "Manual of Surveying Instructions for the Survey of Public Lands" was issued in 1902 and may be obtained from the Superintendent of Documents, Government Printing Office, Washington, D. C., price 75 cents per copy. A new edition of the Manual is promised for 1915. The circular on the "Restoration of Lost and Obliterated Corners" mentioned in the next paragraph gives instructions for making resurveys, and may be obtained free hy addressing the Department of Interior, General Land Office, Washington, D. C.

Restoration of Lost or Obliterated Corners.*—"An obliterated corner is one where no visible evidence remains of the work of the original surveyor in establishing it. Its location may, however, have been preserved beyond all question hy acts of landowners, and by the memory of those who knew and recollect the true position of the original monument. In such cases it is not a lost corner.

"A lost corner is one whose position can not be determined beyond reasonable doubt, either from original marks or reliable external evidence."

General Rules.—The following rules are derived from a brief synopsis of congressional legislation relating to surveys.

"(1) The boundaries of the public lands established and returned by the duly appointed government surveyors, when approved by the surveyor general and accepted by the government, are unchangeable.

"(2) The original township, section, and quarter-section corners established by the government surveyors must stand as the true corners which they were intended to represent, whether the corners be in place or not.

"(3) Quarter-quarter corners not established by the government surveyors shall be placed on the straight line joining the section and quarter-section corners and midway between them, except on the last half mile of section lines closing on the north and west boundaries of the townships, or on other lines between fractional sections.

"(4) All subdivisional lines of a section running between corners established in the original survey of a township

* Circular on the "Restoration of Lost and Obliterated Corners and Subdivision of sections," Department of Interior, General Land Office, Washington, D. C. must be straight lines, running from the proper corner in one section line to its corresponding corner in the opposite section line.

"(5) That in a fractional section where no opposite corresponding corner has been or can be established, any required subdivision line of such section must be run from the proper original corner in the boundary line due east and west, or north and south, as the case may be, to the water course, Indian reservation, or other boundary of such section, with due parallelism to section lines."

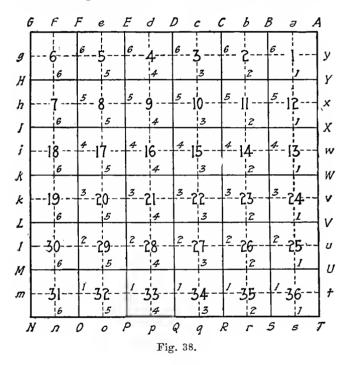
"From the foregoing it will be plain that extinct corners of the government surveys must be restored to their original locations, whenever it is possible to do so; and hence resort should always be first had to the marks of the survey in the field. The locus of the missing corner should be first identified on the ground by the aid of the mound, pits, line trees, bearing trees, etc., described in the field notes of the original survey.

"The identification of mounds, pits, buried memorials, witness trees, or other permanent objects noted in the field notes of survey, affords the best means of relocating the missing corner in its original position. If this can not be done, clear and convincing testimony of citizens as to the place it originally occupied should be taken, if such can be obtained. In any event, whether the locus of the corner be fixed by the one means or the other, such locus should always be tested and confirmed by measurements to known corners. No definite rule can be laid down as to what shall be sufficient evidence in such cases, and much must be left to the skill, fidelity, and good judgment of the surveyor in the performance of his work.

"Actions or decisions by county surveyors which may result in changes of boundaries of tracts of land and involve questions of ownership in connection therewith, are subject to review by the local courts in proceedings instituted in accordance with the local statutes governing such matters."

The pamphlet also contains much additional information of value.

Locations of Principal Meridians.—Principal meridians have been established as the needs of the surveys warranted. There are twenty-four principal meridians in all, the locations of which are given in the "Manual of Instructions," mentioned above. Abridging Field Notes.—The government surveyors use the method of abridging field notes shown in Fig. 38. Corners in the township boundary are referred to by letter; interior section corners are referred to by giving the numbers of the sections meeting at the corner; interior quarter section corners are referred to by giving the number on the section lines produced.



SURVEYS BY METES AND BOUNDS.

That portion of the United States settled before the adoption of the rectangular system was surveyed by the method of metes and bounds. For the most part these surveys were very irregular and often involved complex and conflicting conditions. The entire eastern portion of the United States, and the state of Kentucky, were surveyed in this manner, PROBLEMS.

and further examples are found in the French surveys in the states of Michigan, Indiana, Illinois, Missouri, Louisiana, etc., and the Spanish surveys of Texas, California, etc. The general principles underlying the questions of ownership, priority of survey, the restoration of lost corners, etc., are identical whatever the system of survey used.

PROBLEMS IN LAND SURVEYING.

PROBLEM F1. INVESTIGATION OF A LAND CORNER.

(a) Equipment.-Digging outfit, tape, etc., as required.

(b) *Problem.*—Collect complete evidence relative to an assigned land corner, and after giving due weight to the same, make a decision as to the true corner.

(c) Methods.—(1) Make careful examination of the official field notes and records pertaining to the land corner in question and make extracts from the same for further reference. (2)Seek oral evidence from those acquainted with the history of the corner. (3) Make a survey of fence lines and other physical evidence, such as witness trees or their stumps, etc., near the corner under investigation. (4) Make

	J. Dos, Surveyor:
INVESTIGATION OF S.W. CORNER,	SECTION 8, T-19N., R.9E., 3D. P.M.
Original United States Field Notes, on File	
	as "Post in Mound," the corner being
located on the Prairie remote From	the heavy timber which surrounds the
	Original survey was made about 1822.
	d for informs tion about the corner under
	when he was a boy, Mr. Campbell, who
	on to re-establish the SW. Cor., Sec. 8. At
	near the come, were occupied by rail
	r (a pioneer sets ler) pointed out to the
	ces of a mound which he believed marked
	mpbell, the surveyor dug cerefully at the
	a sassafrars stake which unquestionably
	at in Mound "est blished some 25 years
	· Col·Busey stat es that he himself carried
	y the County Surveyor to pepetuate the
	nt was not disturbed until it was re-
	the roads were opined upon the section
lines.	F and
	of the road . For many years. About 1894
	Commission or under the direction of the
	ade since the stone was lowered, indicate
that its present position is identical	
	ble statement with the corroboration From
	abscence o. P conflicting evidence of any

recognized is the true SW corner of Section 8, 7.19.4., R.9 E.31

careful examination of the site of the corner with the digging outfit; the digging should be done cautiously so as to avoid disturbance of existing stakes or other monuments. (5) If more than one monument be found, make due record of their character and positions, and make further inquiry respecting them. (6) If no monument of any sort be found at first, continue the search diligently and do not give up finding the true corner as long as there is a remote chance of locating it. In any event, avoid wanton disturbance of any object or evidence that may have a bearing on the same. Keep a clear and concise record.

PROBLEM F2. PERPETUATION OF A LAND CORNER.

(a) Equipment.—Digging outfit, a large boulder or other permanent monument, cold chisel, hatchet, plumb bob, string, stakes.

(b) *Problem.*—Replace a temporary land corner by a permanent monument.

(c) Methods.—(1) Uncover the identified temporary monument and carefully determine the true point with consist-

Comm For pla CHAINS 40-00	enced at the SE con of Sec. 14. Fr the cor. which lugh Shafter says h the ungivestioned, as the con. For over maple, 8 ins. ciam., 5-49°W., 77 Iks- bur oak 12 ins. ciam., 9-49°W., 77 Iks- karporary stakes every 10 chs 4 sec. cor. lost. 1 Intersected the W line of Sec. 14, 42. correct point, N28°E., 104 Iks- Fr bearing tree of U-5 Survey, having locust 16 ins. ciam., 5-28°W. bur oak 18 ", N-78°E. Ren thence E on corrected line at si Found ceder stake 3 Ft. below surface No other evidence of cor. to be. 10 other evidence of cor. to be.	dist. dist. dist. then ran W• on random, var 2°15'E; setting in line. ks. S· of the cor. Found rotten stake at om stump of wh• oak, 24 ins- diam., og survayor's mark distinct on ii- Set a for cor. Marked: , 116 Ks- dist.
60-18	Planted granite boulder 20×12×6 cor., in true line between gr. po maple, 12 ins. diam., 5×16°E. burr cak, 16 ++ ++ ++ ++ ++ ++ ++ ++ ++ ++ ++ ++ ++	st and sec- cor- and marked: 55 lks-dist.

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ent exactness. (2) Reference out the point by driving two pairs of stakes with strings stretched so as intersect squarely over the corner. (3) After carefully checking the referencing, dig out the old monument to a depth sufficient to receive the boulder and permit its top to set several inches beneath the natural surface if located in a road or where disturbance is probable. (4) Cut a plain cross mark on the top of the stone, and set it in place in the hole. packing the earth about it, testing the position of the mark by means of the reference stakes and strings and plumb bob; finally leave the boulder set firmly in the correct position. (5) Make reference measurements to suitable permanent points such as marks on curbing, gas pipes, witness trees, etc., selected with respect to good intersections, and make reliable record of the witness notes after checking the same. (Other forms of permanent monuments are: gas pipe; fish plate; section of T-rail; farm tile or vitrified pipe filled with cement mortar; post hole filled with mortar: special solid monument burned like farm tile: special casting similar to a gas main valve box, with hole in top to receive flag pole; etc.)

PROBLEM F3. REESTABLISHING A QUARTER-SECTION CORNER.

(a) Equipment-Transit party outfit, digging tools, etc.

(b) *Problem.*—Reestablish a quarter-section corner that has been obliterated or lost.

(c) Methods.—(1) Collect and record all the available evidence which may assist in the discovery and identification of the corner. Examine the field notes of the original survey, the surveyors' plat book and the county atlas on file at the court house, and make diligent inquiry for credible and competent information, either written or oral as to the location of the corner. (2) Make a careful search for the monument. Trace all the lines of the original survey, paying particular attention to bearing and sight trees. Dig in all the places indicated by the different lines and give up the search only after you have exhausted every possible clue. (3) If the corner cannot be found, reestablish it, giving due weight to all the evidence. The surveyor should remember that the corner should be reestablished where it originally was and not where it ought to be. After having located a stake at the supposed location of the original monument, reference it out and renew the search. (4)

After the monument has been relocated, mark it in a permanent manner as indicated in Problem F2, by a stone with a cross cut in its top or with a gas pipe well driven into the ground. Reference it out to at least two permanent objects selected with a view to securing a first class intersection. Make a careful record and preserve consistent accuracy in the work.

PROBLEM F4. REESTABLISHING A SECTION CORNER.

(a) Equipment.—Transit party outfit, digging tools, etc.

(b) *Problem.*—Reestablish an obliterated or lost section corner.

(c) Methods.—Follow the various methods described in Problem F3, giving special attention to the search for the original corner; upon failing to find trace of it, run out lines with reference to the section, quarter, and quarterquarter corners in the four directions, with linear measurements from the same and finally reach the most consistent decision with reference to such survey lines, ownership lines, fences, hedges, road centers, etc. (A fruitful cause of disturbance of section and other corners is careless use of road graders, or the failure to lower the corner sufficiently below the surface of the road.)

PROBLEM F5. RESURVEY OF A SECTION.

(a) Equipment.-Transit party outfit, digging tools, etc.

(b) Problem.-Make a resurvey of an assigned section.

(c) Methods.—(1) Make extracts from the field notes of the original survey and of all resurveys on file at the court house, and other notes that may be of value. Make diligent inquiry among the property owners for evidence as to the location of corners. (2) Retrace the lines, recording the location of old fences, timber markings and other evidences as to prior recognition of lines and corners. Use consistent accuracy. Record the original notes as given in the forms. Record the field notes in narrative style using the designation of corners as given in the resurvey plat in the form. Make a plat of the section in the manner prescribed by state law for a resurvey.

PROBLEMS.

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	ESTIGA OLLECT	10N 0	FEVIC	DENCE		Surveyor, J. Doe. OF SEC. 8, T. 19 N., R. 9 E., 3 RD. P.M. Apr. 25, 1899. of Resurveys of Champaign County.
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	ning plat					running thence N. to p.155, showing exist-
	anument.					
	by the C					an excess of 40 lks.
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			p.157)			ing N-352 E; 188 1ks.
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	usey the					the NW. Cor. oF the 5W#
Begin	ning sur	vey at 5	W.Cor.3	<i>вс∙8</i> w.	here	of the 5W2, of Sec. 5.
						(Signed) Thos.B.Kyle
						Co-Surveyor.
						Surveyor, J. Doe.
(1NV		TION O		CODA	EPS A	F SEC.8, T.19 N., R.9 E., 3RD P.M.
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5,6,7,8	W.Oak		20	N-36°E.	230	DESCRIPTIONS OF "OBJECTS ON THE LINES" (P.75)
		Manad	20	11.30 E.	6.16	
7,8,17,18	POST IN	Mound		N-32"E.	44	
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8.9.16.17	{B.Waln		24		1	
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LAND SURVEYING.

\int				HeadChainn Rear #			
RESU CHAINS	RVEY OF SEC 27, TI2N, R-16 W., 3D.	₽₽	FOR	THE ESTA	TE OF JO	онн W. Sn	11TH ·
	Began at 7 · Found stake in place and both bearing trees standing · Planted stoDe 25"x 8"x 6"; marked + for cor-			IRVEY R			. ,
	Thence N on random, var. 230'E, setting temp stakes every 10 chs.			9	<u> </u>	-	Ť
80-22	Intersected sec. line 26 lks. W. of 5. At 5 Found rotten stake at correct point, 9-28°W, 66 lks. from stump of wh. oak,	16		8	a	F	//
	bearing tree of U-5-Survey · Drova stake for cor and put broken earthenware and glass around it			0		Ь	6
	Mkd. wh.oak,12"diam, N.66° E., 42 lks., also wh. oak 18" diam., N.34°W., 63 lks.	8					ľ
	From 5 ran E. on random, setting temp- stakes every 10 chs.	J5		<u>h</u>	. c	9	- 12
	Intersected sec. line 12 lks. N. of 2. At 2 found earthen post in correct position and bearing trees of resurvey standing.		4		7	/3	3
	Thence W. on corrected line.		•		•	10	-
	Set stake on true line · f on next page)						

(Resurvey. Sec.27, Smith	ESTATE	(CONTINUED)
CHAINS			
19.96	(Line 5-2 cont'd) At 10 set stake with		1
	stones around it and marked :		1
	pine, 12" diam., 11-46°W., 79 Iks.		
0000	red oak, 24" diam., 5:192°W, 72 1ks.		
29.94	Set stake on true line.		
	From 10 ran S. on random, var 2'19'E-		
1	and set temp stakes at 20 and 40 chs.		
	0.00 000 10.0p. 370 x c3 07 20 0.00 40 CM2-		
	Then went to 6. Found post and bearing		
	trees of resurvey standing.		(
	Ran thence W.on random, var. 2°20'E.		
20.02	Intersected random line From N- 6 Iks.		1
	5. of temp. stake.		1
40.18	Intersected random & line & lks. N. of		
00.00	temp. stake.		
80.04	Intersected sec. line 10 lks. 5. of 8.		1
1 1	Cor post dug out in road Set iron plaw beam for cor., 5-29°W., 76 Iks.,		
	From bearing tree of U.S. Survey.		
1 1	Thence E. on corrected line.		
	At intersection of quarter lines set		
	post		1
	•		
)

PROBLEM F6. RESURVEY OF A CITY BLOCK.

(a) Equipment.—Transit, 100-foot steel tape, chaining pins, axe, hubs, stakes, 4 pieces one-inch gas pipe 2 feet long, notes of previous surveys, etc.

(b) Problem.—Make a resurvey of an assigned city block.

(c) Methods.-(1) Procure full notes of all the surveys and resurveys of the assigned block from the records at the court house and from any other source available. (2) Make a resurvey of the block, using the notes, and drive hubs for temporary corners. (3) Compute the latitudes and departures of the courses, and if consistent balance the survey. (4) If the corners of the block as located are consistent with the existing property and street lines, drive gas pipes as permanent corners. (5) Subdivide the block into lots as shown in the notes. (6) Make a plat of the block on manila paper to the prescribed scale, showing block and lot lines, distances and angles obtained in making the survey, the names of the owners of the property and the names of the streets. Prepare a surveyors' certificate as provided by law. Trace the map if required. (The accuracy attained should be based on the valuation and other local conditions. Before beginning the survey use every possible care to find the corners with reference to which the original survey was made. When lots are sold by number, the excess or deficiency should be divided pro rata. However, when lot lines have been long acquiesced in, it is doubtful if the courts will uphold the surveyor in interfering with the ancient lines of ownership. It then becomes necessary either to make a compromise survey that will be satisfactory to the owners, or to make a survey that is strictly according to the letter of the law, and submit the map and certificate to the courts for settlement. The surveyor should remember that he is simply an expert witness and that he had no final judicial powers.)

PROBLEM F7. RESURVEY BY METES AND BOUNDS.

(a) Equipment.—Transit party outfit, digging tools, etc.

(b) Problem.—Make a resurvey of an assigned tract whose original survey was made by metes and bounds.

(c) Methods.—(1) Collect full notes and data relating to the monuments, magnetic bearings, magnetic variation, date of survey, lengths of lines, etc. (2) Make a careful investigation of the lines and corners on the ground and

make notes of any evidence there found. (3) Locate and identify with certainty as many as possible of the original monuments: where double or contested corners exist, locate each definitely for further reference; if corners are generally lacking or doubtful, concentrate attention on at least two which give most promise of definite relocation, and reestablish these corners as carefully as possible. (4) Having at least two corners, retrace by random line the perimeter of the tract, according to the original description, beginning at one and closing on the other corner; set temporary corner stakes at the several points: note the linear and angular error of closure of the random traverse on the last monument. (5) Calculate the latitudes and departures of the random survey, and determine the angular and linear relations between the random and the original survey; also fix the position of the several random stakes relative to the supposed true positions of the respective corners. (6) Set stakes in the true positions, as calculated, reference them out, and renew the search for the original monuments. (7) Finally reestablish each corner in the most consistent position, put permanent corners in place, and take witness notes for each, making complete notes of the proceedings. Follow the form.

PROBLEM F8. PARTITION OF LAND.

(a) Equipment.--Transit party and digging outfits, etc.

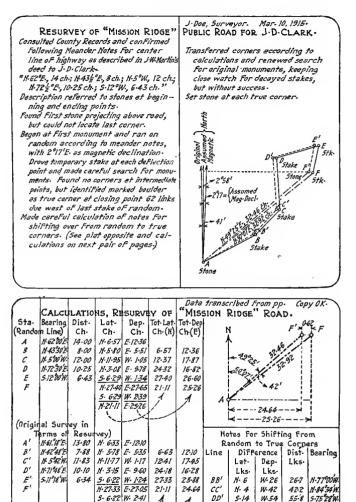
(b) *Problem.*—Make a partition of an assigned tract of land in accordance with instructions.

(c) Methods.—(1) Make the necessary resurveys of the assigned tract, identifying original monuments, and reestablishing lost corners as required. (2) Make a plat of the partition. (3) Subdivide the land and set permanent corners; carefully establish witnesses to the corners and secure witness notes. (4) Prepare and file plat and description as required by law.

PROBLEM F9. DESIGN AND SURVEY OF A TOWN SITE (OR ADDITION).

(a) Equipment.—Equipment for topographic survey for both field and office.

(b) *Problem.*—Make a preliminary topographic survey of the proposed town site (or addition), design the plat, and make the surveys for blocks, lots, etc.



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(c) Methods.-(1) Make a careful resurvey of the entire tract. Reference the existing monuments and carefully relocate all missing corners. (2) After the monuments have been carefully located, remeasure the distances and angles very carefully. Before beginning the chaining, a standard should be established as described in Problem A23. (3) Fill in the topographic details with the transit and stadia. unless directed otherwise, using consistent accuracy. (4) Make a complete topographic map of the tract. (5) Design the townsite and sketch it in on the map. The questions of surface drainage, sewerage, possible overflow, street gradients, principal thoroughfares, diagonal streets, alleys, etc., should be carefully considered. The streets should be of ample width, and be laid out with reference to ease of grading both the street and adjacent property. Residences should face desirable streets and the cross streets in the residence district should not be too numerous. The principal thoroughfare should pass through the business portion and have minimum gradients. The system of sewerage and drainage should he worked out roughly before the design is completed. Much expensive construction can be avoided by using care in designing the town site. (6) Make preliminary profiles of all the streets on Plate A profile paper to the prescribed scale. (7) Carefully locate the block and other important corners and mark them by permanent monuments of stone, gas pipe, tiling, etc. (8) Subdivide the blocks into lots and mark the lot corners by means of gas pipes or hubs. (9) After the streets have been located carefully, take levels on the same, make profiles. and lay grade lines for all streets, sidewalks, and improvements.

Use accuracy consistent with the value of the property throughout the problem. Make a careful record of the notes. Complete the maps and profiles.

CHAPTER VIII.

RAILROAD SURVEYING.

Classification.—For the purpose of class instruction, railroad surveying will be discussed under the following heads: (1) curve practice, (2) reconnaissance, (3) preliminary survey, (4) location survey, (5) construction, (6) maintenance.

Curve practice is designed to give the student familiarity with the methods of running curves so that the location survey may be made without needless delay. It consists of a series of typical problems covering the usual range of conditions found in such surveys.

The reconnaissance is a rapid preliminary examination of a district or area for the purpose of selecting ruling points to control the general routes of the preliminary survey lines. The distances are paced or scaled from a map; elevations are determined by means of the barometer or hand level.

The preliminary survey is designed to obtain information and to obtain it rapidly, as a guide in making the location survey. A rapid deflection angle traverse is rnn, following the general route of the proposed line, but keeping in clear ground as far as may be to gain time; levels are rnn, topography including contours taken, the map made, and one or more location lines projected on the map.

The location survey fixes the exact lines, including the curves, preparatory to building the proposed railroad. Some engineers prefer to run one or more trial location lines, but it is best practice to locate the line as projected on a reliable contour map.

Construction surveys are made for the purpose of fixing the roadbed limits and other constructive details, and estimating earthwork and other quantities.

Maintenance surveys and resurveys are made after the line is built, for ballasting, yard construction or other purpose. Field Organization of Class.—In order to carry out the foregoing steps, the following field parties are required: (a) transit party, (b) leveling party, (c) topography party, (d) land-line party, (e) cross-sectioning party, (f) bridge and masonry party, (g) resurvey party.

General Requirements.—Each party should work with snap and vigor and accomplish the best results practicable, both as to quality and quantity. To this end each member of the party should not only be careful, exact, and rapid in the discharge of his own duties, but avoid interfering with the work of others, such as obstructing the view of the transitman. In order to give each student practice in all the positions, the posts will be shifted daily, progressing to the higher positions in the party. The student should not underrate his practice in the subordinate positions, nor fail to make proper use of his more responsible duties. The usual decorum of field parties will be observed.

TRANSIT PARTY.—It is the duty of the transit party to establish the traverse line upon which to base the levels and topography. The student transit party will consist of the following members: (1) chief of party, (2) transitman, (3) head chainman, (4) rear chainman, (5) stakeman, (6) axeman, (7) front flagman, (8) rear flagman. The duties and equipment of the respective members are stated below.

Chief of Party.—(Party list, map of line, 50-foot metallic tape, railroad curve text book.) The chief of party is responsible for the general progress and quality of the work. It is his duty to direct the survey; see that each man does his work properly and with sufficient accuracy and despatch; check the transitman's work when necessary; keep the transit notes if the transitman is pushed; and make himself generally useful. He should be thoroughly acquainted, before going to the field, with the situation and with the data applicable to the work of the day. In requiring subordinate members of the party to perform their work properly, he should carefully preserve the dignity of his own position. Should there be no chief, these duties will be shared by the transitman and head chainman under the former's directions.

Transitman.—(Transit, reading glass, adjusting pin, transit note book, railroad curve text book, figuring pad.) The transitman runs the transit, keeps the notes, and in the absence of the chief, directs the work of the party. He should do careful and exact as well as rapid work, since the progress and character of the survey are usually controlled chiefly by the skill of the transitman.

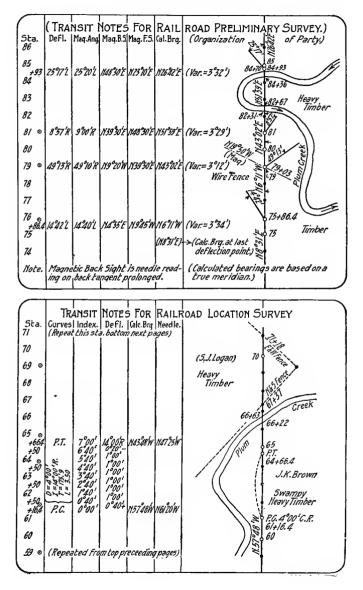
In leveling up, keep the lower parallel plate about level. Avoid undue tightness of foot screws. In setting the vernier to zero, use a quick converging motion with the tangent movement and note the adjacent graduations. If the transit has lost motion. learn which way to get the slack on the tangent screws. As a rule, use the lower motion by preference. Habitually back sight to the rear with telescope reversed, then plunge the telescope on prolongation and read the deflection right or left. If practicable, base the calculated bearings on a true meridian; otherwise. allow for the magnetic declination at a station which seems to be free from local attraction and thus obtain a reference meridian. Check all deflection angles by needle reading, both as to amount and direction. Lack of proper adjustment is no excuse for error. Always prolong a tangent line by double sightings. Also check deflection angles from time to time, by double sightings. Check on hack sight before finally approving any precise point; likewise never fail to conclude the observations at each transit station by checking on the back sight. In such check it is usually best to sight back precisely on the point and then note whether the vernier has the proper reading. Assist the flagman in plumhing the pole, and always sight as near the bottom of the pole as possible. The transitman should admonish the chainmen, etc., to keep clear of the line.

On preliminary surveys, usually let the rear chainman line in the head chainman by eye, at least for short stretches. Do not hesitate to offset or zig-zag more or less along open ground to gain time. A rapid method for passing through heavy timber is to zig-zag on slight deflection angles right and left, tabulate the lengths in stations and deflections in minutes, and the products of the two in separate columns on the right hand page. The original line is regained by making the algebraic sum of the products zero, and the original direction is resumed by turning off a deflection which balances the deflection angle columns.

On location, each stake should be lined in carefully by transit. Small obstructions, such as trees, may be passed by parallel lines, using offsets of one foot or so at two hubs a few stations apart; the line is resumed in like manner. Where plate readings are used in rectangular or other offset methods, no sights shorter than 50 feet should be used. The equilateral triangle one station or more on a side is often used. Obstructions on curves may usually be passed readily with the aid of tables of long chords and mid-ordinates.

Curve index-readings should be calculated as though the entire curve were to be run in from the P. C.; starting with the index-reading of P. C. always equal to zero. check the calculations by noting that the index of M. C. is 1/4 I, and of P. T. is 1/4 I. In using the notes, remember that with the transit at any point whatever on the curve, the following rules apply: (1) When pointing to any station, the vernier must always be set to read the index-reading for that station; and (2) when pointing on tangent at any station, the vernier must be set to read the index-reading for that station. As a rule, the hest program in curve location is: Having P. I. located, (1) measure I and assume D; (2) calcnlate T and E; (3) establish P. T. by chaining off T on front tangent; (4) establish M. C. by laving off E on hisecting line; (5) locate P. C. by interpolating hub at calculated station number on back tangent; (6) move transit to P. C. and foresight on P. I.; (7) calculate curve notes (if not already done); (8) check sight on P. T. and M. C. and if satisfactory; (9) run in curve, checking for distance and angle on M. C. and P. T., moving transit ahead if desirable or necessary; (10) set up at P. T. and resume front tangent. One minute is the limit of allowable error in any curve. Mistakes in calculations or in measurements of angles will be counted serious errors. On final location the curves will be spiraled. After the line is located, reference out P. C., P. T. and other important hub points by two intersecting lines and take careful notes of the same (see method (g), Fig. 5, Chapter II).

The transit notes should be reliable, complete, neat and distinct. Each entry should have but one reasonable meaning and that the correct one. Record station numbers from the hottom upwards, usually with ten stations per page. Repeat the last station at the bottom of the next page. Allow two lines per station so as to provide for sketching at 200 feet to the inch. On the middle line of the right hand page mark each station with a dot and number every fifth station which should also be enclosed in a circle. The transit notes should include sketches of prominent land and street lines, stream crossings and other prominent topographic details, with pluses shown in the sketch. The notes should include date, weather, organization of party. etc. An appropriate title page giving name of survey, date



of commencement and completion, etc., should be prepared. The notes will be kept in the prescribed form. The field notes are to be returned at the close of the day's work. All estimated data should be noted as such.

Completeness and neatness of notes and records, facility and accuracy in handling the instrument, and promptness in advancing the progress of the survey will count in the estimate of the work of the transitman.

Head Chainman.--(Flag pole.) The progress of the chaining depends chiefly on the activity of the head chainman. After setting a stake he should move off briskly (preferably at a trot) and be prepared for the "halt" signal as he approaches the next station. When the full chain length is pulled out, the head chainman turns, holding the flag pole in one hand and the chain handle in the other, and sets the pole in line hy signal from the rear chainman or transitman. Much time can be saved in this process if the head chainman habitually walks about on line and if he sights back over the two stakes last set. If on curve location, he should line himself in on the prolongation of the preceding station chord, and then offset by pacing or with flag pole a distance in feet equal to 134 times the degree of the curve; the calculation is made mentally and the pole can usually be set within a few inches of the correct position by the time a speedy transitman has the deflection angle set off. Having the line established, the pole is shifted to the correct distance, and the stake is driven plumb in the hole made by the flag pole spike. If the survey is a rapid preliminary line, the head chainman hastens ahead the instant the stake is started at the proper point, although in a more careful preliminary the chainmen check the distance to the driven stake. On location surveys it is customary for the chainmen to wait until the stake is driven and mark the exact distance on the top of the stake with the axe blade, and the exact line of signal from the transitman. In this process the head chainman should keen in mind the convenience of the transitman, and in case the line is being run to a front flag, the chainman should be careful to clear the line frequently to allow check sights ahead. In breaking chain on steep slopes the full length of chain should usually be pulled out ahead and the chain thumbed at the breaking points so as to avoid blunders; a plumb bob or flag pole should be used in the process. In passing over fences it often saves time to drive a 10-d nail. with "butterfly" attached, in the top plank to serve as a

check back sight from the next transit point. The chainmen should carefully avoid obstructing the transitman's view, to which end they should walk on the outside when locating curves.

Rear Chainman.—(100-foot chain or tape, chaining pins (if allowed), figuring pad or note book.) As the rear chainman approaches the stake just set, he calls out "halt" and holds the end of the chain approximately over the stake, quickly lines in the flag pole in the hand of the head chainman (or the pole is lined in by the transitman), the precise distance is given, and the chainmen move on briskly. As a rule, pluses should be read by the rear chainman, the front end being held at the point to be determined. Fractions will usually be taken to the nearest 0.1 foot, although 0.01 foot may at times be properly noted. It is the duty of the rear chainman to keep a record of pluses and topographic details when the transitman is not at hand. This record may be kept on a figuring pad and the memoranda handed at the first opportunity to the transitman, who transfers the data to his book and carefully preserves the slips for future reference. It is usually better, however, to keep the auxiliary notes in a memorandum book instead of on the loose slips. The chainmen should carefully avoid disturbing the transit legs.

The responsibility for correct numbering of the station stakes rests chiefly on the rear chainman. It is his duty to remember the number of the previous station so as to catch blunders on the part of the stakeman. As he reaches the stake just driven, he mentally verifies its number and repeats it distinctly for the guidance of the stakeman in marking the stake to be driven; the stakeman responds by calling the new number, and each repeats his number as a check before final approval. The rear chainman then charges his mind with the numbers and checks the newly set stake on reaching it. In case of doubt he returns to the preceding stake and notes its number.

Stakeman.—(Sack of flat and hub stakes, marking crayon, handaxe.) The stakeman with his supply of flat and hub stakes in a sack, should keep up with the head chainman and be standing, with stake and marking keel in hand, ready to number the new station stake on hearing the rear chainman call out the preceding station number; the numbering is repeated, as already explained, before the stake is driven. Chaining pins are not used, but their equivalent in checking tallies may be had by numbering the

stakes ahead and tieing them up in sets of ten. By numbering stakes at slack moments the stakeman gains time to assist the axeman in clearing the line, etc. However, special care should be taken to avoid omissions and duplicates. The stakeman should finish numbering the stake and hand it to the axeman by the time the head chainman has fixed the exact station point. The stakes should be numbered in a bold and legible manner, the keel being pressed into the wood for permanency. The number should read from the top of the stake downward. Stakes on an offsetted line should be so marked as 4'L or 2'R, beneath the station number. When survey lines are lettered, the serial letter should precede the station number. Guard stakes for P. I., P. C., P. T., reference points (R. P.), etc., should be clearly marked. The stakeman should assist the axeman in clearing the line and should drive stakes when the axeman is delayed. He should carefully avoid obstructing the transitman's view. The stakeman is under the direction of the head chainman.

Axeman.—(Axe, tacks, (and if so instructed) an extra sack of stakes with marking keel.) It is the duty of the axeman to drive stakes, remove underbrush from the line, clear an ample space about the transit station, etc. He is expressly warned, however, in student field practice, not to hack or cut trees or damage other property in any way, and in general, not to trespass on the rights of owners of premises entered in the progress of the survey.

The flat station stakes are driven firmly crosswise to the line with the numbered face to the rear. Hubs are driven about flush and usually receive a tack; they are properly witnessed by a flat guard stake driven 10 inches or so to the left, the marked face slanting towards the hub, as shown in Fig. 9. Chapter II. The axeman receives the marked stake from the stakeman and drives it plumb at the point marked by the spike of the flag pole. On location or careful preliminary surveys when the stakes are being lined in by transit, the axeman should stand on one side when driving and keep a lookout for signals from the transitman. In shifting the stake as signaled he should use combined driving and drawing blows with the axe. When the precise point comes much to one side of the top of the hub. another hub should be driven alongside and the first one driven out of sight before the tack is set. The axeman should move ahead briskly and avoid delay to the chaining. The stakeman should, when necessary, drive the stake with

the spare handaxe. When the field force is scant, one man may serve in both capacities. The axeman is under the direct charge of the head chainman.

Front Flagman.-(Flag pole, small supply of hubs and guard stakes in stake sack, handaxe, a few 10-d nails.) Τt is the duty of the front flagman to establish hub points ahead of the chaining party under the direction of the chief and transitman. In selecting transit stations he should keep in mind visibility and length of both fore sight and back sight, and to this end, points should be taken on ridge lines and where underbrush, etc., is least in the way. The practice of planting the flag pole behind the hub may be warranted occasionally, as for example, when the field party is shorthanded, but never when the regular flagman is not specially detailed for other duties. The front flagman should keep close watch on the transitman and should habitually stand with the spike of the flag pole on the tack head and plumh the pole by standing squarely behind it and supporting it between the tips of the fingers of the two hands. Should the front flagman be flagging for an interpolated point depending on a foresight which his pole would conceal, he should clear the line for a check sight by leaning the pole to one side. When crossing fences he should, when convenient, establish check sights on the top plank hy driving a spike and attaching a "butterfly"

Bear Flagman.—(Flag pole, hatchet, slips of paper.) The rear flagman gives back sight on the preceding transit station. The details of his duties are much the same as those of the front flagman. It is an excellent plan for him to cut a straight sapling or limb and plant it exactly behind the hub when signaled ahead. This picket pole is made more visible by splitting the top and inserting a slip of paper, to make a "butterfly." A series of such pickets on a long tangent line often affords a fine check on the work when an elevated transit point is reached.

LEVEL PARTY.—It is the purpose of the level party to secure data concerning the elevations of the points along the line so that an accurate profile may be made and the grade line established. The leveling party should be on the alert to detect errors in the work of the transit party, such as omitted or duplicated stations, etc. The party consists of two members: (1) leveler, (2) rodman. In very brushy country an axeman may be added, but this is usually unnecessary if the line cleared by the transit party is followed.

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Leveler.-(Level, adjusting pin, level note book.) The leveler should follow the most approved methods described under the head of differential and profile leveling in Chapter IV. The nearest 0.01 foot should be observed on turning points and bench mark rod readings and elevations and on occasional important profile points. The fore sight rod readings on ground profile points are to be taken only to the nearest 0.1 foot and the nearest 0.1 foot in the height of instrument is to be used in calculating the elevation. (Beginners sometimes calculate elevations to 0.01 foot when the rod readings are taken only to the nearest 0.1 foot.) The leveler should be rapid with his level as well as with figures. He should calculate elevations as fast as the rod readings are taken and should systematically check up the turning point and instrument heights as the work proceeds. As results are verified the same should be indicated by check marks. Each page of notes should be checked by summing up turning point back and fore sight rod readings, and comparing their difference with the difference between the first and last elevations or instrument heights, as the case may be, on the page. Follow the prescribed form. As far as

possible, bench marks should be checked by including them in the circuit as turning points. Balance back and fore sight distances on turning points. Permanent bench marks should be established at least every 1500 feet, and located in places at once convenient and free from disturbance during construction. Later levels should check within 0.05 foot into the square root of the length of circuit in miles. When a discrepancy is found, a line of check levels must be run to fix responsibility for the error. In crossing streams, secure high water elevations, with dates, especially of extraordinary floods, also low water level. In crossing highways obtain elevations each side for some distance with a view to avoid grade crossings. In going up or down steep slopes, gain all the vertical distance possible each setting, and follow a zig-zag course. The bottom of deep gullies may be determined by hand level. Assist the rodman in plumbing the rod, and on turning points and benches have the rod gently swung in a vertical plane to and from the instrument and take the minimum reading. The self-reading rod is to be preferred. Many levelers use the Philadelphia rod without target. If the target is used on turning points, the leveler should check the rod reading when practicable.

Completeness, correctness and neatness of notes and records, and facility and accuracy in handling the level will be given chief weight in fixing the merit of the leveler's work. The level notes are to be returned at the end of the day's work.

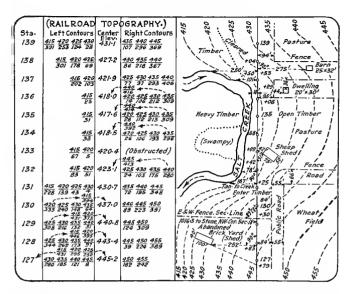
Bodman.—(Leveling rod, peg book, hatchet, turning point pegs, spikes, keel.) The rodman holds the rod at station stakes and at such plus points as may be required to make a representative profile. It is his duty to identify each station point and be on the lookont for duplicated or omitted stations. To this end he should habitually pace in each station, especially in grass or underbrush, and call out or signal the station number to the leveler. Should a blunder in station numbering appear, he should positively confirm the fact by retracing several stations, and then carry the corrected stationing ahead. The rod should be held truly plumb, which is hest done by standing squarely behind the rod and supporting it with the tips of the fingers of both hands. On turning points, the rod should be waved gently in a vertical plane to and from the instrument. The rodman should pay special attention to placing the target right for long rods and examine it to note if it has slipped before reading the rod. Errors of 1 foot, 0.1 foot, etc.. should be carefully guarded against. Turning points should be selected with special reference to their solidity, and care should be taken not to disturb them. Station pegs and hubs are often used for turning points; when so used, the precise fore sight to 0.01 foot should follow the usual ground rod reading to the nearest 0.1 foot. The rodman should use good judgment in selecting bench marks, locating them out of reach of probable disturbance during construction and describing them so as to be easily found. He should be active and do his best to keep close up with the transit party. The rodman should keep a peg book for recording turning points and instrument heights, and check his computations independently and compare results with the leveler.

TOPOGRAPHY PARTY.-It is the purpose of the topography party to secure full data for mapping contours. property lines, buildings, roads, streams, and other important topographic details. The width of territory to be embraced in the survey depends on local conditions; in places it may be as much as one-fourth or one-half mile from the line, although it is usually better to run alternate lines when the distance to be included becomes so great. The topography party often consists of only two men, but a party of four is much more efficient. Sometimes no regular topography party is provided, but after running a few miles of line ahead, the transit and level parties are formed into several parties to bring the topography up to the end of the preliminary line. For student practice the topography party will consist of four members: (1) topographer, (2) assistant topographer, (3) topography rodman. (4) tapeman.

Topographer.—(Topography board, topography sheet (or several sheets), hard pencil, compasses, eraser, etc.) The topography sheet should be prepared before going to the field, showing the alinement and other data needed from the transit notes, and elevations of all stations and pluses from the level notes. Cross-section paper is to be preferred. The center line may be plotted to one side of the center line of the sheet, when the topography is to be taken farther in one direction than the other. In order to secure full details, the scale of the field plat may well be double (or even more) that of the finished map. The topography sheet should show local conditions, such as gravel banks, rock ledges, etc., suitable for ballast or other constructive use; out-croppings of rock or other material which may

affect the classification of the graduation; character of substrata at sites of bridge or other masonry work; springs. wells, streams, etc., suitable for water supply: approximate flood levels and other data relating to waterways or surface drainage; location of streams, especially with reference to desirable crossings, freedom from probable change of channel, etc.; location of highways including elevations some distance either way with special reference to avoiding grade crossings; other railroad lines, with the same point in view: character and condition of crops and other farm improvements, names of owners, etc.,-in short, any and all information that is at all likely to be of service in mapping the route, projecting the location, during construction, etc. In locating a group of buildings some distance from the line, fix the principal one by tie lines, by intersection or polar coordinates, and the others by measurement and sketch from it. Locate buildings near the line by rectangular offsets, or by intersections of the principal outlines with the survey line. Contours are located by means of the hand level used by the assistant topographer. The contour interval should be five feet ordinarily, but may be increased to ten or more feet on very steep slopes. The contonr data should be selected with special reference to ridge and gully lines (see problem and plat on contour leveling, Chapter IV). Ordinarily hand level lines may be run out at right angles; angling lines along gulches and ridges may be located by estimation, pocket compass or tie lines. The plat is made by the topographer from data collected by the other members of the party. A common fault with the beginner in such work is the omission from the plat of important numerical data, such as station numbers of landline crossings, etc., owing to an undue attention to the minute details of the drafting work. A good topography record with contour notes on the left hand page and field sketch showing all numerical data on the right, is shown in the accompanying form.

Assistant Topographer.—(Hand level, pocket compass, topography note book.) It is the duty of the assistant topographer to collect data for the use of the topographer in making the plat. He uses the hand level, notes station numbers, distances, bearings, etc., and makes such record of the same as may be required to fit local conditions. In contouring, a special rod with adjustable base (see Fig. 19, Chapter IV.), if available, may be used; otherwise, an ordinary flag pole with alternate feet red and white is em-



ployed. Beginning with the known profile elevation, as extracted from the leveler's record, even five-foot contours are located, as a rule, nominally every 200 to 500 feet at right angles to the line, except as ruling ridges or gullies may suggest other directions. His record should be ample and legible, and include data and information which may not properly be placed on the plat. All estimated elevations, distances or dimensions should be noted as such. The assistant topographer works under the direction of the topographer, but is expected to take the initiative in the collection of data so as to permit his superior to devote proper attention to the field plat.

Topography Rodman.—(Topography rod with adjustable base (see (f), Fig. 19, Chapter IV.) or flag pole, hatchet.) It is the duty of the rodman to hold the topography rod as directed by the assistant topographer. He should be active and continually on the alert for information or data which the record book or sheet should contain. The rodman holds the zero end of the tape in measuring the distances. He should acquire skill in pacing on rough as well as smooth ground, and when sufficiently exact especially on ground remote from the surveyed line, he should gain time by pacing in the distances to contour lines.

Tapeman.—(Metallic (or band) tape, set of chaining pins, flag pole.) It is the duty of the tapeman to detcrmine distances with the help of the rodman. He should be vigilant in checking up tallies, reading fractions, leveling the tape, breaking chain, plumbing down ends, etc., and should never be the cause of needless delay in the work. When required, he should measure angles, take tie lines, etc., with the tape.

OFFICE WORK.—The office work of each student includes: (1) reconnaissance map, profile and report; (2) map showing preliminary lines with topography and projected location lines; (3) preliminary profile with grade lines, approximate estimate of quantities, etc.; (4) final location map (traced from preliminary map); (5) location profile; (6) copies of field notes; (7) cross-section notes and estimate of graduation quantities; (8) estimate of cost of constrution; (9) monthly estimates, progress profile, haul, prismoidal and curvature corrections, vouchers, etc., final estimate.

Reconnaissance Report.—The reconnaissance map showing the area examined will be based upon such maps of the route as may be available. It should show the several ruling points and general routes selected for actual survey. The profile should be based upon barometric or hand level observations and distances scaled from the map or determined roughly by pacing or otherwise on the ground. The report should refer to the map and profile and state the general scheme, the several ruling considerations or conditions, the details of the examination, a rough comparison of the several alternative routes, and a final summary and conclusion with definite recommendations. The report should be made in accordance with best usage as to form, composition, etc.

(Considering the limited point of view of the beginner, the reconnaissance reports may not be required until the actual surveys are well along. In such case, however, the student is not to draw data from sources other than those above outlined.)

Preliminary Map.—The mapping should be the best product of the student's skill as a draftsman, and should conform closely to the department standards, which are based upon best current usage of leading American railroads. Unless otherwise instructed, the preliminary map

RAILROAD SURVEYING.

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$\begin{array}{c c c c c c c c c c c c c c c c c c c $	From Sta. Tangen 26 43+55£ 6/+681 93+65	To Sta. <i>† Main</i> <i>26</i> <i>43+556</i> <i>61+68-1</i> <i>93+65</i> <i>102+512</i>	Length Tang'ts Ft. <i>Track</i> , <i>1755-6</i> 3196-9	Length Curve Ft. 1.8.&C. 100.0 2500.0 1812.5	Angle I <i>R.R.</i> <i>1'30'R.</i> 25'W'R. 36'15'R.	Degree D. <i>730'</i> <i>1°00'</i> <i>2°00'</i>	Radius R· Ft. <i>764.1</i> <i>5730.0</i> <i>2865.0</i>	Tan Die T Ft <i>50.</i> <i>1270</i> . 937.2	t Dist. Pl·toRI. Ft. 3963.7 4580.1	Calc- Bearing 5-3515F. (5-2745E. 5-245F. 5-3330W.	{Lat. Dep. Ft. P.I.= S. F. P.I.= S. P.I.= S. P.I.= S. F. P.I.=	Jot. D Ft. 66. Ft. 1000/140	Procession (manne
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	From Sta. <i>Tangen</i> <i>Q</i> <i>1</i> <i>26</i> <i>43:</i> 55 <i>8</i> <i>61:</i> 4681 <i>93:</i> 465 <i>102:</i> 4512	To Sta. <i>t Main</i> 26 43+556 61+68-1 93+65 102+512 143+90	Length Tang'ts Ft. <i>Track</i> , <i>1755-6</i> 3196-9	Length Curve Ft. 1.B.&C. 100.0 2500.0 1812.5 886.7	Angle I <i>1*30'R.</i> 25*0'R. 36°15'R. 13°18'L-	Degree D. <i>1°30'</i> <i>1°00'</i> <i>2°00'</i> <i>1°30'</i>	Radius R. Ft. <i>764.1</i> <i>5730.0</i> <i>2865.0</i> <i>3820.0</i>	Tan-Die T Ft- <i>50.</i> <i>1270</i> . <i>937.2</i> <i>445.</i>	t Dist. Pl·toRl. Ft. <i>1320.4</i> <i>3963.7</i> <i>4580.1</i> <i>5185.7</i>	Calc- Bearing 5-3515F. (5-2745E. 5-245F. 5-3330W.	$\begin{cases} Lat. \\ Dep. \\ Ft. \\ P.J. = \\ 5. \\ 5. \\ 5. \\ 5. \\ 5. \\ 7. \\ 7. \\ 7.$	Filled Frident	Procession (manne
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	From Sta. <i>Tangen</i> <i>0</i> <i>1</i> <i>26</i> <i>43+55£</i> <i>61+681</i> <i>93+65</i> <i>102+512</i> <i>143+90</i>	To Sta. <i>t</i> <u>Main</u> <u>76</u> 43+556 61+68-1 93+65 102+512 143+90 155+562	Length Tang'ts Ft. <i>Track, -</i> <i>1755-6</i> <i>3196-9</i> <i>4138-3</i>	Length Curve Ft. 1.B.&C. 100.0 2500.0 1812.5 886.7	Angle I <i>1*30'R.</i> 25*0'R. 36°15'R. 13°18'L-	Degree D. <i>1°30'</i> <i>1°00'</i> <i>2°00'</i> <i>1°30'</i>	Radius R. Ft. <i>764.1</i> <i>5730.0</i> <i>2865.0</i> <i>3820.0</i>	Tan-Die T Ft- <i>50.</i> <i>1270</i> . <i>937.2</i> <i>445.</i>	t Dist. P.I. toRI. Ft. <i>J 320.4</i> <i>3963.7</i> <i>4580.1</i> <i>5185.7</i>	Calc. Beering 5.3515/F. (5.2745/E. 5.245/E. 5.3330/W. 5.2012/W.	$\begin{cases} Lat. \\ Dep. \\ Ft. \\ P.J. = \\ S. \\ S. \\ S. \\ S. \\ S. \\ P.J. = \\ S. \\ P.J. = \\ S. \\ W. \\ P.J. = \\ M. \\ P.J. = \\ M. \\$	Filled Frident	each states (110-100 - 19
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	From Sta. 7angen 0 1 26 43+556 61+681 93+65 102+512 143+90 155+762	To Sta. <i>f</i> Main 26 43+556 61+68-1 93+655 102+512 143+90 155+621 170+43	Length Tang'ts Ft. <i>Track, -</i> <i>1755-6</i> <i>3196-9</i> <i>4138-3</i>	Length Curve Ft. 1.B.&C. 100.0 2500.0 1812-5 886-7 1186-7	Angle I <i>R.R.</i> <i>130/R.</i> 25%/R. 36°15′R. 13°18′L- 23%4′L	Degree D. <i>1°30'</i> <i>1°00'</i> <i>2°00'</i> <i>1°30'</i> <i>2°00'</i>	Redius R: Ft. 764.1 5730.0 2865.0 3820.0 2865.0	Tan Dia T Ft. 50. 1270. 937. 445. 602.0	t Dist. Pl. toRI- Ft. 33963.7 4580.1 5185.7 2618.3	Calc. Beering 5.3515/F. (5.2745/E. 5.245/E. 5.3330/W. 5.2012/W.	$\begin{cases} Lat. \\ Dep. \\ Ft. \\ P. \\ S. \\ S. \\ S. \\ S. \\ S. \\ S. \\ S$	to be filled This 99.4 00	each states (110-100 - 19
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	From Sta. 720900 726 43+556 61+681 93+65 102+512 143+90 155+762 170+43	To Sta. <i>f</i> Main 26 43+556 61+68-1 93+655 102+512 143+90 155+62 170+43 181+292	Length Tang'ts Ft. <i>Track</i> , <i>1755-6</i> <i>3196-9</i> <i>4138-3</i> <i>1466-3</i>	Length Curve Ft. 1.B.&C. 100.0 2500.0 1812-5 886-7 1186-7	Angle I <i>R.R.</i> <i>130/R.</i> 25%/R. 36°15′R. 13°18′L- 23%4′L	Degree D. <i>1°30'</i> <i>1°00'</i> <i>2°00'</i> <i>1°30'</i> <i>2°00'</i>	Redius R: Ft. 764.1 5730.0 2865.0 3820.0 2865.0	Tan Dia T Ft. 50. 1270. 937. 445. 602.0	t Dist. Pl. toPl. Ft. 3963.7 4580.1 51857 2618.3	Calc. Beering 5:35'15'F. (5:27'45'E 5:2845'E 5:3330'M 5:20'12'M 5:33'32'F. 5:33'32'F.	$\begin{cases} Lat. \\ Dep. \\ Ft. \\ F. \\ S. \\ S. \\ S. \\ S. \\ S. \\ S. \\ S$	to be filled This 99.4 00	a construction 000 m
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	From Sta. 720,000 43,455.8 61,468.1 93,465.2 102,451.2 170,433 181,429.2 181,429.2	To Sta. <i>t</i> <u>Main</u> <u>76</u> 43+55 <u>6</u> 61+68 <u>1</u> 93+65 <u>1</u> 143+990 155 <u>+</u> 76 <u>1</u> 170+43 181+291 184+590	Length Tang'ts Ft. <i>Track</i> , <i>1755-6</i> <i>3196-9</i> <i>4138-3</i> <i>1466-3</i>	Length Curve Ft: <i>1.B.&C-</i> <i>100-0</i> <i>2\$00-0</i> <i>1812-5</i> <i>886-7</i> <i>1186-7</i> <i>1086-7</i>	Angle I 1'30'k. 25'0'k. 36'15'k. 13'18'L- 23'44'L 21'44'k.	Degree D. 1°30' 1°00' 2°00' 2°00' 2°00'	Redius R: Ft. <i>764.1</i> <i>5730.0</i> <i>2865.0</i> <i>2865.0</i> <i>2865.0</i> <i>2865.0</i>	Tan-Die T Ft- 50. 1270- 937-2 445-4 602-0 550-0	t Dist. Pl. toRI. Ft. <i>1320.4</i> <i>3963.7</i> <i>4580.1</i> <i>5185.7</i> <i>2618.3</i> <i>1307.3</i>	Calc. Beering 5:35'15'F. (5:27'45'E 5:2845'E 5:3330'M 5:20'12'M 5:33'32'F. 5:33'32'F.	$\begin{cases} Lat. \\ Dep. \\ Ft. \\ Ft. \\ F. \\ F. \\ F. \\ F. \\ F. \\$	to be filled This 99.4 00	a construction 000 m
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	From Sta. <i>Tangen</i> <i>Q</i> <i>43+25.8.</i> <i>61+68.1.</i> <i>93+65.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i> <i>102+51.2.</i>	To Sta. <i>t</i> Main <i>Z</i> 6 43+556 61+68- 93+65 102+552 183+65 155+762 170+43 181+292 184+506 193+195	Length Tang'ts Ft. 1755-6 3196-9 4138-3 1466-3 320-9	Length Curve Ft: <i>1.B.&C-</i> <i>100-0</i> <i>2\$00-0</i> <i>1812-5</i> <i>886-7</i> <i>1186-7</i> <i>1086-7</i>	Angle I 1'30'k. 25'0'k. 36'15'k. 13'18'L- 23'44'L 21'44'k.	Degree D. 1°30' 1°00' 2°00' 2°00' 2°00'	Redius R: Ft. <i>764.1</i> <i>5730.0</i> <i>2865.0</i> <i>2865.0</i> <i>2865.0</i> <i>2865.0</i>	Tan-Die T Ft- 50. 1270- 937-2 445-4 602-0 550-0	t Dist. Pl. toRI. Ft. <i>33963.7</i> <i>4580.1</i> <i>5185.7</i> <i>2618.3</i> <i>1307.3</i>	Calc. Bearing 5-35°15'F. (52745'E 5-2°45'E 5-33'30'W 5-20°12'W 5-3°32'F. 5-38°12'W	$\begin{cases} Lat: \\ Dep. \\ Ft & \\ P.I = \\ S. \\ $	to be filled This 99.4 00	a construction 000 m
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	From Sta. <i>Tangen</i> <i>Q</i> <i>154</i> <i>134558</i> <i>614681</i> <i>93465</i> <i>1024512</i> <i>1024512</i> <i>1707451</i> <i>184595</i> <i>184595</i> <i>184595</i> <i>184595</i>	To Sta. <i>f</i> Main <i>I</i> <i>G</i> <i>43+555 (02+5)1</i> <i>143+90</i> <i>155+761</i> <i>170+433</i> <i>181+506</i> <i>193+195</i> <i>193+195</i> <i>193+195</i> <i>215-66</i>	Length Tang'ts Ft. 1755-6 3196-9 4138-3 1466-3 320-9	Length Curve Ft- 1.B.&C. 1000 25000 1812-5 886-7 1186-7 1086-7 868-9	Angle I 130k 2500k 36°15 k 13°18'1- 2344'1 21'44'k 13°02'k	Degree D. 7°30' 1°00' 2°00' 2°00' 2°00' 1°30'	Redius R· Ft. 57300 28650 38200 28650 28650 38200	Ten Die T Ft. 50. 1270. 937. 445. 602.0 550.0 436.4	t Dist. Pl. toRL Ft. <i>1320.4</i> <i>3963.7</i> <i>4580.1</i> <i>5185.7</i> <i>2618.3</i> <i>1307.3</i> <i>2816.9</i>	Calc. Bearing 5-35°15'F. (52745'E 5-2°45'E 5-33'30'W 5-20°12'W 5-3°32'F. 5-38°12'W	$\begin{cases} Lat: \\ Dep. \\ Ft: \\ F: \\ F: \\ F: \\ F: \\ F: \\ F: \\ F$	nums are to be filled into 20 1 4	ciervas es escu suscerit 000 m
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	From Sta. <i>Tangen</i> <i>25</i> <i>43</i> <i>43</i> <i>43</i> <i>45</i> <i>55</i> <i>16</i> <i>155</i> <i>16</i> <i>155</i> <i>16</i> <i>170</i> <i>43</i> <i>195</i> <i>18</i> <i>195</i> <i>195</i> <i>18</i> <i>45</i> <i>293</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i> <i>195</i>	To Sta. <i>t</i> Main 26 43+556 61+68-1 93+65-2 143+90 143+90 155+76-1 170+43 181+291 184+506 193+195+196 195+196+196 195+196+196 195+196+196+196 195+196+196+196+196+196+1	Length Tang'ts Ft. 17556 3196.9 4138-3 1466-3 320-9 1986-9	Length Curve Ft- 1.B.&C. 1000 25000 1812-5 886-7 1186-7 1086-7 868-9	Angle I 130k 2500k 36°15 k 13°18'1- 2344'1 21'44'k 13°02'k	Degree D. 7°30' 1°00' 2°00' 2°00' 2°00' 1°30'	Redius R· Ft. 57300 28650 38200 28650 28650 38200	Ten Die T Ft. 50. 1270. 937. 445. 602.0 550.0 436.4	t Dist. Pl. toRL Ft. <i>1320.4</i> <i>3963.7</i> <i>4580.1</i> <i>5185.7</i> <i>2618.3</i> <i>1307.3</i> <i>1307.3</i> <i>1307.3</i>	Calc. Beering 5-35%55 5-27455 5-24555 5-3336/41 5-3072'41 5-3872'41 5-31872'41	$\begin{cases} Lat: \\ Dep. \\ Ft: \\ P. \\ F: \\ S: \\ S: \\ S: \\ S: \\ S: \\ S: \\ S:$	colums are to be filled invite 1	ciervas es escu suscerit 000 m
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Check 25752-7 $\overline{39}^{\circ}SVR\left[(st,T+iast,T) = \frac{1+319}{1040248}\right]$ check totals $\overline{536'15'E}$ Trangents VR in 5th by Σ	From Sta. 790 gen 20 43 4556 61 + 681 93 + 65 107 + 512 135 + 62 135 + 62 1	To Sta. <i>t</i> Main <i>Z</i> 6 43+556 61+68-1 93*65-1 102*57-62 102*57-62 102*57-62 102*57-62 102*57-62 103+198 235-698 235-698 235-698 235-698 235-698 235-698 235-698 235-698 235-698	Length Tang'ts Ft. 1755-6 3196-9 4138-3 1466-3 320-9 1986-9 963-8 986-0	Length Curve Ft. 18.7C-5 2500-0 1812-5 886-7 1186-7 1086-7 868-9 784-4 1195-0 <u>517-1</u>	Angle I 130k. 250k. 36°15'k. 13°18'1- 23\$44'1 21\$44'k 13°02'k. 11\$46'1- 23\$4'k. 38\$47'1-	Degree D. 7'30' 1'00' 2'00' 1'30' 2'00' 1'30' 1'30' 1'30' 1'30' 7'30'	Radius R. Ft. 764.1 5730-0 2865-0 3820-0 3820-0 3820-0 3820-0 2865-0 764.1	Ten. Di. T T Ft. 50. 1270. 237. 445. 602.0 550.0 436.4 393.6 606.4 268.5 556.0	 b) Dist. p) to RI. p) to	Calc. Beering 5-35/5/F. (5-2745/E) 5-28/5/F. 5-33/30/12 5-30/2/W. 5-38/2/W. 5-38/26/W. 5-43/22/W.	$\begin{cases} \text{Lat:} \\ \text{Dep.} \\ \text{Ft.} \\ \text{S.E.} \\ S$	(Last two colume are to be filled in the second checked by early ethology 25 4	In all merver by each states () 000 a
$\frac{535'/5'E}{2} \sum Tangents = \frac{10802'8}{148/4.7} \qquad in 5th \qquad by \Sigma$	From Sta. 790 gen 20 43 4556 61 + 681 93 + 65 107 + 512 135 + 62 135 + 62 1	To Sta. <i>t</i> Main <i>Z</i> 6 43+556 61+68-1 93*65-1 102*57-62 102*57-62 102*57-62 102*57-62 102*57-62 103+198 235-698 235-698 235-698 235-698 235-698 235-698 235-698 235-698 235-698	Length Tangts Ft. <i>1755-6</i> <i>3196-9</i> <i>4138-3</i> <i>1466-3</i> <i>320-9</i> <i>1986-9</i> <i>963-8</i> <i>986-0</i> <u>14814-7</u>	Length Curve Ft. 18.2.700 25000 1812-5 88607 1186-7 1086-7 868-9 784-4 1195-0 <u>517-1</u> 10938-0	Angle I 730k 250k 36°15'k 13°18'1- 23\$44'1 21\$44'k 13°02'k 11\$46'1- 23\$4'k 38 <u>\$47'1-</u> 17 <u>255 k</u>	Degree D. 1°30' 1°30' 1°30' 2°00' 1°30' 1°30' 1°30' 1°30' 1°30' 7°30' 7°30' 7°30'	Radius R. Ft. 57300 28650 28650 28650 28650 38200 38200 38200 28650 764.1 pin Trk-	Ten. Dī: T Ft. 50. 1270. 237. 445. 445. 445. 436. 436. 436. 436. 436. 436. 436. 436	+ Dist. Pl-toRL Ft. 1320.4 3963.7 4580.1 51857 2618-3 1307.3 1307.3 1307.3 1307.3 1307.3 1307.3 1363.8 1963.8 1963.8 1964.3	Calc- Beering 5-35%5/5 (5-2745/5) 5-245/5 5-3330/44 5-3330/44 5-3372/5 5-372/5 5-372/5 5-372/5 5-3374/44 5-3372/44 5-4357/44	$\begin{cases} \text{Lat:} \\ \text{Dep.} \\ \text{Ft.} \\ \text{S.E.} \\ S$	(1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	A main merer of each street in the
chul c eratu E Tangents = 14814-7	From Sta. 720 20 12 13 13 15 15 15 15 15 15 15 15 15 15 15 15 15	To Sta. 7 26 43 43 64 64 64 64 64 64 64 64 64 64 64 64 64	Length Tangts Ft. 779Ck, 1755-6 3196-9 4138-3 1466-3 320-9 1986-9 963-8 986-0 14814-7 70495-0	Length Curve Ft. 18.2.700 25000 1812-5 88607 118607 108607 86809 78404 119500 517-1 10938-0	Angle I <i>R.R.</i> <i>130'R.</i> <i>25'0'R.</i> <i>36'15'R.</i> <i>13'18'L-</i> <i>23'84'L</i> <i>23'84'L</i> <i>23'84'L</i> <i>13'02'R.</i> <i>13'02'R.</i> <i>13'02'R.</i> <i>38'97'L.</i> <i>23'35'L</i>	Degree D. 7'30' 1'00' 2'00' 2'00' 1'30' 1'30' 1'30' 1'30' 7'30' 7'30' 7'30' 7'30' 7'30' 7'30'	Radius R. Ft. 764.1 5730.0 2865.0 2865.0 2865.0 2865.0 3820.0	Ten. Di. T Ft. 50. 1270. 937. 445. 602.0 550. 436. 393.6 606. 2560. 2560. 2560. 2550. 1270. 550. 1270. 550. 1270.	+ Dist. Pl-toRL Ft. 13204 33963.7 4580.1 51857 2618.3 7 2618.3 7 1307.3 7816.9 1963.8 1861.3 25617.5	Calc. Beering 5-35%5/2 (5-2745/2) 5-245/2 5-3390/2 5-3390/2 5-397/2 5-397/2 5-397/2 5-397/2 5-43572/2 5-43572/2 (5ee	$\begin{cases} \text{Lat:} \\ \text{Dep.} \\ \text{Ft.} \\ \text{S.E.} \\ S$	test (Last two colums are to be filled in the internation of the second to each strutent 95 + 4	A no circan a carrent a contraint and a
Check 25617-5	From Sta. 720 20 12 13 13 15 15 15 15 15 15 15 15 15 15 15 15 15	To Sta. 7 26 43 43 64 64 64 64 64 64 64 64 64 64 64 64 64	Length Tangts Ft. 779Ck, 1755-6 3196-9 4138-3 1466-3 320-9 1986-9 963-8 986-0 14814-7 70495-0	Length Curve Ft. 18.2.700 25000 1812-5 88607 118607 108607 86809 78404 119500 517-1 10938-0	Angle I <i>R.R.</i> <i>150k.</i> 2500 & 36°15 & 13°18'L- 23%4'L 21%4'& 13°02'& 11°46'L- 23%4'& <u>38°47'L.</u> <u>177255' 87°35'</u> & <u>39°50'</u> &	Degree D. 1°30' 2°00' 1°30' 2°00' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30' 1°30'	Radius R. Ft. 5730-0 2865-0 3820-0 2865-0 3820-0 3820-0 3820-0 2865-0 3820-0 2865-0 3820-0 2865-0 38200-0 38200-0 38000000000	Ten. Di: T Ft. 50: 1270- 937-2 445-4 602-0 550-0 436-4 393-6 606-4 268-9 5560-0 268-9 71727-8 5560-1 208-9 71727-8 71727-9 71727-8 71727-9 7172	t Dist. Pi-toRi- Ft. 1 320.4 3 3963.7 4 580.1 5 185-7 7 2618.3 1 307.3 1 307.3 1 307.3 1 36.9 1 46.9 1 46	Calc. Beering 5:35/5/5 (5:27356) 5:23/5/5 5:33/5/6 5:33/5/6 5:33/2/6 5:33/2/6 5:31/4/6 5:31/2/6 5:43/22/6 5:43/5/6 (5ee Check	$\begin{cases} \text{Lat:} \\ \text{Dep.} \\ \text{Ft.} \\ \text{S.E.} \\ S$	to terry (Last two columns are to be filled in a 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	א א ווו בווה הובראבה הא בפרוו בוחרפווה סייי ש
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will be made on eggshell or paragon paper. There are three ways to plot the skeleton of the preliminary survey: (1) by laying off each successive deflection angle and distance from the preceding line; (2) by laying off the successive calculated courses and distances from a precisely drawn meridian or other reference line; and (3) by rectangular coordinates. The first method should not be used. since cumulative errors are probable. The second is rapid and free from serious objection; if preferred, a modified base line may be assumed and the calculated bearings transferred to the same; the angles may be laid off by means of scale and table of natural trigonometric functions from a precisely drawn base line and then transferred, as required, by parallel ruler or triangle; this method is used most in practice. The third method is the most exact, and will be used by the student unless the second is specified. It involves the calculation of a plotting sheet, as shown in the accompanying form. The axis is usually a meridian line, but any line may be taken and the courses changed to suit. In making the plotting table, the data, calculated bearings, distances, etc., should be carefully checked through to the last point in the skeleton before the plotting is begun. Only one axis should be plotted, preferably the one having greater totals, so as to give short perpendiculars. Starting from the origin, 1000-foot points are pricked in along the axis to the specified scale, and marked 0. 10. 20. etc.: the totals are interpolated on the axis and lettered; exact perpendiculars about the right length are erected; the second point is established by scaling the perpendicular and the line is checked back on the preceding point; if correct, the stations are pricked in and every fifth station and deflection points are enclosed in a small circle and neatly numbered : the next course is so located and checked back by length of hypothenuse, the stations fixed and numbered, and so on to the end of the line; the courses should be taken in their order and none passed without checking satisfactorily. After the skeleton is completed, the topographic details are penciled in, and the map finished and inked. The title, border, meridian (both true and magnetic), etc., should be first-class in quality and in keeping with the rest of the map. Crude or careless lettering or other details of the map will cause its rejection. The title of the map, profile, etc., should be given in brief on the outside of the sheet or roll at each end.

Preliminary Profile.-Use Plate A profile paper in making the profiles. The level notes should first be carefully verified and then one person should read off while another plots the data. A hard pencil, 6H or 7H, sharpened to a long needle point should be used. The stations are first numbered along the bottom from left to right (or the reverse, as prescribed); leaving six inches or so at the left for a title, and beginning at a prominent line with station 0. every tenth station is so numbered. The notes are examined for lowest and highest elevation and a prominent line is assumed as an even 50 or 100-foot value relative to the The horizontal scale is 400 feet and the vertical datum. scale 20 feet to the inch. Points should be plotted no heavier than necessary, since the surface of profile paper will not permit much erasing. The surface line should be traced in close up to the plotted points, owing to the danger of overlooking abrupt breaks such as streams, ditches, etc. Pluses should be fixed by estimation. The surface line when completed should be inked with a ruling pen used freehand; the weight of the line should be about the average of the ruled lines on the profile paper. (A special profiling or contouring pen is much used for this purpose.) The profile should show the grade line, grade intersection, elevations and rates of grade in red; water levels, and data relative to same in hlue; surface line, station numerals, etc., in black; the alinement, important landlines, streams, etc., should be shown at the bottom of the profile in black. The grade line should be laid nominally with a view to balance the cut and fill quantities, but this should be varied to suit local conditions, such as drainage, the elimination of grade crossings, classification of materials, etc. The maximum gradients, the rate of compensation for curvature, etc., will be made to suit the specified The compensation for curvature will be alconditions. lowed for on the preliminary profile by dropping the grade line on maximum gradients at each deflection point. Grade intersection elevations and rates of grade will be given to the nearest 0.01 foot.

Approximate Estimates.—Rapid estimates of earthwork quantities may be made direct from the profile either by reference to a table of level sections, or preferably by means of an earthwork scale. Estimates made in this way from the profile of a careful preliminary survey, often do not vary more than five per cent from the final construction quantities. Location Map.—The location map may be traced from the preliminary map and should include the topography and such details as usually appear in the final record map of the located line. Contour lines may be traced in cadmium yellow to insure satisfactory blue printing.

Location Profile.—The location profile should be executed according to the standard specimen, and should include estimates of earthwork as determined from the actual cross-section notes, and quantities of other construction materials. Curvature compensation will be shown ou the location profile by reduced maximum gradients. Vertical curves will be calculated at a rate of change not to exceed 0.05 foot per station, except at summits where it may be 0.10 foot or more per station. It should be prepared as the final record profile. Approximate profiles of projected lines, determined from the contour map, with rough estimates of quantities will also be prepared, as specified.

Office Copies of Notes.—The complete level and transit notes, and topography notes as assigned, must be copied in the individual books by each student. These copies will be in pencil (or ink if so specified) and will be executed in a faithful and draftsmanlike manner according to the department standards of lettering, etc.

Estimates of Quantities.—The cross-section notes will be copied and the quantities of excavation and embankment calculated, as assigned. The cross-sectional areas will be calculated arithmetically and checked, especially on rough ground, by means of planimeter. The quantities will be calculated by average end areas, by tables, and by diagrams, so as to afford ample practice for the student in all the current methods. The estimate will also include all the other materials of construction.

Estimate of Cost.—Each student will make a detailed summary of the quantities, fix prices, and estimate the probable total cost of the work, or of the assigned section. The prescribed form will be followed. The prices should be based on local conditions as far as possible.

Construction Estimates.—Monthly estimates, estimates of haul, borrow pit estimates, classification, prismoidal and curvature corrections, progress profile, vouchers, force account, etc., and final estimate will be prepared by each student in accordance with prescribed forms and standards.

Right of Way Records.—Each student will be assigned a share of work in the preparation of right of way deeds and record maps. The following forms (from the "Engineering Rules and Instructions," Northern Pacific R. R.) will be used as models in preparing right of way descriptions.

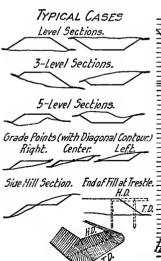
(Through government subdivisions): "A strip, piece or parcel of land one hundred feet in width, situated in the northwest quarter of the northwest quarter of section ten, in township two north, range one west (S. 10, T. 2 N., R. 1 W.), Madison county, Montana, and having for its boundaries two lines that are parallel with and equidistant from the center line of the railroad of the ———— Railway Company, as the same is now located (and constructed). For a more particular description, reference may be had to the plat drawn upon and made a part of this deed."

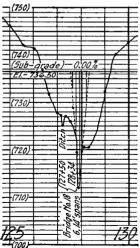
(Lots in platted tracts): "Lot seven (7), block six (6), in Smith's addition to Helena, Lewis and Clark county, Montana, according to the recorded plat thereof."

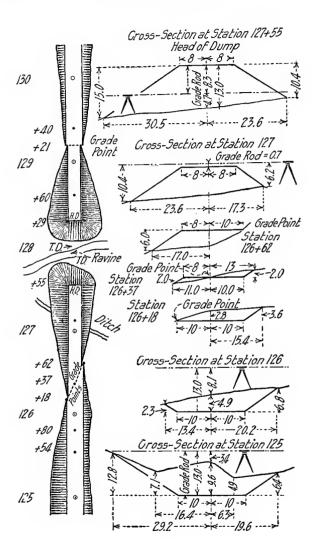
CROSS-SECTIONING PARTY.—It is the dnty of the cross-sectioning party to set slope stakes for the proposed roadbed and to secure data for the calculation of earthwork quantities. The data should first be transcribed from the location level notes and profile into the cross-section book, including station numbers, surface and grade elevations, rates of grade, bench mark record, etc. In order to avoid confusion in relation to directions right and left, the station numbers should run up the page, and plenty of space left for pluses in the notes, especially on rough ground. As shown in the form, the left hand page should be used for data and the other for the cross-section notes.

The organization and equipment of the cross-sectioning party when using the engineers' level is: (1) recorder (note book), (2) leveler (engineer's level), (3) rodman (self-reading leveling rod, 50-foot tape), (4) axemen (axe, sack of flat stakes, marking keel). The usual routine is: (1) Determine height of instrument by back sight on identified bench or turning point. (When a bench mark is remote and an original turning point can not be found, it may suffice in an emergency to check on the ground at several stations to the nearest 0.1 foot and use the mean height of instrument. Such places should be verified later.) (2)Having the height of instrument, check the original elevation of the station about to be cross-sectioned, reading the rod and checking off the elevation if it does not differ more than 0.1 foot or so; in case of a new plus, take a rod reading and record the elevation. (3) Determine the "grade rod" for the station by subtracting the height of instru-

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' I				FORM	FOR	CROSS	S-SECT	ION	NOTES	
Sta.	Elev	Grade	la te	Surf Rod	GradeRođ 7 747-67	<u>_</u> X	L	C	R	Remarks
130	742.5	736-50	5	5.2	11.2	A 728-22	+5.4	+60	+8.0	(3-level section in cut)
+40	739·8	736-50		7.9	11.2	F.S. 0.57	+3.3	+3-3	+3.8	(Level section in cut)
					A 739.61	B.S. 11.96				
+21	736·5			(3·1)-	-3.0	Л 739-61 FS- 2-03	<u>0.0</u> 10.0	0.0	0.0	(Grade point, L, C and L)
129		736-30			<u>3+1</u> T 128-22	0 737-58 B-S-10-09	- <u>4./</u> 14.3	-4.2		(3 level section In Fill)
+60	723.9	736-50		4.3	- 8.3	A 747.67	-12.6 26.9	-12-6	26.5	(Level section in Fill)
+34			0			<u>F-5-5-48</u> c742-19	=18-0			Nend stringer, Br. Hº 18
H.D. +29	720.5		151	7.7	- 8-3	+ Check on	<u>-/6.0</u> 32.0		<u>/6.0</u> 32.0	(Head of Dump)
T-D-+05 128		736-50 736-50	35	7.7 8.1	- 8.3	B·M·No·12 (below)	<u>0.0</u> 8.0	(-16-0	0.0	(Toe of Dump)
+90	7/2.2	13050	2	8.1		1.000.00				Bridge Nº18 {128+34
4210	116.6		Sta.		- 8.3	7 737-23	0.0	-		6,14 spans (127+50
T.D. (+81.4 +738			20		- 83	<u>F-5-JQ-15</u> 0727-08	8.0 00	-	0.0	(Toe of Dump (right.)
HD-+55	723.5	736-50	81	4.7	-83	8.5.1.14	-15.0		-12.4 8:0 -10:4 23:6	(Head of Dump)
1+50	1.50			1.1		A 128-22	30-5	1.50	23.6	Send stringer, Br. Nº 18
+/3	1		518		* 7 7 7 7 7 7					Ditch 2.4 × 4.7 × 53.
127	727.8	736-30		9.4	X 137:23 0.7	T 749-51	-10.4	-87	- 6.2 17.3	(3 level section in Fill)
162	731.9	736-50	Ű.	5.3	0.7	F.S. 12.58	-6.0 17.0	-4.6		(Grade point right)
+37	736·5	736-30	90	(OT)	-07	0736-93 B-5-0-30	-2.0	0.0	+2.0 13.0	(Grade point center)
+18	739.3	736-50	5	10.2	X749-51 13-0	1737-23	10.0	+2.8	13.6	(Grade point left)
126	74 <i>1</i> ·4	736-50		8-1	13.0		+2.3 13.4	14.9	+6.8	(3 level section in cut)
+80	741-7	736-30	ß	7.8	13.0		+5·2 17·8	+52	+6.2 17.8	(Level section in cut)
+54	742.2	736-50	0	7.3	13-0	B·M·№12 742·17	<u>+10.0</u> +6.8 25.0 12.2	+5.7	+40 16.0	(4 level section in cut,
125	746-1	736-50		3.4	13.0	B-5-7-34	<u>+/2.8</u> +7.1 29.2 /6.4	+9.6	+ <u>4-9</u> + <u>6-4</u> 6-3 19-6	(5 level section in cut)
						174901		}	100 100	Cuts 20, 12:1, Fills 16, 12:1.







ment from the grade elevation; then note that cut or fill at any point of the cross-section is equal to surface rod minus grade rod (counting rods as minus when downward from the plane of the level and those upward as plus, this rule gives results always plus for cut and minus for fill, which agrees with the conception that cross-section notes are rectangular coordinates of the sectional area referred to the center of the finished roadbed as an origin). (4) If the ground is level transversely, that is, does not vary more than 0.1 foot or so within the limits of the proposed grading, then the distance from the center out to each side slope stake is half width of roadhed plus center cut or fill times rate of side slope; (thus for 20-foot roadbed, side slopes 1 to 1, and a cut of 18.6 feet, the distance out to slope stake on a level section would be 28.6 feet, or with a slope of 114 to 1, the distance out would be 10 plus 114 times 18.6, or 37.9 feet. Calculations of this sort should be done mentally in an instant). (5) On three-level ground estimate the rise or fall of the surface from the center to about where the side slope stake should come, and add the same to, or subtract it from the center cut or fill, as the case may be; compute the distance out to the point where the side slope line would pierce the ground surface and test the same with tape, rod and level by the foregoing rule for cut or fill; continue to construct points on the side slope line until the common point is found. (6) The axeman marks "S. S." (slope stake) on one side of the stake with the cut or fill to the nearest 0.1 foot (as C 6.8 or F 10.2) and the station number on the other side; the stake is driven slanting towards or away from the center line according as it is cut or fill. (7) On five-level ground or, in general, on ground involving any number of points or angles in the section, the cut or fill is taken at each break. (8) Should there appear to be danger of land slips, the cross-sectioning should be carried well beyond the limits of the slope stake points. (9) The cross-section notes are recorded as in the accompanying form, expressing the coordinates of each point in the form of a fraction, and distinguishing the slope stake points by enclosure in a circle. (10) Having completed the cross-sectioning at the station. the same program is followed at the next point, first checking the elevation obtained in the original location levels: the grade rod should be determined as before by subtracting the height of instrument from the grade elevation, and then checked by applying to the preceding grade rod the

rise or fall of grade from the preceding point. (11)Cross-sections should be taken as a general rule at every station and at such intermediate points as will insure a reliable measurement of the earthwork quantities. It is not necessarily the lowest and highest points that are required, but those points which, when joined by straight lines, will give the contents as nearly as possible equal to the true volume; if the "average end areas" method is to be used in calculating the quantities, sections should be taken every 50 feet when the difference of center height is as much as 5 feet; as a rule, slope stakes need not be set at cross-sections taken between stations. (12) "Grade point" stakes (marked 0.0), should be set where the center line and each edge of the roadbed pierce the ground; and also in side-hill sections in both cut and fill, where the roadbed plane cuts the ground line; if the width of roadbed is different in cut and fill, the greater half-width is commonly used in locating the side grade point; in the simplest case a contour line is perpendicular to the center line and the three grade points are at the same cross-section, forming two wedges; in the more usual case the contour line is diagonal, and the three grade points are not in the same section, so that two pyramids are formed; if the station numbers of the two side grade points differ by only a few feet, it is usual to simplify the record by taking the notes as for a wedge at the station number of the center grade point, although the side grade point stakes are set in their true positions: as a rule, a complete crosssection is taken at each grade point. (13) In cross-sectioning for the end of an embankment at a wooden trestle the end slope is made the same as the side slope, and the end and side planes are joined by conical quadrants; the distance between "heads of dump" (H. D.) is usually 10 feet (5 feet at each end) less than the total length of stringers; a complete cross-section is taken at the "head of dump," and the "toe of dump" (T. D.) on each edge of the end slope is located and recorded; on level ground the volume of the wedge-like solid so formed is found by dividing it into a triangular prism and two right conical quadrants; on ground sloping transversely the end of dump is made up of a middle prismoid and two conical quadrants, each of the latter being generated by a variable triangle revolved about a vertical axis through a corner of the top roadhed plane at "head of dump."

The calculations in the foregoing method of cross-section-

ing may be simplified by preparing a table of distances out for the standard roadbed widths and slopes, or by using a special tape having the zero graduation at a distance from the end equal to the half-width of roadbed, and the remaining graduations modified to suit the side slope ratio. The calculations may be further simplified by using a special rod having an endless sliding tape graduation. The student will be given practice with these labor saving devices after he has first acquired familiarity with the principles of cross-sectioning without these aids.

Cross-sectioning with rods alone is done in much the same manner as that described above. Two rods are used. The usual length of the rods is ten feet, and each is graduated to tenths and has a bubble vial in one or both ends. The slope stake point is determined by leveling out from the ground at the center stake with reference to the center cut or fill, each rod being held alternately level and plumb. Other points in the cross-section, as well as grade points. etc., are determined in the same manner. The notes are kept as in the other method. On very rough ground, the rod method is usually the more rapid. Some engineers cross-section on rough ground by taking the elevation of each point and plotting the notes on cross-section paper. then using the planimeter to determine the areas. Borrow pits are often cross-sectioned by taking elevations at the intersections of two series of parallel lines forming squares.

Land-Line Party.-It is the duty of the right of way party to secure data for the preparation of right of way deeds. The party should consist of at least four: (1) recorder, (2) transitman, (3) head chainman, (4) rear chainman. (the chainmen also to serve as axemen and flagmen as required). Their equipment is the usual one of a transit party for such work. The party should secure ties with all section and other land lines whenever crossed. The notes should show station numbers and angles of intersection and distance along land line to the nearest identified land corner and also to important fences. As a rule, make the intersection by running through from one corner to the other. Where the line passes through a town, tie the center line to the plats, block lines, monuments, etc. Secure any records and make tracings of any plats, etc., at the recorder's office, that may be of service in preparing deeds.

Bridge and Masonry Party.—The bridge and masonry survey party will determine drainage areas for culverts and other waterways, prospect for foundations, and stake out trestles, masonry work, etc. The usual organization will be four men: (1) recorder (in charge), (2) transitman or leveler, (3) chainman, rodman, flagman, etc., (4) chainman, axeman, flagman, etc., as the work assigned may demand.

Resurvey Party.—The resurvey party will be assigned to such duties as the resurvey of yards, the collection of data for crossings frogs, running centers on old track, including spiraling, etc. It will usually be a party of four.

PROBLEMS IN RAILROAD SURVEYING.

PROBLEM G1. ADJUSTMENTS OF LEVEL AND TRANSIT.

(a) Equipment.—Engineers' level and transit, adjusting pin.

(b) *Problem.*—Test the essential adjustments of the assigned instruments and correct any discrepancies found.

(c) Methods.—This problem is designed to freshen the student's knowledge of the adjustments of the instruments, as well as to place the equipment in condition for accurate work. The adjustments will be made under the personal direction of the instructor. The student should attempt to be speedy as well as accurate in testing and making the adjustments.

PROBLEM G2. USE OF FIELD EQUIPMENT.

(a) Equipment.—Complete equipment for railroad transit and level party, as specified in foregoing pages.

(b) *Problem.*—Practice the detailed duties of each position in the transit and level party.

(c) Methods.—This problem is designed as a "breaking in" exercise preparatory to engaging in the regular field work of railroad location. With the manual in hand the duties of each position will be studied and practiced in turn.

For example, each student will go through the following exercise with the transit as briskly as possible: (1) set transit over tack in hub, (2) level up. (3) set plate to zero, (4) reverse telescope and sight on back flag, (5) release needle, (6) plunge telescope, (7) read and record needle on back line prolonged, (8) sight at front flag pole, (9) read and record deflection angle right or left, (10) read and record needle on front line, (11) lift needle, (12) plunge telescope and check on back flag, (13) calculate needle

angle and compare with plate reading, and if checked, shoulder transit; now repeat entire process at the same hub, more briskly than at first, if practicable, avoiding reference to preceding record until the full series of steps is completed.

	and the second secon
	tion of Curve Elements.
N. 1. 1	$ \begin{cases} I = \delta c^{0} / J^{2} R. \\ C = \delta^{0} / J^{2} \\ (R) = \delta^{0} / J^$
	$\begin{array}{rl} n \ 30\ 08.5 \pm 0.58066 \\ \text{Sec} \ 30\ 08.5 \pm 0.5636 \\ \text{Part.} & (o) & (b) \\ \text{Pirt} \ 60\ 23\ 33\ + \\ \text{Pirt} \ 60\ 23\ 33\ + \\ \text{Pirt} \ 60\ 23\ 33\ + \\ \text{Pirt} \ 60\ 20\ 30\ - \\ \text{Pirt} \ 60\ 20\ 30\ - \\ \text{Pirt} \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \\ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ 60\ - \ \ \ 60\ - \ \ \ 60\ - \ \ \ 60\ - \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
Indicated Wark.	Calculations.
Length of Curve, L, $L = \frac{60^{\circ}77}{4^{\circ}77}$ (a) = $\frac{3617}{2877} = (4.07^{\frac{23}{23}})$ (b) = $\frac{60^{\circ}2833}{4^{\circ}2833} = (4.07^{\frac{23}{23}})$	257)36(7) <u>74.0739</u> <u>257</u> <u>647</u> <u>1047</u> <u>1028</u> <u>1790</u> <u>1790</u> <u>1799</u> <u>2968</u> <u>1799</u> <u>2968</u> <u>1799</u> <u>2968</u> <u>1799</u> <u>2968</u> <u>17158</u> <u>2977</u> <u>38</u> <u>2313</u> <u>77</u>
$\begin{array}{r} \underline{\text{Tangent Distance, 7.}} \\ \hline \textbf{Tangent Distance, 7.} \\ \hline (a) \ T = R \ tan \frac{1}{2} I \\ = \ 1337.65 \times 0.58066 \\ = \hline (776.7) \\ \hline (b) \ T = \ \frac{7_{1} \cdot c_{.}}{D} \\ = \ \frac{33227.15}{4.2833} \\ = \ (776.7) \end{array}$	$\begin{array}{cccc} , & & & & & & & & & & & & & & & & & & $
External Distance, E. (a) $E = R$ exsec $\frac{1}{2}I$ $= \frac{133765 \times 0.15636}{209.13}$ (b) $E = \frac{E_{1} \times C_{1}}{D}$ $= \frac{898.995}{42233}$ = (209.17)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

Let the student prepare a similar numbered program for each of the other positions and practice the same systematically. This series of exercises may profitably occupy two or more assignments, since the speed and quality of the actual surveys to follow are certain to be much enhanced.

PROBLEM G3. PRELIMINARY FIELD CURVE PRAC-TICE.

(a) Equipment.—Transit party equipment, as prescribed in instructions.

(b) *Problem.*—Run out the assigned practice curves in the field, with the prescribed organization and conditions.

(c) *Mcthods.*—The preliminary curve practice is designed to give the student a practical knowledge of the principles of railroad curves and the routine methods used in location surveys. The several positions in the field party will be filled in succession, and each student is expected to respond heartily to the spirit of the practice, whatever his assigned duties. Each member of the party should engage in the calculations as far as practicable. The report of the field work should state the precision of linear and angular checks. The field practice will be based in part on the indoor curve problems.

PROBLEM G4. CURVE PROBLEMS.

(a) Equipment.—Drafting instruments, paper, etc.

(b) *Problem.*—Solve the assigned problems in railroad curves and submit results in a neat and draftsmanlike form.

(c) Methods.—(1) Draw a plain figure to the largest convenient scale. (2) State problem and present data in a concise and systematic manner. (3) Show the separate steps clearly; first state formulas in general terms, then substitute values and give results; as a rule, show actual calculations adjacent to the indicated work; habitually verify results by an independent process; use common sense checks and contracted methods of calculation; in general, make full use of the opportunity to gain skill as a computer. (As a rule, the nearest 0.1 foot only is required in field measurements on curve location, but it is excellent practice, especially for the beginner, to preserve the nearest 0.01 foot in the calculations.)

CHAPTER IX.

ERRORS OF SURVEYING.

Errors.—Errors of observations are of three kinds, viz., (1) mistakes; (2) systematic errors; (3) accidental errors. Systematic errors include all errors for which corrections can be made, as erroneous length of standard, errors of adjustment, refraction, etc. Accidental errors are those which still remain after mistakes and systematic errors have been eliminated from the results.

It has been found from experience that accidental errors are not distributed at random but follow mathematical laws. These laws are fundamental in the Theory of Least Squares and are: (1) small errors are more frequent than large ones; (2) positive and negative errors are equally numerous; (3) very large errors do not occur.

Arithmetical Mean.—The most probable value of a quantity obtained by direct measurements is the arithmetical mean of all the determinations where the observations are of equal weight, or is the weighted mean where the observations are of unequal weight.

Precision of Observations.—In the adjustment of observations it is often necessary to combine results of different degrees of precision or weight. It is also desirable to have some means of comparing observations so that the computer may know what degree of confidence to place in the results. The quantity commonly used for comparing the precision of observations is the probable error.

Probable Error.—The probable error is such a quantity that it is an even wager that the number of errors greater is the same as the number of errors less than the probable error. It is also the limit within which the probability is one-half that the truth will fall. For example, if $4.63\pm$ 0.12 is the mean of a number of observations, the true value is as likely to be between 4.51 and 4.75 as it is to be some value greater or less.

Probable error is also useful in finding the relative weights that should be given different sets of observations, as it has been found that the weights of observations vary inversely as the squares of their probable errors. Formulas:

Let $E_1 =$ probable error of a single observation.

 $E_m =$ probable error of the mean of all the observations.

n = the number of observations.

d = the difference between any observation and the mean of all the observations.

 $\Sigma =$ symbol signifying sum of.

Then from the Theory of Least Squares

$$E_1 = 0.6745 \sqrt{\frac{\Sigma d^2}{n-1}} \tag{1}$$

$$E_m = 0.6745 \sqrt{\frac{\Sigma d^2}{n(n-1)}}$$
(2)

$$=\frac{E_1}{\sqrt{n}}$$
(3)

The probable error of the weighted or general mean is

$$E_0 = 0.6745 \sqrt{\frac{\Sigma p \cdot d^2}{(n-1)\Sigma p}} \tag{4}$$

where $\Sigma p =$ summation of the weights.

The probable error of a quantity with a weight p is equal to E_{q} divided by the square root of p.

The probable error of Z, where $Z = z_1 \pm z_2$, and R_1 , r_1 , and r_2 are the probable errors of Z, z_1 and z_2 , respectively, is

$$R_1^2 = r_1^2 + r_2^2 \tag{5}$$

The probable error of Z, where $Z \equiv a$. z is

$$R_1^2 = a^2 \cdot r^2 \tag{6}$$

The probable error of Z, where $Z = z_1$. z_2 is

$$R_1^2 = z_1^2 \cdot r_2^2 + z_2^2 \cdot r_1^2 \tag{7}$$

This would be the probable error of the area of a rectangle where r_1 and r_2 are the probable errors of the sides z_1 and z_2 , respectively.

Example.—As an example of the application of these formulas consider the two following series of measurements of an angle given in Table I. The first set was taken with a transit reading to 10 seconds, the second with a transit reading to 30 seconds.

	FI	RST 1	TRANS	SIT.			SEC	OND	TRAN	NSIT.	
No.	A	ngle	e.	d	d^2	No.	А	ngle		d	d^2
1 2 3 4 5 6 7 8 9 10	34	55 56 55	$\begin{array}{c} & \\ & 35 \\ & 35 \\ & 20 \\ & 05 \\ & 15 \\ & 40 \\ & 10 \\ & 30 \\ & 50 \\ & 30 \end{array}$	$ \begin{array}{c} 2\\ 2\\ 13\\ 28\\ 42\\ 7\\ 23\\ 3\\ 17\\ 3 \end{array} $	4 169 784 1764 49 529 9 289 9	1 2 3 4 5 6 7 8 9 10	34	56 55	$\begin{array}{c} & \\ 15 \\ 30 \\ 30 \\ 15 \\ 00 \\ 45 \\ 30 \\ 30 \\ 00 \\ 45 \end{array}$	$ \begin{array}{r} 39 \\ 66 \\ 21 \\ 24 \\ 9 \\ 6 \\ 6 \\ 24 \\ 9 \\ 9 \end{array} $	$1521 \\ 36 \\ 4356 \\ 441 \\ 576 \\ 81 \\ 36 \\ 36 \\ 576 \\ 81$
Mea	n_34°	55'	33″	$\Sigma d^2 =$	= 3610	Mean	n 34°	55'	36″	$\Sigma d^2 =$	=7740
$E_m =$	$E_m = 0.6745 \sqrt{\frac{3610}{9 \times 10}} = \pm 4^{\prime\prime}.3 \qquad E_m = 0.6745 \sqrt{\frac{7740}{9 \times 10}} = \pm 6^{\prime\prime}.3$										

TABLE I

The weights of these mean values vary inversely as the squares of the probable errors, or in this case the weights are as $\frac{1}{4.3^2}$ to $\frac{1}{6.3^2}$ or as 12 to 5. The most probable value of the angle measured with the two transits will be the weighted mean.

$$Z = 34^{\circ} 55' + \frac{33 \times 12'' + 36 \times 5''}{17}$$

= 34^{\circ} 55' 33''.9

The probable error of this result from (5) since

$$Z = \frac{1}{17} \frac{2}{7} z_1 + \frac{5}{17} z_2, \text{ is}$$
$$R_1^2 = (\frac{1}{17})^2 r_1^2 + (\frac{5}{17})^2 r_2^2$$

Substituting $r_2^2 = \frac{12}{5}r_1$ we have

$$\begin{aligned} R_1^2 &= \left(\frac{1}{17}\right)^2 r_1^2 + \left(\frac{5}{17}\right)^2 \left(\frac{12}{5}\right) r_1^2 \\ &= \frac{1}{17} r_1^2 \\ R_1 &= \pm 4.''3 \ \sqrt{\frac{12}{17}} = \pm 3''.6. \end{aligned}$$

For other examples in the use of probable error see probable error of measuring a base line, probable error of setting a level target, probable error of setting a flag pole.

Angle Measurement.—The measurement of an angle requires two pointings and two readings. If r_r and r_s are the probable errors of reading and pointing, respectively; the probable error of the measurement of an angle will from (5) be

 $R_{1} = \sqrt{r_{r}^{2} + r_{s}^{2}}$ If r_{1} is the probable error of a single reading $r_{r} = r_{1}\sqrt{2}$

If the value of an angle is determined by *n* separate measurements the probable error due to reading will be

$$r_r = \frac{r_1 \sqrt{2}}{\sqrt{n}}$$

If the value of an angle is determined by measuring the angle n times by repetition the probable error due to reading will be

$$r_r = \frac{r_1 \sqrt{2}}{n}$$

It will thus be seen that the probable error due to reading is very much reduced by measuring an angle by the method of repetition. The errors of pointing, etc., however, make it doubtful whether it is ever advantageous to make n exceed 5 or 6 with an engineers' transit.

Angle Adjustment.—When the three angles of a triangle have been measured with equal care they should be adjusted by applying one-third of the error as a correction to each angle.

When the interior angles of a polygon having n sides have been measured with equal care they should be adjusted by applying *one-nth* of the error as a correction to each angle.

When n-1 angles and their sum angle at a point have been measured with equal care they should be adjusted by applying *one-nth* part of the error as a correction to each angle.

In a quadrilateral the true values of the angles fulfil the following geometrical conditions: (1) the sum of the angles of each triangle is equal to 180° plus the spherical excess

(the spherical excess in seconds of arc is equal approximately to the area in square miles divided by 78); (2) the computed length of any side when obtained from any other side through two independent sets of triangles is the same in both cases.

When the angles of a quadrilateral have been measured, errors are certain to be present and the corrections that satisfy one of these conditions will not satisfy the other. The most probable values of the corrections to the angles are then determined by the Theory of Least Squares.

TESTS OF PRECISION.

Practical Tests.—In careful surveying where blunders are eliminated and the systematic and accidental errors are small and under control, it is found that the magnitude of the errors increases in close accord with the foregoing rational basis, that is, as the square root of the number of observations. The following practical tests of precision are based on this truth.

Linear Errors.—Cumulative or systematic errors usually increase directly as the length of the line chained, while compensating or accidental errors vary about as the square root of the length. While both kinds of errors affect all linear measurements, the former chiefly control the results of crude and the latter of accurate chaining. It is thus fairly consistent to express the precision of chaining in crude work in terms of the simple ratio of the length; but as the chaining becomes more and more exact, the variation of the differences between duplicate measurements approximates more and more closely to the law of square roots.

Coefficients of precision derived from the latter relation may be based on either 100-foot units or foot units in the distance chained, as preferred. The former basis is used in the chaining diagram while the latter is found in the last paragraph of the explanatory matter on the second page referring to the precision of traverse surveys.

The diagram of chaining errors shows chaining ratios by right lines radiating from the origin, and the law of square roots by means of parabolas. The coefficient of precision for a given observed difference between duplicate chainings is determined by inspection from the diagram, interpolating between curves if an additional decimal place is desired in the result. In actual practice a pair of careful chainmen may determine the coefficient corresponding to a given degree of oare, and then use this value either in testing their duplicate results, or in estimating the probable uncertainty of the lengths chained.

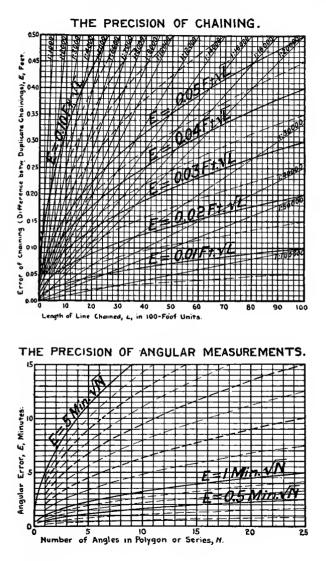
For accurate chaining with the steel tape, duplicate measurements reduced for temperature, etc., or made under sensibly identical conditions, should not differ more than 0.05 foot into the square root of the distance in 100-foot units. Careful work with the common chain (estimating fractions to 0.1 foot) should not differ more than 0.1 foot into the square root of the distance in 100-foot units.

Angular Errors.—In measuring deflection angles by altitude reversals, as in railroad traversing, there is, of course a cumulative discrepancy due to the collimation error, but generally speaking, careful angular measurements with good instruments are subject only to compensating or accidental errors. Under the latter conditions the magnitude of the error of closure in a series of angles, either in a closed polygon or about a point, varies about as the square root of the number of angles. This relation is indicated graphically in the diagram of angular errors.

In measuring angles with a transit reading to the nearest minute, the compensating uncertainty of a single reading is probably somewhat under 0.5 minute per angle, or about one minute for the closure of a triangle. If a reading glass be used and the vernier reads to the nearest half minute, the uncertainty is still further reduced.

Again, in estimating the needle reading of a compass to the nearest 5 minutes (one-sixth part of a half-degree), the uncertainty of reading alone is perhaps 3 minutes, although this is increased by other conditions such as sluggishness of needle, etc., probably causing an uncertainty of as much as 5 minutes per angle, which later limit would produce an error of closure of a triangle of say 10 minutes, and of a five-sided polygon of perhaps the same amount. (See diagram.)

Traversing Errors.—The errors of traversing are made up of the combined errors of linear and angular measurements. If the error of closure as determined from the latitudes and departures is large, the work should be scanned closely to detect blunders such as the substitution of sine for cosine, errors of 100 feet in chaining, misplacing decimal point, etc. After establishing the consistency of the residual errors, they should be distributed either in proportion to the lengths of the several courses, as in the more



THE PRECISION OF TRAVERSE SURVEYS.

The error of closure of a traverse is usually expressed as the ratio of the calculated linear error to the length of the perimeter of the field or polygon. The following table shows the limits prescribed by various authorities

Prescribed Limits For Closure Of Traverses.

Authority.	Conditions.	Limits.
Gillespie. (1855). "Surveying," p. 149.	Compass Surveys.	1:300 to 1:1000
Alsop. (1857). "Surveying," p.199.	Compass Surveys. Transit Surveys.	1:500 1:1000 to 1:1500
Davies. (1870). "Surveying," p.127.	Farm Surveys.	1:500 to 1:1000
Jordan. (1877). "Handbuch der Vermessungs- Kunde," Vol.1, p.296.	German Gov't Surveys. Baden Instructions. Prussian Instructions. Swiss Gov't Surveys. Ordinary Country. Mountainous Gountry.	1:400 1:333 to 1:1000 1:400 to 1:800 1:267 to 1:533
Hodgman. (1885). "Surveying," p. 119.	Compass Surveys.	1:300 to 1:1000
Johnson. (1886). "Surveying," p.201. Baker. * (1888). "Engineers' Surveying Instruments," p.53.		1:300 1:1000 to 1:5000 (See Footnote).
Carhart. (1888). "Surveying," p. 161.	Ordinory Farm Surveys. Level Ground. Rough Ground. Average Transit Surveys.	1:500 1:1000 1:200 to 1:300 1:1200
Wood. (Roanoke,Va., 1892). (Baltimore, Md., 1894).	(See Footnote). {Precise Traverses with Repeated Angles. {	(See Footnote). 1:10 00 0 1:15 000 + .04 Ft.
Raymond. (1896). "Surveying," p. 144.	Ordinary Farm Surveys. Good Farm Surveys.	1:500 1:2000

*Baker derives the formula $E = P \sqrt{\frac{1}{d^2} + \frac{a^2}{12\,000\,000}}$ where

E is the permissible linear error of closure, P the length of the perimeter, 1:d the ratio of the chaining error, and a the angular error of closure in minutes. A thorough test of this formula under a wide range of Conditions proves if to be trustworthy.

However, the use of a chaining ratio, 1:d, presumably of fixed value for the same chainmen, does not accord with the results of experience in careful work; for it is found that the differences between duplicate chainings vary about as the square root of the length of line.

On the following page a simplified formula is obtained by assuming the more consistent relation just stated for the chaining errors. The results are about the same as those obtained with Bakers formula, and the form of the expression is identical with that used by Wood in the Baltimore Survey.

THE PRECISION OF TRAVERSE SURVEYS.

The reasonable or permissible error of closure of a traverse survey may be determined by the formula derived Lelow, pravided the errors of field work are under control and their magnitude the errors at field worn are ander som is known, at least approximately. Let P=length of perimeter. L= calculated error of lotitudes.

D=calculated error of departures.

D=calculated error of departures. E_= actual or calculated linear error of closure of traverse. c= coefficient of precision of chaining. C= linear error of clasure due to chaining errors.

a= angular error of closure in minutes.

A = linear error of closure due to angular errors. Ep=permissible or reasonable linear error of closure due to errors of chaining and angle.

In the triangle of error the hypothenuse is $E_{a}=\sqrt{L^{2}+D^{2}}$. In Diagram A below values of E_{a} may be read close enough for most cases. Diagram A may also serve as a crude graphical trav-erse table, and blunders in the field work may be located by it.

In coreful chaining by men of some training, the error varies about as the square root of the distance. If a be the compensating error for the unit distance, then $C \in \sqrt{P}$.

The angular error of closure in coreful surveys probably eccurs omong the sides in proportion to their lengths. Assuming this to be the case, the resulting linear error is A = a P.arc I'= .0003aP.

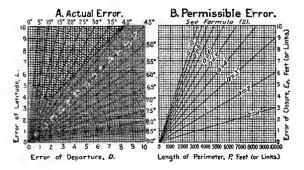
In good work the errors ore small in amount and equally liable to be plus and minas. Hence, the probable error at closure due to the two causes, i.e. the reasonable or permissible linear error of closure is $E_p = \sqrt{A^2 + c^2} = \sqrt{(.0003a^2)^2 + c^2}$

This formule may be much simplified by completing the square and dropping the negative term under the radical, whence with sufficient exoctness, there results the general formula

The very exact standard, P+15000+04ft, used at Baltimore, (see table, preceding poge), may be obtained from (1) by mating a samewhat less than 2 minute, and c=005 ft, these values being consistent with the field work of that survey.

The value of c may be determined for the given chainmen, ar the chaining term of (1) may be taken as follows:- For best work (c(.005ft), 05ft; for dverage work (c(.010), 2ft; for fair work (c(.013), 4 ft; and for poor work (c(.020), 3ft. In care-ful traverse survers the angle term alone affords o rigid test, so that formula (2) may be used except when a =0. Diagram B gives (2) for the general run of traverse problems,

 $E_p = 0003 \ aP = \frac{3aP}{10000} \cdots \cdots \cdots (2)$



THE PRECISION OF LEVEL CIRCUITS. (For Good Average Practice.)

When the length of the level circuit is known in 100-ft. stations, or when merely the number of settings of the instrument and the approximate average distance covered per setting ore known, the following modifications of the preceding test are valuable.

For good overage work with the engineers' level

E =	0.05 A.VM
F =	0007AVE

from which

and $E = 0.007 ft \gamma LS$

250-*

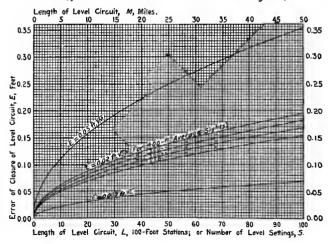
for a very ropid approximate check under ordinary conditions, it may be assumed that E=0.02fr.VS. A graphical representation of these formulas is given below.

Ľ=5.

E = 0.0154 A.1/5

Permissible Error of Closure of Level Circuits For Careful Work with a Good Engineers' Level.

Length of Circuit Given in Miles (Upper Curve); or in the Number of Instrumental Settings (Middle Graup of Curves); or in 100-Foot Units (Lower Curve in Diagram).



THE PRECISION OF LEVEL CIRCUITS.

The precision of spirit leveling is expressed by the formula

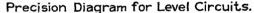
Error of Closure = Constant VLength of Circuit.

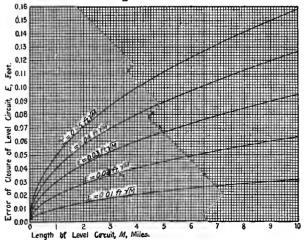
In the following summary of practice in representative Surveys of the United States, E is the maximum limit of error of closure of a level circuit having a length of K kilometers or M miles.

Precision of Leveling in Representative Surveys.

	MAXIMUM PERMISSI		
	Metric Units.	British	
NAME OF SURVEY.	Coefficient to nearest mm.	Coefficient 1 0.001 ft.	o nearest 0.01 ft.
Chicago Sanitary District.	E= 3mm.VK = 0		=0.01 ft.VM
Missouri River Commission.	E = 3 <i>mm.</i> √2K = 0		
Mississippi River Commission. (1891).	E= 3mm.\2K=0		
Mississippi River Com'n (Before 189.	I). E = 5mm.√K = 0	1.021 ft.√M)	
United States Coast Survey.	E = 5mm.√2K = 0	.029 ft. VM	<i>= 0.0</i> 3 ft.√M
United States Lake Survey.	E=10 mm.VK == 0		
United States Geological Survey.	E⇒ 0	.050 ft. VM	= 0.05 ft.VM

A simple practical test of the degree of precision attained in spirit Jeveling is found in the last column of the above table. This graduated scale of precision is given below graphically for distances to ton miles.





common usage, or in the proportion of the respective latitudes and departures, as would seem to be more consistent. If the several courses have not been surveyed with like precision, weights should be assigned in distributing the errors. Absurd refinement should be avoided in making the distribution of errors.

Leveling Errors.—Perhaps in no phase of surveying measurements is it more clearly established that accidental errors follow the law of square roots than in careful leveling. The precision diagrams are based on best current usage.

CHAPTER X.

METHODS OF COMPUTING.

Introduction.—To no one is the ability to make calculations accurately and rapidly of more value than to the engineer. Many fail to appreciate the value of rapid methods of calculation, and have no conception of the amount of time that can be saved by the skillful use of arithmetic, logarithms, reckoning tables and computing machines.

In the field the engineer has to depend upon the ordinary methods of arithmetic, or a table of logarithms for his results. The use of these aids should therefore receive special attention, for the engineer cannot afford to lose the time of his assistants while he makes unnecessary or extended computations.

In the office tables of squares, reckoning tables, slide rules and computing machines can be used in many cases with profit.

Consistent Accuracy.—It is safe to say that at least onethird of the time expended in making computations is wasted in trying to attain a higher degree of precision than the nature of the work requires.

In making arithmetical computations where decimals are involved it is a common practice to carry the result out to its farthest limit and then drop a few figures at random.

In using logarithms time and labor are lost by using tables that are more extensive than the data will warrant. The relative amount of work in using four, five, six and seven-place tables is abont as 1, 2, 3 and 4. Besides the extra labor involved, the computer has a result that is liable to give him an erroneous idea of the accuracy of his work.

In making computations, in general, calculate the result to one more place than it is desired to retain.

If several numbers are multiplied or divided, a given percentage of error in any one of them will produce the same percentage of error in the result. In taking the mean of a series of quantities it is consistent to retain one more place than is retained in the quantities themselves.

In direct multiplication or division retain four places of significant figures in every factor for an accuracy of about one per cent; retain five places of significant figures in every factor for an accuracy of about one-tenth of one per cent.

LOGARITHMIC CALCULATIONS.

Logarithm Tables.—Logarithm tables contain the decimal part of the logarithm called the mantissa, the integral part called the characteristic is supplied by the computer.

Four-place tables give the mantissa to four decimal places of numbers from 1 to 999, and by interpolation give the mantissa of numbers from 1 to 9,999. Four-place logarithms should be used where four significant figures are sufficient, and should not be used where an accuracy greater than one-half of one per cent is required.

Five-place tables give the mantissa to five decimal places of numbers from 1 to 9,999, and by interpolation give the mantissa of numbers from 1 to 99,999. Five-place logarithms should be used where five significant figures are sufficient, and should not be used where an accuracy greater than one-twentieth of one per cent is required. Five-place tables are sufficiently accurate for most engineering work.

Six-place tables give the mantissa to six decimal places of numbers from 1 to 9,999, and by interpolation give the mantissa of numbers from 1 to 99,999, the same as the fiveplace tables. Six-place tables give practically no gain in precision over five-place tables since the same numbers of significant figures are given in both tables, and in addition the labor of using a six- instead of a five-place table is about as 3 to 2, due to interpolation with larger differences. For the above reasons five-place tables have been selected for use in this book as being the most suitable tables for use in surveying.

Seven-place tables give the mantissa to seven decimal places of numbers from 1 to 99,999, and by interpolation of numbers from 1 to 999,999. Seven place tables are rarely needed in engineering work, except in triangulation work where the angles are measured by repetition.

ARITHMETICAL CALCULATIONS.

Requirements.—To become a rapid computer the following requirements are essential:

(1) À good memory for retaining certain standard numbers for reference.

(2) The power of performing the ordinary simple arithmetical operations of multiplication, division, etc., on numbers with facility, quickness and accuracy.

(3) The power of registration, *i. e.*, of keeping a string of numbers in the mind and working accurately upon them.

(4) The power of devising instantly the best method of performing a complicated problem as regards facility, quickness and certainty.

It is obvious that all do not have the ability to become rapid computers, but even these can become fairly skillful by constant practice and perseverance. The ordinary processes of arithmetic should be performed with numbers in all possible positions. No more figures should be put down than necessary, and all operations should be performed mentally whenever possible. In the mental part the results should alone be stated, much time being lost by repeating each separate figure.

Checks.—In order to check his work the computer should keep the following well known properties of numbers well fixed in his mind:

(1). The sum or difference of two even or of two odd numbers is even.

(2) The sum or difference of an even and odd number is odd.

(3) The product of two even numbers is even.

(4) The product of two odd numbers is odd.

(5) The product of an even number and an odd number is even.

(6) Checking results by the familiar operation of casting out the 9's depends upon the following properties of numbers:

(a) A number divided by 9 leaves the same remainder as the sum of the digits divided by 9. For example:

$$4384 \div 9 = 487 + 1$$

$$(4+3+8+4) \div 9 = 2+1$$

(b) The excess of 9's in the product equals the excess of 9's in the product of the excesses of the factors.

METHODS OF COMPUTING.

$$\begin{array}{cccc} 473,295 & \text{Excess} = & 3 \\ 4,235 & \text{Excess} = & 5 \\ \hline & & & & 15 \\ 2,004,404,325 & \text{Excess} = & & 6 \\ \end{array}\right\} \text{Check}$$

(c) The excess of 9's in the dividend equals the excess of 9's in the product of the excesses in the divisor and quotient, plus the excess in the remainder:

56)2443	Excess	$_{ m in}$	divisor	=2	
$\frac{1}{43} + 35$	Excess	in	quotient	= 7	
	Excess	in	remainder	= 8	
	Excess	in	$(2 \times 7 + 8)$	=4	,
	Excess	in	$(2 \times 7 + 8)$ dividend	$=4 \int^{Cne}$	eĸ

(7) Results should be checked by taking aliquot parts wherever possible, and by performing the operations in inverse order or performing inverse operations. Computations performed by means of logarithms should be checked by making the computations roughly by means of arithmetic. The probability of error should be recognized and precaution taken to verify results.

ADDITION.—Since the eye is accustomed to pass from left to right time can be saved, where the columns are not too long, by adding in the same way. The device of increasing or diminishing the numbers to make them multiples of ten and then subtracting or adding to the result is very convenient, especially where several columns are added at one time.

	96	
	47	143
212	69	
	32	
	87	331
	49	
	380	

The mental work in detail is as follows:

 $\begin{array}{c} 100 + 47 = 147; \ 147 - 4 = 143; \ 143 + 70 = 213; \ 213 - 1 = \\ 212; \ 212 + 30 + 90 = 332; \ 332 - 1 = 331; \ 331 + 50 = 381; \\ 381 - 1 = 380. \end{array}$

Expert accountants use the method of adding columns in groups of 10, 20, 30, etc., small figures, indicating the number of the group, being placed along the column at intervals depending upon the computer. This method is well adapted to the addition of long columns where one is liable to be called away from his work. The progress of the work being then shown by the number of the group, plus the excess.

MULTIPLICATION.—In order to make the best use of the methods given, the computer should have perfect command of the multiplication table as far as 20 at least.

(1) When the tens differ by unity and the sum of the units equals 10, numbers may be multiplied by the following rule: From the squares of the tens of the larger number subtract the square of the units of the larger number. For the numbers may be represented by (a + b) and (a - b), and the product will be $(a + b)(a - b) = a^2 - b^2$.

Ex. 1.— $(93 \times 87) = 90^2 - 3^2 = 8,100 - 9 = 8,091.$

(2) The product of composite numbers is best obtained mentally by resolving them into their factors and taking the products of the factors.

Ex. 2.— $26 \times 36 \pm 9 \times 13 \times 8 \pm 936$.

Ex. 3.—
$$48 \times 24 = (24)^2 \times 2 = 1,152.$$

Multiples of 10.—To multiply by some number which is a factor of 10 or some multiple of 10, for example: Multiply

A by B, where
$$B = \frac{C10^n}{d}$$

Annex *n* ciphers to *A*, multiply by *C* and divide by *d*. *Ex.* 1.-4,324 × 625 = 4,324 $\frac{5 \times 10^3}{8}$ =(4,324.000 × 5) ÷ 8 = 2,702,500.

$$Ex. 2.-7,924 \times 25 = 792,400 \div 4 = 198,100.$$

Squaring Small Numbers.—Numbers may be squared mentally by the following rule: Add to or subtract from one factor enough to make its units figure zero. Subtract from or add to the other factor the same amount. Multiply together this sum and difference, and to the product add the square of the amount by which the factors were increased or diminished.

Proof.—
$$a^2 - b^2 = (a + b) (a - b)$$

 $a^2 = (a + b) (a - b) + b^2$.
Ex. 1.— $(76)^2 = (72 \times 80) + 4^2 = 5,776$.

Ex. 2.— $(127)^2 = (124 \times 130) + 3^2 = 16,129.$ *Ex.* 3.— $(6\frac{1}{2})^2 = (6 \times 6\frac{1}{2}) + (\frac{1}{4})^2 = 39\frac{1}{16}.$ *Ex.* 4.— $(6\frac{1}{2})^2 = (6 \times 7) + (\frac{1}{2})^2 = 42\frac{1}{4}.$ *Ex.* 5.— $(7.5)^2 = (7 \times 8) + (.5)^2 = 56.25.$

It will be seen that the process is very simple where the units place is 5.

(2) Having the square of any number the square of the number next higher is obtained by the following rule: To the known square add the number and the next higher and the result will be the square of the next higher number.

Ex. 6.— $(25)^2 = 625$. $(26)^2 = 625 + 25 + 26 = 676$.

(3) A very close approximation to the square of a quantity which is very near unity is obtained by adding algebraically two times the difference between the quantity and unity to the quantity.

Proof.— $(1 \pm b)^2 = 1 \pm 2b + b^2 = 1 \pm 2b$, (approximate).

Ex. 7.
$$(1.05)^2 = 1 + 2(1.05 - 1) = 1 + 10 = 110$$
.

Ex. 8.
$$(.94)^2 = 1 - 2(1 - .94) = 1 - .12 = 88$$
.

Ex. 9.
$$(2.034)^2 = 2^2(1+2 \times .017) = 4(1.034) = 4.136.$$

Cross-Multiplication.—This consists in taking the product of each digit in the multiplicand by each digit in the multiplier and taking the sums, products of the same denomination being determined thus: units \times units gives units; tens \times units and units \times tens gives tens; units \times hundreds, tens \times tens and hundreds \times units give hundreds etc. All products are added mentally, only the final result being put down.

Ex. 1.— $(2,347)^2 = 5,508,409$ the final result being all that it is necessary to write down. The mental work is as follows, the figures in heavy t pe being figures in the product; $7 \times 7 = 49$; $4 + 2(7 \times 4) = 60$; $6 + 2(7 \times 3) + 4^2 =$ 64; $6 + 2(2 \times 7) + 2(3 \times 4) = 58$; $5 + 2(2 \times 4) + 3^2 = 30$; $3 + 2(3 \times 2) = 15$; $1 + 2^2 = 5$.

Ex. 2.—The product of any two numbers may be found in the same manner.

The mental work is as follows: $3 \times 2 = 6$; $3 \times 3 + 8 \times 2$ = 25; $2 + 3 \times 4 + 8 \times 3 + 5 \times 2 = 48$; $4 + 3 \times 9 + 8 \times 4$ + $5 \times 3 + 2 \times 2 = 82$; $8 + 8 \times 9 + 5 \times 4 + 2 \times 3 = 106$; $10 + 5 \times 9 + 2 \times 4 = 63$; $6 + 2 \times 9 = 24$.

Ex. 3.—The process of cross-multiplication may be simplified as follows: Required to multiply 4,328 by 736; write the multiplier on a slip of paper in inverse order and place it below the multiplicand with the left hand figure below the units place of the multiplicand thus:

1,32	28	
[637	

Multiply together the figures in the same vertical column $6 \times 8 = 48$; set down the 8 and carry the 4; then move the slip one space to the left thus:

4,328	
63	7
8	

Multiplying together the figures in the same vertical columns and taking the sum, $4 + 6 \times 2 + 3 \times 8 = 40$; set down the 0 and carry the 4; then move the slip one space to the left, multiplying together the figures in the same vertical columns, adding, etc., we will finally have the work standing thus:

	4,328
Γ	637
3,	185,408

Removing the slip we have

The multiplier may be written on the bottom of a sheet in inverse order and placed above the multiplicand instead as above described. The work, however, is very much simplified by simply writing the multiplier in inverse order without using the slip:

The mental work being as follows: $6 \times 8 = 48$; $4 + 6 \times 2 + 3 \times 8 = 40$; $4 + 6 \times 3 + 2 \times 3 + 7 \times 8 = 84$; $8 + 6 \times 4 + 3 \times 3 + 7 \times 2 = 55$; $5 + 3 \times 4 + 7 \times 3 = 38$; $3 + 7 \times 4 = 31$. It will be seen that this device removes most of the mental strain, there being no cross-products.

CONTRACTED MULTIPLICATION.—In multiplying decimals, when the product is required to a few places of decimals, the work may be shortened as follows: Required a product correct to the *nth* decimal place. Write the multiplier with its figures in reverse order, its units place under the *nth* decimal place of the multiplicand. Multiply the multiplicand by the figures in the multiplier, beginning with the right hand figure; rejecting those figures in the multiplicand which are to the right of the figures as a multiplier, increasing each product by as many units as would have been carried from the rejected part of the multiplicand, taking the nearest unit in each case; place the right hand figure of each partial product in the same column, and add as in common multiplication.

In most cases it is best to compute one more place than required. The following examples illustrate the process:

Ex. 1.—The radius of a circle is 420.17 ft. What is its semicircumference to nearest 0.01 ft.? ($\pi = 3.14159265$.)

In the work below the partial products in the contracted multiplication are seen to correspond to the partials of the common method, taken in reverse order, the part to the right of the vertical line being rejected. The contracted multiplication is carried one more place than required. A dot is placed above each figure when it is rejected from the multiplicand.

420.170	420.17
1260510	126051
42017	378153
16807	210085
420	4 2 011 7
210	168068
38	42017
1	126051
1320.003	1320.00313081

Ex. 2.—The observed length of a line is 2231.63 ft. with a tape having a length of 100.018 ft. Required the reduced length of the line to the nearest 0.01 ft.

Noting that each foot of the tape = 1.00018 ft.

2231.63 81000.1	$2\ 2\ 3\ 1.6\ 3$
223163	$\frac{1.00018}{17 85304}$
22 18	$egin{array}{c} 2&2&3&1&6&3\\ 2&2&3&1&6&3&0&0&0 \end{array}$
2232.03	$2\ 2\ 3\ 2.0\ 3 1\ 6\ 9\ 3\ 4$

Ex. 3.—Same observed length with a tape 99.982 ft. long. Required the reduced length.

Each foot of the tape = 0.99982 = (1 - 0.00018) ft.

2 2 3 1.6 3	$2\ 2\ 3\ 1.6\ 3$
81000.0	0.9 9 9 8 2
22	446326
_18	1785304
$\frac{-0.40}{2231.23}$	2008467
	2008467
	2008467
	2231.2283066

Ex. 4.—To compare contracted multiplication with logarithmic work, calculate 861.3 ft. $\times \sin 17^{\circ}$ 19' to the nearest 0.1 ft.

8 6 1.3	log. 8 6 1.3 = 2.9 3 5 1 5
5 6 7 9 2.0	log. sin 17° 19' = 9.4 7 3 7 1
$ \begin{array}{r} 1723 \\ 776 \\ 60 \\ 5 \\ 2564 \end{array} $	log. $(256.4) = 2.40886$

CONTRACTED DIVISION.—If the quotient is desired correct to the *nth* decimal place, the following method may be used: Find one-half of the desired figures in the quotient in the usual way and do not bring down a figure for the last remainder. Drop a figure from the right of the divisor and find another figure in the quotient. Then without bringing down any more figures continue to discard figures from the divisor until the required places are obtained.

Ex 1.—Divide 443.9425 by 24.311 to nearest hundredth. There will be four figures in the quotient, so we will find the first two in the ordinary way. A dot is placed over each figure in the divisor when it is rejected.

$$\begin{array}{r} 2 \ 4.3 \ 2 \\ 2 \ 4.3 \ 2 \\ 2 \ 4.3 \ 2 \\ \hline 2 \ 0 \ 0 \ 7 \ 4 \\ \hline 2 \ 0 \ 0 \ 7 \ 4 \\ \hline 1 \ 9 \ 4 \ 5 \ 6 \\ \hline 6 \ 1 \ 8 \\ \hline 4 \ 8 \ 6 \\ \hline 1 \ 3 \ 2 \\ \hline 1 \ 2 \ 2 \\ \hline 1 \ 0 \\ \hline \end{array}$$

Divisor Near Unity.—When the divisor is near unity a very close approximation is given by the method shown in the following problems:

Ex. 1. $-\frac{5}{1.003254} = 5(1 - .003254) = 5 \times .996746 = 4.98373$

correct to within one unit in the fifth place.

Ex. 2.— $\frac{7}{.9982} = 7(1 + (1 - .9982)) = 7 \times 1.0018 = 7.0126$ correct to the last place.

CONTRACTED SQUARE ROOT.—A result correct to a required number of decimal places may be found by a process similar to the method employed for contracted division.

Ex. 1.—Required the square root of 12,598.87325 correct to thousandths. We see by inspection that the root will contain six figures. Find in the ordinary way the first three figures. Form a new trial divisor in the usual way,

$$\begin{array}{r} 12598.87325(112.245) \\
\underline{1}\\21)25 \\
\underline{21}\\222)498 \\
\underline{444}\\2244)548 \\
\underline{448}\\100 \\
\underline{89}\\11 \\
\underline{11}\\2
\end{array}$$

232

and bring down only one figure for the dividend in place of two. Find the remaining figures by contracted division.

The last figure brought down is not increased whatever it may be followed by, since the contracted process tends to make the result a little too large. This method may be applied to the extraction of cube roots, where it saves much work in finding long trial divisors.

Square Root of Small Numbers.—The approximate square roots of small numbers may be found by means of the following rule: Divide the given number by the number whose square is nearest the given number. The arithmetical mean of the quotient and divisor will be the approximate square root of the number. The nearer the number is to a perfect square the less the error. For example,

Ex. 1.— $\sqrt{35} = (35\% + 6) \div 2 = 5.92$. *Ex.* 2.— $\sqrt{8} = (\% + 3) \div 2 = 2.83$. *Ex.* 3.— $\sqrt{79} = (7\% + 9) \div 2 = 8.89$. *Ex.* 4.— $\sqrt{128} = (12\%1 + 11) \div 2 = 11.31$.

Square Root by Subtraction.—While it possesses no points of merit in this connection, it would not be proper to pass the subject of square root without presenting the novel method of extracting square roots used with the Thomas Computing machine. The method depends upon the relation existing between odd numbers and squares in the system of numbers having a radix ten. If we sum up the odd numbers, beginning at 1, we will observe the following relation:

 $1 = 1^2$; $1 + 3 = 4 = 2^2$; $1 + 3 + 5 = 9 = 3^2$; $1 + 3 + 5 + 7 = 16 = 4^2$, etc. It will be seen that the square root of the sum in each case is the number of the group.

The method of extracting square roots is as follows: Point off in periods of two figures each. Subtract from the left hand period the odd numbers in order, beginning at unity, until a remainder is obtained less than the next odd number. Write for the first figure in the root the number which represents the number of subtractions made. Double the root already found and annex unity. Subtract as before, using for subtrahends the successive odd numbers, the root figure being the number of subtractions made. Ex. 1.-Extract the square root of 53,824.

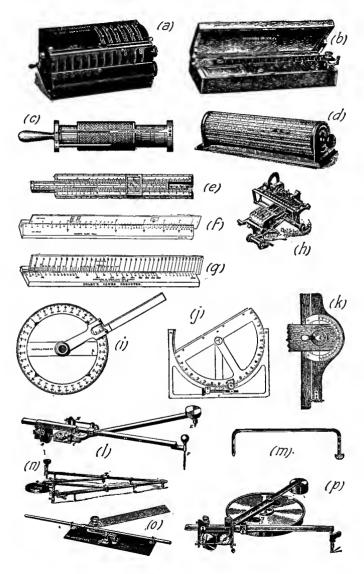
```
53824(232
    1
    4
    3...
            . 2 subtractions,
41)138
     41
     97
     43
     54
     45....3 subtractions.
 461)924
       461
       463
       463...2 subtractions.
         ō
```

RECKONING TABLES.—Tables for use in computing are so numerous and well known that it would be useless to try to refer to them by name. Two valuable tables for obtaining products of numbers—which are well known in Germany, but comparatively unknown in this country—are, "Crelle's Rechentafeln," which gives the products of numbers of three significant figures by three significant figures to 999 by 999; and "Zimmerman's Recheutafeln," which gives the products of numbers of two places of significant figures by numbers of three significant figures to 100 by 999.

COMPUTING MACHINES.—In Fig. 40, (a) is a Kuttner reckoning machine; (b) a Thomas computing machine; (c) a Fuller slide rule; (d) a Thacher slide rule; (e) an ordinary slide rule; (f) a Colby Stadia slide rule; (g) a Colby sewer slide rule; (h) a Grant calculating machine; (i) a full circle protractor; (j) a Crozet protractor; (k) a protractor tee square; (l) a polar planimeter; (m) a "jack knife" planimeter; (n) a pantagraph; (o) a section liner; (p) a spherical planimeter.

In using the "jack knife" planimeter, the point is placed at the center of gravity, and the knife edge is placed on a line passing through the center of gravity of the figure. The point is then made to traverse the perimeter of the figure to be measured; passing out to the perimeter and returning to the center of gravity of the figure on the same line. The distance from the final position of the knife edge to the line through the center of gravity, multiplied by the

COMPUTING INSTRUMENTS.



length of the arm of the planimeter will give the area of the figure. The arm of the planimeter is usually made ten inches long and the distance measured in inches.

The correct area may be obtained by means of the hatchet planimeter, without using the center of gravity of the figure, as follows: (1) Draw a tangent to the figure. (2) Trace the figure with the point starting with the hatchet on the tangent and the point at the point of tangency. (3) Trace the figure as before except that the point is to move around in the opposite direction. (4) The arithmetical mean of the two areas will be the true area. That this method is correct can be easily proved by the student.

The other machines are described in the instructions accompanying them when purchased.

CHAPTER XI.

TOPOGRAPHIC DRAWING AND LETTERING.

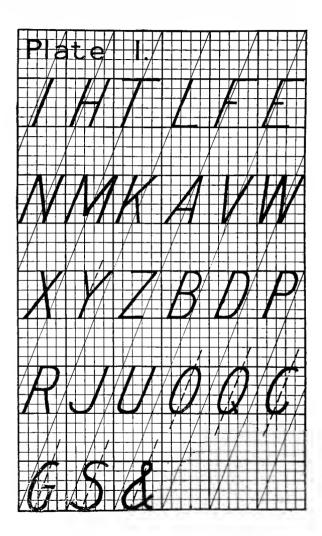
LETTERING.—A magnified scale is used in the first six plates to give familiarity with form of letter and numeral, and also to produce freedom of hand motion. The six plates should first be made with a soft pencil sharpened to a needle point, and afterward with pen and india ink. In Plate 7 the height of letter is that prescribed in Chapter I. This standard size is not only well adapted to field notes and general drafting, but is economical of execution.

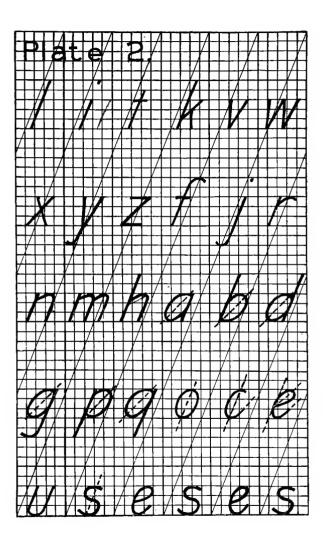
The student should train the eve and acquire a "swing" of the hand by industrious practice in such exercises as the following: (1) Pass a line freehand through two points: first sketch in the line roughly by a free swing of the forearm; then partially erase and retrace; finally test result with ruler. (2) Pass a circular arc through three points freehand; follow sketch method just described and, after perfecting the arc, sketch in the chords and locate the center freehand; test result mechanically. (3) Inscribe a circle in a square. (4) Inscribe an ellipse in a rectangle. (5)Inscribe an ellipse in an oblique parallelogram. (In the last three exercises give particular attention to points and lines of tangency and axes of symmetry.) After making the line or figure satisfactorily with pencil, it should be executed freehand in India ink.

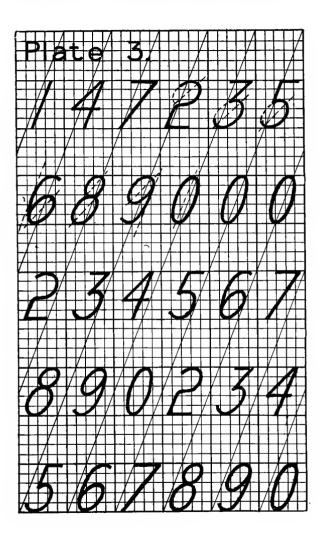
Practice should include spacing of letters and words, and for this purpose it is suggested that the student use the "specifications for a good engineer" following the preface.

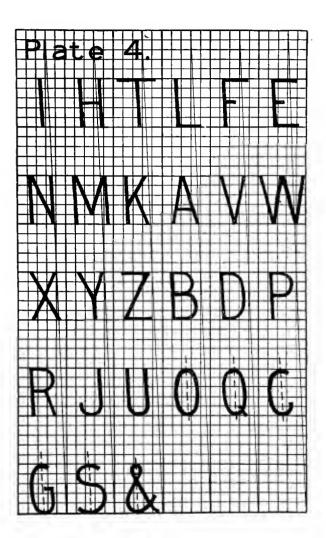
The student should not be content until he can make letters freehand so well that a close inspection is required to determine that they were not made mechanically.

Freehand Titles.—Good freehand titles suffice for most drawings. In a good title consistent emphasis is given to the several parts, and the title as a whole accords with the purpose and character of the drawing. Elaborate and ornamental titles have a limited application, and should not be attempted at all unless the draftsman has special skill

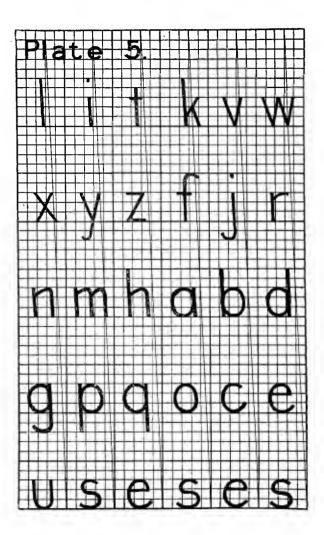


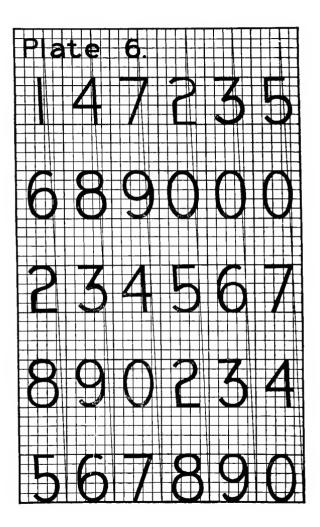


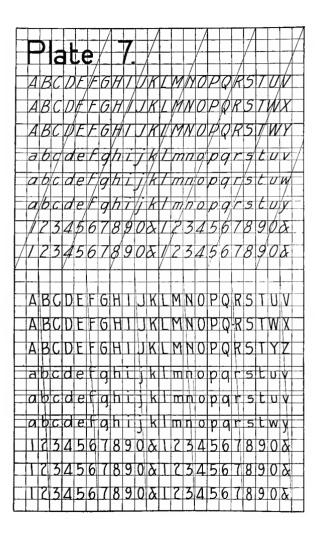




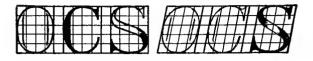
241







in such work. In designing titles, whether freehand or mechanical, skill in sketching in the outlines, guide lines, axes of symmetry, etc., is of much importance. On the following pages are a few examples of good titles.





DRAWING PENS.—The following pens, arranged in order of fineness, will give sufficient variety for ordinary work.

Gillott's 170, very fine, for very small lettering.

Gillott's 303, extra fine, for small lettering.

Gillott's 404, fine, for small lettering.

Hunt 21, medium, for ordinary lettering.

Hunt 512, Shot Point, for ordinary lettering.

Leonardt 510, E. F. Ball Point, for large lettering and titles.

Hunt 513, Round Point, for large lettering and titles.

Leonardt 516, E. F. Ball Point, for large lettering and titles.

Leonardt 516 F., Ball Point, for very large lettering and titles.

Payzant Pens, K. & E. Co., Nos. 6, 5, 4, 3, 2, 1, for titles. The following rules should be observed in making letters on drawings free hand.

Use the quill in inking the pen.

Never dip the pen in the ink bottle.

Keep the pen clean.

Ink must not be allowed to dry on the pen and spread the points.

Before using a new pen moisten the points and wipe it dry to insure a free flow of ink.

TOPOGRAPHIC SYMBOLS.—The standard symbols for topographic drawings adopted by the American Railway Engineering Association are given on pages 248 to 251.

RIGHT-OF-WAY MAP NEW YORK AND DENVER R.R.

Station 331+55 to Station 542+75 Scale 1 in.=400 Ft. January 3, 1915 Office of Chief Engineer Denver, Colorado.

RIGHT-OF-WAY MAP NEWYORK AND DENVER R.R. Station 331+55 to Station 511+10 Scale 1 in = 400 ft. January 30, 1915 Office of Chief Engineer Denver, Colorado.

TOPOGRAPHIC MAP

CITY OF BOULDER, COLORADO

Surveyed by the GLASS IN TOPOGRAPHIC SURVEYING UNIVERSITY OF COLORADO FIRST SEMESTER 1914-19 Scale 1117=500 ft.

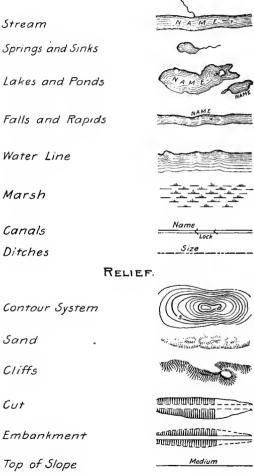
Right-of-Way Map NEW YORK AND DENVER R. R.

Station 331+55 to Station 542+75 Scale 1 in = 400 Ft. January 3,1915 Office of Chief Engineer Denver, Colorado.

RIGHT-OF-WAY MAP NEW YORK & DENVER R.R. Station 331+55 to Station 511+10 Scale 1 in=400ft. January 1, 1915 Office of Chief Engineer Denver, Colorado.

Topographic Map of the CITY OF BOULDER, COLORADO Surveyed by the Class in Topographic Surveying University of Colorado First Semester 1914-15 Scale 1in=500st.

248 TOPOGRAPHIC DRAWING AND LETTERING.



HYDROGRAPHY.

Marsh

Canals

Ditches



Contour System

Sand

Cliffs

Cut

Embankment

Top of Slope Bottom of Slope

Fine ____

* RAILWAYS (TOPOGRAPHICAL MAPS.)

* RAILWAY TRACKS (TRACK MAPS.)

Railway Track or Old Track to Remain	
Old Track to be Taken up	
Proposed Tracks	Red
Proposed (Future) Tracks	
Foreign Tracks	Color other thon Red or Black with Initials of Road
Alinement { 4°Curve to Right } 2° , Left }	4°C.R. 2°C.L

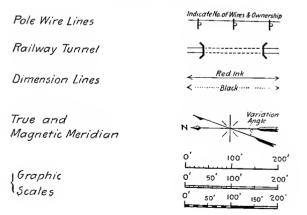
BOUNDARY AND SURVEY LINES.

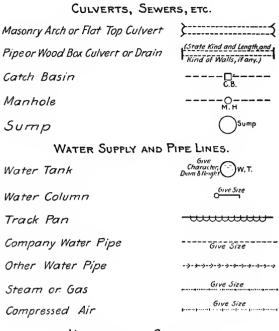
{Political Divisions; State, County or Township Lines. {Government Surveys, Base, Meridian, Township, Section or Harbor Line	<u>Bethel</u> Twp Wayn <u>e</u> Co., Mich. Posey Twp Adams Ca., Ind. <u>Sec. 18, T. 12 N., R. 15, 3rd P.M.</u> Sec. 13, T. 11 N., R. 16, 3 rd P.M.
Street, Block or other Property Line	
Survey Lines	Red Preliminary
Center Lines	Original (Track or)Center Line 19 If Monumented, Show Location and Proper Symbol
Company Property Line	
Fence (on Street Line)	State Kind and Height
Fence (on Company Property Line)	State Kind and Height

* For Railway Track and Yard Studies Use Single or Double Lines.

City	
Village	
City Limits	
Fire Limits	
Section Corner	17 16
Section Center	
Triangulation Station or Transit	Point 🛆
Bench Mark	B.M.×1232
Stone Monument	
Iron Monument	

MISCELLANEOUS.





HIGHWAYS AND CROSSINGS.

Public and Main Roads	
Private and Secondary Roads	====
Trails	
Street and Public Road Crossings	=/
Private Road Crossing	









BRIDGES.

Girder

Truss

Trestle

SURVEYING MANUAL Part II

FIELD AND OFFICE TABLES FOR USE IN SURVEYING.

ВY

WILLIAM D. PENCE

AND

MILO S. KETCHUM

Table 1. Logarithms of Numbers.

Table 2. Logarithmic Functions of Angles.

Table 3. Natural Functions of Angles.

Table 4. Squares, Cubes, Square Roots, Cube Roots and Circles.

Table 5. Trigonometric Functions.

Explanation of Tables.

The authors wish to thank the J. B. Lippincott Company for the use of Tables 1 and 2 taken from Suplee's "Five Place Logarithms," and Table 3 taken from Suplee's "Mechanical Engineers' Reference Book"; and the McGraw-Hill Book Company for the use of Tables 4 and 5, taken from Harger and Bonney's "Highway Engineers' Handbook."

All of the above tables are fully protected by copyright.

Num. 100 to 139. Log. 000 to 145.

	N	L	0 4	1	2	3	4	5	6	7	8	9	P. P.
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	101		432	475	518	561	604	647	689	732	775	817	1 4.4 4.3
	102		860	903	945	988	*030	*072	*115	*157	*199	*242	2 8.8 8.6
	103	01	284	326	368	410	452	494	536	578	620	662	
1060.21131062.02.32.40.00.03.010710.83.685.85.285.285.28.385.285.25.3 <t< td=""><td>104</td><td></td><td>703</td><td>745</td><td>787</td><td>828</td><td>870</td><td>912</td><td>953</td><td>995</td><td>*036</td><td>*078</td><td>5 22.0 21.5</td></t<>	104		703	745	787	828	870	912	953	995	*036	*078	5 22.0 21.5
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11506070108145183221258296333371408937.8311644648352155859563367070774478140117819856893930967*004*004*078*115*15111180718822526229835337240844548251814.0119555591628664700737773809846882112.01120918954990*027*063*099*135*171*207*24311.2012.0112108279314350386422458493529565600624.02122636672707743778814849884920955838.2.6391240934237712447482517552587621656338118.8112569170210614017520924327881234618.811.6111.61.41.51.611.61.41.51.61.61.81.61.61.81.61.61.81.6 <td< td=""><td>114</td><td></td><td>690</td><td>729</td><td>767</td><td>805</td><td>843</td><td>881</td><td>918</td><td>956</td><td>994</td><td>*032</td><td>7 29.4 28.7</td></td<>	114		6 9 0	729	767	805	843	881	918	956	994	*032	7 29.4 28.7
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12108279314350353135111 513 111 513 111 513 111 513 <td>119</td> <td></td> <td>555</td> <td>591</td> <td>628</td> <td>664</td> <td>700</td> <td>737</td> <td>773</td> <td>809</td> <td>846</td> <td></td> <td>2 8.0 7.8</td>	119		555	591	628	664	700	737	773	809	846		2 8.0 7.8
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129 11 059 093 126 160 193 227 261 294 327 361 5 19.0 11 6 19.0 11 6 19.0 11 6 19.0 11 6 19.0 11 6 19.0 11 6 12.8 7 361 5 19.0 11 6 22.8 2 12 327 361 5 19.0 11 6 22.8 2 561 594 628 661 694 7 26.6 22 131 727 760 793 826 860 893 92.6 959 992 492.4 8 30.4 2 93.4 2 32.4 2 32.4 2 33.4 12 33 365 14.8 506 858 857 967 969 9001 1 1.6 14 34 710 743 775 808 840 872 965 937 969 9001 1 1.6 1 1.6 1.6 1.8 1	128		721	755	789	823	857	890	924	958	992	*025	
130 394 428 461 494 528 561 594 628 661 694 7 26.6 22 131 727 760 793 826 860 893 926 959 992 *024 8 30.4 22 9 322 254 287 320 352 9 92 *024 9 9 34.2 2 9 34.2 12 9 34.2 33 385 418 450 483 516 548 581 613 646 678 36<	129	11	Q59	003	126	160	19 3	227	261	294	327	361	5 19.0 18.5
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	131		727	760	793	826	860	893	9 26	959	992	*024	8 30.4 29.6
133 385 418 450 483 516 548 581 613 646 678 36 134 710 743 775 808 840 872 905 937 969 *001 1 3.6 1 135 13 033 066 098 130 162 194 226 258 290 322 2 7.7 3 10.8 14 14.8 14 14.8 14 14.8 14 14.8 14 14.8 14 14.4 <td< td=""><td>132</td><td>12</td><td>057</td><td>090</td><td>123</td><td>166</td><td>189</td><td>222</td><td>254</td><td>287</td><td>320</td><td>352</td><td>9 34.2 33.3</td></td<>	132	12	057	090	123	166	189	222	254	287	320	352	9 34.2 33.3
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138 988 *019 *051 *082 *114 *145 *176 *208 *239 *270 6 21.6 2 139 14 301 333 364 395 426 457 489 520 551 582 8 28.8 2 4 27 25.2 2 2 140 613 644 675 706 737 768 799 829 860 891 9 32.4 3													4 14.4 14.0
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140 613 644 675 706 737 768 799 829 860 891 9 32.4 3		14						1					7 25.2 24.5
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Num. 140 to 179. Log. 146 to 255.

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140	14	613	644	675	706	737	768	799	829	860	891		34	33
141		922	953		*014			*106			*198			
142	15	229	259	290	320	351	381	412	442	473	503	$\frac{1}{2}$	3.4 6.8	3.3 6.6
143		534	564	594	625	655	685	715	746	776	806	3	10.2	9.9
144		836	866	897	927	957	987	*017		*077	*107	4	13.6	13.2
											100	5 6	$17.0 \\ 20.4$	$16.5 \\ 19.8$
145	16	137	167	197	227	256	286	316	346	376	406	7	23.8	23.1
146		455	465	495	524	554	584	613	643	673	702	8	27.2	26.4
147		732	761	791	820	850	879	909	938	967	997	9	30.6	29.7
148	17	026	056	085	114	143	173	202	231	260	289		32	31
149		319	348	377	406	435	464	493	522	551	580			3.1
150		609	638	667	696	725	754	782	811	840	869	$\frac{1}{2}$	3.2 6.4	6.2
151		898	926	955	984	*013	*041	*070	*099	*127	*156	23	9.6	9.3
152	18	184	213	241	270	298	327	355	384	41 2	441	45	$12.8 \\ 16.0$	$12.4 \\ 15.5$
153		469	498	526	554	583	611	639	667	696	724	6	19.2	18.6
154		752	780	808	837	865	893	921	949	977	*005	7	22.4	$\frac{21.7}{24.8}$
155	19	033	061	089	117	145	173	201	229	257	285	89	25.6 28.8	24.8
156	10	312	340	368	396	424	451	479	507	535	562	-		
157		590	618	645	673	700	728	756	783	811	838		30	29
158		866	893	921	948	976	*003	*030		*085	*112	1	3.0	2.9
159	20	140	167	194	222	249	276	303	330	358	385	2	6.0	5.8
					100	500	F 40		400		050	34	9.0 12.0	8.7
160		412	439	466	493	520	548	575	602	629	656	5	15.0	14.5
161		683	710	737	763	790	817	844	871	898	925	6	18.0	17.4
162	~	952	978	*005	*032		*085				*192	78	$21.0 \\ 24.0$	20.3 23.2
163	21	219	245	272	299	325	352	378		431 696	$\frac{458}{722}$	9	27.0	26.1
164		484	511	537	564	590	617	643	669	090	722		28	27
165		748	775	801	827	854	880	906	932	958	9 85			
166	22	011	037	063	089	115	141	167		220	246	1	2.8	2.7
167		272	298	324	350	376	401	427		479	505	2	5.6 8.4	5.4
168		531	557	583	608	634	660	686		737	763	34	11.2	10.8
169		789	814	840	.866	891	917	943	968	994	*019	56	14.0 16.8	$13.5 \\ 16.2$
170	23	045	070	096	121	147	172	198	223	249	274	7	19.6	18.9
171		300	325	850	376	401	426	452	477	502	528	89	$22.4 \\ 25.2$	21.6 24.3
172		553	578	603	629	654	679	704	729	754	779	9	20.2	24.0
173		805	830	855	880	905	930	955	980	*005	*030		26	25
174	24	055	080	105	130	155	180	204	229	254	279	1	2.6	2.5
175		304	329	353	378	403	428	452	477	502	527	23	5.2	5.0
175		551	576	601	625	650	674	699			773	34	7.8	7.5
170		797	822	846	871	895	920	944			*018	- 5	10.4	10.0 12.5
177	25	042	066	091	115	139	164				261	6	15.6	15.0
179	40	285	310	334	358	382	406	431		479	503	7	$18.2 \\ 20.8$	17.5
1							648	672			744	9	20.8 23.4	20.0
180		527	551	575	600	624						_		
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Num. 180 to 219. Log. 255 to 342.

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180	25	527	551	575	600	624	648	672	696	720	744		24	ł
181		768	792	816	840	864	888	912	935	959	983	1	2.4	. ·
182	26	007	031	055	079	102	126	150	174	198	221	$\begin{array}{c} 1\\ 2\end{array}$	4.8	
183		245	269	293	316	340	364	887	411	435	458	3	7.5	2
184		482	505	529	553	576	600	623	647	670	694	4	9.0	
											000	5	12.0 14.4	
185		717	741	764	788	811	834	858	881	905	928	7	16 \$	8
186		951	975			*045		*091				8	19	2
187	27	184	207	231	254	277	300	323	346	370	393	9	21.0	j
188		416	439	462	485	508	531	554	57 <u>7</u>	600	623		23	3
189		646	669	692	715	738	761	784	807	830	852		2.1	
190		875	898	921	944	967	989			*058		$\frac{1}{2}$	4.0	6
191	28	103	126	149	171	194	217	240	262	285	307	3	6. 9.	9
192		330	353	375	398	421	443	466	488	511	533	4 5	9.11.1	2 5
193		556	578	601	623	646	668	691	713	735	758	6	13.	
194		780	803	825	847	870	892	914	937	959	981	78	$16.1 \\ 18.4$	1
195	29	003	026	048	070	092	115	137	159	181	203	9	20.	
196		226	248	270	292	314	336	358	380	403	425		22	•
197		447	469	491	513	535	557	579	601	623	645		44	5
198		667	688	710	732	754	776	798	820	842	863	1	2.3	
199		885	907	929	951	973		*016	*038	*060	*081	$\begin{bmatrix} 2\\ 3 \end{bmatrix}$	4.4	
200	30	103	125	146	168	190	211	233	255	276	298	45	8. 11.	8
201		320	341	363	384	406	428	449	471	492	514	6	13.	2
202		535	557	578	600	621	643	664	685	707	728	7	15.	4
203		750	771	792	814	835	856	878	899	920	942	8	17. 19.	
204		963	984	*006	*027	*048	*069	*091	*112	*1 33	*154	5		
205	31	175	197	218	239	260	281	302	323	345	366		2	1
206		387	408	429	450	471	492	513	534	555	576	1	2.	1
207		597	618	639	660	681	702	723	744	765	785	23	4. 6.	2
208		806	827	848	869	890	911	931	952	973	994		8.	
209	32	015	035	056	077	098	118	139	160	181	201	5	10.	5
210		222	243	263	284	305	325	346	366	387	408	67	12.14.	7
211		428	449	469	490	510	531	552	572	593	613	8	16.	
212		634	654	675	695	715	736	756	777	797	818	9	18.	a
213		838	858	879	899	919	940	960	980		*021		20	19
214	33	041	062	082	102		143	163	183	203	224		2.0	1.9
215		244	264	284	304	325	345	365	385	405	425	2	4.0	3.8
216		445	465	486	506	526	546	566	586	606	626		6.0	5.7
210		646	666	686	706	726	746	766	786	806	826		$\left \begin{array}{c} 8.0 \\ 0.0 \end{array} \right $	7.6 9.5
217		846	866	885	905	925	945	965	985		*025	6 1	2.0	11.4
218	34	044	064	084	104	5_5 124	143	163	183	203	223	7 1	4.0	$\frac{13}{15.2}$
220		242	262	282	301	321	341	361	380	400	420		8.0	
N		0	1	2	3	4	5	6	7	8	9	p	. P	
		-		~				-			-	1	-	

Num. 220 to 259. Log. 342 to 414.

N	. L	0	ť	2	3	4	5	6	7	8	9	P. P.
220	34	242	262	282	301	321	341	361	380	400	420	
221		439	459	479	498	518	537	557	577	596	616	20
222		635	655	674	694	713	733	753	772	792	811	1 2.0
223		830	850	869	889	908	928	947	967	986	*005	2 4.0
224	35	025	044	064	083	102	122	141	160	180	199	3 6.0 4 8.0
225		218	238	257	276	295	315	334	353	372	392	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
226		411	430	449	468	488	507	526	545	564	583	7 14.0
227		603	622	641	660	679	698	717	736	755	774	8 16.0 9 18.0
228		793	813	832	851	870	889	908	927	946	965	3 10.0
229		984	*003	*021	*040	*059	*078	*097	*116	*135	*154	
230	36	173	192	211	229	248	267	286	305	324	342	19
231		361	380	399	418	436	455	474	493	511	530	19
232		549	568	586	605	624	642	661	680	698	717	1 1.9
233		736	754	773	791	810	829	847	866	884	903	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
234		922	940	959	977	996	*014	*033	*051	*070	*088	4 7.6
235	37	107	125	144	162	181	199	218	236	254	273	6 11.4
236		291	310	328	346	365	383	401	420	438	457	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
237		475	493	511	530	548	566	585	603	621	639	8 15.2 9 17.1
238		658	676	694	712	731	749	767	785	803	822	
239		840	858	876	894	912	931	949	967	985	*003	
240	38	021	039	057	075	093	112	130	148	166	184	
241		202	220	238	256	274	292	310	328	346	364	18
242		382	399	417	435	453	471	489	507	525	543	
243		561	578	596	614	632	650	668	686	703	721	1 1.8
244		739	757	775	792	810	828	846	863	881	899	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
245		917	934	952	970	987	*005	*023	*041	*058	*076	4 7.2 5 9.0
246	39	094	111	129	146	164	182	199	217	235	252	6 10.8
247		270	287	305	322	340	358	375	393	410	428	7 12.6
248		445	463	480	498	515	533	550	568	585	602	$\begin{array}{c cccc} 7 & 12.6 \\ 8 & 14.4 \\ 9 & 16.2 \end{array}$
249		620	637	655	672	690	707	724	742	759	777	5 10.2
250		794	811	829	846	863	881	898	915	933	950	
251		967	985	*002	*019	*037	*054	*071	*088	*106	*123	
252	40	140	157	175	192	209	226	243	261	278	295	
253		312	329	346	364	381	398	415	432	449	466	17
254		483	500	518	535	552	569	586	603	620	637	1 1.7
255		654	671	688	705	722	739	756	773	790	807	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
256		824	841	858	875	892	909	926	943	960	976	4 6.8
257		993	*010	*027	*044	*061	*078	*095	*111		*145	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
258	41	162	179	196	212	229	246	263	280	296	313	7 11.9
259		330	347	363	380	397	414	430	447	464	481	$\begin{array}{c ccc} 7 & 11.9 \\ 8 & 13.6 \\ 9 & 15.3 \end{array}$
260		497	514	531	547	564	581	597	614	631	647	3 1 1010
N	L	0	1	2	3	4	5	6	7	8	9	P. P.

Num. 260 to 299. Log. 414 to 476.

					. 414	Log	299.	υ το	. 20	Num			
. Р.	Р	9	8	7	6	5	4	3	2	1	0	L.	N
		647	631	614	597	581	564	547	531	514	497	41	260
		814	797	780	764	747	731	714	697	681	664		261
		979	963	946	929	913	896	880	863	847	830		262
		144	*127	*111	*095	*078	*062	*045	*029	*012	996		263
17		308	292	275	259	243	226	210	193	177	160	42	264
1.7	1	472	455	439	423	40 6	390	374	357	341	325		265
3.4	2	635	619	602	586	570	553	537	521	504	488		266
5.1	3	797	781	765	749	732	716	700	684	667	651		267
$6.8 \\ 8.5$	4 5	959	943	927	911	894	878	862	846	830	813		268
10.2 11.9	5 6 7	*120	*104	*088	*072	*056	*040	*024	*008	991	975		269
13.6	78	281	265	249	233	217	201	185	169	152	136	43	270
15.3	9	441	425	409	393	377	361	345	329	313	297		271
		600	584	569	553	537	521	505	489	473	457		272
		759	743	727	712	696	680	664	648	632	616		273
		917	902	886	870	854	838	823	807	791	775		274
		*075					996	981	965	949	933		275
16		232	217	201	185	170	154	138	122	107	091	44	276
		389	373	358	342	326	311	295	279	264	248		277
$\frac{1.6}{3.2}$	$\frac{1}{2}$	545	529	514	498	483	467	451	436	420	404		278
4.8	3	700	685	669	654	638	623	607	592	576	560		279
$\begin{array}{c} 6.4 \\ 8.0 \end{array}$	4 5	855	840	824	809	793	778	762	747	731	716		280
9.6	5 6	*010		979	963	948	932	917	902	886	871		281
$\frac{11.2}{12.8}$	$\frac{7}{8}$	163	148	133	117	102	086	071	056	040	025	45	282
14.4	9	317	301	286	271	255	240	225	209	194	179		283
		469	454	439	423	408	393	378	362	347	332		284
		621	606	591	576	561	545	530	515	500	484		285
		773	758	743	728	712	697	682	667	652	637		286
		924	909	894	879	864	849	834	818	803	788		287
		*075		*045			*000		969	954	939		288
15		225	210	195	180	165	150	135	120	105	090	46	289
$1.5 \\ 3.0$	1	374	359	345	330	315	300	285	270	255	240		290
4.5	$\frac{2}{3}$	523	509	494	479	464	449	434	419	404	389		291
6.0	4	672	657	642	627	613	598	583	568	553	538		292
7.5 9.0	5	820	805	790	776	761	746	731	716	702	687		293
10.5	6 7 8	967	953	938	923	909	894	879	864	850	835		294
12.0 13.5	8 9		*100					*026		997	982		295
	_	261	246	232	217	202	188	173	159	144	129	47	296
		407	392	378	363	349	334	319	305	290	276		297
		553	538	524	509	494	480	465	451	436	422		298
		698	683	669	654	640	625	611	596	582	567		299
		842	828	813	799	784	770	756	741	727	712		300
. Р.	Р	9	8	7	6	5	4	3	2	1	0	L	N

Num. 300 to 339. Log. 477 to 531.

N	L	0	1	2	3	4	5	6	7	8	9	Ρ.	Р.	_
300	47	712	727	741	756	770	784	799	813	828	842			
301		857	871	885	900	914	929	943	958	972	986			
302	48	001	015	029	044	058	073	087	101	116	130			
303		144	159	173	187	202	216	230	244	259	273			
304		287	302	31 6	330	344	359	373	387	401	416		14	
305		430	444	458	473	487	501	515	530	544	558	1	1.4	
306		572	586	601	615	629	643	657	671	686	700	23	2.8	
307		714	728	742	756	770	785	799	813	827	841	34	4.2 5.6`	
308		855	869	883	897	911	926	94 0	954	968	982	5	7.0	
309		9 9 6	*010	*024	*038	*052	*066	*080	*094	*108	*122	6 7	8.4 9.8	
310	49	136	150	164	178	192	206	220	234	248	262	8	11.2	
311		276	290	304	318	332	346	360	374	388	402	9	12.6	
312		415	429	443	457	471	485	499	513	527	541			
313		•554	568	582	596	610	624	638	651	665	679			
314		693	707	721	734	748	762	776	790	803	817			
315		831	845	859	872	886	90 0	914	927	941	955			
316		969	982		*010				*065		*092		13	
317	50	106	120	133	147	161	174	188	202	215	229			
318		243	256	270	284	297	311	325	338	352	365	$\frac{1}{2}$	$\frac{1.3}{2.6}$	
319		379	393	406	420	433	447	461	474	488	501	3	3.9	
320		515	529	542	556	569	583	596	610	623	637	4 5	$5.2 \\ 6.5$	
321		651	664	678	691	705	718	732	745	759	772	6	7.8	
322		786	799	813	826	840	853	866	880	893	907	7	9.1	
323		920	934	947	961	974	987		*014		*041	8 , 9	10.4 11.7	
324	51	055	068	081	095	108	121	135	148	162	175			
325		188	202	215	228	242	255	268	282	295	308			
326		322	335	348	362	375	388	402	415	428	441			
327		455	468		495	508	521	534	548	561	574	1		
328		587	601	614	627	640	654	667	680	693	706			
329		720	733	746	759	772	786	799	812	825	838		12	
330		851	865		891	904	917	930	943	957	970	$\frac{1}{2}$	$1.2 \\ 2.4$	
331		983			*022		*048		*075		*101	$\frac{2}{3}$	2.4 3.6	
332	52	114		140			179	192	205	218	231	4	4.8	
333		244		270			310	323	336	349	362	5	$\frac{6.0}{7.2}$	
334		375	388	401	414	427	440	453	466	479	492	7	8.4	
335		504				556	569	582	595	608	621	8	9.6 10.8	
336		634		660			699	711	724		750	'		
337		763					827	840	853	866	879			
338		892					956	969	982		*007			
339	53	020	033	046	058	071	084	097	110	122	135			
340		148	161	173	186	199	212	224	237	250	263			
N	L	0	1	2	3	4	5	6	7	8	9	D	. Р.	

Num. 340 to 379. Log. 531 to 579.

N	L	0	1	2	3	4	5	6	7	8	9	Р	. Р.
340	53	148	161	173	186	199	212	224	237	250	263		
341	00	275	288	301	314	326	339	352	364	377	390		
342		403	415	428	441	453	466	479	491	504	517		
					441 567		593	605	618	631	643		
343		529	542	555		580					769		
344		656	668	681	694	706	719	732	744	757	109		13
345		782	794	807	820	832	845	857	870	882	895	1	1.3
346		908	920	933	945	958	970	983	995	*008	*020	2	2.6
347	54	033	045	058	070	083	095	108	120	133	145	$\overline{2} \\ 3$	3.9
348		158	170	183	195	208	220	233	245	258	270	4	5.2
349		283	295	307	320	332	345	357	370	382	394	$\frac{5}{6}$	$\begin{array}{c} 6.5 \\ 7.8 \end{array}$
350		407	419	432	444	456	469	481	494	506	518	789	9.1 10.4
351		531	543	555	568	580	593	605	617	630	642	9	11.7
352		654	667	679	691	704	716	728	741	753	765		
353		777	790	802	814	827	839	851	864	876	888		
354		900	913	925	937	949	962	974	986		*011		
355	55	023	035	047	060	072	084	096	108	121	133		
356		145	157	169	182	194	206	218	230	242	255		
357		267	279	291	303	315	328	340	352	364	376		12
358		388	400	413	425	437	449	461	473	485	497	1	1.2
359		509	522	534	546	558	570	582	594	606	618	$\frac{\overline{2}}{3}$	$\frac{2.4}{3.6}$
360		630	642	654	666	678	691	703	715	727	739	45	4.8
361		751	763	775	787	799	811	823	835	847	859	6	7.2
362		871	883	895	907	919	931	943	955	967	979	7	8.4
363		991	*003	*015	*027	*038	*050	*062	*074	*086	*098	8	9.6 10.8
364	56	1 10	122	134	146	158	170	182	194	205	217	5	10.0
365		229	241	253	265	277	289	301	312	324	336		
366		348	360	372	384	396	407	419	4 3 1	443	455		
367		467	478	490	502	514	526	538	549	561	573		
368		585	597	608	620	632	644	656	667	679	691		
369		703	714	726	738	750	761	773	785	797	808		11
370		820	832	844	855	867	879	891	902	914	926	1	1.1
371		937	949	961	972	984	996	*008	*019	*031	*043	2	2.2
372	57	054	066	078	089	101	113	124	136	148	159	3 4	3.3 4.4
373		171	183	194	206	217	229	241	252	264	276	5	5.5
374		287	299	310	322	334	345	357	368	380	392	67	6.6
375		403	415	426	438	449	461	473	484	496	507	89	8.8 9.9
376		519	530	542	553	565	576	,588	600	611	623	3	1 9.9
377		634	646	657	669	680	692	703	715	726	738	1	
378		749	761	772	784	795	807	818	830	841	852		
379		864	875	887	898	910	921	933	944	955	967		
380		978	990	*001	*013	*024	*035	*047	*058	*070	*081		
N	L	0	1	2	3	4	5	6	7	8	9	P	. P.

Num. 380 to 419. Log. 579 to 623.

N													
	L	0	1	2	3	4	5	6	7	8	9	Р.	р.
380	57	978	990	*001	*013	*024	*035	*047	*058	*070	*081		
381	58	092	104	115	127	138	149	161	172	184	195		
382		206	218	229	240	252	263	274	286	297	309 -		
383		320	331	343	354	365	377	388	399	410	422		
384		433	444	456	467	478	490	501	512	524	535		11
385		546	557	569	580	591	602	614	625	636	647	1	1.1
386		659	670	681	692	704	715	726	737	749	760	$\frac{1}{2}$	2.2
387		771	782	794	805	816	827	838	850	861	872	3	3.3
388		883	894	906	917	928	939	950	961	973	984	4	4.4
389		995	*006	*017	*028	*040	*051	*062	*073	*084	*095	2 3 4 5 6 7	$5.5 \\ 6.6$
390	59	106	118	129	140	151	162	173	184	195	207	89	7.7 8.8
391		218	229	240	251	262	273	284	295	306	318	9	9.9
392		329	340	351	362	-373	384	395	40 6	417	428		
393		439	450	461	472	483	494	506	517	528	539		
394		550	561	572	583	594	605	616	627	638	649		
395		660	671	682	693	704	715	726	737	748	759		
396		770	780	791	802	813	824	835	846	857	868		10
397		879	890	901	912	923	934	945	956	966	977		
398		988	999		*021				*065			1	1.0
399	60	097	108	119	130	141	152	163	173	184	195	$ \begin{array}{c} 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{array} $	2.0 3.0
400		206	217	228	239	249	260	271	282	293	304	4	4.0 5.0
401		314	325	336	347	358	369	379	390			6	6.0
402		423	433	444	455	466	477	487	498	509	520	7	7.0
403		531	541	552	563	574	584	595	606	617	627	8	8.0 9.0
404		638	649	660	670	681	692	703	713	724	735	5	0.0
405		746	756	767	778	788	799	810	821	831	842		
406		853	863	874	885	895	906	917	927	938	949		
407		959	970	981	991	*002	*013	*023	*034	*045	*055		
408	61	066	077	087	098	109	119	130	140	151	162		
409		172	183	194	204	215	225	236	247	257	268		
410		278	289	300	310	321	331	342	352	363	374		
411		384	395	405	416	426	437	448	458	469	479		
412		490	500	511	521	532	542	553	563	574	584		
413		595	606	616	627	637	648	658	669	679	690		
414		700	711	721	731	742	752	763	773	784	794		
415		805	815	826	836	847	857	868	878	888	899		
416		909	920	930	941		962		982		*003		
417	62	014	024	034	045	055	066	076	086	097	107		
418		118	128	138	149		170		190	201	211	1	
419		221	232	242	252	263	273	284	294	304	315		
420		325	335	346	356	366	377	387	397	408	418		
N	L	0	1	2	3	4	5	6	7	8	9	P	. Р.

Num. 420 to 459. Log. 623 to 662.

N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
420	62	325	335	346	356	366	377	387	397	408	418		
421		428	439	449	459	469	480	490	500	511	521	1	
422		531	542	552	562	572	583	593	603	613	624	t i	
423		634	644	655	665	675	685	696	706	716	726		
424		737	747	757	767	778	788	798	808	818	829		
425		839	849	859	870	880	890	900	910	921	931		
426		941	951	961	972	982	992	*002	*012				
427	63	043	053	063	073	083	094	104	114	124	134		
428		144	155	165	175	185	195	205	215	225	236		10
429		246	256	266	276	286	296	306	317	327	337		
430		347	357	367	377	387	397	407	417	428	438	$\begin{array}{c}1\\2\end{array}$	$\begin{array}{c} 1.0 \\ 2.0 \end{array}$
431		448	458	468	478	488	498	508	518	528	538	3	3.0
432		548	558	568	579	589	599	609	619	629	639	3 4 5	4.0 5.0
433		649	659	669	679	689	699	709	719	729	739	67	6.0
434		749	759	769	779	789	799	809	819	829	839	78	7.0 8.0
435		849	859	869	879	889	899	909	919	929	939	9	9.0
436		949	959	969	979	988	998	*008	*018	*028	*038		
437	64	048	058	068	078	088	098	108	118	128	137	ł	
438		147	157	167	177	187	197	207	217	227	237		
439		246	256	266	276	286	296	306	316	326	335		
440		345	355	365	375	385	395	404	414	424	434		
441		444	454	464	473	483	493	503	513	523	532		
442		542	552	562	572	582	591	601	611	621	631		
443		640	650	660	670	680	689	699	709	719	729		
444		738	748	758	768	777	787	797	807	816	826		0
445		836	846	856	865	875	885	895	904	914	924		9
446		933	943	953	963	972	982	992	*002	*011	*021	1	0.9
447	65	031	040	050	060	070	079	089	099	108	118	$\begin{vmatrix} 2\\ 3 \end{vmatrix}$	1.8
448		128	137	147	157	167	176	186	196	205	215	4	$2.7 \\ 3.6$
449		225	234	244	254	263	273	283	292	3 02	312	5	4.5 5.4
450		321	331	341	350	360	369	379	389	398	408	7	6.3
451		418	427	437	447	456	466	475	485	495	504	8 9	7.2 8.1
452		514	523	533	543	552	562	571	581	591	600		
453		610	619	629	639	648	· 658	667	677	686	69 6		
454		706	715	725	734	744	753	763	772	782	792		
455		801	811	820	830	839	849	858	868	877	887		
456		896	906	916	925	935	944	954	963	973	982		
457		992	*001		*020		*039	*049	*058		*077		
458	66	087	096	106	115	124	134	143	153	1 62	172		
459		181	191	200	210	219	229	238	247	257	266		
460		276	285	295	304	314	323	332	342	351	361		
1	L	0	1	2							9		

LOGARITHMS OF NUMBERS.

Num. 460 to 499. Log. 662 to 698.

N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.
460	66	276	285	295	304	314	323	332	342	351	361		
461		370	380	389	398	408	417	4 27	436	445	455		
462		464	474	483	492	502	511	521	530	539	549		
463		558	567	577	586	596	605	614	624	633	642		
464		652	661	671	680	689	6 99	708	717	727	736		
465		745	755	764	773	783	792	801	811	820	829		
466		839	848	857	867	876	885	894	904	913	922		
467		932	941	950	960	969	978	987		*006			
468	67	025	034	043	052	062	071	080	089	099	108		10
469		117	127	136	145	154	164	173	182	191	201		
470		210	219	228	237	247	256	265	274	284	293	$ \begin{array}{c} 1 \\ 2 \\ 3 \end{array} $	1.0 2.0
471		302	311	321	330	339	348	357	367	376	385	3	3.0 4.0
472		394	403	413	422	431	440	449	459	468	477	45	4.0
473		486	495	504	514	523	532	541	550	560	569	5 6	6.0
474		578	587	596	605	614	624	633	642	651	660	78	7.0 8.0
475		669	679	688	6 97	706	715	724	733	742	752	9	9.0
476		761	770	779	788	797	806	815	825	834	843		
477		852	861	870	879	888	897	906	916	9 25	934		
478		943	952	961	970	979	988		*00 6	*015		1	
479	68	034	043	052	061	070	079	088	097	106	115]	
480		124	133	142	151	160	169	178	187	19 6	205		
481		215	224	233	242	251	260	269	278	287	296		
482	1	305	31 4	323	332	341	350	359	368	377	386		
483		395	404	413	422	431	440	449	458	467	476		
484		485	49 4	502	511	520	529	538	547	556	565		9
485		574	583	592	601	6 10	619	628	637	646	655		
486		664	673	681	690	699	708	717	726	735	744	1	0.9
487		753	762	771	780	789	797	806	815	824	833		2.7
488		842	851	860	869	878	886	895	904	913	922	2 3 4 5	3.6
489		931	940	949	958	966	975	984	9 93	*002	*011	5	4.5
490	69	920	028	037	04 6	055	064	073	082	090	099	67	6.3
491	-	/108	117	126	135	144	152	162	170	179	188	8	7.2 8.1
492		197	205	214	223	232	241	249	258	267	276		10.1
493		285	294	302	311	320	329	338	346	355	364		
494		373	381	390	399	408	417	425	434	443	452		
495		461	469	478	487	49 6	504	513	522	531	539		
496		548	557	566	574	583	592	601	609	618	627		
497		636	644	653	662	671	679	688	697	705	714	.	
498		723	732	740	749	758	767	775	784	793	801	· ·	
499		810	819	827	836	845	854	862	871	880	888		
500		897	90 6	914	923	932	940	949	958	966	975		
N	L	0	1	2	3	4	5	6	7	8	9		Р.

263

Num. 500 to 539. Log. 698 to 732.

							-						
P. P.	Р	9	8	7	6	5	4	3	2	1	0	L	N
		975	966	958	949	940	932	922	914	906	897	69	500
		*062	*053	*044	*036	*027	* 018	*010	*001	992	984		501
		148	140	131	122	114	105	096	088	079	070	70	502
		234	226	217	209	200	191	183	174	165	157		503
	t	321	312	303	295	286	278	269	260	252	243		504
		406	398	389	381	372	361	355	346	338	329		505
		492	484	475	467	458	449	441	432	424	415		506
		578	569	561	552	544	535	526	518	509	501		507
9		663	655	646	638	629	621	612	603	595	586		508
		749	740	731	723	714	706	697	689	680	672		509
$\begin{array}{c c} 1 & 0.9 \\ 2 & 1.8 \end{array}$	$\begin{vmatrix} 1 \\ 2 \end{vmatrix}$	834	825	817	808	800	791	783	774	766	757		510
$\begin{array}{c c} 3 & 2.7 \\ 4 & 3.6 \end{array}$	3	919	910	902	893	885	876	868	859	851	842		511
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	45	*003		986	978	969	961	952	944	935	927		512
6 5.4	6	088	079	071	063	054	046	037	029	020	012	71	513
$\begin{array}{c c} 7 & 6.3 \\ 8 & 7.2 \end{array}$	7	172	164	155	147	139	130	122	113	105	096		514
9 8.1	9	257	248	240	231	223	214	206	198	189	181		515
		341	332	324	315	307	299	290	282	273	265		516
		425	416	408	399	391	383	374	366	357	349		517
		508	500	492	483	475	466	458	450	441	433		518
		592	584	575	567	559	550	542	533	525	517		519
		675	667	659	650	642	634	625	617	609	600		520
		759	750	742	734	725	717	709	700	692	684		521
		842	834	825	817	809	800	792	784	775	767		522
		925	917	908	900	892	883	875	867	858	850		523
8		*008	999	991	983	975	966	958	950	941	933		524
0		090	082	074	066	057	049	041	032	024	016	72	525
1 0.8	1	173	165	156	148	140	132	123	115	107	099		526
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	2	255	247	239	230	222	214	206	198	189	181		527
4 3.2	4	337	329	321	313	304	296	288	280	272	263		528
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	5	419	411	403	395	387	378	370	362	354	346		529
7 5.6	7	501	493	485	477	469	460	452	444	436	428		530
8 6.4 9 7.2	8	583	575	567	558	550	542	534	526	518	509		531
3 1.2	9	665	656	648	640	632	624	616	607	599	591		532
		746	738	730	722	713	705	697	689	681	673		533
		827	819	811	803	795	787	779	770	762	754		534
		908	900	892	884	876	868	860	852	843	835		535
		989	981	973	965	957	949	941	933	925	916		536
		*070	062	*054	*046	*038	*030	*022	*014	*006	997		537
		151	143	135	127	119	111	102	094	086	078	73	538
		231	223	215	207	199	191	183	175	167	159		539
		312	304	296	288	280	272	263	255	247	239		540
P. P.	P	9	8	7	6	5	4	3	2	1	0	L	N

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LOGARITHMS OF NUMBERS.

Num. 540 to 579. Log. 732 to 763.

N	L	0	1	2	3	4	5	6	7	8	9	Р.	Р.
540	73	239	247	255	263	272	280	288	296	304	312		
541		320	328	336	344	352	360	368	376	384	392	!	
542		400	408	416	424	432	440	448	456	464	472		
543		480	488	496	504	512	520	528	536	544	552		
544		560	568	576	584	592	600	608	616	624	632		
545		640	648	656	664	672	679	687	695	703	711		
546		719	727	735	743	751	759	767	775	783	791		
547		799	807	815	823	830	838	846	854	862	870		
548		878	886	894	902	910	918	926	933	941	949		8
- 549		957	965	973	981	989	997	*005	*013	*020	*028	ĺ.,	
550	74	036	044	052	060	068	076	084	092	09 9	107	$\begin{vmatrix} 1\\ 2\\ 3 \end{vmatrix}$	$ 0.8 \\ 1.6 $
551		115	123	131	139	147	155	162	170	178	186	3	2.4
552		194	202	210	218	225	233	241	249	257	265	4 5	3.2
558		273	280	288	296	304	312	320	327	335	343	6	4.8
554		851	35 9	367	374	382	390	398	406	414	421	5 6 7 8	5.6
555		429	437	445	453	461	468	476	484		500	9	7.2
556		507	515	523	531	53 9	547	554	562	570	578		
557		586	593	601	609	617	624	632	640	648	656		
558		663	671	679	687	695	702	710	718	726	733		
559		741	749	757	764	772	780	788	796	803	811		
560		819	827	834	842	850	858	865	873	881	889	•	
561		896	904	9 12	920	927	935	943	950	9 58	9 66		
562		974	981	989		*005		*020		*035			
563	75	051	059	066	074	082	089	097	105	113	120	1	
564		128	136	143	151	159	166	174	182	189	197		-
565		205	213	220	228	236	243	251	259	266	274		7
566		282	289	297	305	312	320	328	335	343	351	1	0.7
567		358	366	374	381	389	397	404	412	420	427	3	$1.4 \\ 2.1$
568		435	442	450	458	465	473	481	488	496	504	4	2.8
569		511	519	526	534	542	54 9	557	565	572	580	2 3 4 5 6 7	$\frac{3.5}{4.2}$
570		587	595	603	610	618	626	633	641	648	656	7	4.9 5.6
571		664	671	679	686	694	702	709	717	724	732	9	6.3
572		740	747	755	762	770	778	785	793	800	808		
573		815	823	831	838	846	853	861	868	876	884		
574		891	899	906	914	921	929	937	944	952	959		
575		967	974	9 82	989	997					*035		
576	76	042	050	057	065	072	080	087	095	103	110		
577		118	125	133	140	148	155	163	170	178	185		
578		193	200	208	215 2 9 0	223	230 305	238 313	245 320	253 328	260 225		
579		268	275	283		298					335		
580		343	350	358	365	373	380	388	395	403	410		
N	L	0	1	2	3	4	5	6	7	8	9	P.	

265

Num. 580 to 619. Log. 763 to 792.

N	L	0	1	2	3	4	5	6	7	8	9	P	Р.
580	76	343	350	358	365	373	380	388	395	403	410		8
581		418	425	433	440	448	455	462	470	477	485		
582		492	500	507	515	522	530	537	545	552	559	1 2	0.8
583		567	574	582	589	597	604	612			634		2.4
584		641	649	656	664	671	678	686	693	701	708	45	3.2
585		716	723	730	738	745	753	760	768	775	782	67	4.8 5.6
586		790	797	805	812	819	827	834	842	849	856	8	6.4
587		864	871	879	886	893	901	908	916	923	930	9	7.2
588		938	945	953	960	967	975	982	989	997	*004		
589	77	012	019	026	0 34	041	048	056	063	070	078		
590		085	093	100	107	115	122	129	137	144	151	ł	
591		159	166	173	181	188	195	203	210	217	225		
592		232	240	247	254	262	269	276	283	291	298		
593		305	313	320	327	335	342	349	357	364	371		
594		379	386	393	401	408	415	422	430	437	444		
595		452	459	466	474	481	488	495	503	510	517		
596		525	532	539	546	554	561	568	576	583	590		
597		597	605	612	619	627	634	641	648	656	663		7
598		670	677	685	692	699	706	714	721	728	735		· •
599		743	750	757	764	772	779	786	793	801	808	1 2	0.7
600		815	822	830	837	844	851	859	866	873	880	2 3 4 5	2.1
601		887	895	902	909	916	924	931	938	945	952	5	$\frac{2.8}{3.5}$
602		960	967	974	981	988	996	*003	*010	*017	*025	67	4.2
603	78	032	039	046	053	061	068	075	082	089	097	7	4.9
604		104	111	118	125	132	140	147	154	161	168	89	$5.6 \\ 6.3$
605		176	183	190	197	204	211	219	226	233	240		
606		247	254	262	269	276	283	290	297	305	312		
607		319	326	333	340	347	355	362	369	376	383		
608		390	398	405	412	419	. 426	433	440	447	455	1	
609		462	469	476	483	490	497	504	512	519	526		
610		533	5 40	547	554	561	569	576	583	5 90	597		
611		604	611	618	625	633	640	647	654	661	668		
612		675	682	689	696	704	711	718	725	732	739		
613		746	753	760	767	774	781	789	796	802	810		
614		817	824	831	838	845	852	859	866	873	880		
615		888	895	902	909	916	923	930	937	944	951		
616		958	965	972	979	986	993	*000	*007	*014	*021		
617	79	029	036	043	050	057	064	071	078	085	092		
618		099	106	113	120	127	134	141	148	155	162		
619		169	176	183	190	197	204	211	218	225	232		
620		239	246	253	260	267	274	281	288	29 5	302		
N	L	0	1	2	3	4	5	6	7	8	9	P.	

Num. 620 to 659. Log. 792 to 819.

N	L	0	1	2	3	4	5	6	7	8	9	Р.	Р.
620	79	239	246	253	260	267	274	281	288	295	302		
621		309	316	323	330	337	344	351	358	365	372		
622		379	386	393	400	407	414	421	428	435	442		
623		449	456	463	470	477	484	491	498	505	511		
624		518	525	532	539	546	553	560	567	574	581		
625		588	595	602	609	616	623	630	637	644	650		
626		657	664	671	678	685	692	699	706	713	720		
627		727	734	741	748	754	761	768	775	782	789	2	
628		796	803	810	817	824	831	837	844	851	858		
629		865	872	879	886	893	900	906	91 3	920	927		
630		934	941	948	955	962	969	975	982	989	9 96		
631	80	003	010	017	024	030	037	044	051	058	065		
632		072	079	085	092	099	106	113	120	127	134		
633		140	147	154	161	168	175	182	188	195	202		
634		209	216	223	229	236	243	250	257	264	271		
635		277	284	291	298	305	312	318	325	332	339		
636		346	353	359	366	373	380	387	393	400	407		7
637		414	421	428	434	441	448	455	462	468	475		
638		482	489	496	502	509	516	523	530	536	543	$\begin{vmatrix} 1\\ 2 \end{vmatrix}$	0.7
639		550	557	564	570	577	584	591	598	604	611	34	2.1 2.8
640		618	625	632	638	645	652	659	665	672	679	5	3.5
641		686	693	699	706	713	720	726	733	740	747	56	$3.5 \\ 4.2$
642		754	760	767	774	781	787	794	801	808	814	7	4.9 5.6
643		821	828	835	841	848	855	862	868	875	882	9	6.3
644		889	895	902	909	916	922	929	936	943	949	ľ	
645		956	963	969	976	983	990		*003				
646	81	023	030	027	043	050	057	064	070	077	084		
647		090	097	104	111	117	124	131	137	144	151		
648		158	164	171	178	184	191	198	204	211	218		
649		224	231	238	245	251	258	265	271	278	285	ĺ	
650		291	298	305	311	318	325	331	338	345	351		
651		358	365	371	378	385	391	398	405	411	418		
652		425	431	438	445	451	458	465	471	478	485		
653		491	498	505	511	518	525	531	538	544	551		
654		558	564	571	578,		591	598	604	611	617		
655		624	631	637	644	651	657	664	671	677	684		
656		690	697	704	710	717	723	730	737	743	750		
657		757	763	770	776	783	790	796	803	809	816		
658		823	829	836	842	849	856	862	869	875	882		
659		889	895	902	908	915	921	928	935	941	948		
660		954	961	968	974	981	987	994	*000	*007	*014		
N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.

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Num. 660 to 699. Log. 819 to 845.

N	L	0	1	2	3	4	5	6	7	8	9	P	. P.
660	81	954	961	968	974	981	987	994	*000	*007	*014		7
661	82	020	027	033	040	046	053	060	066	073	079		
662		086	092	099	105	112	119	125	132	138	145	$\begin{bmatrix} 1\\ 2 \end{bmatrix}$	0.7
663		151	158	164	171	178	184	191	197	204	210	5	2.1
664		217	223	230	236	243	249	256	263	269	276	4 5	$\frac{2.8}{3.5}$
665		282	289	295	302	308	315	321	328	334	341	6 7	4.2
666		347	354	360	367	373	380	387	393	400	406	8	5.6
667		413	419	426	432	439	445	452	458	465	471	9	6.3
668		478	484	491	497	504	510	517	523	530	536		
669		543	549	556	562	569	575	582	588	5,95	601		
670		607	614	620	627	633	640	646	653	659	666		
671		672	679	685	692	698	705	711	718	724	730		
672		737	743	750	756	763	769	776	782	789	795		
673 674		802 866	808 872	814 879	$821 \\ 885$	827 892	834 898	840 905	847 911	853 918	860 924		
675		930	937	943	950	956	963	969	975	982	988		
676				*008					*040				
677	83	059	065	072	078	085	091	097	104	110	117		
678	0.9	123	129	136	142	149	155	161	168	174	181		6
679		187	193	200	206	213	219	225	232	238	245	1	
680		251	257	264	270	276	283	289	296	302	308	$\frac{2}{3}$	$1.2 \\ 1.8$
681		315	321	327	334	340	347	353	359	366	372	4 5	$\frac{2.4}{3.0}$
682		378	385	391	398	404	410-		423	429	436	6	3.6
683		442	448	455	461	467	474	480	487	493	499	7	4.2
684		506	512	518	525	531	537	544	550	556	563	8	$\frac{4.8}{5.4}$
685		569	575	582	588	594	601	607	613	620	626		
686		632	639	645	651	658	664	670	677	683	689		
687		696	702	708	715	721	727	734	740	746	753		
688		759	765	771	778	784	790	797	803	809	816		
689		822	828	835	841	847	853	860	866	872	879		
690		885	891	897	904	910	916	923	929	935	942		
691		948	954	960	967	973	979	985	992		*004		
692	84	011	017	023	029	036	042	048	055	061	067		
693		073	080	086	092	098	105	111	117	123	130		
694		136	142	148	1 55	161	167	173	180	186	192		
695		198	205	211	217	223	230	236	242	248	255		
696		261	267	273	280	286	292	298	305	311	317		
697		323	330	336	342	34 8	354	361	367	373	379		
698		386	392	398	404	410	417	423	429	435	442		
6 99		448	454	460	466	473	479	485	491	497	504		
700		510	516	522	528	535	541	547	553	559	566		
N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.

Num. 700 to 739. Log. 845 to 869.

						39.							
N	L	0	1	2	3	4	5	6	7	8	9	Р.	Р.
700	84	510	516	522	528	535	541	547	553	559	566		
701		572	578	584	590	597	603	609	615	621	628		
702		634	640	646	652	658	665	671	677	683	689		
703		696	702	708	714	720	726	733	739	745	751		
704		757	763	770	776	782	788	794	800	807	813		
705		819	825	831	837	814	850	856	862	868	874		
706		880	887	893	899	905	911	917	924	930	936		
707		942	948	954	960	967	973	979	985	991	997		
708	85	003	009	016	022	028	034	040	046	052	058		
709		065	071	077	083	089	095	101	107	114	120		
710		126	132	138	144	150	156	163	169	175	181		
711		187	193	199	205	211	217	224	230	236	242		
712		248	254	260	266	272	278	285	291	297	303		
713		309	315	321	327	333	339	345	352	358	364		
714		370	376	382	388	394	400	406	412	418	425		
715		431	437	443	449	455	461	467	473	479	485		
716		491	497	503	509	516	522	528	534	540	546		
717		552	558	564	570	576	582	588	594	600	606		б
718		612	618	625	631	637	643	649	655	661	667	1	0.6
719	•	673	679	685	691	697	703	709	715	721	727	$2 \\ 3 \\ 4$	$1.2 \\ 1.8$
720		733	739	745	751	757	763	769	775	781	788	4	2,4
721		794	800	806	812	818	824	830	836	842	848	5	3.0 3.6
722		854	860	866	872	878	884	890	896	902	908	7	4.2
723		914	920	926	932	938	944	950	956	962	968	8	4.8
724		974	980	986	992	998		*010		*022		9	5.4
725	- 86	034	040	046	052	058	064	070	076	082	088		
726		094	100	106	112	118	124	130	136	141	147		
727	ļ	153	159	165	171	177	183	189	195	201	207		
728		213	219	225	231	237	243	249	255	261	267		
729		273	279	285	291	297	303	308	314	320	326		
730		332	338	344	350	356	362	368	374	380	386		
731		392	398	404	410	415	421	427	433	439 499	445 504		
732		451	457	463	469 528	475 524	481 540	487	493 552	499 558	$504 \\ 564$		
733		510	516	522 591		534 502	599	546 605	611	558 617	623		
734		570	576	581	587	593							
735		629	635	641	646	652	658	664	670	· 676 735	682 741		
736		688	694	700	705	711	717	723	729	735	741		
737		747	753	759	764	770	776	782	788		800		
738 739		806 864	812 870	817 876	823 882	829 888	835 894	841 900	847 906	853 911	859 917		
		923	929	935	941	947	953	958	964	970	976		
740					~								
N	L	0	1	2	3	4	5	6	7	8	9	P	. P.

Num. 740 to 779. Log. 869 to 892.

N	L	0	ť	2	3	4	5	6	7	8	9	P	. Р.
740	86	923	929	935	941	947	953	958	964	970	976		
741		982	988	994	999	*005	*011	*017	*023	*029	*035	1	
742	87	040	046	052	058	064	070	075	081	087	093		
743		099	105	111	116	122	128	134	140	146	151		
744		157	163	169	175	181	186	192	198	204	210		
745		216	221	227	233	239	245	251	256		268		
746		274	280	286	291	297	303	309	315		326		
747		332	338	344	349	355	361	367	373	379	384		
748		390	396	402	408	413	419	425	431	437	442		
749		448	454	460	466	471	477	483	489	495	500		
750		506	512	518	523	529	535	541	547	552	558	1	
751		564	570	576	581	587 C 45	593	599	604	610	616		
752		622	628	633	639	645	651	656	662	668	674		
753 754		679 737	685 743	691 749	697 754	703 760	708 766	714 772	720 777	726 783	731 789		
755		795	800	806	812	818	823	829	835	841	846		
756		852	858	864	869	875	881	887	892	898	904		
757		910	915	921	927	933	938	944	950	955	961		6
758		967	973	978	984	990	996		*007				
759	88	024	030	036	041	047	053	058	064	070	076	1 2	0.6
760		081	087	093	098	104	110	116	121	127	133	3	1.8
761		138	144	150	156	161	167	173	178	184	190	5	3.0
762		195	201	207	213	218	224	230	235	241	247	67	3.6
763		252	258	264	270	275	281	287	292	298	304	8	4.2 4.8
764		309	315	321	326	332	338	343	349	355	360	j ğ	5.4
765		366	372	377	383	389	395	400	406	412	417		
766		423	429	434	440	446	451	457	463	468	474		
767		480	485	491	497	502	508	513	519	525	5 30		
768		536	542	547	553	559	564	570	576	581	587		
769		593	598	604	610	615	621	627	632	638	643		
770		649	655	660	666	672	677	683	689	694	700	Į	
771		705	711	717	722	728	734	739	745	750	756	1	
772		762	767	773	779	784	790	795	801	807	812	ł	
773		818	824	829	835	840	846	852	857	863	868		
774		874	880	885	891	897	902	908	913	919	925	İ	
775		930 696	936 400	941	947	953	958	964	969	975	981	1	
776	00	986	992		*003		1		*025				
777	89	042	048	053	059	064	070	076	081	087	092		
778		098 154	104	109	115	120	126	131	137	143	148		
779		154	159	165	170	176	182	187	193	198	204		
780		209	215	221	226	232	237	243	248	254	260		
N	L	0	1	2	3	4	5	6	7	8	9	P	Ρ.

Num. 780 to 819. Log. 892 to 913.

N 780	L	0	1	2			-		_	-		1	
780				4	3	4	5	6	7	8	9	Р.	Р.
	89	209	215	221	226	232	237	243	248	254	260		
781		265	271	276	282	287	293	298	304	310	315		
782		321	326	332	337	343	348	354	360	365	371		
783		376	382	387	393	398	404	409	415	421	426		
784		432	437	443	44 8	454	459	465	470	476	481		
785		487	492	498	5 0 4	509	515	520	526	531	537		
786		542	548	553	559	564	570	575	581	586	592		
787		597	603	609	614	620	625	631	636	642	647		
788		653	658	664	669	675	680	686	691	697	702		
789		708	713	719	724	730	735	741	746	752	757		
790		763	768	774	779	785	790	796	801	807	812		
791		818	823	829	834	840	845	851	856	862	867		
792		873	878	883	889	894	900	905	911	916	922		
793		927	933	938	944	949	955	960	966	971	977		
794		982	988	993	9 98	*004	*009	*015	*020	*026	*031		
795	90	037	042	048	053	059	064	069	075	080	086		
796		091	097	102	108	113	119	124	129	135	140		
797		146	151	157	162	168	173	179	184	189	195		5
798		200	206	211	217	222	227	233	238	244	249	1	0.5
799		255	260	266	271	276	282	287	293	298	304	$1\\2$	1.0
800		309	314	320	325	331	336	342	347	352	358	3 4	$1.5 \\ 2.0$
801		363	369	374	380	385	390	396	401	407	412	5	2.5
802		417	423	428	434	439	445	450	455	461	466	6 7	3.0 3.5
803		472	477	482	488	493	499	504	509	515	520	8	4.0
804		526	531	536	542	547	553	558	563	569	574	9	4.5
805		580	585	590	596	601	607	612	617	623	628		
806		634	639	644	650	655	660	666	671	677	682	ļ	
807		687	693	698	703	709	714	720	725	730	736	1	
808		741	747	752	757	763	768	773	779	784	789		
809		795	800	806	811	816	822	827	832	838	843		
810		849	854	859	865	870	875	881	886	891	897		
811		902	907	913	918	924	929	934	940	945	950		
812		956	961	966	972	977	982	988	993		*004	1	
813	91	009	014	020	025	030	036	041	046	052	057	1	
814		062	068	073	078	084	089	094	100	105	110		
815		116	121	126	132	137	142	148	153	1 58	164		
816		1 69	174	180	185	190	196	201	206	212	217		
817		222	228	233	238	243	249	254	259	265	270		
818		275	281	286	291	297	302	307	312	318	323		
819		328	334	339	344	350	355	360	365	371	376		
820		381	387	392	397	403	408	413	418	424	429		
N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.

Num. 820 to 859. Log. 913 to 934.

N	L	0	1	2	3	4	5	6	7	8	9	P	. Р.
820	91	381	387	392	397	403	408	413	418	424	429		
821		434	440	445	450	455	461	466	471	477	482		
822		487	492	498	503	508	514	519	524	529	535		
823		540	545	551	556	561	566	572	577	582	587	1	
824		593	598	603	609	614	619	624	630	635	640		
825		645	651	656	661	666	672	677	682	687	693		
826		698	703	709	714	719	724	730	735	740	745	1	
827		751	756	761	766	772	777	782	787	793	798		
828		803	808	814	819	824	829	834	840	845	850		
829		855	861	866	871	876	882	887	892	897	90 3		
830		908	913	918	924	929	934	939	944	950	955		
831		960	965	971	9 76	981	986	991	9 97	*002	*007		
832	92	012	018	023	028	033	038	044	049	054	059		
833		065	070	075	080	085	091	096	101	106	111		
834		117	122	127	1 32	137	143	148	153	158	163	1	
835		169	174	179	184	189	195	200	205	210	215		
836		221	226	231	236	241	247	252	257	262	267		
837		273	278	283	288	293	298	304	309	314	319		5
838		324	330	335	340	345	350	355	361	366	371	1	0.5
839		376	381	387	392	397	402	407	412	418	423	23	1.0
840		428	433	438	443	449	454	459	464	469	474	4	$ \begin{array}{c} 1.5 \\ 2.0 \\ 2.5 \end{array} $
841		480	485	490	495	500	505	511	516	521	526	5	2,5
842		531	536	542	547	552	557	562	567	572	578	67	3.0 3.5
843		583	588	593	598	603	609	614	619	624	629	8	4.0
844		634	639	645	650	655	660	665	670	675	681	9	4.5
845		686	691	696	701	706	711	716	722	727	732		
846		737	742	747	752	758	763	768	773	778	783		
847		788	793	799	804	809	814	819	824	829	834		
848		840	845	850	855	860	865	870	875	881	886		
849		891	896	901	906	911	916	921	927	932	937		
850		942	947	952	957	962	967	973	978	983	988	}	
851		993		*003					*029	*034	*0 39		
852	93	044	049	054	059	064	069	075	080	085	090		
853		095	100	105	110	115	120	125	131	1 36	141		
854		146	151	156	161	166	171	176	181	186	192		
855		197	202	207	212	217	222	227	232	237	242		
856		247	252	258	263	268	273	278	283	288	293		
857		298	303	308	313	318	323	328	334	339	344		
858		319	354	359	364	369	374	379	384	38 9	394		
859		399	404	409	41 4	420	425	430	435	440	445		
860		450	455	460	465	470	475	480	485	490	495		
N	L	0	1	2	3	4	5	6	7	8	9	Р.	D

273

Num. 860 to 899. Log. 934 to 954.

1															
N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.		
860	93	450	455	460	465	470	475	480	485	490	495				
861		500	505	510	515	520	526	531	536	541	546				
862		551	556	561	566	571	576	581	586	591	596				
863		601	606	611	616	621	626	631	636	641	646				
864		651	656	661	666	671	676	682	687	692	697				
865		702	707	712	717	722	727	732	737	742	747				
866		752	757	762	767	772	777	782	787	792	797				
867		802	807	812	817	822	827	832	837	842	847				
868		852	857	862	867	872	877	882	887	892	897				
869		902	907	912	917	922	927	932	937	942	947				
870		952	957	962	967	972	977	982	987	9 92	997				
871	94	002	007	012	017	022	027	032	037	042	047				
872		052	057	062	067	072	077	.085	086	091	096				
873		101	106	111	116	121	126	131	136	141	146				
874		151	156	161	166	171	176	181	186	191	196				
875		201	206	211	216	221	226	231	236	240	245				
876		250	255	260	265	270	275	280	285	290	295				
877		300	305	310	315	320	325	330	335	340	345		5		
878		349	354	359	364	369	374	379	384	389	394	1	0.5		
879		399	404	409	414	419	424	429	433	438	443	2	1.0		
880		448	453	458	463	468	473	478	483	488	493	2 3 4 5 6 7	$1.5 \\ 2.0$		
881		498	503	507	512	517	522	527	532	537	542	5	2.5		
882		547	552	557	562	567	571	576	581	586	591	57	$\frac{3.0}{3.5}$		
883		596	601	606	611	616	621	626	630	635	640	8	4.0		
884		645	650	655	660	665	670	675	680	685	689	9	4.5		
885		694	699	704	709	714	719	724	729	734	738				
886		743	748	753	758	763	768	773	778	783	787				
887		792	797	802	807	812	817	822	827	832	836				
888		841	846	851	856	861	866	871	876	880	885				
889		890	895	900	905	910	915	919	924	929	934				
890		939	944	949	954	959	963	968	973	978	983				
891		988	993		*002		1		*022						
892	95	036	041	046	051	056	061	066	071	075	080				
893		085	090	095	100	105	109	114	119	124	129				
894		134	139	143	148	153	158	163	168	173	177				
895		182	187	192	197	202	207	211	216	221	226				
896		231	236	240	245	250	255	260	265	270	274				
897		279	284	289	294	299 .	303	308	313	318	323				
898		328	332	3 37	842	347	352	357	361	366	371				
899		376	381	386	390	395	400	405	410	415	419				
900		424	429	434	439	444	448	453	458	463	468				
N	L	0	1	2	3	4	5	6	7	8	9	Р.	Р.		

Num. 900 to 939. Log. 954 to 973.

N	L	0	t	2	3	4	5	6	7	8	9	Р.	Р.
900	95	424	429	434	439	444	448	453	458	463	468		
901		472	477	482	487	492	497	501	506	511	516		
902		521	525	530	535	540	545	550	554	559	564		
903		569	571	578	583	588	593	598	602	607	612		
904		617	622	626	631	636	641	646	650	655	660		
905		665	670	674	679	684	689	694	698	703	708		
906		713	718	722	727	732	737	742	746	751	756		
907		761	766	770	775	780	785	789	794	799	804		
908		809	813	818	823	828	832	837	842	847	852		
909		856	861	866	871	875	880	885	890	895	899		
910		904	909	914	918	923	928	933	938	942	947		
911		952	957	961	966	971	976	980	985	990	995		
912		999	*004	*009	*014	*019	*023	*028	*033	*038	*042		
913	96	047	052	057	061	066	071	076	080	085	090		
914		095	099	104	109	114	118	123	128	133	137		
915		142	147	152	1 56	161	166	171	175	180	185		
916	-	190	194	199	204	209	213	218	223	227	232		
917		237	242	246	251	256	261	265	270	275	280		5
918		284	289	294	298	303	308	313	317	322	327	1	0.5
919		332	336	341	346	350 *	355	360	365	369	374	2	1.0
920		379	384	388	393	398	402	407	412	417	421	2 3 4	$1.5 \\ 2.0$
921		426	431	435	440	445	450	454	459	464	468	5 6	2.5
922		473	478	483	487	492	497	501	506	511	515	7	$\frac{3.0}{3.5}$
923		520	525	530	534	539	544	548	553	558	562	8	4.0
924		567	572	577	581	586	591	595	600	605	609	9	4.5
925		614	619	624	628	633	638	642	647	652	656		
926		661	666	670	675	680	685	689	694	699	703		
927		708	713	717	722	727	731	736	741	745	750		
928		755	759	764	769	774	778	783	788	792	797		
929		802	806	811	816	820	825	830	834	839	844		
930		848	853	858	862	867	872	876	881	886	890	1	
931		895	900	904	909	914	918	923	928	932	937		
932		942	946	951	956	960	965	970	974	979	981		
933		988	993	997	*002	*007	*011	*016	*021	*025	*030	ļ	
934	97	035	039	044	049	053	058	063	067	072	077]	
935		081	086	090	095	100	104	109	114	118	123		
936		128	132	1 37	142	146	151	155	160	165	169		
937		174	179	183	188	192	197	202	206	211	216		
938		220	225	230	234	239	243	248	253	257	262		
939		267	271	276	280	285	290	294	299	304	308		
940		313	\$17	322	327	331	336	340	345	350	354		
N	L	0	1	2	3	4	5	6	7	8	9	P	Ρ.

Num. 940 to 979. Log. 973 to 991.

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N	L	0	1	2	3	4	5	6	7	8	9	P. P.
940	97	313	317	322	327	331	336	340	345	350	354	
941		359	364	368	373	377	382	387	391	396	400	
942		405	410	414	419	424	428	433	437	442	447	
943		451	456	460	465	470	474	479	483	488	493	
944		497	502	506	51 1	516	520	525	529	534	539	
945		543	548	552	557	562	566	571	575	580	585	
946		589	594	598	603	607	612	617	621	626	630	
947		635	640	644	649	653	658	663	667	672	676	
948		681	685	690	695	699	704	708	713	717	722	
949		727	731	736	740	745	749	754	759	763	768	5
950		772	777	782	786	791	795	800	804	809	813	1 0.5
951		818	823	827	832	836	841	845	850	855	859	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
9 52 {		864	868	873	877	882	886	891	896	900	905	4 2.0
953		909	914	918	923	9 28	932	937	941	946	950	5 2.5
954		955	959	964	968	973	978	982	987	991	9 96	6 3.0 7 3.5 8 4.0 9 4.5
955	98	000	005	009	014	019	023	028	032	037	041	8 4.0 9 4.5
956		046	050	055	059	064	068	073	078	082	087	
957		091	096	100	105	109	114	118	123	127	132	
958		137	141	146	150	155	159	164	168	173	177	
9 59		182	186	191	195	200	204	209	214	2 1 8	223	
960		227	232	236	241	245	250	254	259	263	268	
961		272	277	281	286	290	295	299	304	308	313	
962		318	322	327	331	336	340	345	349	354	358	
963		363	367	372	376	381	385	390	394	399	403	1
964		408	412	417	421	426	430	435	439	444	448	
965		453	457	462	466	471	475	480	484	489	493	4
966		498	502	507	511	516	520	525	529	534	538	1 0.4
967		543	547	552	556	561	565	570	574	579	583	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
968		588	592	597	601	605	610	614	619	623	628	4 1.6
9 69		632	637	641	646	650	655	659	664	668	673	$\begin{array}{c cccc} 5 & 2.0 \\ 6 & 2.4 \\ 7 & 2.8 \end{array}$
970		677	682	686	691	695	700	704	· 709	713	717	7 2.8
971		722	726	731	735	740	744	749	753	758	762	8 3.2 9 3.6
972		767	771	776	780	784	789	793		. 802	807	010.0
973		811	816	820	825	829	834	838	843	847	851	-
974		856	860	865	869	874	878	883	887	892	896	
975		900	905	909	914	918	923	927	932	936	941	
976		945	949	954	958	963	967	972	976	981 *005	985 *000	
977		989	994		*003				*021			
978 979	99	034 078	038 083	043 087	<u>047.</u> 092	052 096	056	061 105	065 109	069 114	074 118	
		123	127	131	136	1 40	145	149	154	158	162	
980												
N	L	0	1	2	3	4	5	6	7	8	9	P. P.

. .

		N	um.	980	το	1000.	Log	. 99	1 10	999 .			
N	L	0	1	2	3	4	5	6	7	8	9	Р.	Р.
980	99	123	127	131	136	140	145	149	154	1 58	162		
981		167	171	176	180	185	189	193	198	202	207		
982		211	216	220	224	229	233	238	242	247	251		
983		255	260	264	269	273	277	282	286	291	295		
984		300	304	308	313	317	322	326	330	335	339		
9 85		344	348	352	357	361	366	370	374	379	383		
986		388	392	396	401	405	410	414	419	423	427		
987		432	436	441	445	449	454	458	463	467	471		
988		476	480	484	489	493	498	502	506	511	515		
989		520	524	528	533	537	542	546	550	555	559		4
990		564	568	572	577	581	585	590	594	599	603	1	0.4
991		607	612	616	621	625	629	634	638	642	647	$\frac{2}{3}$	$0.8 \\ 1.2$
992		651	656	660	664	669	673	677	682	686	691	4	1.6
993		695	699	704	708	712	717	721	726	730	734	5	2.0
994		739	743	747	752	756	760	765	769	774	778	6 7	$\frac{2.4}{2.8}$
995		782	787	791	795	800	804	808	813	817	822	8 9	$3.2 \\ 3.6$
996		826	830	835	839	843	848	852	856	861	865	9	9.0
997		870	874	878	883	887	891	896	900	904	909		
998		913	917	922	926	930	935	939	944	948	952		
999		957	961	965	970	974	978	983	987	991	996		
1000	000	000	043	087	130	174	217	260	304	347	391		
N	L	0	1	2	3	4	5	6	7	8	9	P.	Р.

Num. 980 to 1000. Log. 991 to 999.

Logarithms of Important Numbers.

Number.	Logarithm.
$\pi = 3.141593$	0.497 150
$\frac{4}{3}\pi$ = 4.188 790	0.622 089
$h\pi = 0.523599$	1.718 999
$\frac{1}{\pi}$ = 0.318 310	1.502 850
$\pi^2 = 9.869\ 604$	0.994 300
$\frac{1}{\pi^2}$ = 0.101 321	1.005 700
$\pi = 1.772454$	0.248 575
$\frac{1}{1}\pi = 0.564\ 190$	1.751 425
$I^{3} \frac{\pi}{\pi} = 1.464 592$	0.165 717
$\frac{1}{r_{\pi}^2} = 0.682~784$	1.834 283
$\sqrt[3]{rac{6}{\pi}} = 1.240$ 701	0.093 667

 4	4

0 °			Logar	ithms.		1	179°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine,	М.
0	Inf. Neg.	lnfinite.	Inf. Neg.	Infinite.	10.00000	10.00000	60
1	6.46373	13.53627	$6.4637\bar{3}$	13.53627	00000	00000	59
2	76476	23524	76476	23524	00000	00000	58
3	94085	05915	94085	05915	00000	00000	57
4	$7.06579 \\ 7.16270$	$12.93421 \\ 12.83730$	$7.06579 \\ 7.16270$	$12.93421 \\ 12.83730$	$00000 \\ 10.00000$	00000 10.00000	56 55
5 6	24188	75812	24188	75812	00000	00000	54
7	30882	69118	30882	69118	00000	00000	53
7 8	36682	63318	36682	63318	00000	06000	52
9	41797	58203	41797	58203	00000	00000	51
10	7.46373	12.53627	7.46373	12.53627	10.00000	10.00000	50
11	50512	49488	50512	49488	00000	00000	49
12	54291	45709 42233	54291 57767	45709 42233	00000	00000	48
$\frac{13}{14}$	57767 60985	42233 39015	60986	39014	00000	00000	47
14	7.63982	12.36018	7.63982	12.36018	10.00000	10.00000	45
16	66784	33216	66785	33215	00000	00000	44
17	69417	30583	69418	30582	00001	9.99999	43
18	71900	28100	71900	28100	00001	99999	42
19	74248	25752	74248	25752	00001	99999	41
20	7.76475	12.23525	7.76476	12.23524	10.00001	9.99999	40
21	78594	21406	78595	21405	00001	99999	39
22	80615	19385	80615	19385	00001	99999	38
23	82545	17455 15607	82546 84394	17454 15606	00001 00001	99999 99999	37
24 25	84393 7.86166	12,13834	7.86167	12.13833	10.00001	9.99999	36 35
26	87870	12.13334	87871	* 12129	00001.	99999	34
27	89509	10491	89510	10490	00001	999999	33
28	91088	08912	91089	08911	00001	99999	32
29	92612	07388	92613	07387	00002	99998	31
30	7.94084	12.05916	7.94086	12.05914	10.00002	9.99998	30
31	95508	04492	95510	04490 -	00002	99998	29
32	96887	03113	96889	03111	00002	99998	28 27
33 34	98223 99520	01777 00480	98225 99522	01775 00478	00002	99998 99998	26
34 35	8.00779	11,99221	8.00781	11.99219	10.00002	9.99998	25
36	02002	97998	02004	97996	00002	99998	24
37	03192	96808	03194	96806	00003	99997	23
38	04350	95650	04353	95647	00003	99997	22
39	05478	94522	05481	94519	00003	99997	21
40	8.06578	11.93422	8.06581	11.93419	10.00003	9.99997	20
41	07650	92350	07653	92347	00003	99997	19
42	08696	91304 90282	08700 09722	91300 90278	00003	99997 99997	18
43 44	09718 10717	89283	10720	89280	00003	99996	16
44	8.11693	11.88307	8.11696	11.88304	10.00004	9,99996	15
46	12647	87353	12651	87349	00004	99996	14
47	13581	86419	13585	86415	00004	99996	13
48	14495	85505	14500	85500	00004	99996	12
49	15391	84609	15395	84605	00004	99996	11
50	8.16268	11.83732	8.16273	11.83727	10.00005	9.99995	10
51	17128	82872 82029	17133	82867 82024	00005	99995 99995	9
52 53	17971 18798	82029 81202	17976 18804	82024 81196	00005	99995	87
53 54	18798	80390	19616	80384	00005	99995	6
55	8.20407	11.79593	8.20413	11.79587	10.00006	9.999994	6 5 4
56	21189	78811	21195	78805	00006	99994	4
57	21958	78042	21964	78036	00006	99994	32
58	22713	77287	22720	77280	00006	99994	2
59	23456	76544	23462	76538	00006	99994	1 1
60	24186	75814	24192	75808	00007	99993	0
M.	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M,

Logarithms.

1 -			Logar	nums.			170
M.	Sine,	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	8.24186	11.75814	8.24192	11.75808	10.00007	9.99993	60
1	24903	75097	24910	75090	00007	99993	59
$\frac{2}{3}$	25609	74391	25616	74384	00007	99993	58
3	26304	74391 73696	26312	73688	00007	99993	57
4	26988	73012	26996	73004	00008	99992	56
4 5 7 8 9	8.27661	11.72339	8.27669	11.72331	10.00008	9.99992	55 ,
6	28324	71676	28332	71668	00008	99992	54
7	28977	71023	28986	71014 70371	00008	99992	53
8	29621	70379	29629	70371	00008	99992 99991	52
10	30255 8.30879	69745 11.69121	30263 8.30888	69737 11.69112	10.00009	9.99991	51 50
11	31495	68505	31505	68495	00009	99991	49
$\widetilde{11}$ 12	32103	67897	32112	67888	00010	99990	48
13	32702	67298	32711	67289	00010	99990	47
14	33292	66708	33302	66698	00010	99990	46
15	8.33875	11.66125	8.33886	11.66114	10.00010	9.99990	45
15 16	34450	65550	34461	65539	00011	99989	44
17	35018	64982	. 35029	64971	00011	99989	43
18	35578	64422	35590	64410	00011	99989	42
19	36131	$63869 \\ 11.63322$	36143	63857	00011	99989	41
20	8.36678	11.63322	8.36689	11.63311	10.00012	9.99988	40
21	37217	62783	37229	62771	00012	99988	39
19 20 21 22 23 24	37750	62250 61724	37762 38289	62238 61711	00012	99988	38
20	38276 38796	61204	38809	61711	00013	99987	37 36
25	8.39310	11.60690	8.39323	11.60677	10.00013	99987 9.99987	35
26	39818	60182	39832	60168	00014	99986	34
27	40320	59680	40334	59666	00014	99986	33
$\frac{1}{27}$ 28	40816	59184	40830	59666 59170	00014	99986	32
29 30	41307	58693	41321	58679	00015	99985	31
30	8.41792	17 58208	8 41807	11.58193	10.00015	9.99985	30
31	42272	57728	42287	57713	00015	99985	29
32	42746	57254	42762	57238	00016	99984	28
33	43216	56784	43232	56768	00016	99984	27
34 35	43680 8.44139	56320 11.55861	43696	56304 11.55844	00016 10.00017	99984	26
36	44594	55406	8.44156 44611	55389	10.00017	9.99983	25 24
37	45044	54956	44611 45061	54939	00017 00017	99983 99983	24
38	45489	54511	45507	54493	00017	99982	22
39	45930	54070	45948	54052	00018	99982	21
40	8.46366	11.53634	8.46385	11.53615	10.00018	9.99982	20
41	46799	53201	46817	53183	00019	99981	19
42	47226	52774	47245 47669	$52755 \\ 52331$	00019	99981	18
43	47650	52350	47669	52331	00019	99981	17
44	48069	51931 11.51515	48089 8.48505	51911	00020	99980	16
45	8.48485	11.51515	8.48505	11.51495	10.00020	9.99980	15
46 47	48896 49304	51104 50696	48917	51083	00021	99979	14
48	49504	50696	49325 49729	50675	00021	99979	13
49	50108	49892	50130	50271 49870	00021 00022	99979 99978	$ \begin{array}{c} 12 \\ 11 \end{array} $
50	8.50504	11.49496	8.50527	11.49473	10.00022	99978 9.99978	10
51	50897	49103	50920	49080	00022	99977	9
52 53	51287	48713 48327 47945	51310	48690	00023	99977	8
53	51673 🖌	48327	51696	48304	00023	99977 -	8 7 6 5 4
54	52055	47945	52079	47921 11,47541	00024	99976	6
55	8.52434	11.47566 47190	8.52459	11.47541	10.00024	9.99976	5
56	52810 53183	47190	52835	47165	00025	99975	4
57	52550	46817	53208	46792	00025	99975	32
58 59	53552 53919	46448 46081	53578 53945	46422	00026	99974	2
60	54282	45718	54308	46055 45692	00026	99974 99974	1
M.	Cosine,	Secant.	Cotangent,		Cosecant.	Sine.	<u>м</u> .
· · · ·					Coscoant.	ome.	AR.

91°

883

178°

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2 °			Logar	ithms.			177°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine,	M.
0	8.54282	11.45718	8.54308	11.45692	10.00026	9.99974	60
1	54642	45358	54669	45331 44973	00027	99973	59
$\frac{2}{3}$	54999	45001	55027	44973	00027	99973	58
3	55354 55705	44646 44295	55382 55734	44618 44266	00028	99972 99972	57 56
4 5 6	8.56054	11.43946	8,56083	11.43917	10.00029	9.99971	55
ő	56400	43600	56429	43571	00029	99971	54
7	56743	43257	56773	43227	00030	99970	53
8	57084	42916	57114	42886	00030	99970	52
9	57421	42579	57452	42548	00031	99969	51
10 11	8.57757	11.42243 41911	8.57788	11.42212	10.00031	9.99969 99968	50 49
12	$58089 \\ 58419$	41911 41581	58121 58451	41879 41549	00032	99968	49
13	58747	41253	58779	41221	00033	99967	47
14	59072	40928	59105	40895	00033	99967	46
15	8.59395	11.40605	8.59428	11.40572	10.00033	9.99967	45
16	59715	40285	59749	40251	00034	99966	44
17	60033	39967	60068	39932	00034	99966	43
18 19	60349 60662	39651 39338	60384 60698	39616	00035	99965 99964	42 41
20	8.60973	39338 11.39027	8.61009	39302 11.38991	10.00036	99964	41
$\tilde{21}$	61282	38718	61319	38681	00037	99963	39
22	61589	38411	61626	38374	00037	99963	38
23	61894	38106	61931	38069	00038	99962	37
24	62196	37804	62234	37766	00038	99962	36
25	8.62497	11.37503	8.62535	11.37465	10.00039	9.99961	35
26 27	62795	37205	62834	37166	00039	99961 99960	34 33
28	63091 63385	36909 36615	63131 63426	36869 36574	00040 00040	99960	33
29	63678	36322	63718	36282	00040	99959	31
30	8.63968	11.36032	8.64009	11.35991	10.00041	9.99959	30
31	64256	35744	64298	35702	00042	99958	29
32	64543	35457	64585	35415	00042	99958	28
33	64827	35173	64870	35130	00043	99957	27
34 35	65110 8.65391	34890 11,34609	65154 8.65435	$34846 \\ 11.34565$	00044 10.00044	99956 9.99956	25
36	65670	34330	65715	34285	00045	99955	24
37	65947	34053	65993	34007	00045	99955	23
38	66223	33777	66269	33731	00046	99954	22
39	66497	33503	66543	33457	00046	99954	21
40	8.66769	11.33231	8.66816	11.33184	10.00047	9.99953	20
41 42	67039	32961 32692	67087	$32913 \\ 32644$	00048	99952 99952	19 18
43	67308 67575	32425	67356 67624	32376	00048	99951 99951	17
44	67841	32159	67890	32110	00049	99951	16
45	8.68104	11.31896	8.68154	11,31846	10.00050	9.99950	15
46	68367	31633	68417	31583	00051	99949	14
47	68627	31373	68678	31322	00051	99949	13
48	68886	31114	68938	31062	00052	99948 00048	12
49 50	69144 8.69400	30856 11.30600	69196 8,69453	$30804 \\ 11.30547$	00052 10.00053	99948 9,99947	11 10
51	69654	30346	69708	30292	00054	99946	9
52	69907	30093	69962	30038	00054	99946	87
53	70159	29841	70214	29786	00055	99945	
54	70409	29591	70465	29535	00056	99944	6
55	8.70658	11.29342	8.70714	11.29286	10.00056	9.99944	5
56	70905	29095 28849	70962	29038	00057	99943	4
57 58	71151 71395	28849 28605	71208 71453	$28792 \\ 28547$	00058	99942 99942	1 3
59	71638	28005	71455	28303	00058	99942 99941	
60	71880	28120	71940	28060	00060	99940	Ō
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

3°			Logar	ithms.			170
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M
0	8.71880	11.28120	8.71940	11.28060	10.00060	9.99940	6
1	72120	$27880 \\ 27641$	72181 72420	27819 27580 27341	00060	99940	59
$^{2}_{3}$	72359	27641	72420	27580	00061	99939	51
	72597	27403	72659	27341	00062	99938	5
4	72834	27166	72896	27104	00062	99938	5
5 6	8.73069	11.26931	8.73132	11.26868	10.00063	9.99937	5
5	73303	26697	73366	26634	00064	99936	5
7	73535 73767	26465 26233	73600 73832	26400 26168	00064	99936 99935	53
8 9	73997	26003	74063	25937	00065	99933	
10	8.74226	11.25774	8.74292	11.25708	10.00066	9,99934	51
11	74454	25546	74521	25479	00067	99933	4
12	74680	25320	74748	25252	00068	99932	4
13	74906	25094	74974	25026	00068	99932	47
î 4	75130	24870	75199	24801	00069	99931	4
15	8.75353	11.24647	8.75423	11.24577	10.00070	9.99930	45
16	75575	24425	75645	24355	00071	99929	44
17	75795	24205	75867	24133	00071	99929	43
18	76015	23985	76087	23913	00072	99928	42
19	76234	23766	76306	93604	00073	99927	41
20	8.76451	11.23549	8.76525 76742	11.23475	10.00074	9.99926	40
$\frac{1}{21}{22}$	76667	23333	76742	23258	00074	99926	39
22	76883	23117	76958	23042	00075	99925	38
23	77097	22903	77173	22827	00076	99924	37
24	77310	22690	77387	22613	00077	99923	36
25	8.77522	11.22478	8.77600	11.22400	10.00077	9.99923	35
26	77733	22267	77811	22189	· 00078	99922	34
26 27 28	77943	22057	78022	21978	00079	99921	33
28	78152	21848	78232	21768	00080	99920	32
29	78360	21640	78441	21559	00080	99920	81
30 31	8.78568	11.21432	8.78649	11.21351	10.00081	9.99919	30
$\frac{31}{32}$	78774 78979	21226 21021	78855	21145	00082	99918	29
$\frac{32}{33}$	79183	20817	79061	20939	00083	99917	28
34	79386	20614	79266 79470	$20734 \\ 20530$	00083	99917	27
35	8.79588	11.20412	8.79673	11.20327	00084	99916	26
86	79789	20211	79875	20125	10.00085 00086	$9.99915 \\ 99914$	25 24
37	79990	20010	80076	19924	00087	99914 99913	24
38	80189	19811	80277	19723	00087	99913	22
39	80388	19612	80476	19524	00088	99912	21
40	8.80585	11.19415	8.80674	11.19326	10.00089	9.99911	20
ii	80782	19218	80872	19128	00090	99910	19
12	80978	19022	81068	18932	00091	99909	18
13	81173	18827	81264	18736	00091	99909	17
14	81367	18633	81264 81459	18736 18541	00092	99908	16
15	8.81560	11.18440	8.81653	11.18347	10.00093	9.99907	15
16	81752	18248	81846	18154	00094	99906	14
7	81944	18056	82038	17962	00095	99905	13
8	82134	17866	82230	17770	00096	99904	12
9	82324	17676	82420	17580	00096	99904	11
0	8.82513	11.17487	8.82610	17580 11.17390	10.00097	9.99903	10
$\frac{1}{2}$	82701 82888	17299 17112	82799	17201	00098	99902	9
3	82888 83075	16925	82987	17013	00099	99901	8 7 6
4	83261	16925	83175 83361	16825	00100	99900	7
5	8.83446	16739 11.16554	8.83547	16639	00101	99899	6
6	83630	16370	83732	$11.16453 \\ 16268$	10.00102	9.99898	5
7	83813	16187	83916	16084	00102	99898	4
8	83996	16004	84100	15900	00103	99897	3
ğ	84177	15823	84282	15718	00104 00105	99896	5 4 3 2 1
ŏ	84358	15642	84464	15536	00105	99895 9989 4	10
-!-		[10000	00100	33034	U
ſ.	Cosine.	Secant.	Cotangent.	Tangent.			

28	1
20	٠

4°			Logar	ithms.			175°
М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	8.84358	11.15642	8.84464	11.15536	10.00106	9.99894	60
1	84539	$15461 \\ 15282$	84646 84826	15354	00107	99893	59
2	84718 84897	15282	84820	15174 14994	00108	99892 99891	58 57
34 56	85075	14925	85185	14815	00109	99891	56
5	8.85252	11.14748	8.85363	11.14637	10.00110	9.99890	55
6	85429	14571	85540	14460	00111	99889	54
7 8	85605 85780	14395 14220	85717 85893	14283 14107	00112 00113	99888 99887	53
9	85955	14045	86069	13931	00113	99886	52 51
1ŏ	8.86128	11.13872	8.86243	11.13757	10.00115	9,99885	50
11	86301	13699	86417	13583	00116	99884	49
12	86474 86645	13526 13355	86591 86763	13409 13237	00117 00118	99883 99882	48
13 14	86816	13355	86935	13237	00118	99882 99881	47 46
15	8.86987	11.13013	8.87106	11.12894	10.00120	9,99880	45
16	87156	12844	87277	12723	00121	99879	44
17	87325	12675	87447	12553	00121	99879	43
18	87494	12506	87616	12384	00122	. 99878 99877	42
19 20	87661 8.87829	$\begin{array}{r}12506\\12339\\11.12171\end{array}$	87785 8.87953	$12215 \\ 11.12047$	00123 10.00124	9,99876	41 40
21	87995	12005	88120	11880	00125	99875	39
22	88161	11839	88287	11713	00126	99874	38
23	88326	11674	88453	11547	00127	99873	37
24 25	88490 8.88654	$11510 \\ 11.11346$	88618	$\frac{11382}{11.11217}$	00128 10.00129	99872 9.99871	36
26	88817	111183	8.88783 88948	11.11217	00130	99870	35 34
27	88980	11020	89111	10889	00131	99869	33
28	89142	10858	89274	10726	00132	99868	32
29	89304	10696	89437	10563	00133	99867	31
30 31	8.89464 89625	11.10536	8.89598 89760	$11.10402 \\ 10240$	10.00134 00135	9.99866 99865	30 29
32	89784	10375 10216	89920	10080	00136	99864	28
33	89943	10057	90080	09920	00137	99863	27
34	90102	09898	90240	09760	00138	99862	26
35 36	8.90260 90417	11.09740 09583	8.90399 90557	11.09601 09443	10.00139 00140	9.99861 99860	25 24
30 37	90574	09426	90557	09445	00140	99859	24
38	90730	09270	90872	09128	00142	99858	22
39	90885	09115	91029	08971	00143	99857	21
40	8.91040	11.08960	8.91185	11.08815	10.00144	9,99856	20
41 42	91195 91349	08805 08651	91340 91495	08660 08505	00145 00146	99855 99854	19 18
42	91502	08498	91650	08350	00140	99853	17
44	91655	08345	91803	08197	00148	99852	16
45	8.91807	11.08193	8.91957	11.08043	10.00149	9.99851	15
46 47	91959 92110	08041 07890	92110 92262	07890 07738	00150 00152	99850 99848	14 13
47	92261	07739	92414	07586	00153	99847	12
49	92411	07589	92565	07435	00154	99846	îĩ
50	8.92561	11.07439	8.92716	11.07284	10.00155	9.99845	10
51	92710	07290	92866	07134	00156	99844	9
52 53	92859 93007	07141 06993	93016 93165	 06984 06835 	00157 00158	99843 99842	8
54	93154	06846	93313	06687	00158	99841	6
55	8.93301	11.06699	8.93462	06687 11.06538	10.00160	9.99840	5
56	93448	06552	93609	06391	00161	99839	4
57	93594	06406	93756	06244	00162	99838	32
58 59	93740 93885	06260 06115	93903 94049	06097 05951	00163 00164	99837 99836	1
60 60	94030	05970	94049	05805	00164	99834	Ō
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

Logarithms.

174°

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	5°			Logar	ithms.			174°
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	М.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	8 94030	11.05970	8 94195	11 05805	10.00166	9.99834	60
$\begin{array}{cccccccccccccccccccccccccccccccccccc$								59
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	2		05683	94485	05515	00168	99832	58
	3		05539	94630	05370			
	4							
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	5		11.05254					
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	6				04940			
	7			95202				
	õ					00176	99824	51
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	10	8 95450	11 01550					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$					04233	00178		49
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	12		04272		04092	00179	99821	48
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	13		04133	96047				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	14	96005	03995	96187	03813	00181		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				8.96325				
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$								
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $								
$\begin{array}{c c c c c c c c c c c c c c c c c c c $							99014	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						10 00188	9 99812	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	21				02850	00190		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	23	97229		97421	02579			37
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	24	97363	02637					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	25				11.02309	10.00194		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	26	97629	02371	97825	02175			
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			02238		02041			33
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	28							32
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	29							
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	31		01712		01510			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	32	98419	01581		01378			28
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	33				01247		99796	27
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			01321					26
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					11.00985	10.00207		25
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						00208		24
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			00934		00725	00209		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								22
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								
$\begin{array}{cccccccccccccccccccccccccccccccccccc$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			00296					18
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		99830	00170	9.00046	10.99954	00217	99783	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$						00218		16
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				00553				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				00805		00223		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			99172					9
	52	00951	99049	01179	98821	00228	99772	8
	53	01074	98926	01303	98697	00229	99771	7
	54	01196			98573		99769	6
59 01803 98197 02040 97960 00237 99763 1 60 01923 98077 02162 97838 00239 99761 0	55							5
59 01803 98197 02040 97960 00237 99763 1 60 01923 98077 02162 97838 00239 99761 0			98560	01673	98327	00233		4
59 01803 98197 02040 97960 00237 99763 1 60 01923 98077 02162 97838 00239 99761 0	58							
<u>60</u> 01923 98077 02162 97838 00239 99761 0		01803	98197			00230		Ĩ
M. Cosine, Secant. Cotangent, Tangent, Cosecant. Sine, M.		01923						Ô
	М.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

95°

	Logarithms.									
Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.					
9.01923	10.98077	9.02162	10,97838	10.00239	9.99761					
02043	97957	02283	97717	00240	99760					
02163	97837	02404	97596	00241	99759					
02283	97717	02525	97475	00243	99757					
02402	97598	02645	97355	00244	99756					
9.02520	10.97480	9.02766	10.97234	10.00245	9.99755					
02639	97361	02885	97115	00247	99753					
02757	97243	03005	96995	00248	99752					

<u>M</u> .	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.01923	10.98077	9.02162	10,97838	10.00239	9.99761	60
1	02043	97957	02283	97717	00240	99760	59
23	02163	97837	02404	97596	00241	99759	58
3	02283	97717	02525	97475	00243	99757	57
4	02402	97598	02645	97355	00244	99756	56
5	9.02520	10.97480	9.02766	10.97234	10.00245	9,99755	55
4 5 6	02639	97361	02885	97115	00247	99753	54
7	02757	97243	03005	96995	00248	99752	53
8	02874	97126	03124	96876	00249	99751	52
9	02992	97008	03242	96758	09251	99749	51
10	9.03109	10.96891	9.03361	10.96639	10.00252	9.99748	50
11	03226	96774	03479	96521	00253	99747	49
12	03342	96658	03597	96403	00255	99745	48
13	03458	96542	03714	96286	00256	99744	47
14	03574	96426	03832	96168	00258	99742	46
15	9.03690	10.96310	9.03948	10.96052	10.00259	9.99741	45
16	03805	96195	04065	95935	00260	99740	44
17 18	03920	96080	04181	95819	00262	99738	43 42
19	04034 04149	95966 95851	04297 04413	95703 95587	00263 00264	99737 99736	42
20	9.04262	10.95738	9.04528	10.95472	10.00266	9.99734	40
21	04376	95624	04643	95357	00267	99733	39
22	04370	95510	04758	95242	00269	99731	38
23	04603	95397	04873	95127	00270	99730	37
24	04715	95285	04987	95013	00272	99728	36
25	9.04828	10,95172	9.05101	10.94899	10.00273	9.99727	35
26	04940	95060	05214	94786	00274	99726	34
27 28	05052	94948	05328	94672	0.)276	99724	33
28	05164	94836	05441	94559	00277	99723	32
29	05275	94725	05553	94447	00279	99721	31
30	9.05386	10.94614	9.05666	10.94334	10.00280	9.99720	30
31	05497	94503	05778	94222	00282	99718	29 28
32	05607	94393	05890	94110	00283	99717	28
33	05717	94283	06002	93998	00284	99716	27
34	05827	94173	06113	93887	00286	99714	26 25
35	9.05937	10.94063	9.06224	10.93776	10.00287	9.99713	20
36 37	06046 06155	93954 93845	06335 06445	93665 93555	00289 00290	99711 99710	24
38	06264	93736	06556	93444	00290	99708	23
39	06372	93628	06666	93334	00293	99707	21
40	9.06481	10.93519	9.06775	10.93225	10.00295	9.99705	20
4ĭ	06589	93411	06885	93115	00296	99704	19
$\hat{4}\hat{2}$	06696	93304	06994	93006	00298	99702	18
43	06804	93196	07103	92897	00299	99701	17
44	06911	93089	07211	92789	00301	99699	16
45	9.07018	10.92982	9.07320	10.92680	10.00302	9.99698	15
46	07124	92876	07428	92572	00304	99696	14
47	07231	92769	07536	92464	00305	99695	13
48	07337	92663	07643	92357	00307	99693	12
49	07442	92558	07751	92249	00308	99692	11
50	9.07548	10.92452	9.07858	10.92142	10.00310	9.99690	10
51	07653	92347	07964	92036	00311	99689	9
52	07758	92242	08071	91929	00313	99687	8 7 6 5 4
53 54	07863	92137 92032	08177 08283	91823 91717	00314 00316	99686 99684	
55 55	07968 9.08072	10.91928	9.08283	10.91611	10.00315	99684 9.99683	0
ээ 56	9.08072	91824	08495	91505	00319	9.99683	1
50 57	08170	91824	08495	91400	00319	99680	3
58	08383	91617	08705	91295	00320	99678	2
59	08486	91514	08810	91190	00323	99677	3 2 1
60	08589	91411	08914	91086	00325	99675	ō
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.
060							830

M.

283 173°

M.

LOGARITHMIC	ANGULAR I

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7 °			172°				
M,	Sine,	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.08589	10.91411	9.08914	10,91086	10.00325	9.99675	60
1 2 3 4 5	08692	91308	09019	90981	00326	99674	59
2	08795	91205	09123	90877	00328	99672	58
3	08897	91103	09227	90773	00330	99670	57
4	08999	91001	09330	90670	00331	99669 9.99667	56 55
0	9.09101 09202	10.90899 90798	9.09434 09537	10.90566 90463	10.00333 00334	999666	54
6 7	09202	90696	09640	90360	00336	99664	53
8	09405	90595	09742	90258	00337	99663	52
9	09506	90494	09845	90155	00339	99661	51
10	9.09606	10.90394	9.09947	10.90053	10.00341	9.99659	50
11	09707	90293	10049	89951	00342	99658	49
12	09807	90193	10150	89850	00344	99656	48
13	09907	90093	10252 10353	89748	00345	99655	47
14	10006	89994	10353	89647	00347	99653	46
15	9.10106	10.89894	9.10454	10.89546	10.00349	9.99651	45
16 17	$10205 \\ 10304$	89795	10555	89445	00350	99650 99648	44
18	10304	89696 89598	10656 10756	89344 89244	00352	99648	$\frac{43}{42}$
19	10501	89499	10856	89144	00355	99645	41
20	9.10599	10.89401	9.10956	10.89044	10.00357	9,99643	40
$\tilde{2}\tilde{1}$	10697	89303	11056	88944	00358	99642	39
22	10795	89205	11155	88845	00360	99640	38
23	10893	89107	11254	88746	00362	99638	37
24	10990	89010	11353	88647	00363	99637	36
25	9.11087	10.88913	9.11452	10.88548	10.00365	9.99635	35
26	11184	88816	11551	88449	00367	99633	34
$\frac{27}{28}$	11281	88719	11649	88351	00368	99632	33
28 29	$\frac{11377}{11474}$	88623 88526	$11747 \\ 11845$	88253 88155	00370	99630 99629	32 31
30	9.11570	10.88430	9.11943	10.88057	10.00373	9.99627	30
31	11666	88334	12010	87960	00375	99625	29
32	11761	88239	12138	87862	00376	99624	28
33	11857	88143	12235	87765	00378	99622	27
34	11952	88048	12332	87668	00380	99620	26
35	9.12047	10.87953	9.12428	10.87572	10.00382	9.99618	25
36	12142	87858	12525	87475	00383	99617	24
37	$12236 \\ 12331$	87764	12621	87379	00385	99615	23
38 39	12331	87669	12717	87283	00387	99613	22 21
40	$12425 \\ 9.12519$	$87575 \\ 10.87481$	12813 9.12909	87187 10.87091	00388 10.00390	99612 9.99610	20
41	12612	87388	13004	86996	00392	99608	19
42	12706	87294	13099	86901	00393	99607	18
43	12799	87294 87201	13194	86806	00395	99605	17
44	12892	87108	13289	86711	00397	99603	16
45	9.12985	10.87015	9.13384	10.86616	10.00399	9.99601	15
46	13078	86922	13478	86522	00400	99600	14
47	13171	86829 86737	13573	86427	00402	99598	13
48	13263	86737	13667	86333	00404	99596	12
49 50	$13355 \\ 9.13447$	$86645 \\ 10.86553$	13761	86239	00405	99595	11
51	13539	86461	9.13854 13948	$10.86146 \\ 86052$	10.00407 00409	9.99593 99591	10
52	13630	86370	14041	85959	00409	99589	
53	13722	86278	14134	85866	00411	99588	8
54	13813	86187	14227	85773	00414	99586	6
55	9.13904	10.86096	9.14320	10.85680	10.00416	9.99584	6 5
56	13994	86006	14412	85588	00418	99582	4
57	14085	85915	14594	85496	00419	99581	ŝ
58 59	14175	85825	14597	85403	00421	99579	2
- 59 - 60	$14266 \\ 14356$	$85734 \\ 85644$	14688	85312	00423	99577	
			14780	85220	00425	99575	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine,	M .

97°

-		Logarithms.					
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine,	M.
0	9.14356	10.85644	9.14780	10.85220	10.00425	9.99575	60
1	14445	85555	14872	85128	00426	99574	59
$\overline{2}$	14535	85465	14963	85037	00428	99572	58
3	14624	85376	15054	84946	00430	99570	57
45	14714	85286	15145	84855	00432	99568	56
5	9.14803	10.85197	9.15236	10.84764	10.00434	9.99566	55
67	14891	85109	15327	84673	00435	99565	54
~	14980	85020	15417	84583	00437	99563	53
89	$15069 \\ 15157$	84931	15508	84492	00439	99561	52
10	9.15245	84843 10.84755	15598	84402	00441	99559 9.99557	51
11	15333	84667	9.15688 15777	$10.84312 \\ 84223$	$10.00443 \\ 00444$	99556	50 49
12	15421	84579	15867	84133	00446	99554	48
13	15508	84492	15956	84044	00448	99552	47
14	15596	84404	16046	83954	00450	99550	46
15	9.15683	10.84317	9.16135	10.83865	10.00452	9.99548	45
16	15770	84230	16224	83776	00454	99546	44
17	15857	84143	16312	83688	00455	99545	43
18	15944	84056	16401	83599	00457	99543	42
19	16030	83970	16489	83511	00459	99541	41
20	9.16116	10.83884	9,16577	10.83423	10.00461	9,99539	40
21	16203	83797	16665	83335	00463	99537	39
22	16289	83711	16753	83247	00465	99535	38
23	16374	83626	16841	83159	00467	99533	37
24	16460	83540	16928	83072	00468	99532	36
25	9.16545	10.83455	9.17016	10.82984	10.00470	9.99530	35
26	16631	83369	17103	82897	00472	99528	34
27	16716	83284	17190	82810	00474	99526	33
28	16801	83199	17277	82723	00476	99524	32
27 28 29 30	16886	83114	17363	82637	00478	99522	31
30	9.16970	10.83030	9.17450	10.82550	10.00480	9.99520	30
31 32	$17055 \\ 17139$	82945 82861	17536		00482	99518	29 28
33	17139	82777	17622 17708	82292	00483 (00485	$99517 \\ 99515$	23
34	17307	82693	17794	82206	00487	99513 99513	26
35	9,17391	10.82609	9.17880	10.82120	10.00489	9.99511	25
36	17474	82526	17965	82035	00491	99509	24
37	17558	82442	18051	81949	00493	99507	23
38	17641	82250	18136	81864 81779 10.81694	00495	99505	22
39	17724	82276	18221	81779	00497	99503	21
40	9,17807	10.82193	9.18306	10.81694	10.00499	9.99501	20
41	17890	82110	18391	81609	00501	99499	19
42	17973	82027	18475	81525	00503	99197	18
43	18055	81945	18560	81440	00505	99495	17
44	18137	81863	18644	31356	00506	99494	16
45	9.18220	10.81780	9.18728	10.81272	10.00508	9.99492	15
46	18302	81698	18812	81188	00510	99490	14
47	18383	81617	18896	81104	00512	99488	13
48	18465	81535	18979	81021	00514	99486	12
49	18547	81453	19063	80937	00516	99484	11
50	9.18628	10.81372	9.19146	10.80854	10.00518	9.99482	10
51	18709	81291	19229	80771	00520	99480 99478	9
52 53	18790	81210	19312	80688	00522		87
54	$ 18871 \\ 18952 $	81129 81048	19395 19478	80605 80522	00524 00526	99476 99474	6
54 55	9.19033	10.80967	9,19561	10,80439	10,00528	99474	5
55 56	9.19033 19113	80887	19643	80357	00530	9.99472 99470	4
57	19113	80807	19043	80275	00532	99470 99468	3
58	19193	80727	19725	80193	00534	99466	
59	19353	80647	19889	80155	. 00536	99464	1 1
60	19433	80567	19971	80029	00538	99462	l ô

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	M.	Sine.	Cosecant,	Tangent,	Cotangent	Secant.	Cosine.	1
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								- -
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	5	19509						
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	3	19672	80328		79784			
6 19909 80091 20459 79460 00552 99448 8 20067 79933 20021 79379 00554 99448 9 20145 79855 20701 79299 00556 99444 10 10 9.20223 10.79777 9.20782 10.72138 00566 99444 10 11 20302 79698 20862 79138 00566 99438 4 12 20380 78620 20942 78078 00564 99438 4 13 20458 79542 21022 78978 00564 99439 4 15 9.20613 10.79387 9.21182 10.78818 10.00577 99427 4 20 9.20921 79078 21499 78540 00575 99427 4 21 21076 78944 21657 78343 00581 99417 3 21 21076 78944 21657	4							
6 19909 80091 20459 79460 00552 99448 8 20067 79933 20021 79379 00554 99448 9 20145 79855 20701 79299 00556 99444 10 10 9.20223 10.79777 9.20782 10.72138 00566 99444 10 11 20302 79698 20862 79138 00566 99438 4 12 20380 78620 20942 78078 00564 99438 4 13 20458 79542 21022 78978 00564 99439 4 15 9.20613 10.79387 9.21182 10.78818 10.00577 99427 4 20 9.20921 79078 21499 78540 00575 99427 4 21 21076 78944 21657 78343 00581 99417 3 21 21076 78944 21657	5				10 79622			1
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	6				79541			- E
8 20067 79933 20021 79370 00554 99444 10 9.20145 79855 20701 79299 00556 99444 1 11 20302 79698 20862 79138 00560 99442 1 12 20380 79620 20942 78078 00564 99438 4 13 20458 79620 21022 78978 00564 99434 4 14 20555 79465 21102 78898 00566 99432 4 16 20691 73399 21261 78739 00571 99427 4 20 9.20768 79232 21341 78560 00577 99423 4 21 21076 78924 21657 78843 00581 99417 3 22 21153 78847 21736 78264 00583 94117 3 23 21205 777751 00559	7							18
9 20145 79855 20701 79299 00556 99444 2 11 20302 79698 20862 79138 00566 99442 1 12 20380 79620 20942 79058 00564 99438 4 12 20380 79620 20942 78078 00564 99432 4 14 20535 79465 21102 78898 00566 99432 4 15 9.26613 10.79387 9.21182 10.78818 10.00568 9.9432 4 16 20691 79309 21241 78580 00577 99427 4 18 20845 79155 21420 78580 00577 99427 4 21 20767 7843 00581 99417 3 2 2 2134 00581 94117 3 22 21153 7847 21736 78244 00581 94117 3	8							Ē
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	9							
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	10		10.79777					5
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			79698					4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			79620	20942				4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		20458	79542	21022				4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		20535	79465					4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	15		10.79387	9,21182	10.78818	10.00568		4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	16			21261	78739		99429	4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			79232	21341	78659		99427	4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			79155	21420	78580	00575	99425	4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	19		79078	21499	78501		99423	4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	20				10.78422	10.00579	9.99421	4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	21					00581	99419	3
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	22	21153			78264	00583	99417	3
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	23				78186	00585		3
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								3
$\begin{array}{c c c c c c c c c c c c c c c c c c c $				9.21971		10.00589		3
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	26	21458		22049	77951	00591		3
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	27		78466					33
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		21610	78390	22205		00596		3:
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	29	21685			77717	00598		31
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	30		10.78239					
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			78164	22438				29
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	52 59			22516	77484			28
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		0.00197	10 77938	22670				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		90911						25
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	27				77176			24
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			77620	22901	77099			
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		22001	77565	02054	77023			
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		9 22509	10 77401	20001	76946	00619		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		22583	77.117	9.20100	10.76870	10.00621		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		22657	77949		70794	00623	99377	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		22731				00025		
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		22805			76565			
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $			10.77122		10 76100	10.00030		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		22952			7641.4			
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	7							
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	8		76902	23737				
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		23171		23812	76188	00641		
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		9.23244		9,23887				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		23317					99355	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			76610	24037				8
9 9.3007 10.76333 9.24261 10.75739 10.00554 9.99346 5 5 23679 76321 24335 75665 00656 99344 4 7 23752 76248 24410 75590 00658 99342 3 8 23823 76177 24484 75516 00660 99340 2 9 23895 76105 24558 75442 00663 99337 1 9 23967 76633 24632 75368 00665 99335 0 . Cosine, Secant, Cotangent, Tangent, Cosecant, Sine, M,		23462	76538	24112	75888			7
9 9.3007 10.76333 9.24261 10.75739 10.00554 9.99346 5 5 23679 76321 24335 75665 00656 99344 4 7 23752 76248 24410 75590 00658 99342 3 8 23823 76177 24484 75516 00660 99340 2 9 23895 76105 24558 75442 00663 99337 1 9 23967 76633 24632 75368 00665 99335 0 . Cosine, Secant, Cotangent, Tangent, Cosecant, Sine, M,	1	23535	76465	24186				6
5 23679 76321 24335 75665 00656 99344 4 7 23752 76248 24410 75590 00658 99342 3 3 23823 76177 24484 75516 00660 99340 2 9 23895 76105 24558 75442 00663 99337 1 9 23967 76033 24632 75368 00665 99335 0 . Cosine, Secant, Cotangent, Tangent, Cosecant, Sine, M.			10.76393	9.24261	10.75739			5
7 23752 76248 24410 75590 00658 99342 3 8 23823 76177 24481 75516 00660 99340 2 9 23895 76105 24558 75442 00663 99337 1 0 23967 76033 24632 75368 00665 99335 0 . Cosine, Secant, Cotangent, Tangent, Cosecant, Sine, M,		23679	76321	24335	75665			4
5 23823 76177 24481 75516 00660 99340 2 9 23895 76105 24558 75442 00663 99337 1 0 23967 76033 24632 75368 00665 99335 0 . Cosine, Secant, Cotangent, Tangent, Cosecant, Sine, M,	7	23752	76248	24410				3
9 23895 76105 24555 75442 00663 99337 1 0 23967 76033 24632 75368 00665 99335 0 . Cosine, Secant, Cotangent, Tangent, Cosecant, Sine, M.	8		76177					- 9
0 23967 76033 24632 75368 00665 99335 0 . Cosine, Secant, Cotangent, Tangent, Cosecant, Sine, M,			76105	24558				ĩ
in grant angenet, i concentit, bille, in,	<u> </u>	23967	76033	24632				
	.	Cosine,	Secant.	Cotangent.	Tangent,	Cosecant.	Sine,	М.

10°			Logar	ithms.			169°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.23967	10.76033	9.24632	10.75368	10.00665	9.99335	60
1	24039	75961	24706	75294	00667	99333	59
$\frac{\overline{2}}{3}$	24110	75890	24779	75221 75147	00669	99331	58
3	$24181 \\ 24253$	75819 75747	24853 24926	75074	00672 00674	99328 99326	57 56
4 5	9.24324	10.75676	9.25000	10.75000	10.00676	9.99324	55
6	24395	75605	25073	74927	00678	99322	54
7 8	24466	75534	25146	74854	00681	99319	53
8	24536	75464	25219	74781	00683	99317	52
9 10	$24607 \\ 9.24677$	75393	25292 9.25365	74708	00685 10,00687	99315 9.99313	51
11	24748	10.75323 75252	25437	10.74635 74563	00690	99310	50 49
12	24818	75182	25510	74490	00692	99308	48
13	24888	75112	25582	74418	00694	99306	47
14	24958	75042	25655	74345	00696	99304	46
15	9.25028	10.74972	9.25727	10.74273	10.00699	9.99301	45
16 17	25098 25168	74902 74832	25799 25871	74201 74129	00701 00703	99299 99297	44
18	25237	74763	25943	74057	00706	99294	43
19	25307	74693	26015	73985	00708	99292	41
20	9.25376	10.74624	9.26086	10.73914	10.00710	9.99290	40
21	25445	74555	26158	73842	00712	99288	39
22	25514	74486	26229	73771	00715	99285	38
23 24	25583 25652	74417 74348	26301 26372	73699 73628	00717 00719	99283 99281	37
25	9.25721	10.74279	9.26443	10.73557	10.00722	9.99278	35
26	25790	74210	26514	73486	00724	99276	34
27	25858	74142	26585	73415	00726	99274	33
28	25927	74073	26655	73345	00729	99271	32
29	25995	74005	26726	73274	00731	99269	31
$\frac{30}{31}$	9.26063 26131	10.73937 73869	9.26797 26867	10.73203 73133	10.00733 00736	9.99267 99264	30 29
32	26199	73801	26937	73063	00738	99262	28
33	26267	73733	27008	72992	00740	99260	27
34	26335	73665	27078	72922	00743	99257	26
35	9.26403	10.73597	9.27148	10.72852	10.00745	9.99255	25
36	26470	73530	27218	72782	00748	99252	24
37 38	26538 26605	73462	27288 27357	72712 72643	00750 00752	99250 99248	23 22
39	26672	73328	27427	72573	00755	99245	21
40	9.26739	10.73261	9.27496	10.72504	10.00757	9.99243	20
41	26806	73194	27566	72434	00759	99241	19
42	26873	73127	27635	72365	00762	99238	18
43 41	26940	73060 72993	27704 27773	72296	00764 00767	99236 99233	17
45	27007 9.27073	10.72927	9.27842	72227 10.72158	10.00769	9.99231	15
46	27140	72860	27911	72089	00771	99229	14
47	27206	72794	27980	72020	00774	99226	13
48	27273	72727	28049	71951	00776	99224	12
49	27339	72661	28117	71883	00779	99221 9.99219	11
$\frac{50}{51}$	$9.27405 \\ 27471$	$10.72595 \\ 72529$	9.28186 28254	10.71814 71746	$10.00781 \\ 00783$	9.99219 99217	10 9
52	27537	72463	28323	71677	00786	99214	8
53	27602	72398	28391	71609	00788	99212	87
54	27668	72332	28459	71541	00791	99209	6
55	9.27734	10.72266	9.28527	10.71473	10.00793	9.99207	5
56	27799	72201	28595	71405	00796	99204	4
57 58	$27864 \\ 27930$	72136 72070	28662 28730	71338 71270	00798 00800	99202 99200	3
59	27950	72005	28798	71202	00803	99197	í
60	28060	71940	28865	71135	00805	99195	ô
M.	Cosine.	Secant,	Cotangent.	Tangent.	Cosecant.	Sine.	M .

11°		Logarithms.					
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.28060	10.71940	9,28865	10.71135	10.00805	9.99195	60
1	28125	71875	28933	71067	00808	99192	59
$\frac{2}{3}$	28190	71810	29000	71000	00810	99190	58
3	28254	71746	29067	70933	00813	99187	57
4	28319	71681	29134	70866	00815	99185	56
5	9.28384	10.71616	9.29201	10.70799	10.00818	9.99182 99180	55
6	28448	71552	29268	70732	00820 00823	99177	54 53
7	28512	$71488 \\ 71423$	29335 29402	70665 70598	00825	99177	52
8	$28577 \\ 28641$	71359	29462	70532	00828	99172	51
10	9.28705	10.71295	9,29535	10.70465	10.00830	9.99170	50
11	28769	71231	29601	70399	00833	99167	49
12	28833	71167	29668	70332	00835	99165	48
13	28896	71104	29734	70266	00838	99162	47
14	28960	71040	29800	70200	00840	99160	46
15	9.29024	10.70976	9.29866	10.70134	10.00843	9.99157	45
16	29087	70913	29932	70068	00845	99155	44
17	29150	70850	29998	70002	00848	99152	43
18	29214	70786	30064	69936	00850	99150	42
19	· 29277	70723	30130	69870	00853	99147	41
20	9.29340	10.70660	9.30195	10.69805	10.00855	9.99145	40
21	29403	70597	30261	69739	00858	99142	39
22	29466	70534	30326	69674	00860	99140	38
23	29529	70471	30391	69609	00863	99137	37
24	29591	70409	30457	69543	00865	99135	36
25	9.29654	10.70346	9.30522	10.69478	10.00868	9.99132	35
26	29716	70284	30587	$69413 \\ 69348$	00870 00873	99130 99127	34 33
27	29779	70221	30652 30717	69283	00876	99127 99124	32
28 29	29841 29903	70159 70097	30782	69218	00878	99122	31
29 80	9.29966	10.70034	9,30846	10.69154	10.00881	9.99119	30
31	30028	69972	30911	69089	00883	99117	29
32	30090	69910	30975	69025	00886	99114	28
33	30151	69849	31040	68960	00888	99112	27
84	30213	69787	31104	68896	00891	99109	26
35	9.30275	10.69725	9,31168	10.68832	10.00894	9.99106	25
36	30336	69664	31233	68767	00896	99104	24
37	30398	69602	31297	68703	00899	99101	23
38	30459	69541	31361	68639	00901	99099	22
39	30521	69479	31425	68575	00904	99096	21
40	9.30582	10.69418	9.31489	10.68511	10.00907	9.99093	20
41	30643	69357	31552	68448 68384	$00909 \\ 00912$	99091 99088	19 18
42 43	30704 30765	69296	31616 31679	68321	00912	99088	17
43	30826	$69235 \\ 69174$	31743	68257	00917	99083	16
45	9.30887	10.69113	9.31806	10.68194	10.00920	9.99080	15
46	30947	69053	31870	68130	00922	99078	14
47	31008	68992	31933	68067	00925	99075	13
48	31068	68932	31996	68004	00928	99072	12
49	31129	68871	32059	67941	00930	99070	11
50	9.31189	10.68811	9.32122	10.67878	10.00933	9.99067	10
51	31250	68750	32185	67815	00936	99064	9
52	31310	68690	32248	67752	00938	99062	8
53	31370	68630	32311	67689	00941	99059	7
54	31430	68570	32373	67627	00944	99056	6
55	9.31490	10.68510	9.32436	10.67564	10.00946	9.99054	5
56	31549	68451	32498	67502	00949	99051	4
57	31609	68391	32561	67439	00952	99048	3
58	31669	68331	32623	67377	00954	99046	2
59 60	$31728 \\ 31788$	$68272 \\ 68212$	$32685 \\ 32747$	67315 67253	00957 00960	99043 99040	
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

Logarithms. 1							
ingent,	Cotangent.	Secant.	Cosine.	M.			
.32747	10.67253	10.00960	9.99040	60			
32810	67190	00962	99038	59			
32872	67128	00965	99035	58			
32933	67067	00968	99032	57			
22005	67005	00070	00030	56			

M [.] .	Sine.	Cosecant.	Tangent,	Cotangent.	Secant.	Cosine.	М.
0	9.31788	10.68212	9.32747	10.67253	10.00960	9.99040	60
1	31847	68153 68093	32810	67190	00962	99038	59
2	31907	68093	32872	67128 67067 67005	00965	99035	58
3	31966	68034 67975	32933	67067	00968	99032	57
4	32025	67975	32995	67005	00970	99030	56
5	9.32084	10.67916	9.33057	10.66943	10.00973	9.99027	55
6	32143	67857	33119	66881 66820 66758	00976	99024	54
7	32202	67798	33180	66820	00978	99022 99019	53
8	32261	67739	33242	66758	00981	99019	52
9	32319	67681	33303	66697	00984	99016	51
10	9.32378	10.67622	9.33365	10.66635	10.00987	9.99013	50
11	32437	67563	33426	66574	00989	99011	49
12	32495	67505	33487	66513	00992	99008	48
13	32553	67447	33548	66452	00995	99005	47
14	32612	67447 67388 10.67330	33609	66391 10.66330	00998 10.01000	99002 9.99000	46
15	9.32670	10.67330	9.33670	10.66330	10.01000	9.99000	40
16	32728	67272 67214	33731	66269	01003	98997 98994	44
17	32786	67214	33792	66208	01006	98991	43 42
18	32844	67156	33853	66147		98989 -	41
19	32902	67098	33913	66087	01011	9,98986	40
$ \begin{array}{c} 20 \\ 21 \\ 22 \end{array} $	9.32960	10.67040	9.33974	10.66026	10.01014	98983	39
21	33018	66982	34034	65966	01017 01020	98980	00
22	33075	66925	34095 34155	65905 65845	01020	98978	38 37
23	33133	66867	34155	65785	01022	98975	36
24	33190	66810	34215	10 65794	10.01025	9.98972	35
25	9.33248	10.66752	9.34276 34336	$10.65724 \\ 65664$	01031	98969	34
26	33305	66695		65604	01033	98967	33
27	33362	66638	34396 34456	65544	01035	98964	32
28	33420	66580 66523	34516	65484	01039	98961	31
29 30	33477 9,33534	10 00020	0.24576	10.65424	10.01042	9,98958	30
30	33591	$10.66466 \\ 66409$	9.34576 34635	65365	01045	98955	29
31	33647	66353	34605	65365 65305	01047	98953	28 27
32 33	33704	66296	34695 34755	65245	01050	98950	27
34	33761	66239	34814	65186	01053	98947	26
35	9.33818	10.66182	9.34874	10.65126	10.01056	9,98944	25
36	33874	66126	34933	$10.65126 \\ 65067$	01059	98941	24
37	33931	66069	34992	65008	01062	98938	23
38	33987	66013	35051	64949	01064	98936	22
39	34043	65957	35111 9.35170	64889	01067	98933	21
40	9.34100	10.65900	9.35170	10.64830	10.01070	9.98930	20
$\tilde{41}$	34156	65844	35229	64771	01073	98927	19
42	34212	65788	35229 35288	64712	01076	98924	18
43	34268	65732	35347	64653	01079	98921	17
44	34324	65732 65676	35405	64595	01081	98919	16
45	9,34380	10.65620	9.35464	10.64536	10.01084	9.98916	15
46	34436	65564 65509	35523	64477	01087	98913	14
47	34491	65509	35581	64419	01090	98910	13
48	34547	65453	35640	64360	01093	98907	12
49	34602	65398	35698	64302	01096 10.01099	98904	11
50	9.34658	10.65342	9.35757	10.64243 64185	10.01099	9.98901	10
51	34713	65287	35815	64185	01102	98898	9
52	34769	65231	35873	64127	01104	98896	8
53	34824	65231 65176	35931	64069	01107	98893	7
54	34879	65121	35989	64011	01110	98890	65
55	9.34934	10.65066	9.36047	10.63953	10.01113	9,98887	Ď
56	34989	65011	36105	63895	01116	98884	4
57	35044	64956	36163	63837 63779	01119 01122	98881	3
58	35099	64901	36221	63779	01122	98878	2
59	35154	64846	36279	63721	01125	98875	1
60	35209	64791	36336	63664	01128	98872	0
w	Coninc	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.
Μ.	Cosine.	Becant.	11 Cotangent.	angent.	Ubecalli.	Dine,	
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13°				166°			
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	М.
0	9.35209	10.64791	9.36336	10.63664	10.01128	9.98872	60
11	35263	64737	36394	63606	01131	98869	59
2	35318	64682	36452	63548	01133	98867	58
2 3 4	35373	64627	36509	63491	01136	98864	57
4	35427	64573	36566	$63434 \\ 10.63376$	01139 10.01142	$98861 \\ 9.98858$	56 55
5 6 7	9.35481 35536	$10.64519 \\ 64464$	$9.36624 \\ 36681$	63319	01145	98855	54
7	35590	64410	36738	63262	01148	98852	53
8	35644	64356	36795	63205	01151	98849	52
9	35698	64302	36852	63148	01154	98846	51
10	9.35752	10.64248	9.36909	10.63091	10.01157	9.98843	50
11	35806	64194	36966	63034	01160	98840	49
12	35860	64140	37023	62977	01163	98837	48
13	35914	64086	37080	62920 62863	01166	$98834 \\ 98831$	47
$\frac{14}{15}$	35968 9.36022	64032 10.63978	37137 9.37193	10.62807	01169 10.01172	93331	40
16	36075	63925	37250	62750	01175	98825	44
17	36129	63871	37306	62694	01178	98822	43
18	36182	63818	37363	62637	01181	98819	42
19	36236	63764	37419	62581	01184	98816	41
20	9.36289	10.63711	9.37476	10.62524	10.01187	9.98813	40
21	36342	63658	37532	62468	01190	× 98810	39
22	36395	63605	37588	62412	01193	98807	38
23	36449	63551	37644	62356 62300	01196	98804	37
24	$36502 \\ 9.36555$	63498	37700	10.62244	01199	$98801 \\ 9.98798$	36 35
$\frac{25}{26}$	36608	$10.63445 \\ 63392$	9.37756 37812	62188	10.01202 01205	98795	34
27	36660	63340	37868	62132	01208	98792	33
28	36713	63287	37924	62076	01211	98789	32
29	36766	63287 63234	37980	62020	01211 01214	98786	31
30	9.36819	10.63181	9.38035	10.61965	10.01217	9.98783	30
31	36871	63129	38091	61909	01220	98780	29
32	36924	63076	38147	61853	01223	98777	28
33	36976	63024	38202 38257	61798	01226	98774	27 26
$\frac{34}{35}$	37028 9.37081	62972 10.62919	9.38313	$61743 \\ 10.61687$	01229 10.01232	$98771 \\ 9.98768$	20
36	37133	62867	38368	61632	01235	98765	24
37	37185	62815	38423	61577	01238	98762	23
38	37237	62763	38479	61521	01241	98759	22
39	37289	62711	38534	61466	01244	98756	21
40	9.37341	10.62659	9.38589	10.61411	10.01247	9.98753	20
41	37393	62607	38644	61356	01250	98750	19
42 43	37445 37497	62555 62503	38699	61301	01254	98746 98743	18
43	37549	62303	38754 38808	$61246 \\ 61192$	01257 01260	98745 98740	16
45	9.37600	10.62400	9.38863	10.61137	10.01263	9.98737	15
46	37652	62348	38918	61082	01266	98734	14
47	37703	62297	38972	61028	01269	98731	13
48	37755	62245	39027	60973	01272	98728	12
49	37806	62194	39082	60918	01275	98725	11
50	9.37858	10.62142	9.39136	10.60864	10.01278	9.98722	10
51	37909 37960	62091	39190	60810 60755	01281	98719	9 8
$\frac{52}{53}$	37900 38011	62040 61989	39245 39299	60755 60701	01285 01288	98715 98712	7
54	38062	61938	39353	60647	01288	98709	6
55	9.38113	61938 10.61887	9.39407	10.60593	10.01294	9.98706	5
56	38164	61836	39461	60539	01297	98703	4
57	38215	61785	39515	60485	01300	98700	$\frac{3}{2}$
58	38266	61734	39569	60431	01303	98697	2
59	38317	61683	39623	60377	01306	98694	1
60	38368	61632	39677	60323	01310	98690	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.
107	· · · · · · · · · · · · · · · · · · ·						

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14°			Logar	ithms.			165°
М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.38368	10.61632	9.39677	10.60323	10.01310	9.98690	60
1	38418	61582	39731	60269	01313	98687	59
$\frac{2}{3}$	38469	61531	39785	60215	01316	98684	58
3	38519	61481	39838	60162	01319	· 98681	57
4 5	38570 9.38620	61430 10.61380	39892 9.39945	60108 10.60055	01322 10.01325	98678 9.98675	56 55
6	38670	61330	39999	60001	01329	98671	54
7	38721	61279	40052	59948	01332	98668	53
8	38771	61279 61229	40106	59894	01335	98665	52
9	38821	61179	40159	59841	01338	98662	51
10	9.38871	10.61129	9.40212	10.59788	10.01341	9.98659	50
11	38921	61079	40266	59734	01344	98656	49
$\frac{12}{13}$	$38971 \\ 39021$	61029	40319	59681	01348	98652 98649	48
14	39021	60979 60929	40372 40425	59628 59575	01351 01354	98649	46
15	9.39121	10.60879	9.40478	10.59522	10.01357	9.98643	45
ÎĞ	39170	60830	40531	59469	01360	98640	44
17	39220	60780	40584	59416	01364	98636	43
18	39270	60730	40636	59364	01367	98633	42
19	39319	60681	40689	59311	01370	98630	41
$\begin{array}{c} 20\\ 21 \end{array}$	9.39869 39418	10.60631	9.40742	10.59258	10.01373	9.98627 98623	40
$\frac{21}{22}$	39418	60582 60533	40795 40847	59205 59153	01377 01380	98623	39 38
23	39517	60483	40900	59100	01383	98617	37
24	39566	60434	40952	59048	01386	98614	36
25	9.39615	10.60385	9.41005	10.58995	10.01390	9.98610	35
26	39664	60336	41057	58943	01393	98607	34
27	39713	60287	41109	58891	01396	98604	33
28 29	39762 39811	60238 60189	41161	58839	01399 01403	98601 98597	$\frac{32}{31}$
30	9.39860	10.60140	41214 9.41266	$58786 \\ 10.58734$	10.01405	9.98594	30
31	39909	60091	41318	58682	01409	98591	29
$\tilde{32}$	39958	60042	41370	58630	01412	98588	28
33	40006	59994	41422	58578	01416	98584	27
34	40055	59945	41474	58526	01419	98581	26
35	9.40103	10.59897	9.41526	10.58474	10.01422	9.98578	25
36 37	40152 40200	59848 59800	41578 41629	58422 58371	01426 01429	98574 98571	24 23
38	40249	59751	41629	58319	01429	98568	20
39	40297	59703	41733	58267	01435	98565	21
40	9.40346	10.59654	9,41784	10.58216	10.01439	9.98561	20
41	40394	59606	41836	58164	01442	98558	19
42	40442	59558	41887	58113	01445	98555	18
43 44	40490	59510	41939	58061	01449	98551	17
44	40538 9.40586	$59462 \\ 10.59414$	41990 9.42041	58010 10.57959	01452 10.01455	98548 9.98545	16 15
46	40634	59366	42093	57907	01459	98541	14
47	40682	59318	42144	57856	01462	98538	13
48	40730	59270	42195	57805	01465	98535	12
49	40778	59222	42246	57754	01469	98531	11
50	9.40825	10.59175	9.42297	10.57703	10.01472	9.98528	10
51 59	40873 40921	59127 59079	42348	57652 57601	01475	98525	9
$52 \\ 53$	40921 40968	59079	42399 42450	57601 57550	01479 01482	98521 98518	87
54	41016	58984	42501	57499	01485	98515	6
55	9.41063	10.58937	9.42552	10.57448	10.01489	9.98511	$^{6}_{5}$
56	41111	58889	42603	57397	01492	98508	4
57	41158	58842	42653	57347	01495	98505	3
58	41205	58795	42704	57296	01499	98501	2
59	41252	58748	42755	57245	01502	98498	1
60	41300	58700	42805	57195	01506	98494	0
М.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M .

7 5°

15°			Logar	ithms.			164°
М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.41300	10.58700	9.42805	10.57195	10.01506	9.98494	60
1	41347	58653	42856	57144	01509	98491	59
2 3	41394	58606	42906	57094	01512	98488	58
3 4	41441 41488	58559 58512	42957 43007	57043 56993	01516 01519	98484 98481	57 56
5	9.41535	10.58465	9.43057	10.56943	10.01523	9.98477	55
5 6	41582	58418	43108	56892	01526	98474	54
ž	41628	58372	43158	56842	01529	98471	53
8	41675	58325	43208	56792	01533	98467	52
9	41722	58278	43258	56742	01536	98464	51
10	9.41768	10.58232	9.43308	10.56692	10.01540	9.98460	50
$\frac{11}{12}$	$\frac{41815}{41861}$	58185 58139	43358 43408	56642	01543	98457	49
13	41908	58092	43408	$56592 \\ 56542$	01547 01550	98453 98450	48 47
14	41954	58046	43508	56492	01553	98447	46
15	9.42001	10.57999	9,43558	10.56442	10.01557	9.98443	45
16	42047	57953	43607	56393	01560	98440	44
17	42093	57907	43657	56343	01564	98436	43
18	42140	57860	43707	56293	01567	98433	42
19	42186	57814	43756	56244	01571	98429	41
$\frac{20}{21}$	9.42232 42278	$10.57768 \\ 57722$	9.43806 43855	$ \begin{array}{r} 10.56194 \\ 56145 \end{array} $	10.01574	9.98426 98422	40
$\frac{21}{22}$	42324	57676	43905	56095	01578 01581	98422	39
23	42370	57630	43954	56046	01585	98415	37
24	42416	57584	44004	55996	01588	98412	36
25	9.42461	10.57539	9.44053	10.55947	10.01591	9.98409	35
26	42507	57493	44102	55898	01595	98405	34
27	42553	57447	44151	55849	01598	98402	33
28 29	$42599 \\ 42644$	57401	44201 44250	55799	01602 01605	98398 98395	32 31
30	9.42690	$57356 \\ 10.57310$	9.44299	55750 10.55701	10.01609	98395 9,98391	30
31	42735	57265	44348	55652	01612	98388	29
32	42781	57219	44397	55603	01616	98384	28
33	42826	57174	44446	55554	01619	98381	27
34	42872	57128	44495	55505	01623	98377	26
$\frac{35}{36}$	9.42917 42962	10.57083 57038	9.44544 44592	10.55456	10.01627	9.98373	25 24
37	43008	56992	44641	55408 55359	01630 01634	98370 98366	24 23
38	43053	56947	44690	55310	01637	98363	22
39	43098	56902	44738	55262	01641	98359	21
40	9.43143	10.56857	9.44787	10.55213	10.01644	9.98356	20
41	43188	56812	44836	55164	01648	98352	19
42 43	43233 43278	56767 56722	44884	55116	01651	98349	18
44	43323	56677	44933 44981	55067 55019	01655 01658	$\frac{98345}{98342}$	17 16
45	9,43367	10,56633	9.45029	10.54971	10.01662	9,98338	15
46	43412	56588	45078	54922	01666	98334	14
47	43457	56543	45126	54874	01669	98331	13
48	43502	56498	45174	54826	01673	98327	12
49 50	43546 9.43591	56454 10.56409	45222	54778	01676	98324	11
51	43635	56365	9.45271 45319	$10.54729 \\ 54681$	10.01680 01683	9.98320 98317	$\frac{10}{9}$
52	43680	56320	45367	54633	01687	98313	9
53	43724	56276	45415	54585	01691	98309	8 7
54	43769	56231	45463	54537	01694	98306	6
55	9.43813	10.56187	9.45511	10.54489	10.01698	9.98302	$^{6}_{5}$
56 57	43857	56143	45559	54441	01701	98299	4
57 58	43901 43946	$56099 \\ 56054$	45606	54394	01705	98295	$\frac{1}{2}$
59	43940	56010	45654 45702	$54346 \\ 54298$	01709 01712	98291 98288	12
60	44034	55966	45750	54250	01716	98284 98284	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine,	Μ.

105°

74°

Table 2. LOGARITHMIC ANGULAR FUNCTIONS.

16°			Logar	ithms.			163º
М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.44034	10.55966	9.45750	10.54250	10.01716	9.98284	60
$ \begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{array} $	44078	55922	45797	54203	01719	98281	59
2	44122	55878 55834	45845	54155	01723	98277	58
3	$44166 \\ 44210$	55790	45892 45940	54108 54060	01727 01730	98273 98270	57 56
5	9.44253	10.55747	9.45987	10.54013	10.01734	9.98266	55
6	44207	55703	46035	53965	01738	98262	54
7	44341	55659	46082	53918	01741	98259	53
8	44385	55615	46130	53870	01745	98255	52
9 10	44428 9.44472	55572	46177	53823	01749	98251	51
11	44516	10.55528 55484	9.46224 46271	$10.53776 \\ 53729$	$10.01752 \\ 01756$	9.98248 98244	50 49
12	44559	55441	46319	53681	01760	98240	48
13	44602	55398	46366	53634	01763	98237	47
14	44646	55354	46413	53587	01767	98233	46
15	9.44689	10.55311	9.46460	10.53540	10.01771	9.98229	45
$\begin{array}{c}16\\17\end{array}$	$44733 \\ 44776$	55267 55224	46507 46554	53493 53446	01774 01778	98226 98222	44 43
18	44819	55181	46601	53399	01782	98218	42
19	44862	55138	46648	53352	01785	98215	41
20	9.44905	10.55095	9.46694	10.53306	10.01789	9.98211	40
21 22	44948	55052	46741	53259	01793	98207	39
22	44992	55008	46788	53212	01796	98204	38
23 24	$45035 \\ 45077$	54965 54923	46835 46881	$53165 \\ 53119$	01800 01804	98200 98196	37 36
25	9.45120	10.54880	9.46928	10.53072	10.01808	9.98190	35
26	45163	54837	46975	53025	01811	98189	34
27	45206	54794	47021	52979	01815	98185	33
28	45249	54751	47068	52932	01819	98181	32
29 30	45292 9.45334	54708	47114	52886	01823	98177	31 30
$\frac{30}{31}$	45377	$10.54666 \\ 54623$	9.47160 47207	$10.52840 \\ 52793$	10.01826 01830	9.98174 98170	29
32	45419	54581	47253	52747	01834	98166	28
33	45462	54538	47299	52701	01838	98162	27
34	45504	54496	47346	52654	01841	98159	26
35	9.45547	10.54453	9.47392	10.52608	10.01845	9,98155	25 24
36 37	45589 45632	54411 54368	47438 47484	52562 52516	01849 01853	98151 98147	24 23
38	45674	54326	47530	52470	01856	98144	22
39	45716	54284	47576	52424	01860	98140	$2\overline{1}$
40	9.45758	10.54242	9.47622	10.52378	10.01864	9,98136	20
41	45801	54199	47668	52332	01868	98132	19
42 43	45843 45885	54157 54115	47714 47760	52286 52240	01871	98129 98125	$\frac{18}{17}$
44	45927	54073	47806	52194	01875 01879	98120	16
45	9.45969	10.54031	9.47852	10.52148	10.01883	9.98117	15
46	46011	53989	47897	52103	01887	98113	11
47	46053	53947	47943	52057	01890	98110	13
48 49	46095	53905	47989 48035	52011 51965	01894	98106	12
49 50	46136 9.46178	53864 10.53822	9.48080	10.51920	01898 10.01902	98102 9.98098	10
51	46220	53780	48126	51874	01906	98094	9
52	46262	53738	48171	51829	01910	98090	87
53	46303	53697	48217	51783	01913	98087	7
54	46345	53655	48262	51738	01917	98083	6 5
55 56	9.46386 46428	$10.53614 \\ 53572$	9.48307 48353	$10.51693 \\ 51647$	10.01921	9.98079 98075	5
57	46469	53531	48303	51647	01925 01929	98075	4
58	46511	53489	48443	51557	01929	98067	$\frac{3}{2}$
59	46552	53448	48489	51511	01937	98063	1
60	46594	53406	48534	51466	01940	98060	0
M .	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

Logarithms.

17°			Logar	ithms.			1620
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.46594	10.53406	9.48534	10.51466	10.01940	9.98060	60
1	46635	53365	48579	51421	01944	98056	59
2	46676	53324	48624	51376	01948	98052	58
2 3 4 5 6 7	46717	53283	48669	51331	01952	98048	57
4	46758	53242	48714	$51286 \\ 10.51241$	01956	98044	56
5	9.46800	10.53200	9.48759	10.51241	10.01960 01964	9.98040 98036	55 54
07	$46841 \\ 46882$	53159 53118	$48804 \\ 48849$	$51196 \\ 51151$	01968	98032	53
8	46923	53077	48894	51106	01971	98029	52
9	46964	53036	48939	51061	01975	98025	51
10	9.47005	10.52995	9.48984	$10.51016 \\ 50971$	10.01979	9.98021	50
11	47045	52955	49029	50971	01983	98017	49
12	47086	52914	49073	50927	01987	98013	48
$\overline{13}$	47127	52873	49118	50882 50837	01991	98009	47
14	47168	52832	49163	50837	01995	98005	46
15	9.47209	10.52791	9.49207	10.50793	10.01999	9.98001	45
16	47249	$52751 \\ 52710$	49252 49296	50748	02003	97997 97993	44 43
17	47290 47330	52670	49296	50704 50659	02007	97993	40
18	47371	52629	49385	50615	02014	97986	41
$19 \\ 20$	9.47411	10.52589	9.49430	10.50570	10.02018	9.97982	40
21	47452	52548	49474	50526	02022	97978	39
$\frac{21}{22}$	47492	52508	49519	50481	02026	97974	38
23	47533	52467	49563	50437	02030	97970	38 37
24	47573	52427	49607	50393	02034	97966	36
$ \begin{array}{r} 24 \\ 25 \\ 26 \\ 27 \end{array} $	9.47613	10.52387	9.49652	10.50348	10.02038	9.97962	35
26	47654	52346	49696	50304	02042	97958	34
27	47694	52306	49740	50260	02046	97954	33
28	47734	52266 52006	49784	50216	02050	97950 070.16	32
29 30	47774 9,47814	$52226 \\ 10.52186$	49828 9.49872	$50172 \\ 10.50128$	$02054 \\ 10.02058$	$97946 \\ 9.97942$	31 30
31	47854	52146	49916	50084	02062	97938	29
32	47894	52106	49960	50040	02066	97934	28
33	47934	52066	50004	49996	02070	97930	27
33 34	47974	52026	50048	49952	02074	97926	26
- 35	9.48014	10.51986	9.50092	10.49908	10.02078	9.97922	25
36	48054	51946	50136	49864	02082	97918	24
37	48094	51906	50180	49820	02086	97914	23
38 39	48133	51867	50223	49777	02090	97910	22
39 40	48173	$51827 \\ 10.51787$	50267 9.50311	49733 10.49689	02094 10.02098	97906 9.97902	21 20
40	$9.48213 \\ 48252$	51748	50355	49645	02102	97898	19
42	48292	51708	50398	49602	02102	97894	18
43	48332	51668	50442	49558	02110	97890	17
44	48371	51629	50485	49515	02114	97886	16
45	9.48411	10.51589	9.50529	10.49471	10.02118	9.97882	15
46	48450	51550	50572	49428	02122	97878	14
47	48490	51510	50616	49384	02126	97874	13
48	48529	51471	50659	49341	02130	97870	12
49	48568	51432	50703	49297	02134	97866	11
$\frac{50}{51}$	$9.48607 \\ 48647$	10.51393	9.50746	$10.49254 \\ 49211$	$10.02139 \\ 02143$	9.97861	10
52	48686	$51353 \\ 51314$	50789 50833	49211 49167	02143 02147	97857 97853	9 8 7
53	48725	51275	50876	49124	02147	97849	1 7
54	48764	$51275 \\ 51236 \\ 10.51197$	50919	49081	02155	97845	6
55	9.48803	10.51197	9.50962	10.49038	10.02159	9.97841	5
56 57	48842	51158	51005	48995	02163	97837	4
57	48881	51119	51048	48952	02167	97833	3
58 59	48920	51080	51092	48908	02171	97829	2
59	48959	51041	51135	48865	02175	97825	1
60	48938	51002	51178	48822	02179	97821	0
M	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M .

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180			Logar	ithms.			161°
М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M .
0 1	9.48998	10.51002	9.51178	10.48822	10.02179	9.97821	60
1	49037	50963	51221	48779	02183 02188	97817	59
2	49076 49115	50924 50885	51204	$48736 \\ 48694$	02188	97812 97808	58 57
2 3 4 5 6	49153	50847	51264 51306 51349	48651	02196	97804	56
5	9.49192	10.50808	9.51392	10.48608	02196 10.02200	9.97800	55
6	49231	10.50808 50769	51435	48565	02204	97796	54
7	49269	50731	51478	48522 48480	02208	97792	53
8 9	49308 49347	50692 50653	51520 51563	48430	02212	97788 97784	52 51
10	9.49385	10.50615	9.51606	10.48394	10.02221	9.97779	50
ĩĩ	49424	50576	51648	48352	02225	97775	49
12	49462	50538	51691	48309	02229	97771	48
13	49500	50500	51734 51776	48266 48224	02233	97767	47
$\frac{14}{15}$	49539 9.49577	$50461 \\ 10.50423$	9.51819	48224 10.48181	$02237 \\ 10.02241$	97763 9.97759	46 45
16	49615	50385	51861	48139	02246	97754	40
17	49654	50346	51903	48097	02250	97750	43
18	49692	50308	51946	48054	02254	97746	42
19	49730	50270	51988	48012	02258	97742	41
20	9.49768	10.50232	9.52031	10.47969	10.02262	9.97738	40
21	49806 49844	50194	52073	47927 47885	02266 02271	97734 97729	39 38
$\frac{22}{23}$	49882	50156 50118	52115 52157	47843	02275	97725	37
24	49920	50080	52200	47800	02279	97721	36
25	9.49958	10.50042	9.52242	10.47758	02279 10.02283	9.97717	35
26	49996	50004	52284	47716	02287	97713	34
27	50034	49966	52326	47674	02292	97708	33
$\frac{28}{29}$	50072 50110	49928 49890	52368 52410	47632 47590	02296 02300	97704 97700	32 31
$\frac{29}{30}$	9.50148	10.49852	9.52452	10.47548	10.02304	9.97696	30
31	50185	49815	52494	47506	02309	97691	29
32	50223	49777	52536	47464	02313	97687	28
33	50261	49739	52578	47422	02317	97683	27
34	50298	49702	52620	47380	02321	97679	26
$\frac{35}{36}$	9.50336 50374	$10.49664 \\ 49626$	9.52661 52703	10.47339 47297	10.02326 02330	9.97674 97670	25 24
37	50411	49020	52745	47255	02334	97666	23
38	50449	49551	52787	47213	02338	97662	22
39	50486	49514	52829	47171	02343	97657	21
40	9.50523	10.49477	9.52870	10.47130	10.02347	9.97653	20
41	50561	49439	52912	47088	02351	97649	19
42 43	50598 50635	49402 49365	52953 52995	47047 47005	02355 02360	97645 97640	18 17
44	50655	49327	53037	46963	02364	97636	16
45	9.50710	10.49290	9.53078	10.46922	02364 10.02368 02372	9.97632	15
46	50747	49253	53120	46880	02372	97628	14
47	50784	49216	53161	46839	02377	97623	13
48 49	50821	49179 49142	53202	46798	02381 02385	97619	12 11
49 50	50858 9.50896	10.49104	53244 9.53285	$46756 \\ 10.46715$	10.02390	97615 9.97610	10
51	50933	49067	53327	46673	02394	97606	9
52	50970	49030	53368	46632	02398	97602	8
53	51007	48993	53409	46591	02403	97597	8 7 6
54	51043	48957	53450	46550	02407	97593	6
55 56	$9.51080 \\ 51117$	10.48920 48883	9.53492 53533	$10.46508 \\ 46467$	10.02411 02416	9.97589 97584	5 4
50 57	51154	48846	53574	46426	02410	97580	3
58	51191	48809	53615	46385	02424	97576	2
59	51227	48773	53656	46344	02429	97571	1
60	51264	48736	53697	46303	02433	97567	0
M .	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	М.
400	•						

190			Logar	Logarithms.			
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant,	Cosine.	M.
0	9.51264	10.48736	9.53697	10.46303	10.02433	9,97567	60
1	51301	48699	53738	46262	02437	97563	59
$\frac{2}{3}$	51338	48662	53779	46221	02412	97558	58
3	51374	48626	53820	46180	02146	97554	57
4	51411	48589	53861	46139	$02450 \\ 10.02455$	97550 9.97545	56 55
5	9.51447	10,48553	$9.53902 \\ 53943$	$10.46098 \\ 46057$	02459	97541	54
$\frac{6}{7}$	$51484 \\ 51520$	$48516 \\ 48480$	53984	46016	02464	97536	53
8	51557	48443	54025	45975	02468	97532	52
9	51593	48407	54065	45935	02472	97528	51
10	9.51629	10.48371	9.54106	10.45894	10.02477	9.97523	50
11	51666	48334	54147	45853	02481	97519	49
12	51702	48298	54187	45813	02485	97515	48
13	51738	48262	54228	45772	02490	97510	47
14	51774	48226	54269	45731	02494	97506	46
15	9.51811	10.48189	9.54309	10.45691	10.02499	9.97501	45
16	51847	48153	54350	45650	02503	97497	44
17	51883	48117	54390	45610	02508	97492	43
18	51919	48081	54431	45569	02512	97488	42 41
19	51955	48045	54471	$45529 \\ 10.45488$	$02516 \\ 10.02521$	$97484 \\ 9.97479$	41
$\begin{array}{c} 20\\21 \end{array}$	$9.51991 \\ 52027$	$10.48009 \\ 47973$	9.54512 54552	45448	02525	97479	39
$\frac{21}{22}$	52027	47937	54593	45407	02530	97470	38
23	52099	47901	54633	45567	02534	97466	37
$\frac{23}{24}$	52135	47865	54673	45327	02539	97461	36
$\tilde{25}$	9.52171	10.47829	9.54714	10.45286	10.02543	9.97457	35
26	52207	47793	54754	45246	02547	97453	34
27	52242	47758	54794	45206	02552	97448	33
28	52278	47722	54835	45165	02556	97444	32
29	52314	47686	54875	45125	02561	97439	31
30	9.52350	10.47650	9,54915	10.45085	10.02565	9.97435	30
31	52385	47615	54955	45045	02570	97430	29 28
$\frac{32}{33}$	$52421 \\ 52456$	$47579 \\ 47544$	54995	45005 44965	$02574 \\ 02579$	97426 97421	27
34	52492	47508	55075	44925	02583	97421	26
35	9.52527	10.47473	9,55115	10.44885	10.02588	9.97412	25
36	52563	47437	55155	44845	02592	97408	24
37	52598	47402	55195	44805	02597	97403	23
38	52634	47366	55235	44765	02601	97399	22
39	52669	47331	55275	44725	02606	97394	21
40	9.52705	10,47295	9.55315	10.44685	10.02610	9.97390	20
41	52740	47260	55355	44645	02615	97385	19
42	52775	47225	55395	44605	02619	97381	18
43	52811	47189	55434	44566	02624	97376	17
44	52846	47154	55474	44526	02628	97372 9.97367	16 15
$\frac{45}{46}$	$9.52881 \\ 52916$	$10.47119 \\ 47084$	9.55514 55554	$10.44486 \\ 44446$	$10.02633 \\ 02637$	9.97363	10
47	52951	47049	55593	44407	02642	97358	13
48	52986	47014	55633	44367	02647	97353	12
49	53021	46979	55673	44327	02651	97349	iī
50	9,53056	10.46944	9.55712	10.44288	10.02656	9.97344	10
51	53092	46908	55752	44248	02660	97340	9
52	53126	46874	55791	$44248 \\ 44209$	02665	97335	8
53	53161	46839	55831	44169	02669	97331	7
54	53196	46804	55870	44130	02674	97326	6
55	9.53231	10.46769	9.55910	10.44090	10.02678	9.97322	5
56	53266	46734	55949	44051	02683	97317	4
57	53301	46699	55989	44011	02688	97312	3
58 59	53336 53370	46664	56028	43972	02692	97308	2
60	53405	46630 46595	56067 56107	43933 43893	02697 02701	97303 97299	0
M.	Cosine,	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

20 °			Logar	ithms.			159°
M .	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	М.
0	9.53405	10.46595	9.56107	10.43893	10.02701	9.97299	60
1	53440	46560	56146	43854	02706	97294	59
2	53475	46525 46491	56185	43815	02711	97289	58
3	53509	46491 46456	$56224 \\ 56264$	43776	$\begin{array}{c} 02715 \\ 02720 \end{array}$	97285 97280	57 56
45	53544 9.53578	10.46422	9.56303	43736 10.43697	10.02724	97280	55
6	53613	46387	56342	43658	02729	97271	54
7	53647	46353	56381	43619	02734	97266	53
8	53682	46318	56420	43580	02738	97262	52
9	53716	46284	56459	43541	02743	97257	51
10	9.53751	10.46249	9.56498	10.43502	10.02748	9.97252	50
$\begin{array}{c c} 11\\ 12 \end{array}$	53785 53819	46215 46181	56537 56576	43463 43424	02752 02757	97248 97243	49 48
13	53854	46146	56615	43385	02762	97238	47
14	53888	46112	56654	43346	02766	97234	46
15	9.53922	10.46078	9.56693	10.43307	10.02771	9.97229	45
16	53957	46043	56732	43268	02776	97224	44
17	53991	46009	56771	43229	02780	97220	43
18	54025 54059	45975	56810	43190	02785	97215 97210	42 41
19 20	9.54093	45941 10,45907	56849 9,56887	43151 10.43113	$02790 \\ 10.02794$	97210	40
21	54127	45873	56926	43074	02799	97201	39
	54161	45839	56965	43035	02804	97196	38
$\frac{23}{24}$	54195	45805	57004	42996	02808	97192	37
24	54229	45771	57042	42958	02813	97187	36
25	9.54263	10.45737	9.57081	10.42919	10.02818	9.97182	35
26	54297 54331	45703	57120	42880	02822	97178	34 33
27	54365	45669 45635	57158 57197	42842 42803	02827 02832	97173 97168	32
29	54399	45601	57235	42765	02837	97163	31
28 29 30	9.54433	10.45567	9.57274	10.42726	10.02841	9.97159	30
- 31	54466	45534	57312	42688	02846	97154	29
32 33	54500	45500	57351	42649	02851	97149	28
$\frac{33}{34}$	54534	45466	57389	42611	02855	97145	27 26
34 35	54567 9.54601	45433 10.45399	57428 9.57466	$42572 \\ 10.42534$	$02860 \\ 10.02865$	97140 9.97135	20
36	54635	45365	57504	42496	02870	97130	24
37	54668	45332	57543	42457	02874	97126	23
38	54702	45298	57581	42419	02879	97121	22
39	54735	45265	57619	42381	02884	97116	21
40	9.54769	10.45231	9.57658	10.42342	10.02889	9.97111	20
41 42	54802 54836	45198	57696	42304 42266	02893	97107	19 18
42	54869	45164 45131	57734 57772	42228	02898 02903	97102 97097	17
44	54903	45097	57810	42190	02908	97092	16
45	9.54936	10.45064	9.57849	10.42151	10.02913	9.97087	15
46	54969	45031	57887	42113	02917	97083	14
47	55003	44997	57925	42075	02922	97078	13
48	55036	44964	57963	42037	02927	97073	12
49 50	55069 9,55102	$44931 \\ 10.44898$	58001 9.58039	41999 10.41961	02932 10.02937	97068 9.97063	11 10
51	55136	44864	9.58059	41923	02941	9.97003	9
52	55169	44831	58115	41885	02946	97054	8
53	55202	44798	58153	41847	02951	97049	87
54	55235	44765	58191	41809	02956	97044	6
55	9.55268	10.44732	9.58229	10.41771	10.02961	9.97039	5
56	55301	44699	58267	41733	02965	97035	4
57	55334	44666	58304	41696	02970	97030	$\frac{3}{2}$
58 59	55367 55400	44633	58342 58380	41658 41620	02975 02980	97025 97020	
- 60 - 60	55433	44600 44567	58418	41520	02980	97020	6
М.	Cosine,	Secant,	Cotangent	Tangent.	Cosecant.	Sine.	M.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1580			thms.			2 1°	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $. M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.
				10.41582	9.58418	10.44567	9.55433	0
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			02990					ĭ
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$					58493	44501	55499	$\overline{2}$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$						44468	55532	3
$\begin{array}{c c c c c c c c c c c c c c c c c c c $							55564	4
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				10.41394				5
$\begin{array}{c c c c c c c c c c c c c c c c c c c $						44370		6
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $						44337		7
$\begin{array}{c c c c c c c c c c c c c c c c c c c $				41281				8
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$							55728	-9
$\begin{array}{c c c c c c c c c c c c c c c c c c c $						10.44239		
$\begin{array}{c c c c c c c c c c c c c c c c c c c $						44207		
				41093		44174		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$				41056				
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		9.96942					0 55099	15
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		96937				44044		16
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		96932	03068				55988	17
$\begin{array}{c c c c c c c c c c c c c c c c c c c $						43979		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			03078		59131			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7 40	9.96917	10.03083				9.56085	20
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					59205	43882	56118	21
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				40757				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				40720				23
$\begin{array}{cccccccccccccccccccccccccccccccccccc$								
$\begin{array}{cccccccccccccccccccccccccccccccccccc$							9.56247	25
$\begin{array}{cccccccccccccccccccccccccccccccccccc$							56279	26
$\begin{array}{cccccccccccccccccccccccccccccccccccc$								27
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						43007		28
$\begin{array}{cccccccccccccccccccccccccccccccccccc$								29
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 29	96863	03137	40423				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8 28	96858					56472	
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	3 27	96853	03147	40349		43496		33
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8 26	96848		40312	59688			34
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	3 25	9.96843		10.40275	9.59725	10.43432	9.56568	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$							56599	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				40201	59799	43369	56631	37
$\begin{array}{cccccccccccccccccccccccccccccccccccc$								38
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c} 3 & 21 \\ 8 & 20 \end{array}$	90823	03177			43305	56695	39
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		9,90818	10.03182					40
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		90610	02102					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$						45210	50790	
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$								
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			10.03207				9 56886	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				39870	60130			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		96783						
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	8 1	96778	03222					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		96772	03228	39760	60240	42988		49
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7 1	9.96767	10.03233	10.39724	9.60276	10.42956	9.57044	50
53 57138 42862 60386 39614 03248 96755	2		03238				57075	51
53 57138 42862 60386 39614 03248 9675	7	96757	03243				57107	52
	2 '							53
54 57169 42831 60422 39578 03253 96747 57 6.7509 10.42509 0.00150 10.00141 10.00176 0.00747		96747	03253	39578	60422	42831	57169	54
		9.96742	10.03258				9.57201	55
	5 3	96737 96732					57232	00 577
		96732						- 97 5 P
		96722					57290	98 50
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		96717				42612	57358	
				·				
M. Cosine. Secant. Cotangent. Tangent. Cosecant. Sine.	. M	Sine.	Cosecant.	Tangent.	Cotangent	Secant.	Cosine.	M.

1110

22 °			Logar	ithms.			157°
M .	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	М.
0	9.57358	10.42642	9.60641	10.39359	10.03283	9.96717	60
$\frac{1}{2}$	57389	42611	60677	39323	03289	96711	59
2	57420	42580	60714	39286	03294	96706	58
3 4	57451 57482	42549 42518	60750 60786	39250 39214	03299 03304	96701 96696	57 56
5	9.57514	10.42486	9,60823	10.39177	10.03309	9.96691	55
6	57545	42455	60859	39141	03314	96686	54
6 7	57576	42424	60895	39105	03319	96681	53
8	57607	42393	60931	39069	03324	96676	52
9	57638	42362	60967	39033	03330	96670	51
10 11	9.57669 57700	$10.42331 \\ 42300$	9.61004 61040	10.38996 38960	10.03335 03340	9.96665 96660	50 49
12	57731	42269	61076	38924	03345	96655	48
13	57762	42238	61112	38888	03350	96650	47
14	57793	42207	61148	38852	03355	96645	46
15	9.57824	10.42176	9.61184	10.38816	10.03360	9.96640	45
16 17	57855 57885	$42145 \\ 42115$	61220	$38780 \\ 38744$	03366	96634 96629	44 43
18	57885	42084	61200	38744	03376	96629	43
19	57947	42053	61256 61292 61328	38672	03381	96619	41
20	9.57978	10.42022	9.61364	10.38636	10.03386	9.96614	40
21	58008	41992	61400	38600	03392	96608	39
22 23	58039	41961	61436	38564	03397	96603	38
23	58070 58101	41930 41899	61472 61508	38528 38492	03402 03407	96598 96593	37 36
25	9.58131	10.41869	9.61544	10.38456	10.03412	9.96588	30
$\widetilde{26}$	58162	41838	61579	38421	03418	96582	34
27	58192	41808	61615	38385	03423	96577	33
28	58223	41777	61651	38349	03428	96572	32
29 30	58253 9.58284	41747 10.41716	61687 9.61722 61758	38313	03433	96567	31
30 31	9.58284 58314	41686	9.01722	$10.38278 \\ 38242$	10.03438 03444	9.96562 96556	30 29
32	58345	41655	61794	38206	03449	96551	28
33	58375	41625	61830	38170	03454	96546	27
34	58406	41594	61865	38135	03459	96541	26
35	9.58436	10.41564	9.61901	10.38099	10.03465	9.96535	25
36 37	58467 58497	41533 41503	61936 61972	38064 38028	03470 03475	96530 96525	24 23
38	58527	41473	62008	37992	03480	96520	22
39	58557	41443	62043	37957	03486	96514	21
40	9.58588	10.41412	9.62079	10.37921	10.03491	9.96509	20
41	58618	41382	62114	37886	03496	96504	19
42 43	58648	41352	$62150 \\ 62185$	37850	03502	96498 96493	18 17
43	$58678 \\ 58709$	41322 41291	62185	37815 37779	03507 03512	96493	16
45	9.58739	10.41261	9.62256	10.37744	10.03517	9.96483	15
46	58769	41231	62292	37708	03523	96477	14
47	58799	41201	62327	37673	03528	96472	13
48	58829	41171	62362	37638	03533	96467	12
49 50	58859 9.58889	41141 10.41111	62398 9.62433	37602 10.37567	$03539 \\ 10.03544$	96461 9.96456	11 10
51	58919	41081	62468	37532	03549	96451	9
52	58949	41051	62504	37496	03555	96445	8
53	58979	41021 40991	62504 62539 62574	37461	03560	96440	7
54	59009	40991	62574	37426	03565	96435	6
55	9.59039	10.40961	9.62609	10.37391	10.03571	9.96429	5
56 57	59069 59098	40931 40902	62645 62680	37355 37320	03576 03581	$96424 \\ 96419$	4 3
58	59098 59128	40902 40872	62715	37285	03581	96413	2
59	59158	40842	$62715 \\ 62750$	37250	03592	96408	ĩ
60	59188	40812	62785	37215	03597	96403	Ō
M .	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	М.

23 °			Logar	ithms.			1560
M.	Sine.	Cosecunt.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.59188	10.40812	9.62785	10.37215	10.03597	9.96403	60
1	59218	40782	62820	37180	03603	96397	59
$\frac{1}{2}$	59247	40753	62855	37145	03608	96392	58
3 4	59277	40723	62890	37110	03613	96387	57
4	59307 9,59336	40693	62926	37074	03619	96381	56
$\frac{5}{6}$	59366	$10.40664 \\ 40634$	9.62961 62996	$10.37039 \\ 37004$	10.03624 03630	9.96376 96370	55 54
7	59396	40604	63031	36969	03635	96365	53
78	59425	40575	63066	36934	03640	96360	52
ğ	59455	40545	63101	36899	03646	96354	51
10	9.59484	10.40516	9.63135	10.36865	10.03651	9.96349	50
11	59514	40486	63170	36830	03657	96343	49
12	59543	40457	63205	36795	03662	96338	48
13	59573	40427	63240	36760	03667	96333	47
14	59602	40398	63275	36725	03673	96327	46
15	9.59632	10.40368	9.63310	10.36690	10.03678	9.96322	45
$\frac{16}{17}$	59661 59690	40339	63345 63379	$36655 \\ 36621$	03684 03689	$96316 \\ 96311$	44 43
18	59090 59720	$40310 \\ 40280$	63414	36586	03695	96305	$\frac{43}{42}$
19	59749	40.280	63449	36551	03700	96300	41
20	9.59778	10.40222	9.63484	10.36516	10.03706	9.96294	40
$\tilde{2}\tilde{1}$	59508	40192	63519	36481	03711	96289	39
$\frac{21}{22}$	59837	40163	63553	36447	03716	96284	38
23	59866	40134	63588	36412	03722	96278	37
24	59895	40105	63623	36377	03727	96273	36
25	9.59924	10.40076	9.63657	10.36343	10.03733	9,96267	35
26	59954	40046	63692	36308	03738	96262	34
27	59983	40017	63726	36274	03744	96256	33
28 29	60012	39988	63761	36239	03749	$96251 \\ 96245$	32
30	60041 9.60070	39959 10.39930	63796 9,63830	$36204 \\ 10.36170$	03755	96245 9.96240	31
31	60099	39901	63865	36135	$10.03760 \\ 03766$	9.96240	30 29
32	60128	39872	63899	36101	03771	96229	28
33	60157	39843	63934	36066	03777	96223	27
34	60186	39814	63968	36032	03782	96218	26
35	9.60215	10.39785	9.64003	10.35997	10.03788	9.96212	25
36	60244	39756	64037	35963	03793	96207	24
37	60273	39727	64072	35928	03799	96201	23
38	60302	39698	64106	35894	03804	96196	22
39 40	60331	39669	64140	35860	03810	96190	21
40	9.60359 60388	10.39641	9.64175	10.35825	10.03815	9.96185	20
42	60417	39612 39583	64209 64243	35791 35757	03821 03826	96179 96174	19 18
43	60446	39554	64278	35722	03832	96168	17
44	60474	39526	64312	35688	03838	96162	16
45	9.60503	10.39497	9,64346	10.35654	10.03843	9.96157	15
46	60532	39468	64381	35619	03849	96151	14
47	60561	39439	64415	35585	03854	96146	13
48	60589	39411	64449	35551	03860	96140	12
49	60618	39382	64483	35517	03865	96135	11
50 51	9.60646	10.39354	9.64517	10.35483	10.03871	9.96129	10
$\frac{51}{52}$	60675	39325	64552	35448	03877	96123	9
53	60704 60732	39296 39258	$64586 \\ 64620$	35414 35380	03882 03888	96118	8 7 6
54	60761	39239	64654	35346	03893	$96112 \\ 96107$	
55	9.60789	10.392139	9.64688	10.35312	10.03899	96107 9.96101	5
56	60818	39182	64722	35278	03905	96095	4
57	60846	39154	64756	35244	03910	96090	3
58	60875	39125	64790	35210	03916	96084	$\begin{vmatrix} 3\\2\\1 \end{vmatrix}$
59	60903	39097	64824	35176	03921	96079	1
60	60931	59069	64858	35142	03927	96073	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

113°

24°			Logar	ithms.			155°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.60931	10.39069	9.64858	10.35142	10.03927	9.96073	60
$\frac{1}{2}{3}$	60960	39040	64892	35108	03933	96067	59
2	60988	39012	64926	35074	03938	96062	58
3	$61016 \\ 61045$	38984 38955	64960 64994	35040 35006	03944 03950	96056 96050	57 56
45	9.61073	10.38927	9.65028	10.34972	10.03955	9.96045	55
6	61101	38899	65062	34938	03961	96039	54
7	61129	38871	65096	34904	03966	96034	53
8 9	61158	38842	65130	34870	03972	96028	52
	61186	38814	65164	34836	03978	96022	51
$\frac{10}{11}$	9.61214 61242	$10.38786 \\ 38758$	9.65197	10.34803	10.03983 03989	9.96017 96011	50 49
12	61270	38730	65231 65265 65299	34769 34735	03995	96005	48
$\hat{13}$	61270 61298	38702	65299	34701	04000	96000	47
14	61326	38674	65333	34667	04006	95994	46
15	9.61354	10.38646	9.65366	10.34634	10.04012	9.95988	45
16	61382 61411	38618	65400	34600	04018 04023	95982 95977	44
17 18	61438	38589 38562	65434 65467	34566 34533	04025	95977	43 42
19	61466	38534	65501	34499	04035	95965	41
20	9.61494	10.38506	9.65535	10.34465	10.04040	9.95960	40
21	61522	38478	65568	34432	04046	95954	39
22	$61550 \\ 61578$	38450	65602	34398	04052	95948	38
$\frac{23}{24}$	61578	38422 38394	65636	34364	04058 04063	95942 95937	37
24 25	61606 9.61634	10.38366	65669 9.65703	$34331 \\ 10.34297$	10.04069	9.95931	36 35
26	61662	38338	65736	34264	04075	95925	34
27	61689	38311	65770	34230	04080	95920	33
28	61717 61745	38283	65770 65803	34197	04086	95914	32
29	61745	38255	65837	34163	04092	95908	31
$\frac{30}{31}$	9.61773	10.38227	9.65870 65904	10.34130	10.04098 04103	9.95902 95897	30 29
32	$61800 \\ 61828$	$38200 \\ 38172$	65937	34096 34063	04103	95891	29
33	61856	38144	65971	34029	04115	95885	27
34	61883	38117	66004	33996	04121	95879	26
35	9.61911	10.38089	9.66038	10.33962	10.04127	9.95873	25
36	61939	38061	66071	33929	04132	95868	24
37 38	61966 61994	38034 38006	66104 66138	33896 33862	04138 04144	95862 95856	23 22
39	62021	37979	66171	33829	04150	95850	21
40	9.62049	$37979 \\ 10.37951$	66171 9.66204 66238	10.33796	10.04156	9.95844	20
41	62076	37924	66238	33762	04161	95839	19
42	62104	37896	66271	33729	04167	95833	18
43	62131	37869	66304	33696	04173	95827	17
44 45	$62159 \\ 9.62186$	37841 10.37814	66337 9.66371	33663 10.33629	04179 10.04185	$95821 \\ 9.95815$	$16 \\ 15$
46	62214	37786	66404	33596	04190	95810	14
47	62241	37759	66437	33563	04196	95804	13
48	62268	37732	66470	33530	04202	95798	12
49	62296	37704	66503	33497	04208	95792	11
50	62296 9.62323 62350	10.37677	9.66537 66570	10.33463	10.04214 04220	9.95786	10
$\frac{51}{52}$	62350	37650 37623	66603	33430 33397	04220	95780 95775	9
53	62405	37595	66636	33364	04231	95769	87
54	62432	37568	66669	33331	04237	95763	6
55	9.62459	10.37541	9.66702	10.33298	10.04243	9.95757	5
56	62486	37514	66735	33265	04249	95751	4
- 57 58	$62513 \\ 62541$	37487 37459	66768 66801	33232 33199	$04255 \\ 04261$	95745 95739	3
59	62568	37439	66834	33166	04261	95733	5 4 3 2 1
60	62595	37405	66867	33133	04207	95728	Ō
M .	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	М.

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25°			Logar	ithms.	-		154°
М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine,	М.
0	9.62595	10.37405	9.66867	10.33133	10.04272	9.95728	60
1	62622	37378	66900	33100	04278	95722	59
$\hat{2}$	62649	37351	66933	33067	04284	95716	58
$\frac{3}{4}$	62676	37324	66966	33034	04290	95710	57
45	$62703 \\ 9.62730$	37297 10.37270	66999 9.67032	$33001 \\ 10.32968$	04296 10.04302	95704 9,95698	56 55
6	9.62750 62757	37243	67065	32935	04308	95692	54
7	62784	37216	67098	32902	04314	95686	53
8	62811	37189	67131	32869	04320	95680	52
ğ	62838	37162	67163	32837	04326	95674	51
10	9.62865	10.37135	9.67196	10.32804	10.04332	9,95668	50
11	62892	37108	67229	32771	04337	95663	49
12	62918	37082	67262 67295	32738	04343	95657	48
13	62945	37055	67295	32705	04349	95651	47
14	62972	37028	67327	32673	04355	95645	46
15 16	9.62999 63026	$10.37001 \\ 36974$	9.67360 67393	$10.32640 \\ 32607$	10.04361 04367	9,95639 95633	45
17	63052	36948	67426	32574	04373	95627	44
18	63079	36921	67458	32542	04379	95621	43
19	63106	36894	67491	32509	04385	95615	41
20	9.63133	10.36867	9,67524	10.32476	10.04391	9,95609	40
21	63159	36841	67556	32444	04397	95603	39
22	63186	36814.	67589	32411	04403	95597	38
23	63213	36787	67622	32378	04409	95591	37
24	63239	36761	67654	32346	04415	95585	36
25	9.63266	10.36734	9.67687	10.32313	10.04421	9.95579	35
26	63292	36708	67719	32281	04427	95573	34
$\frac{27}{28}$	$63319 \\ 63345$		67752 67785	$32248 \\ 32215$	04433 04439	95567 95561	33 32
29	63372	36655 36628	67817	32183	04445	95555	31
30	9,63398	10.36602	9.67850	10.32150	10.04451	9.95549	30
31	63425	36575	67882	32118	04457	95543	29
32	63451	36549	67915	32085	04463	95537	28
33	63478	36522	67947	32053	04469	95531	27
34	63504	36496	67980	32020	04475	95525	26
35	9.63531	10.36469	9.68012	10.31988	10.04481	9.95519	25
36 37	63557 63583	$36443 \\ 36417$	68044 68077	31956 31923	04487 04493	95513 95507	24 23
38	63610	36390	68109	31891	04495	95500	23
39	63636	36364	68142	31858	04506	95494	21
40	9.63662	10.36338	9.68174	10.31826	10.04512	9,95488	20
41	63689	36311	68206	31794	04518	95482	19
42	63715	36285	68239	31761	04524	95476	18
43	63741	36259 36233	68271	31729	04530	95470	17
44	63767	36233	68303	31697	04536	95464	16
45 46	9.63794	10.36206	9.68336	10.31664	10.04542	9.95458	15
40	63820 63846	$36180 \\ 36154$	68368 68400	$\frac{31632}{31600}$	$04548 \\ 04554$	95452 95446	14 13
48	63872	36128	68432	31568	04554	95440	13
49	63898	36102	68465	31535	04566	95434	11
50	9.63924	10.36076	9.68497	10.31503	10.04573	9.95427	10
51	63950	36050	68529	31471	04579	95421	9
52	63976	36024	68561	31439	04585	95415	87
53	64002	35998	68593	31407	04591	95409	7
54	64028	35972	68626	31374	04597	95403	6 5 4
55	9.64054	10.35946	9.68658	10.31342	10.04603	9.95397	5
56 57	640S0 64106	35920 35894	68690 68722	31310 31278	04609	95391	4
58	64132	35868	68722	31278	04616 04622	95384 95378	0
59	64158	35842	68786	31240	04622	95378	321
60	64184	35816	68818	31182	04634	95366	Ô
M .	Cosine,	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	м.

115°

26 °			Logar	ithms.			153°
М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.64184	10.35816	9.68818	10.31182	10.04634	9.95366	60
1	64210	35790	68850	31150	04640	95360	59
2	64236	35764	68882	31118	04646	95354	58
3	64262	35738	68914	· 31086	04652	95348	57
4	64288	35712	68946	31054	04659	95341	56
5	9.64313 64339	$10.35687 \\ 35661$	9.68978	10.31022	10.04665	9.95335	55
7	64365	35635	69010 69042	30990 30958	04671 04677	95329 95323	54 53
8	64391	35609	69074	30926	04683	95317	52
9	64417	35583	69106	30894	04690	95310	51
10	9.64442	10.35558	9.69138	10.30862	10.04696	9.95304	50
11	64468	35532	69170	30830	04702	95298	49
12	64494	35506	69202	30798	04708	95292	48
13	64519	35481	69234	30766	04714	95286	47
14	64545	35455	69266	30734	04721	95279	46
15	9.64571	10.35429	9.69298	10.30702	10.04727	9.95273	45
16	64596	35404	69329	30671	04733	95267	44
17 18	64622	35378	69361	30639	04739	95261	43
10	$64647 \\ 64673$	35353 35327	69393 69425	30607 30575	04746 04752	$95254 \\ 95248$	42
20	9.64698	10.35302	9.69457	10.30543	10.04758	9.95248	40
21	64724	35276	69488	30512	04764	95236	39
$\tilde{2}\hat{2}$	64749	35251	69520	30480	04771	95229	38
23	64775	35225	69552	30448	04777	95223	37
24	64800	35200	69584	30416	04783	95217	36
25	9.64826	10.35174	9.69615	10.30385	10.04789	9.95211	35
26	64851	35149	69647	30353	04796	95204	34
27	64877	35123	69679	30321	04802	95198	33
28 29	64902	35098	69710	30290	04808	95192	32
30	$64927 \\ 9.64953$	35073 10.35047	69742 9.69774	30258 10.30226	$04815 \\ 10.04821$	95185 9.95179	31 30
31	64978	35022	69805	30195	04827	9.95179	29
32	65003	34997	69837	30163	04833	95167	28
33	65029	34971	69868	30132	04840	95160	27
34	65054	34946	69900	30100	04846	95154	26
35	9.65079	10.34921	9.69932	10.30068	10.04852	9.95148	25
36	65104	34896	69963	30037	04859	95141	24
37	$\sim >65130$	34870	69995	30005	04865	95135	23
38	65155	34845	70026	29974	04871	95129	22
39 40	65180	34820	70058	29942	04878	95122	21 20
41	$9.65205 \\ 65230$	10.34795 34770	9.70089 · 70121	$10.29911 \\ 29879$	10.04884 04890	$9.95116 \\ 95110$	19
42	65255	34745	70152	29848	04897	95103	18
43	65281	34719	70184	29816	04903	95097	17
44	65306	34694	70215	29785	04910	95090	16
45	9.65331	10.34669	9.70247	10.29753	10.04916	9.95084	15
46	65356	34644	70278	29722	04922	95078	14
47	65381	34619	70309	29691	04929	95071	13
48	65406	34594	70341	29659	04935	95065	12
49	65431	34569	70372	29628	04941	95059	11
50 51	9.65456	10.34544 34519	9.70404	10.29596	10.04948	9.95052	10
52	$65481 \\ 65506$	34319	70435	29565 29534	04954 04961	95046 95039	9
53	65531	34469	70400	29502	04961	95039	2
54	65556	34444	70529	29471	04973	95027	7
55	9.65580	10.34420	9,70560	10.29440	10.04980	9.95020	5
56	65605	34395	70592	29408	04986	95014	4
57	65630	34370	70623	29377	04993	95007	3
58	65665	34345	70654	29346	04999	95001	2
59	65680	34320	70685	29315	05005	94995	1
60	65705	34295	70717	29283	05012	94988	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

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63⁰

27°			Logar	ithms.			152°
M.	Sine.	Cosecant,	Tangent.	Cotangent,	Secant.	Cosine,	M.
0	9.65705	10.34295	9.70717	10.29283	10.05012	9.94988	60
1	65729	34271	70748	29252	05018	94982	59
2	65754	34246	70779	29221	05025	94975	58
3	65779	34221	70810	29190	05031	94969	57
4	65804	34196	70841	29159	05038	94962	56
5	9,65828	10.34172	9.70873	10.29127	10.05044	9.94956	55
6	65853	34147	70904	29096	05051	94949	54
7	65878	34122	70935	29065 29034	05057 05064	94943 94936	53 52
8	65902	34098 34073	70966 70997	29034	05064	94930	51
10	$65927 \\ 9.65952$	10.34048	9.71028	10.28972	10.05077	9.94923	50
11	65976	34024	71059	28941	05083	94917	49
12	66001	33999	71090	28910	05089	94911	48
13	66025	33975	71121	28879	05096	94904	47
14	66050	33950	71153	28847	05102	94898	46
15	9,66075	10.33925	9.71184	10.28816	10.05109	9.94891	45
16	66099	33901	$71215 \\ 71246$	28785	05115	94885	44
17	66124	33876	71246	28754	05122	94878	43
18	66148	33852	71277	28723	05129	94871	42
19	66173	33827	71308	28692	05135	94865	41
20	9.66197	10.33803	9.71339	10.28661	10.05142	9.94858	40
21	66221	33779	71370	28630	05148	94852	39
22	66216	33754	71401	28599	05155	94845	38
23	66270	33730	71431	28569	05161	94839	37
$\frac{24}{25}$	$66295 \\ 9.66319$	$33705 \\ 10.33681$	71462 9.71493	$28538 \\ 10.28507$	$05168 \\ 10.05174$	94832 9.94826	36 35
26	66343	33657	5.71495	28476	05181	94819	30 34
27	66368	33632	71555	28445	05181	94813	33
28	66392	33608	71586	28414	05194	94806	32
29	66416	33584	71617	28383	05201	94799	31
30	9.66441	10.33559	9.71648	10.28352	10.05207	9.94793	30
31	66465	33535	71679	28321	05214	94786	29
32	66489	33511	71709	28291	05220	94780	28
33	66513	33487	71740	28260	05227	94773	07
34	66537	33463	71771	28229	05233	94767	26
35	9.66562	10.33438	9.71802	10.28198	10.05240	9.94760	25
36	66586	33414	71833	28167	05247	94753	24
37	66610	33390	71863	28137	05253	94747	23
38	66634	33366	71894	28106	05260	94740	22
39 40	66658 9.66682	$33342 \\ 10.33318$	71925	$28075 \\ 10.28045$	05266	94734	21
40	9.00082 66706	33294	9.71955	28014	$ \begin{array}{r} 10.05273 \\ 05280 \end{array} $	$9.94727 \\ 94720$	20
42	66731	33269	71986 72017	27983	05286	94720 94714	19 18
43	66755	33245	72048	27952	05293	94707	17
41	66779	33221	72078	27932	05295	94700	16
45	9,66803	10.33197	9.72109	10.27891	10.05306	9.94694	15
46	66827	33173	72140	27860	05313	94687	14
47	66851	33149	72170	27830	05320	94680	13
48	66875	33125	72201	27799	05326	94674	12
49	66899	33101	72231	27769	05333	94667	11
50	9.66922	10.33078	9.72262	10.27738	10.05340	9.94660	10
51	66946	33054	72293	27707	05346	94654	9
52	66970	33030	72323	27677	05353	94647	8
53	66994	33006	72354	27646	05360	94640	76
54	67018	32982	72384	27616	05366	94634	6
55	9.67042	10.32958	9.72415	10.27585	10.05373	9.94627	5
56 57	67066 67090	32934 32910	72445 72476	27555	05380	94620	4
58	$67090 \\ 67113$	32910 32887	72476 72506	$27524 \\ 27494$	05386	94614	3
59	67137	32863	72506	27194 27463	05393	$94607 \\ 94600$	1
60	67161	32839	72567	27403	05400 05407	94593	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

2 8°			Logar	ithms.			1510
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.67161	10.32839	9.72567	10.27433	10.05407	9.94593	60
1	67185	32815	72598	27402	05413	94587	59
$\frac{2}{3}$	67208	32792	72628	27372	05420	94580	58
3	67232	32768	72659	27341	05427	94573	57
45	67256 9.67280	$32744 \\ 10.32720$	72689	$27311 \\ 10.27280$	05433	94567	56
5	9.67280	10.32720	9.72720	10.27280	10.05440	9.94560	55
6 7	67303	32697	72750	27250	05447	94553	54
- 7	67327	32673 32650	72780 72811	27220 27189	05454 05460	94546 94540	53 52
8	67350 67374	32620	72811	27159	05460	94533	51
10	9.67398	10.32602	9.72872	10.27128	10.05474	9.94526	50
11	67421	32579	72902	27098	05481	94519	49
12	67445	32555	72932	27068	05487	94513	48
13	67468	32532	72963	27037	05494	94506	47
14	67492	32508	72993	27007	05501	94499	46
15	9.67515	10.32485	9,73023	10.26977	10.05508	9.94492	45
16	67539	32461	73054	26946	05515	94485	44
17	67562	32438	73084	26916	05521	94479	43
18	67586	32414	73114	26886	05528	94472	42
19	67609	32391	73144	26856	05535	94465	41
20	9.67633	10.32367	9.73175	10.26825	10.05542	9.94458	40
21	67656	32344	73205	26795	05549	94451	39
22	67680	32320	73235	26765	05555 05562	94445 94438	38 37
23 24	67703 67726	32297 32274	73265	26735 26705	05569	94430	36
24 25	9 67750	10.32250	9.73326	10.26674	10.05576	9.94424	35
26	9.67750 67773	32227	73356	26644	05583	94417	34
27	67796	32204	73356 73386	26614	05590	94410	33
28	67820	32180	73416	26584	05596	94404	32
29	67843	32157	73446	26554	05603	94397	31
30	9.67866	10.32134	9.73476	10.26524	10.05610	9.94390	30
31 32	67890	32110	73507	26493	05617	94383	29
32	67913	32087	73537	26463	05624	94376	28
33	67936	32064	73567	26433	05631	94369	27
34	67959	32041	73597	26403	05638	94362	26
35	9.67982	10.32018	9.73627	10.26373	10.05645	9.94355	25 24
36	68006 68029	31994 31971	73657 73687	26343 26313	05651 05658	94349 94342	23
37	68052	31948	73717	26283	05665	94335	22
38 39	68075	31925	73747	26253	05005	94328	21
40	9.68098	10.31902	9.73777	10.26223	10.05679	9.94321	20
41	68121	31879	73807	26193	05686	94314	19
$\overline{42}$	68144	31856	73837	26163	05693	94307	18
43	68167	31833	73867	26133	05700	94300	17
44	68190	31810	73897	26103	05707	94293	16
45	9.68213	10.31787	9.73927	10.26073	10.05714	9.94286	15
46	68237	31763	73957	26043	05721	94279	14
47	68260	31740	73987	26013	05727	94273	13
48	68283	31717	74017	25983	05734	94266	12
49	68305 9.68328	31695	74047	25953 10.25923	05741	94259 9.94252	11
50	9.68328 68351	$10.31672 \\ 31649$	9.74077 74107	10.25923	10.05748 05755	9.94252 94245	10 9
$\frac{51}{52}$	68374	31649	74107	25863	05762	94238	
53 53	68397	31626	74157	25834	05769	94230	8
53 54	68420	31580	74196	25804	05776	94224	6
55	9.68443	10.31557	9.74226	10.25774	10.05783	9.94217	5
56	68466	31534	74256	25744	05790	94210	5
57	68489	31511	74286	25714	05797	94203	3
58	68512	31488	74316	25684	05804	94196	2
59	68534	31466	74345	25655	05811	94189	1
60	68557	31443	74375	25625	05818	94182	0
M.	Cosine.	Secant.	Cotangent	. Tangent.	Cosecant.	Sine.	М.

1180

1.3	sno	

Loganith

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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	034 39
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c} 012 & 36 \\ 005 & 35 \end{array}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1005 55 1998 34
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3963 29
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	927 24
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$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	912 22
41 69479 30521 75588 24412 06109 93 42 69501 30499 75617 243×3 06116 93 43 69523 30477 75667 24353 06124 93 44 69545 30455 75676 24324 06131 93	905 21
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	891 19
44 69545 30455 75676 24324 06131 93	$ 884 18 \\ 876 17 $
	869 16
46 69589 30411 75735 24265 06145 98	855 14
47 60611 20280 75761 21226 06152 69	3847 13
	840 12
49 69655 30345 75822 24178 06167 93	8833 11
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
	819 9
	811 8 804 7
	8797 6
	3789 5
56 69809 30191 76027 23973 06218 93	3782 4
57 69831 30169 76056 23944 06225 98	3775 3
58 69853 30147 76086 23914 06232 98	3768 2
60 69897 30103 76144 23856 06247 98	3753 0
M. Cosme, Secant. Cotangent, Tangent, Cosecant. Sin	ne. M.

1190

30 °			Logar	ithms.		:	149°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.69897	10.30103	9.76144	10.23856	10.06247	9.93753	60
1	69919	30081	76173	23827	06254	93746	59
2	69941	30059	76202	23798	06262	93738	58
3	69963	30037	76231	23769	06269	93731	57
2 3 4 5 6	69984	30016	76261	23739	- 06276	93724	56
5	9.70006	10.29994	9.76290	10.23710	10.06283	9.93717	55
27	70028 70050	29972 29950	76319	23681 23652	06291 06298	93709 93702	$54 \\ 53$
78	70072	29928	76377	23623	06305	93695	52
9	70093	29907	76406	23594	06313	93687	51
10	9.70115	10.29885	9.76435	10.23565	10.06320	9.93680	50
11	70137	29863	76464	23536	06327	93673	49
12	70159	29841	76493	23507	06335	93665	48
13	70180	29820	76522	23478	06342	93658	47
14	70202	29798	76551	23449	06350	93650	46
15	9.70224	10.29776	9.76580	10.23420	10.06357	9.93643	45
16	70245	29755	76609	23391	06364	93636	44
17	70267	29733	76639	23361	06372	93628	43
18	70288	29712	76668	23332	06379	93621	42
19	70310 9.70332	29690 10.29668	76697 9.76725	$23303 \\ 10.23275$	06386 10.06394	93614 9,93606	41
20 21	9.70352 70353	29647	9.76725 76754	23246	06401	93599	39
22	70305	29625	76783	23217	06409	93591	38
23	70396	29604	76812	23188	06416	93584	37
24	70418	29582	76841	23159	06423	93577	36
25	9.70439	10.29561	9.76870	10.23130	10.06431	9.93569	35
26	70461	29539	76899	23101	06438	93562	34
97	70482	29518	76928	23072	06446	93554	33
28	70504	29496	76957	23043	06453	93547	32
28 29 30	70525	29475	76986	23014	06461	93539	31
30	9.70547	10.29453	9.77015	10.22985	10.06468	9.93532	30
31	70568	29432	77044	22956 22927	06475	93525	29
$\frac{32}{33}$	$70590 \\ 70611$	29410 29389	77073	22899	06483	93517 93510	28 27
аа 34	70633	29367	77130	22870	06498	93502	26
35	9.70654	10.29346	9.77159	10.22841	10.06505	9.93495	25
36	70675	29325	77188	22812	06513	93487	24
37	70697	29303	77217	22783	06520	93480	23
38 39	70718	29282	77246	22754	06528	93472	22
39	70739	29261	77274	22726	06535	93465	21
40	9.70761	10.29239	9.77303	10.22697	10.06543	9.93457	20
41	70782	29218	77332	22668	06550	93450	19
42	70803	29197	77361	22639	06558	93442	18
43	70824	29176	77390	22610 22582	06565	93435 93427	17
44 45	70846 9,70867	29154 10.29133	77418 9.77447	10.22553	06573 10.06580	93427	16
46	70888	29112	77476	22524	06588	93412	15 14
47	70909	29091	77505	22495	06595	93405	13
48	70931	29069	77533	22467	06603	93397	12
49	70952	29048	77562	22438	06610	93390	11
50	9.70973	10.29027	9,77591	10.22409	10.06618	9,93382	10
51	70994	29006	77619	10.22409 22381	06625	93375	9
52	71015	28985	77648	22352	06633	93367	8
53	71036	28964	77677	22323	06640	93360	1 7
54	71058	28942	77706	22294	06648	93352	6
55	9.71079	10.28921	9.77734	10.22266	10.06656	9.93344	5
56	71100	28900	77763	22237	06663	93337	4
57	71121	28879 28858	77791	22209 22180	06671	93329	3
58 59	71142 71163	28808	77849	22180	06678	93322 93314	$\begin{vmatrix} 2\\1 \end{vmatrix}$
59 60	71163	28837	77877	22131	06693	93307	
M.	Cosine.	Secant.	Cotangent	Tangent,	Cosecant.	Sine.	M.

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	Cosine.	M.
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	0.0000	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9.93307	60
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	93291	58
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	93284 93276	57 56
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9.93269	55
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	93253	53
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	93246	52
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9.93230	50
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	93223	49
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	93215 93207	48
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9.93192	45
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	93177	43
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	93161	41
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	9.93154 93146	40 39
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	93131	37
27 71747 28253 78647 21353 06900 28 71767 28233 78675 21325 06908 29 71788 28212 78704 21296 06916	93123	36
27 71747 28253 78647 21353 06900 28 71767 28233 78675 21325 06908 29 71788 28212 78704 21296 06916	9.93115	35
$29 \mid 71788 \mid 28212 \mid 78704 \mid 21296 \mid 06916 \mid$	93108	34
$29 \mid 71788 \mid 28212 \mid 78704 \mid 21296 \mid 06916 \mid$	93100 93092	33 32
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	93092 93084	31
	9.93077	30
31 71829 28171 78760 21240 06931	93069	29
32 71850 28150 78789 21211 06939	93061	28
33 71870 28130 78817 21183 06947	93053	27
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	93046 9.93038	26 25
35 9.71911 10.28089 9.78874 10.21126 10.00962 36 71932 28068 78902 21098 06970	93030	20
37 71952 28048 78930 21070 06978	93022	23
38 71973 28027 78959 21041 06986	93014	22
39 71994 28006 78987 21013 06993	93007	21
40 9.72014 10.27986 9.79015 10.20985 10.07001	9.92999	20
41 72034 27966 79043 20957 07009	92991	19
42 72055 27945 79072 20928 07017 43 72075 27925 79100 20900 07024	92983 92976	18
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	92968	16
45 9.72116 10.27884 9.79156 10.20844 10.07040	9.92960	15
46 72137 27863 79185 20815 07048	92952	14
47 72157 27843 79213 20787 07056	92944	13
48 72177 27823 79241 20759 07064	92936	12
49 72198 27802 79269 20731 07071 50 9.72218 10.27782 9.79297 10.20703 10.07079	92929 9,92921	11 10
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	92913	9
52 72259 27741 79354 20646 07095	92905	8
53 72279 27721 79382 20618 07103	92897	7
54 72299 27701 79410 20590 07111	92889	6 5
55 9.72320 10.27680 9.79438 10.20562 10.07119	9.92881	5
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	92874	43
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	92866 92858	2
59 72401 27599 79551 20449 07142		1
60 72421 27579 79579 20421 07158	22000	
M. Cosine. Secant. Cotangent, Tangent. Cosecant.	92850 92842	ō

32°			Logari	ithms.			147º
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	М.
0	9.72421	10.27579	9.79579	10.20421	10.07158	9.92842	60
1	72441	27559 27539	79607	20393	07166	92834	59
$\begin{bmatrix} \overline{2} \\ 3 \end{bmatrix}$	$72461 \\ 72482$	$27539 \\ 27518$	79635 79663	20365 20337	07174 07182	92826 92818	58 57
3	72482 72502	27518 27498	79603	20337	07182	92810	56
45	9.72522	10.27478	9.79719	10.20281	10.07197	9.92803	55
6	72542	27458	79747	20253	07205	92795	54
78	72562	27438	79776	20224	07213	92787	53 52
9	$72582 \\ 72602$	$27418 \\ 27398$	79804 79832	20196 20168	07221 07229	92779 92771	52
10	9.72622	10,27378	9.79860	10.20140	10.07237	9.92763	50
11	72643	27357	79888	20112	07245	92755	49
$12 \\ 13$	72663	27337	79916	20084	07253	92747	48
13	72683	27317	79944	20056	07261	92739	47
14 15	72703 9.72723	$27297 \\ 10,27277$	79972 9,80000	$20028 \\ 10.20000$	$07269 \\ 10.07277$	$92731 \\ 9.92723$	46
16	72743	27257	80028	19972	07285	92715	44
17 18	72763	27257 27237 27217	80056	19944	07293	92707	43
18	72783	27217	80084	19916	07301	92699	42
19 20 21	72803	27197	80112	19888	07309	92691	41
20	9.72823 72843	$10.27177 \\ 27157$	9.80140 80168	10.19860 19832	10.07317 07325	9.92683 92675	40 39
22	72863	27137	80195	19805	07333	92667	38
22 23 24	72883	27117	80223	19777	07341	92659	37
24	72902	27098	80251	19749	07349	92651	36
$\frac{25}{26}$	9.72922	10.27078	9.80279	10.19721	10.07357 07365	9.92643 92635	35
20	72942 72962	27058 27038	80307 80335	19693 19665	07365	92635	33
27 28	72982	27018	80363	19637	07381	92619	32
29	73002	26998	80391	19609	07389	92611	31
29 30 31 32	9.73022	10.26978	9.80419	10.19581	10.07397	9.92603	30
31	73041 73061	26959 26939	80447	19553 19526	07405 07413	92595 92587	29 28
32	73081	26919	80474 80502	19320	07413	92579	27
34	73101	26899	80530	19470	07429	92571	26
35	9.73121	10.26879	9.80558	10.19442	10.07437	9.92563	25
36	73140	26860	80586	19414	07445	92555	24
37 38 39	73160 73180	26840 · 26820	80614 80642	19386 19358	07454 07462	92546 92538	23
39	73200	26800	80669	19331	07470	92530	21
40	9,73219	10.26781	9.80697	10.19303	10.07478	9,92522	20
41	73239	26761	80725	19275	07486	92514	19
42	73259	26741	80753	19247	07494	92506 92498	18
43 44	73278 73298	26722 26702	80781 80808	19219 19192	07502 07510	92498	16
45	9.73318	10.26682	9.80836	10,19164	10.07518	9.92482	15
46	73337	10.26682 26663	80864	19136	07527	92473	14
47	73357	26643	80892	19108	07535	92465	13
48	73377	26623	80919 80947	19081 19053	07543 07551	92457 92449	12 11
49 50	73396 9.73416	26604 10.26584	9.80975	10.19025	10.07559	9.92449	10
51	73435	26565	81003	18997	07567	92433	9
52 53	73455	26545	81030	18970 18942	07575 07584	92425	87
53	73474	26526	81058	18942	07584	92416	7
54	73494	26506	81086	18914	07592 10.07600	92408 9.92400	6
55 56	9.73513 73533	10.26487 26467	9.81113 81141	10.18887 18859	07608	9.92400	5
57	73552	26448	81169	18831	07616	92384	3
57 58	73572	26428	81196	18804	07624	92376	3 2 1
59	73591	26409	81224	18776	07633	92367	
60	73611	26389	81252	18748	07641	92359	0
М.	Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	M.

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4	160	

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	3 °			Logar	ithms.			146°
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	М.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	0	9.73611	10.26389	9.81252	10.18748	10.07641	9.92359	60
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1	73630		81279	18721	07649	92351	59
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2							58
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	3							57
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	4					07674		56
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	5					10.07682		55 54
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	b		20273					53
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	6						02202	52
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	a							51
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								50
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								49
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	12						92260	48
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	13				18389	07748		47
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			26118	81638		07756		46
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$			10.26099	9.81666				45
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								44
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	17				18279			43
$\begin{array}{c c c c c c c c c c c c c c c c c c c $				81748	18252		92211	42
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		73978			18224			41
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	20							40 39
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								38
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								37
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								36
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			10 25907		10.18059	10.07848		35
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						07856	92144	34
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	27							33
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$							92127	32
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								31
$\begin{array}{c c c c c c c c c c c c c c c c c c c $				9.82078				30
$\begin{array}{c c c c c c c c c c c c c c c c c c c $								29
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	32							28 27
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								27
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			10 25716	0 80015			92077	20
$\begin{array}{c c c c c c c c c c c c c c c c c c c $			25697	80243				24
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					17730	07948		23
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								22
$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	39							21
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		9.74379		9.82352	10.17648		9.92027	20
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		74398		82380		07982	92018	19
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			25583		17593			18
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								17
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$						08007		16
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$					10.17511	10.08015	9.91985	15
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								14
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$						08032		13
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								12 11
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								10
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				82653				9
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				82681				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								8
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	54							6
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	55	9.74662	10.25338	9.82762	10.17238	10.08100		5
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				82790	17210	08109		4
59 74737 25263 82871 17129 08134 91866					17183	08117	91883	32
								2
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$								1
	60	74756	25244	82899	17101	08143	91857	0
M. Cosine. Secant. Cotangent. Tangent. Cosecant. Sine.]	M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M:

23°

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34°			Logar	ithms.			145°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
01	9.74756	10.25244	9.82899	10.17101	10.08143	9.91857	60
1	74775	25225	82926	17074	08151	91849	59
$\frac{2}{3}$	$74794 \\ 74812$	25206 25188	82953	17047	08160 08168	91840 91832	58
3	74812	25188	82980 83008	17020 16992	08168 08177	91832 91823	57 56
4 5 6 7 8 9	9.74850	10.25150	9.83035	10.16965	10.08185	9.91815	55
6	74868	25132	83062	16938	08194	91806	54
7	74887	25113	83089	16911	08202 08211	91798	53
8	74906	25094	83117	16883	08211	91789	52
9	74924	25076	83144	16856	08219	91781	51
10	9.74943 74961	10.25057	9.83171	10.16829	10.08228	9.91772	50
11	74901	25039 25020	83198 83225	$\begin{array}{r} 16802 \\ 16775 \\ 16748 \end{array}$	08237 08245	91763 91755	49
$12 \\ 13$	74999	25001	83252	16748	08254	91746	47
14	75017	24983	83280	16720	08262	91738	46
15	9.75036	10.24964	9.83307	10.16693	10.08271	9.91729	45
16	75054	24946	83334	16666	08280	91720	44
17	75073	24927	83361	16639	08288	91712	43
18	75091	24909	83388	16612	08297	91703	42
19	75110	24890	83415	16585	08305	91695	41
20 21	9.75128 75147	$10.24872 \\ 24853$	9.83442 83470	10.16558	10.08314 08323	9.91686 91677	40
22	75165	24835	83497	16530 16503 16476	08331	91669	38
23	75184	24816	83524	16476	08340	91669 91660	37
24	75202	24798	83551	16449	08349	91651	36
25	9.75221	10.24779	9.83578	10.16422	10.08357	9.91643	35
26	75239	24761	83605	16395	08366	91634	34
27 28	75258	24742	83632	16368	08375	91625	33
$\frac{28}{29}$	75276 75294	24724 24706	83659 83686	16341 16314	08383 08392	91617 91608	32
30	9.75313	10.24687	9.83713	10.16287	10.08401	9.91599	30
31	75331	24669	83740	16260	08409	91591	29
32 33 34	75350	24650	83768	$16260 \\ 16232 \\ 16205$	08418	91582	28
33	75368	24650 24632	83768 83795	16205	08427	91573	27
34	75386	24614	83822	16178	08435	91565	26
3 5 36	9.75405	10.24595	9.83849	10.16151	10.08444	9.91556	25
36	75423 75441	24577 24559	83876	16124 16097	08453 08462	91547 91538	24 23
38	75459	24559	83903 83930	16097	08402	91530	22
39	75478	24522	83957	16043	08479	91521	21
40	9.75496	10.24504	9.83984	10.16016	10.08488	9.91512	20
41	75514	24486	84011	15989	08496	91504	19
42	75533	24467	84038	15962	08505	91495	18
43	75551	24449	84065	15935	08514	91486	17
44	75569 9.75587	24431 10.24413	84092	15908 10.15881	08523 10.08531	91477 9.91469	16 15
45 46	75605	24395	9.84119 84146	15854	08540	91460	14
47	75624	24376	84173	15827	08549	91451	13
48	75624 75642	24358	84200	15800	08558	91442	12
49	75660	24340	84227	15800 15773	08567	91433	11
50	9.75678	10.24322	9.84254	10.15746	10.08575	9.91425	10
51	75696	24304	84280	15720	08584	91416	9
52	75714	24286 24267	84307	15693	08593	91407	1 8
$53 \\ 54$	75733 75751	24267 24249	84334 84361	15666 15639	08602 08611	91398 91389 9.91381	87654321
55	9.75769	10.24231	9.84388	10.15612	10.08619	9.91381	5
55 56	75787	24213	84415	15585	08628	91372	4
57	75805	24195	84442	15558	08637	91363	3
58	75823	24177	84469	15531	08646	91354	2
59	75841	24159	84496	15504	08655	91345	
-60	75859	24141	84523	15477	08664	91336	0
М.	Cosine.	Secant.	Cotangent	. Tangent.	Cosecant.	Sine.	M.

\$5°			Logar	ithms.			144°
M.	Sine.	Cosecant.	Tangent,	Cotangent,	Secant.	Cosine.	M.
0	9.75859	10.24141	9.84523	10.15477	10.08664	9,91336	60
1	75877	24123	84550	15450	08672	91328	59
23456	75895	24105	84576	15424	08681	91319	58
- 3	75913	24087	84603	15397	08690	91310	57
4	75931	24069	84630	15370	08699	91301	56
5	9.75949	10.24051	9.84657	10.15343	10.08708	9.91292 91283	55
6 7	75967 75985	24033 24015	84684 84711	$15316 \\ 15289$	08717 08726	91283	54 53
8	75985	24015 23997	84738	15289	08720	91274 91266	52
9	76021	23979	84764	15236	08743	91257	51
10	9.76039	10.23961	9.84791	10.15209	10.08752	9.91248	50
ĩĩ	76057	23943	84818	15182	08761	91239	49
$\hat{1}\hat{2}$	76075	23925	84845	15155	08770	91230	48
13	76093	23907	84872	15128	08779	91221	47
14	76111	23889	84899	15101	08788	91212	46
15	9.76129	10.23871	9.84925	10.15075	10.08797	9.91203	.45
16	76146	23854	84952	15048	08806	91194	44
17	76164	23836	84979	15021	08815	91185	43
18	76182	23818	85006	14994	08824	91176	42
19	76200	23800	85033	14967	08833	91167	41
20	9.76218	10.23782	9.85059	10.14941	10.08842	9.91158	40
21 22 23	76236	23764	85086	14914	08851	91149	39
22	76253	23747	85113	14887	08859	91141	38
23	76271	23729	85140	14860	08868	91132	37
24 25	76289	23711	85166	14834	08877	91123	36
29 26	9.76307 76324	$10.23693 \\ 23676$	9.85193	$10.14807 \\ 14780$	10.08886	9.91114	35 34
20	76342	23658	85220 85247	14780	08895 08904	91105 91096	33
28	76360	23640	85273	14727	08913	91090	32
20	76378	23622	85300	14700	08922	91037	31
29 30	9,76395	10.23605	9.85327	10.14673	10.08931	9.91069	30
31	76413	23587	85354	14646	08940	91060	29
32	76431	23569	85380	14620	08949	91051	28
33	76448	23552	85407	14593	08958	91042	27
34	76466	23534	85434	14566	08967	91033	26
35	9.76484	10.23516	9.85460	10.14540	10.08977	9.91023	25
36	76501	23499	85487	14513	08986	91014	24
37	76519	23481	85514	14486	08995	91005	23
38	76537	23463	85540	14460	09004	90996	22
39	76554	23446	85567	14433	09013	90987	21
10	9.76572 76590	$ \begin{array}{r} 10.23428 \\ 23410 \end{array} $	9.85594	10.14406	10.09022	9.90978	20
12	76607	23393	85620 85647	14380 14353	09031 09040	90969 90960	19 18
13	76625	23375	85674	14326	09049	90900	17
14	76642	23358	85700	14300	09058	90942	16
15	9.76660	10.23340	9.85727	10.14273	10.09067	9,90933	15
iõ	76677	23323	85754	14246	09076	90924	14
17	76695	23305	85780	14220	09085	90915	13
18	76712	23288	85807	14193	09094	90906	12
19	76730	23270	85834	14166	09104	90896	11
10	9.76747	10.23253	9.85860	10.14140	10.09113	9.90887	10
1	76765	23235	85887	14113	09122	90878	9
12	76782	23218	85913	14087	09131	90869	8
13	76800	23200	85940	14060	09140	90860	6
14	76817	$23183 \\ 10.23165$	85967	14033	09149	90851	6
15 16	9.76835 76852		9.85993	10.14007	10.09158	9.90842	5
17	76852 76870	23148 23130	86020	13980	09168	90832	4
8	76887	23130	86046 86073	13954 13927	09177 09186	90823 90814	3 2
9	76904	23096	86100	13900	09180	90814 90805	
õ	76922	23078	86126	13874	09204	90805	Ó
ī.	Cosine,	Secant,	Cotangent.	Tangent.	Cosecant.	Sine,	M.
							1 104.

36°			Logar	ithms.			143°
M.	Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M.
0	9.76922	10.23078	9.86126	10.13874	10.09204	9.90796	60
$\begin{array}{c} 1\\ 2\\ 3\end{array}$	76939	23061	86153	13847	09213	90787	59
2	76957	23043	86179	13821	09223	90777	58
3	76974	23026	86206	13794 13768	09232	90768	57
45	76991	23009	86232 9.86259	13768	09241	90759	56
D	9.77009 77026	10.22991 22974	9.86259	10.13741	10.09250	9.90750	55
6 7	77026	22974 22957	86285 86312	$13715 \\ 13688$	09259 09269	90741 90731	54 53
8	77061	22939	86338	13662	09209	90731	52
9	77078	22922	86365	13635	09287	90713	51
10	77078 9.77095	10.22905	9.86392	10.13608	10.09296	9.90704	50
- îĭ	77112	22888	86418	13582	09306	90694	49
12	77130	22870	86445	13555	09315	90685	48
13	77147	22853	86471	13529	09324	90676	47
14	77164	22836	86498	13502	09333	90667	46
15	9.77181	10.22819	9.86524	10.13476	10.09343	9.90657	45
16	77199 77216	22801	86551	13449	09352	90648	44
17	77216	$22784 \\ 22767$	86577	13423 13397	09361	90639 90630	43 42
18 19	77250	22750	86603	13370	09370 09380	90620	
20	9.77268	10.22732	9.86656	10.13344	10.09389	9.90611	41 40
20	77285	22715	86683	13317	09398	90602	39
22	77302	22698	86709	13291	09408	90592	38
23	77319	22681	86736	13264	09417	90583	37
24	77336	22664	86762	13238	09426	90574	36
25	9.77353	10.22647	9.86789	10.13211	10.09435	9.90565	35
$\frac{25}{26}$	77370	22630	86815	13185	09445	90555	34
27	77387	22613	86842	13158	09454	90546	33
28	77405	22595	86868	13132	09463	90537	32
29 30	77422 9.77439	$22578 \\ 10.22561$	86894 9,86921	$13106 \\ 10.13079$	09473 10.09482	90527 9,90518	31
30	9.77439 77456	22544	9.86921	13053	09491	9.90518	30 29
32	77473	22527	86974	13026	09501	90499	28
33	77490	22510	87000	13000	09510	90490	27
34	77507	22493	87027	12973	09520	90480	26
35	77507 9.77524	10.22476	9.87053	10.12947	10.09529	9.90471	25
36	77541	22459	87079	12921	09538	90462	24
37	77558	22442	87106	12894	09548	90452	23
38	77575	22425	87132	12868	09557	90443	22
39	77592	22408	87158	12842	09566	90434	21
40 41	9.77609	$10.22391 \\ 22374$	9.87185	$10.12815 \\ 12789$	10.09576	9.90424 90415	20 19
41 42	$77626 \\ 77643$	22357	87211 87238	12762	09585 09595	90415	18
43	77660	22340	87264	12736	09604	90396	17
44	77677	22323	87290	12710	09614	90386	16
45	9.77694	10.22306	9 87317	10.12683	10.09623	9.90377	15
46	77711 77728 77744	22289	87343	12657	09632	90368	14
47	77728	22272	87369	12631	09642	90358	13
48	77744	22256	87396	12604	09651	90349	12
49	77761	22239	87422	12578	09661	90339	11
59	9.77778	10.22222	9.87448	10.12552	10.09670	9.90330	10
51 52	77795 77812	$22205 \\ 22188$	87475 87501	12525 12499	09680 09689	90320 90311	9
53	77829	22188	87501	12499	09699	90301	7
54	77846	22154	87554	12473	09099	90292	6
55	9.77862	10.22138	9.87580	10.12420	10.09718	9.90282	5
56	77879	22121	87606	12394	09727	90273	4
57	77896	22104	87633	12367	09737	90263	3
58	77913	22087	87659	12341	09746	90254	2
59	77930	22070	87685	12315	09756	90244	1
60	77946	22054	87711	12289	09765	90235	0
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	M.

57°			Logar	ithms.			142°
М.	Sine.	Cosecant,	Tangent.	Cotangent,	Secant.	Cosine.	М.
0	9.77946	10.22054	9.87711	10.12289	10.09765	9.90235	60
1	77963	22037	87738	12262	09775	90225	59
$\frac{2}{3}$	77980	22020	87764	12236	09784	90216	58
3	77997	22003	87790	12210	09794	90206	57
4	$78013 \\ 9.78030$	$21987 \\ 10.21970$	87817 9.87843	$12183 \\ 10.12157$	09803 10.09813	90197 9,90187	56 55
6	78047	21953	87869	12131	09822	90178	54
4 5 6 7 8 9	78063	21937	87895	12105	09832	90168	53
8	78080 -	21920	87922	12078	09841	90159	52
	78097	21903	87948	12052	09851	90149	51
10	9.78113	10.21887	9.87974	10.12026	10.09861	9,90139	50
11	78130	21870	88000	12000	09870	90130	49
12	78147	21853	88027	11973	09880	90120	48
13	78163	21837	88053	11947	09889	90111	47
$\frac{14}{15}$	78180 9.78197	$21820 \\ 10.21803$	88079 9.88105	$11921 \\ 10.11895$	09899 10.09909	90101 9.90091	46
16	78213	21787	88131	11869	09918	90082	44
17	78230	21770	88158	11842	09928	90072	43
18	78246	21754	88184	11816	09937	90063	42
19	78263	21737	88210	11790	09947	90053	41
20	9.78280	10.21720	9.88236	10.11764	10.09957	9.90043	40
$\frac{21}{22}$	78296	21704	88262	11738	09966	90034	- 39
22	78313	21687	88289	11711	09976	90024	38
23 24	78329	$21671 \\ 21654$	88315	11685	09986	90014	37
25	$78346 \\ 9.78362$	10.21634	88341 9.88367	$11659 \\ 10.11633$	09995 10.10005	90005 9.89995	36 35
26	78379	21621	88393	11607	10.10005	9.89995 89985	34
27	78395	21605	88420	11580	10024	89976	33
28 29	78412	21588	88446	11554	10034	89966	32
29	78428	21572	88472	11528	10044	89956	31
30	9.78445	10.21555	9.88498	10.11502	10.10053	9.89947	30
$\frac{31}{32}$	78461	21539	88524	11476	10063	89937	29
52 33	78478 78494	$21522 \\ 21506$	88550	11450	10073	89927	28
34	78510	21306	88577 88603	$rac{11423}{11397}$	10082 10092	89918 89908	27 26
35	9.78527	10.21473	9.88629	10.11371	10.10102	9,89898	20
36	78543	21457	88655	11345	10112	89888	24
37	78560	21440	88681	11319	10121	89879	23
38	78576	21424	88707	11293	10131	89869	22
39	78592	21408	88733	11267	10141	89859	21
40 41	9.78609	10.21391	9.88759	$10.11241 \\ 11214$	10.10151	9.89849	20
19	$78625 \\ 78642$	21375 21358	88780	11214	10160	89840	19
42 43	78658	21335	88812 88838	$11188 \\ 11162$	10170 10180	89830 89820	18 17
14	78674	21326	88864	11136	10190	89810	16
45	9.78691	10.21309	9.88890	10.11110	10.10199	9.89801	15
16	78707	21293	88916	11084	10209	89791	14
17	78723	21277	88942	11058	10219	89781	13
18	78739	21261	88968	11032	10229	89771	12
19 50	78756	21244	88994	11006	10239	89761	11
51	$9.78772 \\ 78788$	10.21228 91919	9.89020 89046	10.10980	10.10248	9.89752	10
52	78805	21212 21195	89046 89073	$10954 \\ 10927$	$10258 \\ 10268$	89742	9
52 53	78821	21155	89099	10927	10268	89732 89722	8
54	78837	21163	89125	10875	10278	89712	6
55	9.78853	10.21147	9.89151	10.10849	10.10298	9.89702	6 5
6	78869	21131	89177	10823	10307	89693	4
57	78886	21114	89203	10797	10317	89683	
8	78902	21098	89229	10771	10327	89673	2
i9 i0	78918 78934	21082	89255	10745	10337	89663	1
		21066	89281	10719	10347	89653	0
I.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

27°

38°			Logari	ithms.			141°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.78934	10.21066	9.89281	10.10719	10.10347	9.89653	60
1	78950	21050 21033	89307	10693	10357	89643	59
23	78967	21033	89333	10667	10367	89633	58
3	78983 78999	21017 21001	89359 89385	$10641 \\ 10615$	10376 10386	89624 89614	57 56
5	9.79015	10.20985	9.89411	10.10589	10.10396	9.89604	55
6	79031	20969	89437	10563	10406	89594	54
7	79047	20953	89463	10537	10416	89584	53
8	79063	20937	89489	10511	10426	89574	52
- 9	79079	20921	89515	10485	10436	89564 9.89554	51 50
10 11	9.79095 79111	10.20905 20889	9.89541 89567	$10.10459 \\ 10433$	10.10446 10456	9.89544 89544	49
12^{11}	79128	20872	89593	10407	10466	89534	48
$\overline{13}$	79144	20856	89619	10381	10476	89524	47
14	79160	20840	89645	10355	10486	89514	46
15	9.79176	10.20824	9.89671	10.10329	10.10496	9.89504	45
16 17	79192 79208	20808 20792	89697 89723	$ \begin{array}{r} 10303 \\ 10277 \end{array} $	$10505 \\ 10515$	89495 89485	44
18	79208	20792	89749	10277	10525	89475	42
19	79240	20760	89775	10225	10535	89465	41
20	9.79256	10.20744	9.89801	10225 10.10199	10.10545	9.89455	40
21	79272	20728	89827	10173	10555	89445	39
$\frac{22}{23}$	79288	20712	89853	10147	10565	89435	38 37
$\frac{23}{24}$	79304 79319	20696	89879 89905	10121 10095	$10575 \\ 10585$	89425 89415	36
25	9.79335	20681 10.20665	9.89931	10.10069	10.10595	9.89405	35
$\tilde{26}$	79351	20649	89957	10043	10605	89395	34
27	79367	20633	89983	10017	10615	89385	33
28	79383	20617	90009	09991	10625	89375	32
29 30	79399 9.79415	$ 20601 \\ 10.20585 $	90035 9.90061	09965 10.09939	10636 10.10646	89364 9.89354	31 30
31	9.79415	20569	9.90081	09914	10656	89344	29
32	79447	20569 20553	90112	09888	10666	89334	28
32 33	79463	20537	90138	09862	10676	89324	27
34	79478	20522	90164	09836	10686	89314	26
35	9.79494	10.20506	9.90190	10.09810	10.10696	9.89304	25 24
36	79510 79526	$20490 \\ 20474$	90216 90242	09784	10706 10716	89294 89284	23
37 38	79542	20458	90268	09758 09732	10726	89274	22
39	79558	20442	90294	09706	$10726 \\ 10736$	89264	21
·40	9.79573	10.20427	9.90320	10.09680	10.10746	9.89254	20
41	79589	20411	90346	09654	10756	89244	19 18
$\frac{42}{43}$	79605 79621	20395 20379	90371 90397	09629 09603	10767 10777	89233 89223	17
43	79636	20364	90423	09003	10787	89213	16
$\hat{45}$	9,79652	10.20348	9.90449	10.09551	10.10797	9.89203	15
46	79668	20332	90475	09525	10807	89193	14
47	79684	20316	90501	09499	10817	89183	13
48 49	79699	20301	90527 90553	09473	10827 10838	89173 89162	$12 \\ 11$
49 50	79715 9.79731	20285 10.20269	90555	09447 10.09422	10.10848	9.89152	10
51	79746	20254	90604	09396	10858	89142	
$5\hat{2}$	79762	20238	90630	09370	10868	89132	9 8
53	79778	20222	90656	09344	10878	89122	7 6 5 4
54	79793	20207	90682	09318	10888	89112	6
55 56	9.79809 79825	$10.20191 \\ 20175$	9.90708 90734	10.09292 09266	10.10899 10909	9.89101 89091	4
50 57	79820	20175	90759	09200	10909	89081	3
58	79856	20144	90785	09215	10929	89071	32
59	79872	20128	90811	09189	10940	89060	1
60	79887	20113	90837	09163	10950	89050	0
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.
1 10	n						E 10

9 °			Logar	ithms.			140°
VI .	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9,79887	10.20113	9.90837	10.09163	10.10950	9.89050	60
1	79903	20097	90863	09137	10960	89040	59
2	79918	20082	90889	09111	10970	89030	58
3	79934	20066	90914	09086	10980	89020	57 56
4	79950	20050	90940	09060	$10991 \\ 10.11001$	89009 9,88999	55
5 6	9.79965	10.20035	9.90966	10.09034 09008	11011	9.88989	54
7	79981 79996	$20019 \\ 20004$	90992 91018	08982	11022	88978	53
8	79996 80012	19988	91043	08957	11032	88968	52
9	80012	19973	91069	08931	11042	88958	51
10	9,80043	10.19957	9.91095	10.08905	10.11052	9.88948	50
ii	80058	19942	91121	08879	11063	88937	49
12	80074	19926	91147	08853	11073	88927	48
13	80089	19911	91172	08828	11083	88917	47
14	80105	19895	91198	08802	11094	88906 9.88896	46 45
15	9.80120	10.19880	9,91224	$ \begin{array}{r} 10.08776 \\ 08750 \end{array} $	$10.11104 \\ 11114$	9.00090	45
16	80136	$ 19864 \\ 19849 $	91250 91276	08750	11125	88875	43
17 18	$80151 \\ 80166$	19834	91301	08699	11135	88865	42
19	80182	19818	91327	08673	11145	88855	41
20	9.80197	10,19803	9.91353	10.08647	10,11156	9.88844	40
21	80213	19787	91379	08621	11166	88834	39
22	80228	19772	91404	08596	11176	88824	38
23	80244	19756	91430	08570	11187	88813	37
24	80259	19741	91456	08544	11197	88803	36 35
25	9.80274	10.19726	9.91482	10.08518 08493	$10.11207 \\ 11218$	$9.88793 \\ 88782$	30
$\frac{26}{27}$	$80290 \\ 80305$	$19710 \\ 19695$	91507 91533	08467	11218	88772	33
$\frac{27}{28}$	80320	19680	91559	08441	11239	88761	32
29	80336	19664	91585	08415	11249	88751	31
30	9,80351	10,19649	9.91610	10.08390	10,11259	9.88741	30
31	80366	19634	91636	08364	11270	88730	29
32	80382	19618	91662	08338	11280	88720	28
33	80397	19603	91688	08312	11291	88709	27
34	80412	19588	91713	08287	11301	88699	26 25
35	$9.80428 \\ 80443$	10.19572	9.91739 91765	$ \begin{array}{r} 10.08261 \\ 08235 \end{array} $	$10.11312 \\ 11322$	9.88688 88678	20 24
36 37	80443	$19557 \\ 19542$	91765	08209	11332	88668	23
38	80473	19527	91816	08184	11343	88657	22
39	80489	19511	91842	08158	11353	88647	21
40	9.80504	10.19496	9,91868	10.08132	10.11364	9.88636	20
41	80519	19481	91893	08107	11374	88626	19
42	80534	19466	91919	08081	11385	88615	18
43	80550	19450	91945	08055	11395	88605	17
44	80565	19435	91971	$08029 \\ 10.08004$	$11406 \\ 10.11416$	88594 9.88584	$16 \\ 15$
45 46	9.80580 80595	$10.19420 \\ 19405$	9.91996 92022	07978	10.11416	88573	14
47	80610	19390	92048	07952	11437	88563	13
48	80625	19375	92073	07927	11448	88552	12
49	80641	19359	92099	07901	11458	88542	11
50	9.80656	10.19344	9.92125	10.07875	10.11469	9.88531	10
51	80671	19329	92150	07850	11479	88521	9
52	80686	19314	92176	07824	11490	88510	87
53	80701	19299	92202	07798	11501	88499	7
54	80716	19284	92227 9.92253	07773	11511	88489 9.88478	6 5
55 56	$9.80731 \\ 80746$	$10.19269 \\ 19254$	9.92253	$10.07747 \\ 07721$	10.11522 11532	9,88478	4
57	80740	19238	92304	07696	11543	88457	3
58	80777	19223	92330	07670	11553	88447	3 2
59	80792	19208	92356	07644	11564	88436	1
60	80807	19193	92381	07619	11575	88425	0
M. (Cosine,	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	М.

40 °			Logar	ithms.			139°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.80807	10.19193	9.92381	10.07619	10.11575	9.88425	60
1	80822	19178	92407	07593	11585	88415	59
$\frac{2}{3}$	80837	19163	92433	07567	11596	88404	58
3	80852	19148	92458	07542	11606	88394	57
4 5	80867	19133	92484	07516	11617	88383	56
5	9.80882	10.19118	9.92510	10.07490	10.11628	9.88372	55
6	80897	19103	92535	07465	11638	88362	54
7	80912 80927	19088 19073	92561 92587	07439 07413	11649	88351	53
8 9	80942	19073	92612	07388	11660 11670	88340 88330	52 51
10	9.80957	10.19043	9,92638	10.07362	10.11681	9.88319	50
îi	80972	19028	92663	07337	11692	88308	49
12	80987	19013	92689	07311	11702	88298	48
13	81002	18998	92715	07285	11713	88287	47
14	81017	18983	92740	07260	11724	88276	46
15	9.81032	10.18968	9.92766 92792	10.07234 07208 07183	10.11734	9.88266	45
16	81047	18953	92792	07208	11745	88255	44
17	81061	18939	92817	07183	11756	88244	43
18	81076	18924	92843	07157	11766	88234	42
19	81091	18909	92868	07132	11777	88223	41
20	9.81106	10.18894	9.92894	10.07106	10.11788	9.88212	40
21	81121	18879	92920	07080	11799	88201	39
22	81136	18864	92945	07055	11809	88191	38
$\frac{23}{24}$	$81151 \\ 81166$	18849	92971	07029 07004	11820	88180	37
24 25	9.81160	18834 10.18820	92996 9.93022	10.06978	$11831 \\ 10.11842$	88169	36 35
26	81195	10.13520	93048	06952	10.11842 11852	$9.88158 \\ 88148$	30
27	81210	18790	93073	06927	11863	88137	33
28	81225	18775	93099	06901	11874	88126	32
29	81240	18760	93124	06876	11885	88115	31
30	9.81254	10.18746	9.93150	10.06850	10.11895	9.88105	30
31	81269	18731	93175	06825	11906	88094	29
32	81284	18716	93201	06799	11917	88083	28
33	81299	18701	93227	06773 06748	11928	88072	27
34	81314	18686	93252	06748	11939	88061	26
35	9.81328	10.18672	9.93278	10.06722	10.11949	9.88051	25
36	81343	18657	93303	06697	11960	88040	24
37	81358 81372	18642	93329	06671	11971	88029	23
38 39	81387	18628 18613	93354 93380	06646 06620	11982	88018 88007	22
40	9.81402	10.18598	9.93406	10.06594	11993 10.12004	9.87996	20
41	81417	18583	93431	06569	12015	87985	19
$\frac{1}{42}$	81431	18569	93457	06543	12025	87975	18
43	81446	18554	93482	06518	12036	87964	17
44	81461	18539	93508	06492	12047	87953	16
45	9.81475	10.18525	9.93533	10.06467	10.12058	9.87942	15
46	81490	18510	93559	06441	12069	87931	14
47	81505	18495	93584	06416	12080	87920	13
48	81519	18481	93610	06390	12091	87909	12
49	81534	18466	93636	06364	12102	87898	11
50 51	9.81549 81563	10.18451	9.93661	10.06339	10.12113 12123	9.87887	10
52	81579	$ 18437 \\ 18422 $	93687 93712	06313 06288	12123	87877	9
53	81578 81592	18422	93712	06268	12134 12145	87866 87855	87
54	81607	18393	93763	06237	12145	87844	6
55	9.81622	10.18378	9.93789	10.06211	10.12167	9.87833	6 5
56	81636	18364	93814	06186	12178	87822	4
57	81651	18349	93840	06160	12189	87811	3
58	81665	18335	93865	06135	12200	87800	2
59	81680	18320	93891	06109	12211	87789	ī
60	81694	18306	93916	06084	12222	87778	ō
M.	Cosine.	Secant.	Cotangent.	Tangent.	Cosecant.	Sine.	М.

1° Logarithms.							1 3 8°
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine,	М.
0	9.81694	10.18306	9.93916	10.06084	10.12222	9.87778	60
1	81709	18291	93942	06058	12233	87767	59
$\frac{2}{3}$	81723	18277	93967	06033	12244	87756	58
3	81738	18262	93993	06007	12255	87745	57
4 5	81752	18248	94018	05982	12266	87734	56
э 6	9.81767	$10.18233 \\ 18219$	9.94044	$10.05956 \\ 05931$	$10.12277 \\ 12288$	9.87723	55 54
7	$81781 \\ 81796$	18219 18204	94069 94095	05905	12288 12299	87712 87701	53
8	81810	18204	94095	05880	12299	87690	52
9	81825	18175	94146	05854	12321	87679	51
10	9.81839	10.18161	9.94171	10.05829	10.12332	9.87668	50
11	81854	18146	94197	05803	12343	87657	49
12	81868	18132	94222	05778	12354	87646	48
13	81882	18118	94248	05752	12365	87635	47
14	81897	18103	94273	05727	12376	87624	46
15	9.81911	10.18089	9.94299	10.05701	10.12387	9.87613	45
16	81926	18074	94324	05676	12399	87601	44
17	$81940 \sim$	18060	94350	05650	12410	87590	43
18	81955	18045	94375	05625	12421	87579	42
19 20	81969 9.81983	18031 10.18017	$94401 \\ 9.94426$	05599 10.05574	$12432 \\ 10.12443$	$87568 \\ 9.87557$	41 40
20	81998	18002	94452	05548	12454	87546	39
22	82012	17988	94477	05523	12465	87535	38
23	82026	17974	94503	05497	12476	87524	37
$\widetilde{24}$	82041	17959	94528	05472	12487	87513	36
25	9.82055	10.17945	9.94554	10.05446	10.12499	9.87501	35
26	82069	17931	94579	05421	12510	87490	34
27	82084	17916	94604	05396	12521	87479	- 33
28	82098	17902	94630	05370	12532	87468	32
29	82112	17888	94655	05345	12543	87457	31
30 31	9.82126	10.17874	9.94681	10.05319	10.12554	9.87446	30
31 32	$82141 \\ 82155$	$17859 \\ 17845$	94706	05294	12566	87434	29 28
33	82169	17831	94732 94757	05268 05243	$12577 \\ 12588$	$87423 \\ 87412$	27
34	82184	17816	94783	05217	12599	87401	26
35	9.82198	10.17802	9.94808	10.05192	10.12610	9.87390	25
36	89912	17788	94834	05166	12622	87378	24
37	82226	17774	94859	05141	12633	87367	23
38	82240	17760	94884	05116	12644	87356	22
39	82255	17745	94910	05090	12655	87345	21
10	9.82269	10.17731	9.94935	10.05065	10.12666	9.87334	20
11	82283	17717	94961	05039	12678	87322	19
42 43	82297 82311	17703	94986	05014	12689	87311	18
43	82311 82326	17689	95012	04988	12700	87300	17
15	9.82340	$17674 \\ 10.17660$	95037 9.95062	04963 10.04938	$\begin{array}{c} 12712 \\ 10.12723 \end{array}$	87288	16 15
16	82354	17646	95082	04912	10.12723	9.87277 87266	10
17	82368	17632	95113	04887	12745	87255	13
18	82382	17618	95139	04861	12757	87243	12
19	82396	17604	95164	04836	12768	87232	11
50	9.82410	10.17590	9.95190	10.04810	10.12779	9.87221	10
51	82424	17576	95215	04785	12791	87209	9
52	82439	17561	95240	04760	12802	87198	8
53	82453	17547	95266	04734	12813	87187	7
54	82467	17533	95291	04709	12825	87175	6
55 56	9.82481	10.17519	9.95317	10.04683	10.12836	9.87164	5
56 57	82495	17505	95342	04658	12847	87153	4
58	82509 82523	17491	95368	04632	12859	87141	32
59	82523 82537	$17477 \\ 17463$	95393 95418	04607 04582	12870' 12881	87130	1
30	82551	17403	95444	04556	12881 12893	87119 87107	
	02001			01000	12033	0/10/	
¥I.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	М.

		Logar	ithms.			137°
Sine.	Cosecant.	Tangent.	Cotangent,	Secant.	Cosine.	M,
9.82551	10.17449	9.95444	10.04556	10.12893	9.87107	60
82565	17435	95469	04531	12904	87096	59
82579 82593	$17421 \\ 17407$	95495 95520	04505 04480	12915 12927	87085	58 57
82607	17902	95545	04455	12927	87073 87062	56
9.82621	$17393 \\ 10.17379$	9.95571	10.04429	10.12950	9 87050	55
82635	17365	95596	04404	12961	87039	54
82649	17351	95622	04378	12972	87028	53
82663	17337 17323	95647 95672	04353	12984	87016	52
82677	17323	95672	04328	12995	87005	51
9.82691	10.17309	9.95698	10.04302	10.13007	9.86993	50
$82705 \\ 82719$	17295	95723	04277	13018 13030	86982	49
80739	17281 17267 17253	95748 95774 95799	04252 04226	13041	86970 86959	48
82733 82747	17253	95799	04220	13053	86947	46
9.82761	10.17239	9,95825	10.04175	10.13064	9.86936	45
82775	17225	95850	04150	13076	86924	44
82788	17212	95875	04125	13087	86913	43
82802	$\begin{array}{r} 17225 \\ 17212 \\ 17198 \end{array}$	95901	04099	13098	86902	42
82816	17184	95926	04074	13110	86890	41
9.82830 82844	$10.17170 \\ 17156$	9.95952	10.04048	10.13121 13133	9.86879	40
82844 82858	17136	95977 96002	04023 03998	13135	86867 86855	39 38
82872	17128	96022	03972	13156	86844	37
82885	17115	96053	03947	13168	86832	36
9.82899	10.17101	9.96078	10.03922	10.13179	9.86821	35
82913	17087 17073	96104	03896	13191	86809	34
82927	17073	96129	03871	13202	86798	33
82941	17059	96155	03845	13214	86786	32
82955 9,82968	$17045 \\ 10.17032$	96180	03820 10.03795	$13225 \\ 10.13237$	86775	31 30
82982	10.17032	9.96205 96231	03769	13248	9.86763 86752	29
82996	17004	96256	03744	13260	86740	28
83010	16990	96281	03719	13272	86728	27
83023	16977	96307	03693	13283	86717	26
9.83037	10.16963	9.96332	10.03668	10.13295	9.86705 86694	25
83051	16949	96357	03643	13306 13318	86694	24
83065	16935	96383	03617	13318	86682	23
83078 83092	16922 16908	96408 96433	03592 03567	13330 13341	86670 86659	$\frac{22}{21}$
9.89106	10 16804	9.96459	10 03541	10.13353	9.86647	20
9.83106 83120	$10.16894 \\ 16880$	96484	$10.03541 \\ 03516$	13365	86635	19
83133	16867	96510	03490	13376	86624	18
83147	16853	96535	03465	13388	86612	
83161	16839	96560	03440	13400	86600	16
9.83174	10.16826	9.96586	10.03414	10.13411	9.86589	15
83188	16812	96611	03389	13423 13435	86577	14
83202 83215	16798	96636	03364 03338	13435	86565	13 12
83229	16785	96662 96687	03313	13458	$\frac{86554}{86542}$	11
9.83242	$\begin{array}{r}16771\\10.16758\\16744\end{array}$	9.96712	10.03288	10.13470	9.86530	10
83256	16744	9.96712 96738	03262	13482	86518	Îğ
83270	16730	96763	03237	13493	86507	8
83283	16717	96788	03212	13505	86495	7
83297	16703	96814	03186	13517	86483	6
9.83310	10.16690	9.96839	10.03161	10.13528	9.86472	5
83324	16676	96864	03136	13540	86460	4
83338 83351	16662 16649	96890 96915	03110 03085	13552 13564	$86448 \\ 86436$	3
83365	16635	96915	03060	13575	86425	6 5 4 3 2 1
83378	16622	96966	03034	13587	86413	Ô
Cosine.	Secant.	Cotangent	Tangent.	Cosecant.	Sine.	М.

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Logarithms.

43°			Logar	ithms.			1360	
M.	Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M .	
0	9.83378	10,16622	9.96966	10.03034	10.13587	9.86413	60	
ĭ	83392	16608	96991	03009	13599	86401	59	
$\overline{2}$	83405	16595	97016	02984	13611	86389	58	
$\frac{2}{3}$	83419	$ 16581 \\ 16568 $	97042	02958	13623	86377	57	
4	83432	16568	97067	02933	13634	86366	56	
5	9.83446	10,16554	9.97092	10.02908	10.13646	9.86354	55	
6	83459	16541	97118	02882	13658	86342	54	
7	83473	16527	97143	02857	13670	86330	53	
8	83486	16514	97168	02832	13682	86318	52	
9	83500	16500	97193	02807	13694	86306	51	
10	9.83513	10.16487	9.97219	10.02781	10.13705	9.86295	50	
11	83527	16473	97244	02756	13717	86283	49	
12	83540	16460	97269	02731	13729	86271	48	
13	83554	16446	97295	02705	13741	86259	47	
14	83567	16433	97320	02680	13753	86247	46	
15	9.83581	10.16419	9.97345	10.02655	10.13765	9.86235	45	
16	83594	16406	97371	02629	13777	86223	44	
17	83608	16392	97396	02604	13789	86211	43	
18	83621	16379	97421	02579	13800	86200	42	
19	83634	16366	97447	02553	13812	86188	41	
20	9.83648	10.16352	9.97472	10.02528	10.13824	9.86176	40	
21	83661	16339	97497	02503	13836	86164	39	
22	83674	16326	97523	02477	13848	86152	38	
23	83688	16312	97548	02452	13860	86140	36	
24	83701	16299	97573	02427	13872	86128	35	
25	9.83715	10.16285	9.97598	10.02402	10.13884	$9.86116 \\ 86104$	34	
26	83728	16272	97624	02376	13896		33	
27	83741	16259	97649	02351	13908	86092 86080	32	
28	83755	16245	97674	02326	$13920 \\ 13932$	86068	31	
29	83768	16232	97700	02300	13932 10.13944	9.86056	30	
30	9.83781	10.16219	9.97725	$10.02275 \\ 02250$	13956	86044	29	
31	83795	$16205 \\ 16192$	97750 97776	02224	13968	86032	28	
32	83808		97770	02199	13980	86020	27	
33	83821	16179	97801	02199	13992	86008	26	
34	83834	16166	97826 9.97851	10.02149	10.14004	9.85996	25	
35 36	9.83848	10.16152	97851	02123	14016	85984	24	
37	$83861 \\ 83874$	16139 16126	97902	02098	14010	85972	23	
38	83887	16113	97902	02053	14040	85960	22	
39	83901	16099	97953	02047	14052	85948	21	
40	9.83914	10.16086	9,97978	10.02022	10.14064	9,85936	20	
41	83927	16073	98003	01997	14076	85924	19	
42	83940	16060	98029	01971	14088	85912	18	
43	83954	16046	98054	01946	14100	85900	17	
44	83967	16033	98079	01921	14112	85888	16	
45	9.83980	10.16020	9.98104	10.01896	10.14124	9.85876	15	
46	83993	16007	98130	01870	14136	85864	14	
47	84006	15994	98155	01845	14149	85851	13	
48	84020	15980	98180	01820	14161	85839	12	
49	84033	15967	98206	01794	14173	85827	11	
50	9.84046	10.15954	9.98231	10.01769	10,14185	9.85815	10	
51	84059	15941	98256	01744	14197	85803	9	
52	84072	15928	98281	01719	14209	85791	8	
53	84085	15915	98307	01693	14221	85779	87	
54	84098	15902	98332	01668	14234	85766	6	
55	9.84112	10.15888	9.98357	10.01643	10.14246	9.85754	5	
56	84125	15875	98383	01617	14258	85742	4	
57	84138	15862	98408	01592	14270	85730	3	
58	84151	15849	98433	01567	14282	85718	3	
59	84164	15836	98458	01542	14294	85706	1	
60	84177	15823	98484	01516	14307	85693	0	
M.	Cosine,	Secant.	Cotangent	. Tangent,	Cosecant.	Sine.	- <u>M</u> .	

44°			Logar	ithms.			135°
M.	' Sine.	Cosecant.	Tangent.	Cotangent.	Secant.	Cosine.	M.
0	9.84177	10.15823	9.98484	10.01516	10.14307	9.85693	60
1	84190	15810	98509	01491	14319	85681	59
2	84203	15797	98534	01466	14331	85669	58
$ \begin{array}{c} 2 \\ 3 \\ 4 \\ 5 \end{array} $	84216	15784	98560	01440	14343	85657	57
4	84229	15771	98585	01415	14355	85645	56
0	9.84242 84255	10.15758	9.98610	10.01390	10.14368	9.85632	55 54
67	84269	$15745 \\ 15731$	98635 98661	01365 01339	$ \begin{array}{c} 14380 \\ 14392 \end{array} $	85620 85608	53
8	84282	15718	98686	01339	14404	85596	52
9	84295	15705	98711	01289	14417	85583	51
10	9.84308	10.15692	9.98737	10.01263	10.14429	9.85571	50
11	84321	15679	98762	01238	14441	85559	49
12	84334	15666	98787	01238 01213	14453	85547	48
13	84347	15653	98812	01188	14466	85534	47
14	84360	15640	98838	01162	14478	85522	46
15	9.84373	10.15627	9.98863	10.01137	10.14490	9.85510	45
16	84385	15615	98888	01112	14503	85497	44
17	84398	15602	98913	01087 01061	14515	85485	43
18	$84411 \\ 84424$	15589 15576	98939	01061	14527	85473	42
19 20	9.84437	10.15563	98964 9.98989	01036 10.01011	$14540 \\ 10.14552$	85460 9.85448	40
$\frac{20}{21}$	84450	15550	99015	00985	14564	85436	39
$\frac{21}{22}$	84463	15537	99040	00980	14577	85423	38
23	84476	15524	99065	00935	14589	85411	37
24	84489	15511	99090	00910	14601	85399	36
25	9.84502	10.15498	9.99116	10.00884	10,14614	9.85386	35
26 27	84515	15485	99141	00859	14626	85374	34
27	84528	15472	99166	00834	14639	85361	- 33
28	84540	15460	99191	00809	14651	85349	32
29	84553	15447	99217	00783	14663	85337	31
30	9.84566	10.15434	9.99242	10.00758	10.14676	9.85324	30
$\frac{31}{32}$	84579 84592	15421 15408	99267 99293	00733	14688 14701	85312 85299	29 28
33	84605	15395	99318	00707 00682	14701	85287	27
34	84618	15382	99343	00657	14726	85274	26
35	9.84630	10.15370	9.99368	10.00632	10.14738	9.85262	25
36	84643	15357	99394	00606	14750	85250	24
37	84656	15344	99419	00581	14763	85237	23
38	84669	15331	99444	00556	14775	85225	22
39	84682	15318	99469	00531	14788	85212	21
40	9.84694	10.15306	9.99495	10.00505	10.14800	9.85200	20
41	84707	$15293 \\ 15280$	99520	00480	14813	85187	19
42	84720	15280	99545	00455	14825	85175	18
43	84733	$15267 \\ 15255$	99570	00430	14838	85162	17
44 45	84745	10,15242	99596 9,99621	00404	14850	85150 9.85137	-16
40	9.84758 84771	15229	99646	10.00379 00354	$10.14863 \\ 14875$	85125	15
47	84784	15216	99672	00328	14888	85112	13
48	84796	15204	99697	00303	14900	85100	12
49	84809	15191	99722	00278	14913	85087	11
50	9.84822	10.15178	9.99747	10.00253	10.14926	9.85074	10
51	84835	15165	99773	00227	14938	85062	9
52	84847	15153	99798	00202	14951	85049	8 7 6
53	84860	$15140 \\ 15127$	99823	00177 00152	14963	85037	7
54	84873	15127	99848	00152	14976	85024	6
55	9.84885	10.15115	9.99874	10.00126	10.14988	9.85012	5
56	84898	15102	99899	00101	15001	84999	4
57	84911	15089	99924	00076	15014	84986	3
58 59	84923	$15077 \\ 15064$	99949	00051	15026 15039	84974	2
59 60	84936 84949	15054	99975 10.00000	00025	15039	84961 84949	0
00	01717				10031	01919	
M.	Cosine.	Secant.	Cotangent,	Tangent.	Cosecant.	Sine.	M.

22
0

Natural Trigonometrical Functions.

179°

	10		Na	tural I	rigonom	etrical	Punctio	ns.	1	79°
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	đ.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0	.00000	1.0000	Infinite.	.00000	Infinite.	1.0000	.00000	1.0000	60
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1									59
	2	. 0058		1718.9	. 0058	1718.9	.0000	. 0000		58
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$ 5 .00436 .99564 .229.18 .00436 .229.18 .1.0000 .00001 .9999 44 \\ 6 .0465 .9534 .0465 .14.86 .0000 .0001 .9999 44 \\ 7 .0194 .9505 .02.22 .0194 .02.22 .0000 .0001 .9999 44 \\ 7 .0194 .9505 .02.22 .0194 .02.22 .0000 .0001 .9999 43 \\ 7 .0524 .94176 .0099 .0524 .190.88 .0000 .0001 .9998 41 \\ 0 .00582 .99418 .171.89 .00582 .171.88 .0000 .00002 .9998 40 \\ 1 .00582 .99418 .171.89 .00582 .171.88 .0000 .0002 .9998 39 \\ 2 .0640 .9360 .56.26 .0640 .56.26 .0000 .0002 .9998 33 \\ .0669 .9331 .49.47 .0669 .49.46 .0000 .0002 .9998 33 \\ .0668 .9302 .43.24 .0698 .43.24 .0000 .0002 .9998 37 \\ .0698 .9302 .43.24 .0698 .43.24 .0000 .0003 .9997 33 \\ .0775 .9215 .27.32 .0756 .22.22 .0000 .0003 .9997 33 \\ .0755 .9215 .27.32 .0756 .22.27 .0000 .0003 .9997 33 \\ .0755 .9215 .27.32 .0785 .27.32 .0000 .0003 .9997 33 \\ .0087 .9917 .11.59 .00073 .14.59 .0000 .00004 .9996 30 \\ .00073 .9917 .21 .553 .014 .22.77 .0000 .0003 .9997 .32 \\ .0960 .9043 .0114 .083 .0000 .00004 .9996 .33 \\ .0960 .9044 .0174 .0000 .00004 .9996 .23 \\ .0960 .9044 .0171 .0000 .00005 .9995 .25 \\ .01018 .9968 .01.41 .0889 .0111 .0000 .00005 .9995 .25 \\ .01018 .99842 .2.944 .1076 .2.908 .0000 .0006 .9994 .24 \\ .105 .8865 .85.494 .1105 .0463 .0001 .0007 .99995 .25 \\ .1134 .8865 .85.494 .1104 .85.44 .0001 .0007 .99995 .25 \\ .01018 .98845 .3.494 .1134 .85.43 .0001 .0007 .99995 .25 \\ .1133 .88662 .85.494 .1074 .2.998 .00$	3						.0000			
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$0 \ . \ 1745 \ . \ 8255 \ \ 7.299 \ . \ 1745 \ \ 7.290 \ \ .0001 \ \ . \ 0015 \ \ . \ 9985 \ \ 0$	ğ									
I. Cosine, Vrs. sin. Secant. Cotang. Tang. Cosec'nt Vrs. cos. Sine. M.			8255	7.299		7.290				
	Ī.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

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Natural Trigonometrical Functions.

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1.		INA	curar cr	igonom	cuitai i	unction	13.		
M.	Sice.	Vrs. cos.	Cosec'at	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	М.
0	.01745	.98255	57.299	.01745	57.290	1.0001	.00015	.99985	60
ĭ	. 1774	. 8226	6.359	. 1775	6.350	.0001	. 0016	. 9984	59
2	. 1803	. 8196	5.450	. 1804	5.441	.0001	. 0016	. 9984	58
$\frac{2}{3}$. 1832	. 8167	4.570	. 1833	4.561	.0002	. 0017	. 9983	57
4	. 1861	. 8138	3.718	. 1862	3.708	.0002	. 0017	. 9983	56
4 5 6 7	.01891	.98109	52.891	.01891	52.882	1.0002	.00018	.99982	55
6	. 1920	. 8080	2.090	. 1920	2.081	.0002	. 0018	. 9981	54
7	. 1949	. 8051	1.313	. 1949	1.303	.0002	. 0019	. 9981	53
8	. 1978	. 8022	0.558	. 1978	0.548	.0002	. 0019	. 9980	52
9	2007	. 7993	49.826	. 2007	49.816	.0002	. 0020	. 9980	51
10	.02036	.97964	49.114	.02036	49.104	1.0002	.00021	.99979	50
11	. 2065	. 7935	8.422	. 2066	8.412	.0002	. 0021	. 9979	49
12	. 2094	. 7906	.7.750	. 2095	7.739	.0002	. 0022	. 9978	48
13	. 2123	. 7877	7.096	. 2124	7.085	.0002	. 0022	. 9977	47
14	. 2152	. 7847	6.460	. 2153	6.449	.0002	. 0023	. 9977	46
15	.02181	.97818	45.840	.02182	45.829	1.0002	.00024	.99976	45
16 17	. 2210	. 7789	5.237 4.650	2211 2240	5.226	.0002 .0002	0024	. 9975	43
18	. 2240	. 7760	4.030	2269	4.638 4.066	.0002	. 0025	.9975 .9974	42
19	2205	7702	3.520	2203	3.508	.0002	0026	9974	41
20	.02327	.97673	42.976	.02327	42,964	1.0003	00027	.99973	40
21	. 2356	. 7644	2,445	. 2357	2,433	.0003	0028	9972	39
22	2385	. 7615	1.928	2386	1,916	.0003	0028	9971	38
23	. 2414	. 7586	1.423	. 2415	1.410	.0003	0029	. 9971	37
$\bar{24}$. 2443	. 7557	0.930	. 2444	0.917	.0003	. 0030	9970	36
25	.02472	.97528	40.448	.02473	40,436	1.0003	.00030	99969	35
26	. 2501	. 7499	39.978	. 2502	39.965	.0003	. 0031	. 9969	34
27	. 2530	. 7469	9.518	. 2531	9.506	.0003	0032	. 9968	33
28	. 2559	. 7440	9.069	. 2560	9.057	.0003	. 0033	. 9967	32
29	. 2589	. 7411	8.631	. 2589	8.618	.0003	. 0033	. 9966	31
30	.02618	.97382	38.201	.02618	38.188	1.0003	.00034	.99966	30
31	. 2647	. 7353	7.782	. 2648	7.769	.0003	. 0035	. 9965	29
$\frac{32}{33}$. 2676	. 7324	7.371	. 2677	7.358	.0003	0036	. 9964	28
аа 34	2705 2734	. 7295	6.969	2706 2735	$6.956 \\ 6.563$.0004	0036	. 9963 9963	27 26
35	.02763	.97237	6.576 36.191	.02764	36.177	1.0004	.00038	.99962	25
36	. 2792	. 7208	5.814	2793	5.800	.0004	. 0039	. 9961	24
37	. 2821	7179	5.445	2822	5.431	.0004	0040	9960	23
38	2850	7150	5.084	2851	5.069	.0004	0041	. 9959	22
39	. 2879	. 7121	4.729	2880	4.715	.0004	. 0041	. 9958	21
40	.02908	.97091	34.382	.02910	34.368	1.0004	.00042	.99958	20
41	. 2937	. 7062	4.042	. 2939	4.027	.0004	. 0043	. 9957	19
42	. 2967	. 7033	3.708	. 2968	3.693	.0004	. 0044	. 9956	18
43	. 2996	. 7004	3.381	. 2997	3.366	.0004	0045	. 9955	17
44	. 3025	. 6975	3.060	. 3026	3.045	.0004	. 0046	. 9954	16
45	.03054	.96946	32.745	.03055	32.730	1.0005	.00046	.99953	15
46	. 3083	. 6917	2.437	. 3084	2.421	.0005	. 0047	. 9952	14
47	. 3112	. 6888	2.134	. 3113	2.118	.0005	. 0048	. 9951	13
48	. 3141	. 6859	1.836	. 3143	1.820	.0005	. 0049	. 9951	12
49 50	. 3170 .03199	. 6830 .96801	1.544 31.257	.3172 .03201	1.528 31.241	1.0005 1.0005	. 0050	. 9950 .99949	11 10
51	. 3228	. 6772	0.976	. 3230	0.960	.0005	. 0052	. 9948	9
52	. 3257	. 6743	0.699	. 3259	0.683	.0005	. 0053	. 9947	8
53	. 3286	. 6713	0.428	. 3288	0.085	.0005	. 0054	. 9946	2
54	3315	6684	0.161	3317	0.145	.0005	. 0055	. 9945	6
55	.03344	.96655	29.899	.03346	29.882	1.0005	.00056	.99944	5
56	. 3374	. 6626	9.641	. 3375	9.624	.0006	. 0057	9943	4
57	. 3403	. 6597	9.388	. 3405	9.371	.0006	. 0058	. 9942	3
58	. 3432	. 6568	9.139	. 3434	9.122	.0006	. 0059	. 9941	2
59	. 3461	. 6539	8.894	. 3463	8.877	.0006	. 0060	. 9940	1
60	. 3490	. 6510	8.654	. 3492	8.636	.0006	. 0061	. 9939	0
M.	Cosine.	Vrs. sia.	Secaat.	Cotang.	Taog.	Cosec'nt	Vrs. cos.	Sine.	М.

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Natural Trigonometrical Functions.

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20		Na	tural Ti	rigonom	etricai	Function	ns.	1	770
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.03490	,96510	28.654	.03492	28.636	1.0006	.00061	.99939	60
1	. 3519	. 6481	8.417	. 3521	8.399	.0006	. 0062	. 9938	59
2	. 3548	. 6452	8.184	. 3550	8.166	.0006	. 0063	. 9937	58
3	. 3577	. 6423	7.955	. 3579	7.937	.0006	. 0064	. 9936	57
4	. 3606	. 6394	7.730	. 3608	7.712	.0006	. 0065	.9935 .99934	56 55
$\frac{5}{6}$.03635 . 3664	.96365 .6336	27.508	.03638	27.490	.0007	. 00000	. 9933	54
7	. 3693	. 6306	7.075	3696	7.056	.0007	. 0068	9932	53
8	3722	6277	6.864	3725	6.845	.0007	. 0069	. 9931	52
9	. 3751	. 6248	6.655	. 3754	6.637	.0007	. 0070	. 9930	51
10	.03781	.96219	26.450	.03783	26.432	1.0007	.00071	.99928	50
11	. 3810	. 6190	6.249	. 3812	6.230	.0007	. 0073	. 9927	49
12 13	. 3839	. 6161	6.050	. 3842	6.031	.0007	. 0074 . 0075	. 9926 . 9925	48
14	. 3868 . 3897	.6132 .6103	5.854 5.661	. 3871 . 3900	$5.835 \\ 5.642$.0007	. 0076	. 9923	46
15	.03926	.96074	25.471	.03929	25.452	1,0008	.00077	.99923	45
16	. 3955	. 6045	5.284	. 3958	5.264	.0008	. 0078	. 9922	44
17	. 3984	. 6016	5.100	, 3987	5.080	.0008	. 0079	. 9921	43
18	. 4013	. 5987	4.918	. 4016	4.898	.0008	. 0080	. 9919	42
19	. 4042	. 5958	4.739	. 4045	4.718	.0008	. 0082	. 9918	41
20 21	.04071	.95929	24.562	.04075	24.542	1.0008	.00083	.99917 .9916	40 39
22	. 4100 . 4129	. 5900 . 5870	$4.388 \\ 4.216$	$\begin{array}{c} . 4104 \\ . 4133 \end{array}$	4.367	.0008	. 0085	. 9915	38
23	. 4158	. 5841	4.047	. 4162	4.026	.0009	. 0086	. 9913	37
24	4187	5812	3.880	4191	3.859	.0009	. 0088	. 9912	36
25	.04217	.95783	23.716	.04220	23.694	1.0009	.00089	.99911	35
26	. 4246	. 5754	3.553	. 4249	3.532	.0009	. 0090	. 9910	34
27 28	. 4275	. 5725	3.393	. 4279	3.372	.0009	. 0091	. 9908	33
$\frac{28}{29}$. 4304	. 5696	3.235	4308	3.214	.0009	. 0093 . 0094	. 9907	32 3 1
29 30	. 4333	. 5667 .95638	3.079 22.925	. 4337 .04366	$3.058 \\ 22.904$	1.0009	.00094	. 9906 .99905	30
31	. 4391	. 5609	2,774	. 4395	2.752	.0010	. 0096	. 9903	29
32	. 4420	. 5580	2.624	. 4424	2,602	.0010	. 0098	9902	28
33	. 4449	. 5551	2.476	. 4453	2.454	.0010	. 0099	. 9901	27
34	. 4478	. 5522	2.330	. 4483	2.608	.0010	. 0100	. 9900	26
35	.04507	.95493	22.186	.04512	22.164	1.0010	.00102	.99898	25
$\frac{36}{37}$. 4536 . 4565	. 5464 . 5435	2.044	. 4541 . 4570	$2.022 \\ 1.881$.0010	.0103 .0104	. 9897 . 9896	24 23
38	. 4594	. 5405	1.765	. 4599	1.742	.0010	0104	. 9894	22
39	4623	5376	1.629	4628	1.606	.0011	0107	. 9893	21
40	.04652	.95347	21.494	.04657	21.470	1.0011	.00108	.99892	20
41 ·	. 4681	. 5318	1.360	. 4687	1.337	.0011	. 0110	. 9890	19
42	. 4711	5289	1.228	. 4716	1.205	.0011	. 0111	. 9889	18
43	. 4740	5260 5231	1.098	. 4745	1.075	.0011	. 0112	. 9888	17
44 45	.4769 .04798	.95202	$ \begin{array}{c} 0.970 \\ 20.843 \end{array} $. 4774	$0.946 \\ 20.819$.0011 1.0011	0.0114 0.00115	. 9886 .99885	16 15
46	4827	5173	0.717	. 4832	0,693	.0012	. 0116	. 9883	14
47	4856	. 5144	0.593	. 4862	0,569	.0012	. 0118	. 9882	13
48	. 4885	. 5115	0.471	. 4891	0.446	.0012	. 0119	9881	12
49	. 4914	. 5086	0.350	. 4920	0.325	.0012	. 0121	. 9879	11
50	.04943	.95057	20.230	.04949	20.205	1.0012	.00122	.99878	10
$\frac{51}{52}$. 4972 . 5001	. 5028 . 4999	0.112 19,995	. 4978	0.087	.0012 .0012	.0124 .0125	. 9876 . 9875	9
53	5030	4970	9.880	. 5037	19.970 9.854	.0012	0123	. 9873	8
54	. 5059	4941	9.766	5066	9.740	.0013	. 0128	. 9872	6
55	.05088	.94912	19.653	.05095	19.627	1.0013	.00129	.99870	5
56	. 5117	. 4883	9.541	. 5124	9.515	.0013	. 0131	. 9869	4
57	. 5146	. 4853	9.431	. 5153	9.405	.0013	. 0132	. 9867	3
58	. 5175	. 4824	9.322	. 5182	9,296	.0013	. 0134	. 9866	2
59 60	.5204 .5234	. 4795 . 4766	9.214 9.107	5212 5241	9,188 9,081	.0013 .0014	. 0135	. 9864 . 9863	$\begin{vmatrix} 1\\0 \end{vmatrix}$
-									_
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

92°

Natural Trigonometrical Functions.

176°

			.,					125
Sine.	Vrs. cos.	Cosec'ot	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	<u>M.</u>
.05234	.94766	19.107	.05241	19.081	1.0014	.00137	.99863	60
. 5263	. 4737	9.002	. 5270	8.975	.0014	. 0138	. 9861	59
. 5292 . 5321	. 4708	8.897 8.794	. 5299 . 5328	8.871	.0014 .0014	. 0140	. 9860 . 9858	58 57
5350	. 4650	8.692	. 5357	8.665	.0014	. 0142	. 9857	56
.05379	.94621	18.591	.05387	18.564	1.0014	.00145	.99855	55
. 5408	. 4592	8.491	. 5416	8.464	.0015	. 0146	. 9854	54
. 5437	. 4563	8.393	. 5445	8.365	.0015	. 0148	. 9852	53
. 5466	. 4534	8.295	. 5474	8.268	.0015	. 0149	. 9850	52
. 5495	. 4505	8.198	. 5503	8.171	.0015	. 0151	. 9849	51
.05524	.94476	18.103	.05532	18.075	1.0015	.00153	.99847	50
. 5553	• 4447	8.008	. 5562	7.980	.0015	. 0154	. 9846	49
. 5582 . 5611	. 4418 . 4389	7.914 7.821	. 5591 . 5620	7.886	.0016 .0016	. 0156	. 9844 . 9842	48
. 5640	. 4360	7.730	. 5649	7.701	.0016	. 0159	. 9841	46
.05669	.94331	17.639	.05678	17.610	1.0016	.00161	.99839	45
. 5698	. 4302	7.549	. 5707	7.520	.0016	. 0162	. 9837	44
. 5727	. 4273	7.460	. 5737	7.431	.0016	. 0164	. 9836	43
. 5756	. 4244	7.372	. 5766	7.343	.0017	. 0166	. 9834	42
. 5785	. 4214	7.285	. 5795	7.256	.0017	. 0167	. 9832	41
.05814	.94185	17.198	.05824	17.169	1.0017	.00169	.99831	40
. 5843	. 4156	7.113	. 5853	7.084	.0017	. 0171	. 9829 . 9827	39 38
5872 5902	. 4127	7.028 6.944	. 5883 . 5912	6.999 6.915	.0017	. 0172	. 9826	37
. 5902 . 5931	. 4098	6.861	. 5912	6.832	.0018	. 0176	9824	36
.05960	.94040	16.779	.05970	16.750	1.0018	.00178	.99822	35
. 5989	. 4011	6.698	. 5999	6.668	.0018	. 0179	. 9820	34
. 6018	. 3982	6.617	. 6029	6.587	.0018	. 0181	. 9819	- 33
. 6047	. 3953	6.538	. 6058	6.507	.0018	. 0183	. 9817	32
. 6076	. 3924	6.459	. 6087	6.428	.0018	. 0185	. 9815	31
.06105	.93895	16.380	.06116	16.350	1.0019	.00186	.99813	30
. 6134	. 3866	6.303 6.226	. 6145	6.272 6.195	.0019	. 0188	. 9812 . 9810	29 28
. 6163 . 6192	. 3837 . 3808	6.150	. 6175 . 6204	6.119	.0019 .0019	. 0190	. 9808	27
. 6221	. 3777	6.075	. 6233	6.043	.0019	. 0194	9806	26
.06250	.93750	16.000	.06262	15.969	1.0019	.00195	.99804	25
. 6279	. 3721	5.926	. 6291	5.894	.0020	. 0197	. 9803	24
. 6308	. 3692	5.853	. 6321	5.821	.0020	. 0199	. 9801	23
. 6337	. 3663	5.780	6350	5.748	.0020	. 0201	. 9799	22
. 6366	. 3634	5.708	. 6379	5.676	.0020	. 0203	. 9797	21
.06395	.93605	15.637	.06408	15.605	1.0020	.00205	.99795	20
. 6424	. 3576	5,566 5,496	. 6437 . 6467	5.534 5.464	.0021 .0021	. 0206	. 9793 . 9791	19 18
.6453 .6482	. 3547 . 3518	5.490	. 6496	5.394	.0021	. 0210	. 9790	17
. 6511	3489	5.358	. 6525	5.325	.0021	0212	9788	16
.06540	.93460	15.290	.06554	15,257	1.0021	.00214	.99786	15
. 6569	. 3431	5.222	. 6583	5,189	.0022	. 0216	. 9784	14
. 6598	. 3402	5.155	. 6613	5.122	.0022	. 0218	. 9782	13
. 6627	. 3373	5.089	. 6642	5.056	.0022	. 0220	. 9780	12
. 6656	. 3343	5.023	. 6671	4.990	.0022	. 0222	. 9778	11
.06685	.93314	14.958	.06700	14.924 4.860	1.0022	.00224	.99776 . 9774	10 9
. 6714	. 3285 . 3256	4.893 4.829	. 6730 . 6759	4.800	.0023	. 0228	. 9772	
.6743 .6772	. 3230	4.829	6788	4.732	.0023	. 0228	. 9770	87
. 6801	3198	4.702	6817	4.668	.0023	0231	9768	6
.06830	.93169	14.640	.06846	14,606	1.0023	.00233	.99766	5
. 6859	3140	4.578	. 6876	4.544	.0024	. 0235	. 9764	4
6888	. 3111	4.517	. 6905	4.482	.0024	. 0237	. 9762	3
. 6918	. 3082	4.456	. 6934	4.421	.0024	. 0239	. 9760	2
. 6947	. 3053	4.395	. 6963	4.361	.0024	. 0241	. 9758	1
. 6976	. 3024	4.335	. 6993	4.301	.0024	. 0243	9756	0
Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'at	Vrs. cos.	Sine.	<u> </u>
Josine.	, . to, ord.	Secane.	Jonnug.					1

Natural Trigonometrical Functions.

4 °		Na	tural Tr	igonom	etrical l	unction	15.	13	75°
M.	Sine,	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	<u>M.</u>
0	.06976	.93024	14.335	.06993	14.301	1.0024	.00243	99756	60
1	. 7005	. 2995	4.276	. 7022	4.241	.0025	. 0246	. 9754	59
2	. 7034	. 2966	4.217	. 7051	4.182 4.123	.0025	. 0248 . 0250	. 9752 . 9750	58 57
3 4	.7063 .7092	.2937 .2908	4.159 4.101	. 7080	4.123	.0025	. 0252	. 9748	56
5	.07121	. 2308	14.043	.07139	14.008	1.0025	.00254	.99746	55
6	. 7150	2850	3.986	. 7168	3.951	.0026	. 0256	. 9744	54
7	. 7179	. 2821	3.930	7197	3.894	.0026	. 0258	. 9742	53
8	. 7208	. 2792	3.874	. 7226	3.838	.0026	. 0260	. 9740	52
9	. 7237	. 2763	3.818	. 7256	3.782	.0026	. 0262	. 9738	51
10	.07266 . 7295	.92734	13.763	.07285 .7314	$13.727 \\ 3.672$	1.0026 .0027	.00264	.99736 .9733	50°
11 12	. 7324	· 2705 · 2676	$3.708 \\ 3.654$. 7343	3.617	.0027	. 0268	. 9731	48
13	7353	2647	3.600	7373	3.563	.0027	. 0271	. 9729	47
14	7382	. 2618	3.547	7402	3.510	.0027	. 0273	9727	46
15	.07411	.92589	13.494	.07431	13.457	1.0027	.00275	.99725	45
16	. 7440	. 2560	3.441	. 7460	3.404	.0028	. 0277	. 9723	44
17	. 7469	. 2531	3.389	. 7490	3.351	.0028	. 0279	. 9721	43
18	. 7498	. 2502	3.337	. 7519 . 7548	3.299 3.248	.0028 .0028	. 0281	• 9718 • 9716	42
19 20	. 7527 .07556	. 2473 .92444	$3.286 \\ 13.235$.07577	13.197	1,0028	.0284	.99714	40
21	. 7585	. 2415	3.184	7607	3.146	.0029	. 0288	. 9712	39
22	. 7614	2386	3.134	7636	3.096	.0029	. 0290	. 9710	38
23	. 7643	. 2357	3.084	. 7665	3.046	.0029	. 0292	. 9707	37
24	7672	. 2328	3.034	. 7694	2.996	.0029	. 0295	. 9705	36
25	.07701	.92299	12.985	.07724	12.947	1.0030	.00297	.99703	35
26	7730	. 2270	2.937	. 7753	2.898 2.849	.0030	. 0299 . 0301	. 9701	34
$\frac{27}{28}$. 7759 . 7788	2231	2.888	.7782 .7812	2.849	.0030	. 0301	. 9698 . 9696	33
29	7817	2183	2.793	. 7841	2.754	.0031	. 0306	. 9694	31
30	.07846	.92154	12,745	.07870	12.706	1,0031	.00308	.99692	30
31	. 7875	. 2125	2.698	. 7899	2.659	.0031	. 0310	. 9689	29
32	. 7904	. 2096	2.652	. 7929	2.612	.0031	. 0313	. 9687	28 27
33	. 7933	. 2067 . 2038	$2.606 \\ 2.560$. 7958	$2.566 \\ 2.520$.0032	. 0315	. 9685	
$\frac{34}{35}$. 7962	. 2038	12.514	. 7987	12.320	1.0032	.00320	. 9682 .99680	26 25
36	. 8020	. 1980	2.469	. 8046	2.429	.0032	. 0322	. 9678	24
37	. 8049	. 1951	2.424	. 8075	2.384	.0032	. 0324	. 9675	23
38	. 8078	. 1922	2.379	. 8104	2.339	.0033	. 0327	. 9673	22
39	. 8107	. 1893	2.335	. 8134	2.295	.0033	. 0329	. 9671	21
40	.08136	.91864	12.291	.08163	12.250	1.0033	.00331	.99668	20
4 1 42	. 8165 . 8194	. 1835 . 1806	$2.248 \\ 2.204$. 8192 . 8221	2.207 2.163	.0033	. 0334	. 9666 . 9664	19
43	. 8223	1777	2.161	8251	2.103	.0034	. 0339	. 9661	17
44	. 8252	1748	2.118	. 8280	2.077	.0034	. 0341	. 9659	16
45	.08281	.91719	12.076	.08309	12.035	1.0034	.00343	.99656	15
46	. 8310	. 1690	2.034	. 8339	1.992	.0035	. 0346	. 9654	14
47	. 8339	. 1661	1.992	. 8368	1.950	.0035	. 0348	. 9652	13
48	. 8368	. 1632	1.950	. 8397 . 8426	1.909 1.867	.0035	. 0351	. 9649	12
$\frac{49}{50}$. 8397	.91574	11.868	.08456	11.826	1.0036	.00356	. 9647	11 10
51	. 8455	1545	1.828	. 8485	1.785	.0036	. 0358	. 9642	9
52	. 8484	. 1516	1.787	. 8514	1.745	.0036	. 0360	. 9639	8
53	. 8513	. 1487	1.747	. 8544	1.704	.0036	. 0363	. 9637	87
54	. 8542	1458	1.707	. 8573	1.664	.0037	. 0365	. 9634	6 5
55	.08571	.91429	11.668	.08602	11.625	1.0037	.00368	.99632	5
56 57	. 8600 . 8629	. 1400 1371	1.628	. 8632 . 8661	1.585 1.546	.0037 .0037	. 0370	. 9629 . 9627	4
$\frac{57}{58}$. 8658	1342	1.550	. 8690	1.507	.0038	. 0375	. 9624	32
59	. 8687	. 1313	1.512	. 8719	1.468	.0038	. 0378	9622	ĩ
60	. 8715	. 1284	1 474	. 8719	1.430	.0038	. 0380	9619	Ô
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

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NATURAL FUNCTIONS.

5°		Na	tural Tr	igonom	etrical I	unction	is.	į :	74°
М.	Sive.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	М.
0	.08715	.91284	11.474	.08749	11.430	1.0038	.00380	.99619	60
1	. 8744	. 1255	1.436	. 8778	1.392	.0038	. 0383	. 9617	59
$\frac{2}{3}$. 8773	, 1226	1.398	. 8807 . 8837	1.354	.0039	. 0386	. 9614	58
4	. 8802 . 8831	. 1197 . 1168	1.360 1.323	. 8866	1.316 1.279	.0039	. 0391	. 9612	57 56
3	.08860	.91139	11.286	.08895	11.242	1.0039	.00393	.99607	55
6	. 8889	. 1110	1.249	. 8925	1.205	.0040	. 0396	. 9604	54
7	. 8918	. 1082	1.213	. 8954	1.168	.0040	. 0398	. 9601	53
8	. 8947	. 1053	1.176	8983	1.132	.0040	. 0401	. 9599	52
.9	. 8976	. 1024	1.140 11.104	. 9013	1.095	.0040	. 0404	. 9596	51
10 11	.09005	.90995 .0966	1.069	. 9071	11.059 1.024	.0041	. 0409	99594	50
12	. 9063	. 0937	1.033	. 9101	0.988	.0041	. 0411	9588	48
13	. 9092	. 0908	0.998	. 9130	0.953	.0041	. 0414	9586	47
14	. 9121	. 0879	0.963	. 9159	0.918	.0042	. 0417	. 9583	46
15	.09150	.90850	10.929	.09189	10.883	1.0042	.00419	.99580	45
16	. 9179	. 0821	0.894	. 9218	0.848	.0042	. 0422	. 9578	44
17 18	. 9208 . 9237	0792	0.860	· 9247 · 9277	0.814 0.780	.0043	. 0425	. 9575 . 9572	43
19	. 9266	. 0734	0.792	. 9306	0.746	.0043	. 0430	. 9570	41
20	.09295	.90705	10.758	.09335	10.712	1.0043	.00433	.99567	40
21	. 9324	. 0676	0.725	. 9365	0.678	.0044	. 0436	. 9564	39
22	. 9353	. 0647	0.692	. 9394	0.645	.0044	. 0438	. 9562	38
23	. 9382	. 0618	0.659	. 9423	0.612	.0044	. 0441	. 9559	37
$\frac{24}{25}$. 9411	. 0589	0.626	. 9453 .09482	0.579	.0044 1.0045	. 0444	9556 99553	36 35
25 26	. 9469	.90560	0.561	. 9511	0.514	.0045	. 0449	.99551	34
27^{20}	. 9498	. 0502	0.529	. 9541	0.481	.0045	0452	. 9548	33
$\bar{28}$. 9527	. 0473	0.497	. 9570	0.449	.0046	. 0455	. 9545	32
29	. 9556	. 0444	0.465	. 9599	0.417	.0046	. 0458	. 9542	31
30	.09584	.90415	10.433	.09629	10.385	1.0046	.00460	.99540	30
31	. 9613	. 0386	0.402	9658 9688	0.354 0.322	.0046	. 0463	. 9537	29 28
$\frac{32}{33}$. 9642 . 9671	. 0357	0.371	. 9717	0.322	.0047	. 0469	. 9531	27
34	9700	0300	0.309	9746	0.260	.0047	. 0472	9528	26
35	.09729	.90271	10.278	.09776	10.229	1.0048	.00474	.99525	25
36	. 9758	. 0242	0.248	. 9805	0.199	.0048	. 0477	. 9523	24
37	. 9787	. 0213	0.217	. 9834	0.168	.0048	. 0480	. 9520	23
38	. 9816	. 0184	0.187	. 9864 . 9893	0.138	.0048	. 0483	9517 9514	22 21
39 40	. 9845	. 0155 .90126	0.157	.09922	10.078	1.0049	.00489	.99511	20
41	. 9903	. 0097	0.098	. 9952	0.048	.0049	. 0491	. 9508	19
$\hat{42}$. 9932	. 0068	0.068	. 9981	0.019	.0050	. 0494	. 9505	18
43	. 9961	. 0039	0.039	.10011	9.9893	.0050	. 0497	9503	17
44	. 9990	. 0010	0.010	. 0040	.9601	.0050	. 0500	. 9500	16
$\frac{45}{46}$. 10019	.89981 .9952	9.9812	. 10069	9.9310	1.0050 .0051	.00503	.99497	15 14
40	. 0048	. 9932	.9239	. 0128	.8734	.0051	. 0509	. 9491	13
48	0106	. 9894	.8955	. 0158	.8448	.0051	. 0512	. 9188	12
49	. 0134	. 9865	.8672	. 0187	.8164	.0052	. 0515	. 9485	11
50	.10163	.89836	9.8391	.10216	9.7882	1.0052	.00518	.99482	10
51	. 0192	. 9807		. 0246	.7601	.0052	. 0521	. 9479	9
52	0221	9779 9750	.7834	. 0275	.7322	.0053	. 0524	9476	87
$\frac{53}{54}$. 0279	. 9721	.7283	. 0334	.6768	.0053	. 0530	. 9470	6
55	.10308	.89692	9.7010	.10363	9.6493	1.0053	.00533	.99467	5
56	. 0337	. 9663	.6739	. 0393	.6220	.0054	. 0536	. 9464	4
57	. 0366	. 9634	.6469	. 0422	.5949	.0054	. 0539	. 9461	$\frac{3}{2}$
58	. 0395	. 9605	.6200	. 0452	.5679	.0054	. 0542	. 9458	
59	. 0424	. 9576	.5933	. 0481	.5411 .5144	.0055	. 0545	. 9455 . 9452	10
60	. 0453	. 9547	.5668		`	·			
М.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	100sec. ut	Vrs. cos.	1 0108.	M.

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Natural Trigonometrical Functions.

6°		Na	tural Tr	igonom	etrical	Function	ns.	1	73°
М.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
Ø	.10453	.89547	9.5668	.10510	9.5144	1.0055	.00548	.99452	60
1	. 0482	. 9518	.5404	. 0540	.4878	.0055	. 0551	. 9449	59
23	. 0511	• 9489	.5141	. 0569	.4614	.0056	. 0554	. 9446	58
3	. 0540	. 9460 . 9431	.4880	. 0599	.4351	.0056 .0056	. 0557	. 9443 . 9440	57
4 5	.10597	.89402	9.4362	.10657	9.3831	1.0057	.00563	.99437	55
6	. 0626	. 9373	.4105	. 0687	.3572	.0057	. 0566	. 9434	54
7	. 0655	. 9345	.3850	. 0716	.3315	.0057	. 0569	. 9431	53
8	. 0684	. 9316	.3596	. 0746	.3060	.0057	. 0572	. 9428	52
9	. 0713	. 9287	.3343	. 0775	.2806	.0058	. 0575	. 9424	51
$\frac{10}{11}$.10742	.89258 .9229	9.3092 .2842	.10805 .0834	9.2553	1.0058	.00579	.99421 .9418	50 49
12	. 0800	. 9200	.2593	. 0863	.2051	.0058	. 0585	. 9418	49
13	. 0829	. 9171	.2346	. 0893	.1803	.0059	. 0588	. 9412	47
14	. 0858	. 9142	.2100	. 0922	.1555	.0059	. 0591	9409	46
15	.10887	.89113	9.1855	.10952	9.1309	1.0060	.00594	.99406	45
16	. 0916	. 9084	.1612	. 0981	.1064	.0060	. 0597	. 9402	44
17	. 0944	. 9055	.1370	. 1011	.0821	.0060	. 0601	. 9399	43
18 19	. 0973	. 9026 . 8998	.1129	. 1040	.0579	.0061	. 0604	· 9396	42
20	.11031	.88969	.0890 9.0651	.11099	.0338 9.0098	.0061 1.0061	. 0607	. 9393 .99390	40
$\tilde{21}$, 1060	. 8940	.0414	1128	8.9860	.0062	. 0613	. 9386	39
$\overline{2}\overline{2}$	1089	. 8911	.0179	. 1158	.9623	.0062	. 0617	9383	38
23	. 1118	. 8882	8.9944	. 1187	.9387	.0062	. 0620	. 9380	37
24	. 1147	. 8853	.9711	. 1217	.9152	.0063	. 0623	. 9377	36
25	.11176	.88824	8.9479	.11246	8.8918	1.0063	.00626	.99373	35
$\frac{26}{27}$. 1205 . 1234	. 8795 . 8766	.9248 .9018	.1276 .1305	.8686	.0063	. 0630	. 9370 . 9367	34 33
$\frac{2}{28}$	1262	. 8737	.8790	1335	.8435	.0064	. 0636	· 9364	32
29	1291	. 8708	.8563	1364	.7996	.0064	. 0639	. 9360	31
30	.11320	.88680	8.8337	.11393	8.7769	1.0065	.00643	.99357	30
31	. 1349	. 8651	.8112	. 1423	.7542	.0065	. 0646	. 9 354	29
32	. 1378	. 8622	.7888	. 1452	.7317	.0065	. 0649	. 9350	28
33 34	.1407 .1436	. 8593 . 8564	.7665	.1482 .1511	.7093	.0066	. 0653	. 9347	27
35	.11465	.88535	8.7223	.11541	8.6648	1.0066	. 0656	. 9344 .99341	$\frac{26}{25}$
36	. 1494	. 8506	.7004	. 1570	.6427	.0067	. 0663	. 9337	24
37	. 1523	. 8477	.6786	. 1600	.6208	.0067	. 0666	. 9334	23
38	. 1551	. 8448	.6569	. 1629	.5989	.0067	. 0669	, 9330	22
39	. 1580	. 8420	.6353	. 1659	.5772	.0068	. 0673	. 9327	21
40 41	.11609 . 1638	.88391 .8362	8.6138 .5924	.11688 .1718	8.5555	1.0068	.00676	.99324	20
42	1038	. 8333	.5711	. 1747	.5340	.0068	. 0679	. 9320 . 9317	19 18
43	1696	. 8304	5499	1777	.4913	.0069	. 0686	. 9314	17
44	. 1725	. 8272	.5289	. 1806	.4701	.0069	0690	. 9310	16
45	.11754	.88246	8.5079	.11836	8.4489	1.0070	.00693	.99307	$\overline{15}$
46	. 1783	. 8217	.4871	. 1865	.4279	.0070	. 0696	. 9303	14
47	. 1811	. 8188	.4663	. 1895	.4070	.0070	. 0700	. 9300	13
48 49	. 1840 . 1869	.8160 .8131	.4457 .4251	. 1924 . 1954	.3862 .3655	.0071	. 0703	. 9296	12
50	.11898	.88102	8.4046	.11983	8.3449	1.0071	. 0707	. 9293 .99290	11
51	. 1927	. 8073	.3843	2013	.3244	.0072	. 0714	. 9286	10 9
52	. 1956	. 8044	.3640	. 2042	.3040	.0072	. 0717	9283	8
53	. 1985	. 8015	.3439	. 2072	.2837	.0073	. 0721	9279	7
54	. 2014	. 7986	.3238	. 2101	.2635	.0073	. 0724	. 9276	6
55	.12042	.87957	8.3039	.12131	8.2434	1.0073	.00728	.99272	5
56 57	.2071 .2100	. 7928 . 7900	.2840 .2642	. 2160 . 2190	.2234	.0074	. 0731	. 9269	4
58	2129	. 7871	.2042	22190	.1837	.0074	. 0735 . 0738	9265 9262	$\frac{3}{2}$
59	. 2158	7842	.2250	2249	.1640	.0075	. 0742	. 9258	í
60	2187	. 7813	.2055	. 2278	.1443	.0075	. 0745	9255	ō
<u>M.</u>	Cosine,	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

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NATURAL FUNCTIONS.

7°		Natural Trigonometrical Functions. 172										
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	М,			
0	.12187	.87813	8.2055	.12278	8,1443	1.0075	.00745	.99255	60			
1	. 2216	. 7787	.1861	. 2308	.1248 .1053	.0075	. 0749	. 9251	59			
$\begin{bmatrix} \overline{2} \\ 3 \end{bmatrix}$. 2245	. 7755	.1668	. 2337	.1053	.0076	. 0752	. 9247	58 57			
3	2273 2302	. 7726 . 7697	.1476 .1285	. 2367 . 2396	.0860	.0076 .0076	. 0756	. 9244 . 9240	56			
4 5	12331	.87669	8.1094	.12426	8.0476	1.0077	.00763	.99237	55			
6	. 2360	. 7640	.0905	. 2456	.0285	.0077	. 0767	. 9233	54			
6 7	2389	. 7611	.0717	2485	.0095	.0078	. 0770	. 9229	53			
8	. 2418	. 7582	.0529	. 2515	7.9906	.0078	. 0774	. 9226	52			
9	. 2447	7553	.0342	. 2544	.9717	.0078	. 0778	. 9222	51			
10	.12476	.87524	8.0156	.12574	7.9530	1.0079	.00781	.99219	50			
11	. 2504	. 7495 . 7467	7.9971	. 2603	.9344	.0079	. 0785	. 9215	49			
$\frac{12}{13}$	2533 2562	. 7457	.9787 .9604	. 2633 . 2662	.9158 .8973	.0079	. 0788	. 9211 . 9208	48			
14	2591	. 7408	.9604	. 2692	.8789	.0080	. 0792	. 9208	46			
15	.12620	.87380	7.9240	12722	7.8606	1.0080	.00799	.99200	45			
16	, 2649	. 7351	.9059	. 2751	.8424	.0081	. 0803	. 9197	44			
17	. 2678	7322	.8879	. 2781	.8243	.0081	. 0807	. 9193	43			
18	. 2706	. 7293	.8700	. 2S10	.8062	.0082	. 0810	. 9189	42			
19	. 2735	. 7265	.8522	. 2840	.7882	.0082	. 0814	. 9186	41			
20	.12764	.87236	7.8344	.12869	7.7703	1.0082	.00818	.99182	40			
21 22	. 2793	. 7207	.8168	. 2899	.7525	.0083	. 0822	. 9178	39			
22	. 2822	. 7178	.7992	. 2928	.7348	.0083	. 0825	. 9174	38 37			
23	2851 2879	. 7149 7120	.7817	. 2958 . 2988	.7171	.0084 .0084	. 0829	. 9171	36			
25	.12908	.87091	7.7469	.13017	7.6821	1.0084	.00837	.99163	35			
26	. 2937	. 7063	.7296	. 3047	.6646	.0085	. 0840	. 9160	34			
27	. 2966	. 7034	.7124	. 3076	.6473	.0085	. 0844	. 9156	33			
28	. 2995	. 7005	.6953	. 3106	.6300	.0085	. 0848	. 9152	32			
29	. 3024	. 6976	.6783	3136	.6129	.0086	. 0852	. 9148	31			
30	.13053	.86947	7.6613	.13165	7.5957	1.0086	.00855	.99144	30			
31 32	. 3081	. 6918	.6444	. 3195	.5787	.0087	. 0859	. 9141	29			
33	. 3110 . 3139	. 6890 . 6861	.6276	. 3224 . 3254	.5617	.0087	. 0863	9137 9133	28 27			
34	. 3168	. 6832	.5942	3284	.5280	.0088	. 0867	9129	26			
35	.13197	.86803	7.5776	.13313	7.5113	1.0088	.00875	.99125	26 25			
36	. 3226	. 6774	.5611	. 3343	.4946	.0089	. 0878	. 9121	1 24			
37	. 3254	. 6745	.5446	. 3372	.4780	.0089	. 0882	. 9118	23 22 21			
38	. 3283	. 6717	.5282	. 3402	.4615	.0089	. 0886	. 9114	22			
39	3312	. 6688	.5119	. 3432	.4451	.0090	. 0890	. 9110	21			
40 41	.13341	.86659	7.4957	.13461	7.4287	1.0090	.00894	.99106	20			
42	3370	. 6630	.4795	. 3491 . 3520	.4124	.0090	. 0898	. 9102	19			
43	. 3427	6572	.4634	. 3550	.3961	.0091	. 0902	. 9098 . 9094	18			
44	. 3456	. 6544	.4315	. 3580	.3639	.0092	. 0909	. 9090	16			
45	.13485	.86515	7.4156	.13609	7.3479	1.0092	.00913	.99086	15			
46	. 3514	. 6486	.3998	. 3639	.3319	.0092	. 0917	. 9083	14			
47	. 3543	. 6457	.3840	. 3669	.3160	.0093	. 0921	. 9079	113			
48	. 3571	. 6428	.3683	. 3698	.3002	.0093	. 0925	. 9075	12			
49	. 3600	. 6400	.3527	. 3728	.2844	.0094	. 0929	. 9070	11			
50 51	. 3658	.86371	7.3372	.13757	7.2687	1.0094	.00933	.99067	10			
52	3687	. 6313	.3063	3817	.2375	.0095	0937	. 9063 . 9059	9			
-53	3716	6284	.2909	3846	.2220	.0095	. 0945	9055	87			
54 55	. 3744	6255	.2757	. 3876	.2066	.0096	. 0949	. 9055 . 9051	6			
55	.13773	.86227	7.2604	.13906	7.1912	1.0096	.00953	.99047	6 5 4			
56	. 3802	. 6198	.2453	. 3935	.1759	.0097	. 0957	. 9043	4			
57	. 3831	. 6169	.2302	. 3965	.1607	.0097	. 0961	. 9039	3			
58	. 3860	. 6140	.2152	. 3995	.1455	.0097	. 0965	. 9035	3 2 1			
59 60	. 3888	6111	.2002	4024	.1304	.0098	. 0969	. 9031	1			
	. 3917	. 6083	.1003	. 4054	.1154	.0098	. 0973	. 9027	0			
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.			
07	<u>.</u>			,				,	,			

Natural Trigonometrical Functions.

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0-		ina	tural II	rigonom	etrical	1.	/1-		
Μ.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.13917	.86083	7.1853	.14054	7.1154	1.0098	.00973	.99027	60
1	. 3946	. 6054	.1704	. 4084	.1004	.0099	. 0977	. 9023	59
$\frac{\bar{2}}{3}$. 3975	. 6025	.1557	. 4113	.0854	.0099	. 0981	. 9019	58
3	. 4004	. 5996	.1409	. 4143	.0706	.0099	. 0985	. 9015	57
4 5 6 7	. 4032	. 5967	.1263	4173	.0558	.0100	. 0989	. 9010	56
5	.14061	.85939	7.1117	.14202	7.0410	1.0100	.00993	.99006	55
6	. 4090	. 5910	.0972	. 4232	.0264	.0101	. 0998	. 9002	54
7	. 4119	. 5881	.0827	 4262 	.0117	.0101	. 1002	. 8998	53
8	. 4148	. 5852	.0683	. 4291	6.9972	.0102	. 1006	. 8994	52
.9	. 4176	. 5823	.0539	. 4321	.9827	.0102	. 1010	. 8990	51
10	.14205	.85795	7.0396	.14351	6.9682	1.0102	.01014	.98986	50
11	. 4234	. 5766	.0254	. 4380	.9538	.0103	. 1018	- 8982	49
12	 4263 	. 5737	.0112	. 4410	.9395	.0103	. 1022 . 1026	. 8978 . 8973	48
13	. 4292	. 5708	6.9971	. 4440	.9252	.0104	. 1020	. 8969	46
14	. 4320	. 5679	.9830	. 4470	.9110	.0104 1.0104	.01035	.98965	45
15	.14349 . 4378	.85651 . 5622	6.9690	.14499	6.8969 .8828	.0104	. 1039	. 8961	44
16 17	. 4378	. 5593	.9550 .9411	 4529 4559 	.8687	.0105	. 1035	. 8957	43
18	. 4436	. 5564	.9273	4588	.8547	.0106	. 1043	8952	42
19	. 4464	. 5536	.9135	. 4618	.8408	.0106	1052	. 8948	41
	.14493	.85507	6.8998	.14648	6.8269	1.0107	.01056	.98944	40
20 21 22 23	. 4522	. 5478	.8861	. 4677	.8131	.0107	. 1060	. 8940	39
22	4551	. 5449	.8725	4707	,7993	.0107	. 1064	. 8936	38
23	4579	. 5420	.8589	4737	.7856	.0108	. 1068	. 8931	37
24	4608	5392	.8454	4767	.7720	.0108	. 1073	. 8927	36
25	.14637	.85363	6.8320	.14796	6.7584	1.0109	.01077	.98923	35
26	. 4666	, 5334	.8185	. 4826	.7448	.0109	. 1081	. 8919	34
27	4695	. 5305	.8052	. 4856	.7313	.0110	. 1085	. 8914	33
28	. 4723	. 5277	.7919	. 4886	.7179	.0110	. 1090	. 8910	32 ·
24 25 26 27 28 29	. 4752	. 5248	.7787	. 4915	.7045	.0111	. 1094	. 8906	31
30	.14781	.85219	6.7655	.14945	6.6911	1.0111	.01098	.98901	30
31	. 4810	. 5190	.7523	. 4975	.6779	.0111	. 1103	. 8897	29
32	. 4838	. 5161	.7392	. 5004	.6646	.0112	. 1107	. 8893	28
33	. 4867	. 5133	.7262	. 5034	.6514	.0112	. 1111	. 8889	27
34	. 4396	. 5104	.7132	. 5064	.6383	.0113	. 1116	. 8884	26
35	.14925	.85075	6.7003	.15094	6.6252	1.0113	.01120	.98880	25
36	. 4953	. 5046	.6874	· 5123	.6122	.0114	. 1124 . 1129	. 8876	24 23
37 38	. 4982	. 5018	.6745	. 5153	.5992	.0114	.1129 .1133	. 8871 . 8867	23
38 39	. 5011	. 4989 . 4960	.6617	. 5183 . 5213	.5863	.0115	. 1135	. 8862	21
39 40	.15068	.84931	6.6363	.15243	6.5605	1.0115	.01142	.98858	20
41	. 5097	. 4903	.6237	. 5272	.5478	.0116	. 1146	. 8854	19
42	. 5126	4874	.6111	. 5302	.5350	.0116	1151	. 8849	18
43	. 5155	4845	.5985	5332	.5223	.0117	. 1155	. 8845	17
44	. 5183	4816	.5860	. 5362	.5097	.0117	. 1159	. 8840	16
45	.15212	.84788	6.5736	.15391	6.4971	1.0118	.01164	.98836	15
46	. 5241	. 4759	.5612	. 5421	.4845	.0118	. 1168	. 8832	14
47	. 5270	. 4730	.5488	. 5451	.4720	.0119	. 1173	. 8827	13
48	. 5298	. 4701	.5365	. 5481	.4596	.0119	. 1177	. 8823	12
49	. 5328	. 4672	.5243	. 5511	.4472	.0119	. 1182	. 8818	11
50	.15356	.84644	6.5121	.15540	6.4348	1.0120	.01186	.98814	10
51	. 5385	. 4615	.4999	. 5570	.4225	.0120	1190	. 8809	9
52	. 5413	. 4586	.4878	. 5600	.4103	.0121	. 1195	. 8805	87
53	. 5442	. 4558	.4757	. 5630	.3980	.0121	. 1199	. 8800	
54	. 5471	. 4529	.4637	. 5659	.3859	.0122	. 1204	. 8796	6
55	.15500	.84500	6.4517	.15689	6.3737	1.0122	.01208	.98791	5
56	. 5528	. 4471	.4398	. 5719	.3616	.0123	. 1213	. 8787	43
57	. 5557	. 4443	.4279	. 5749	.3496	.0123	. 1217	. 8782	3
58	. 5586	. 4414	.4160	. 5779	.3376	.0124	. 1222	. 8778	2
59	. 5615	. 4385	.4042	. 5809	.3257	.0124	.1227 .1231	. 8773	
60	. 5643	. 4356	.3924	. 5838	.3137	.0125		. 8769	0
<u>M</u> .	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Sine.	Vrs. cos.	M.

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NATURAL FUNCTIONS.

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9 0	a Natural Trigonometrical Functions. 170°									
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	М.	
0	.15643	.84356	6.3924	.15838	6.3137	1.0125	.01231	.98769	60	
1	. 5672	. 4328	.3807	. 5868	.3019	.0125	. 1236	 8764 	59	
2	. 5701	. 4299	.3690	. 5898	.2901	.0125	. 1240	. 8760	58	
34	. 5730	. 4270 . 4242	.3574	. 5928 . 5958	.2783	.0126 .0126	.1245 .1249	. 8755 . 8750	57 56	
- 4	. 5758 .15787	. 4242	.3458 6.3343	.15987	6.2548	1.0127	.01254	.98746	55	
5 6	. 5816	. 4184	.3228	. 6017	.2432	.0127	. 1259	. 8741	54	
7	. 5844	. 4155	.3113	. 6047	.2316	.0128	. 1263	8737	53	
8	. 5873	. 4127	.2999	. 6077	.2200	.0128	 1268 	. 8732	52	
9	. 5902	. 4098	.2885	. 6107	.2085	.0129	. 1272	. 8727	51	
10	.15931	.84069	6.2772	.16137	6.1970	1.0129	.01277 . 1282	.98723	50	
$\frac{11}{12}$. 5959 . 5988	• 4041 • 4012	.2659	. 6167 . 6196	.1856 .1742	.0130 .0130	. 1282	. 8718 . 8714	49	
$\frac{12}{13}$. 6017	3983	.2434	. 6226	.1628	.0131	. 1291	. 8709	47	
14	. 6045	3954	2322	6256	.1515	.0131	. 1296	. 8704	46	
15	.16074	.83926	6.2211	.16286	6.1402	1.0132	.01300	98700	45	
16	. 6103	. 3897	.2100	. 6316	.1290	.0132	. 1305	. 8695	44	
17	. 6132	. 3868	.1990	. 6346	.1178	.0133	. 1310	. 8690	43	
18	. 6160	. 3840	.1880	. 6376	.1066	.0133 .0134	1314 . 1319	• 8685	42	
19 20	. 6189 .16218	.3811 .83782	.1770 6.1661	.6405 .16435	.0955 6.0844	1.0134	.01324	. 8681 .98676	40	
21	. 6246	. 3753	.1552	. 6465	.0734	.0135	. 1328	. 8671	39	
22	. 6275	. 3725	.1443	. 6495	.0624	.0135	. 1333	. 8667	38	
23	. 6304	. 3696	.1335	. 6525	.0514	.0136	. 1338	. 8662	37	
24	. 6333	. 3667	.1227	. 6555	.0405	.0136	. 1343	. 8657	36	
25	.16361	.83639	6.1120	.16585	6.0296	1.0136	.01347	.98652	35	
26	. 6390	. 3610	.1013	. 6615	.0188	.0137 .0137	. 1352	. 8648	34 3 3	
27 28	. 6419 . 6447	. 3581 . 3553	.0900	. 6644 . 6674	.0080	.0138	. 1362	. 8643 . 8638	32	
29	. 6476	. 3524	.0694	. 6704	.9865	.0138	1367	. 8633	31	
30	.16505	.83495	6.0588	.16734	5,9758	1.0139	.01371	.98628	30	
31	. 6533	. 3466	.0483	. 6764	.9651	.0139	. 1376	. 8624	29	
32	. 6562	. 3438	.0379	. 6794	.9545	.0140	. 1381	. 8619	28 27	
33	. 6591	• 3409	.0274	. 6824	.9439	.0140	. 1386	. 8614	26	
$\frac{34}{35}$.6619 .16648	. 3380	.0170 6.0066	. 6854 .16884	.9333 5.9228	$.0141 \\ 1.0141$.01395	. 8609	25	
36	. 6677	. 3323	5.9963	. 6914	.9123	.0142	. 1400	. 8600	24	
37	6705	. 3294	.9860	. 6944	.9019	.0142	. 1405	. 8595	23	
38	. 6734	. 3266	.9758	. 6973	.8915	.0143	. 1410	. 8590	22	
39	. 6763	. 3237	.9655	. 7003	.8811	.0143	. 1415	. 8585	21	
40	.16791	.83208	5.9554	.17033	5.8708	1.0144	.01420	.98580	20	
41 42	. 6820 . 6849	. 3180	.9452 .9351	. 7063 . 7093	.8605	.0144	.1425 .1430	8575 . 8570	19	
42	. 6849	3122	.9250	7123	.8400	.0145	. 1434	. 8565	17	
44	. 6906	3094	.9150	7153	.8298	.0146	. 1439	. 8560	16	
45	.16935	.83065	5.9049	.17183	5.8196	1.0146	.01444	.98556	15	
46	. 6964	. 3036	.8950	. 7213	.8095	.0147	. 1449	. 8551	14	
47	. 6992	. 3008	.8850	. 7243 . 7273	.7994	.0147	. 1454	. 8546	13 12	
48	. 7021	2979 2950	.8751	7303	.7894	.0148	. 1459 . 1464	. 8541 . 8536	11	
49 50	.17078	.82922	5.8554	.17333	5.7694	1.0149	.01469	.98531	10	
51	. 7107	. 2893	.8456	. 7363	.7594	.0150	. 1474	. 8526	Ĩğ	
$\tilde{52}$. 7136	. 2864	.8358	. 7393	.7495	.0150	. 1479	. 8521	8	
53	. 7164	. 2836	.8261	. 7423	.7396	.0151	. 1484	. 8516	8 7 6	
54	. 7193	. 2807	.8163	. 7453	.7297	.0151	. 1489	. 8511	6	
55	.17221	.82778	5.8067	.17483	5.7199	1.0152	.01494	.98506	5 4	
56 57	. 7250 . 7279	2750 2721	.7970	. 7513	.7101	.0152	. 1499	. 8496	3	
57 58	. 7307	2692	.7778	. 7573	.6906	.0153	. 1509	. 8491	3 2 1	
59	. 7336	2664	.7683	7603	.6809	.0154	1514	. 8486		
60	. 7365	. 2635	.7588	. 7633	.6713	.0154	. 1519	. 8481	0	
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.	

Natural Trigonometrical Functions.

169°

10.	_	148	itural li	rgonom	erricar	113.			
Μ.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	<u>M.</u>
0	.17365	.82635	5.7588	.17633	5.6713	1.0154	.01519	.98481	60
1	. 7393	. 2606	.7493	. 7663	.6616	.0155	. 1524	. 8476	59
2 3 4	. 7422	. 2578	.7398	. 7693	.6520	.0155	. 1529	. 8471	58
3	. 7451	. 2549	.7304	. 7723	.6425	.0156	. 1534	. 8465	57
5	. 7479 .17508	. 2521 .82492	.7210 5.7117	. 7753 .17783	.6329 5.6234	.0156 1.0157	. 1539 .01544	. 8460 .98455	56
5 6 7 8	. 7537	. 2463	.7023	. 7813	.6140	.0157	. 1550	. 8450	54
7	7565	2435	.6930	7843	.6045	.0158	. 1555	. 8445	53
8	. 7594	. 2406	.6838	7873	.5951	.0158	. 1560	. 8440	52
9	. 7622	. 2377	.6745	. 7903	.5857	.0159	. 1565	. 8435	51
10	.17651	.82349	5.6653	.17933	5.5764	1.0159	.01570	.98430	50
11	. 7680	. 2320	.6561	. 7963	.5670	.0160	. 1575	. 8425	49
12 13	. 7708 . 7737	2291 2263	.6470	. 7993 . 8023	.5578	.0160	. 1580 . 1585	. 8419 . 8414	48
14	. 7766	2234	.6379 .6288	. 8023	.5485	.0161 .0162	. 1591	. 8409	46
15	.17794	.82206	5.6197	.18083	5.5301	1.0162	.01596	.98404	45
16	. 7823	. 2177	.6107	. 8113	.5209	.0163	. 1601	. 8399	44
17	. 7852	. 2148	.6017	. 8143	.5117	.0163	. 1606	. 8394	43
18	. 7880	. 2120	.5928	. 8173	.5026	.0164	. 1611	. 8388	42
19	. 7909	. 2091	.5838	. 8203	.4936	.0164	. 1617	. 8383	41
$\frac{20}{21}$.17937 .7966	.82062	5.5749	.18233	5.4845	1.0165	.01622	.98378	40
$\frac{21}{22}$. 7905	. 2034 . 2005	.5660 .5572	. 8263 . 8293	.4755	.0165 .0166	.1627 .1632	. 8373 . 8368	39
23	8023	1977	.5484	. 8323	.4003	.0166	. 1638	. 8362	37
24	. 8052	1948	.5396	. 8353	.4486	.0167	1643	. 8357	36
25	.18080	.81919	5.5308	.18383	5.4396	1.0167	.01648	.98352	35
26	. 8109	. 1891	.5221	. 8413	.4308	.0168	. 1653	. 8347	34
27	. 8138	. 1862	.5134	. 8444	.4219	.0169	1659	. 8341	33
28 29	. 8166	. 1834	.5047	. 8474	.4131	.0169	. 1664	. 8336	32
29 30	. 8195 .18223	.1805 .81776	.4960 5.4874	. 8504 .18534	.4043 5.3955	.0170	. 1669	. 8331 .98325	31
31	. 8252	. 1748	.4788	. 8564	.3868	1.0170 .0171	.01674 . 1680	.98320	29
32	. 8281	. 1719	.4702	. 8594	.3780	.0171	. 1685	8315	28
33	. 8309	. 1691	.4617	. 8624	.3694	.0172	1690	. 8309	27
34	. 8338	. 1662	.4532	. 8654	.3607	.0172	. 1696	. 8304	26
35	18366	.81633	5.4447	.18684	5.3521	1.0173	.01701	.98299	25
36 37	. 8395 . 8424	. 1605 . 1576	.4362	. 8714	.3434	.0174	. 1706	. 8293	24
38	. 8452	. 1548	.4278	. 8745 . 8775	.3349 .3263	.0174	. 1712	 8288 8283 	23 22
39	. 8481	1519	.4110	. 8805	.3203	.0175 .0175	.1717 .1722	. 8277	21
40	.18509	.81490	5.4026	.18835	5,3093	1.0176	.01728	.98272	20
41	. 8538	. 1462	.3943	. 8865	.3008	.0176	. 1733	. 8267	19
42	8567	. 1433	.3860	. 8895	.2923	.0177	. 1739	. 8261	18
43	· 8595	. 1405	.3777	. 8925	.2839	.0177	. 1744	. 8256	17
44 45	. 8624 .18652	.1376 .81348	.3695 5.3612	. 8955 .18985	.2755	.0178	. 1749	. 8250	16
46	. 8681	. 1319	.3530	. 9016	5.2671 .2588	1.0179 .0179	.01755 . 1760	.98245 .8240	15 14
47	8709	. 1290	.3449	. 9046	.2505	.0179	, 1766	. 8234	13
48	8738	. 1262	.3367	. 9076	.2422	.0180	. 1771	. 8229	12
49	. 8767	. 1233	.3286	. 9106	.2339	.0181	1777	8223	11
50	.18795	.81205	5.3205	.19136	5.2257	1.0181	.01782	.98218	10
51	. 8824	. 1176	.3124	. 9166	.2174	.0182	. 1788	. 8212	9
52 53	· 8852	. 1147	.3044	. 9197	.2092	.0182	. 1793	. 8207	8
53 54	. 888 1 . 8909	. 1119 . 1090	.2963	. 9227 . 9257	.2011 .1929	.0183	. 1799	. 8201 . 8196	
55	.18938	.81062	5.2803	.19287	5.1848	.0184 1.0184	. 1804	.98190	6 5
56	. 8967	. 1033	.2724	. 9317	.1767	.0185	. 1815	. 8185	4
57	. 8995	. 1005	.2645	. 9347	.1686	.0185	. 1821	. 8179	3
58	. 9024	. 0976	.2566	. 9378	.1606	.0186	. 1826	. 8174	$ \begin{array}{c} 3 \\ 2 \\ 1 \end{array} $
59	. 9052	. 0948	.2487	. 9408	.1525	.0186	. 1832	. 8168	
60 	. 9081	. 0919	.2408	. 9438	.1445	.0187	. 1837	. 8163	0
<u>M</u> .	Cosine.	Vrs. sin.	Secaut.	Cotaug.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.
400	NO								

100°

NATURAL FUNCTIONS.

11º		Na	tural Tr	igonom	etrical 1	Punction	ns.	1	68 ⁰
М.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.19081	.80919	5.2408	.19438	5.1445	1.0187	.01837	.98163	60
1	. 9109	. 0890	.2330	. 9468	.1366	.0188	. 1843	. 8157	59
$\frac{2}{3}$. 9138	. 0862	.2252	. 9498	.1286	.0188	. 1848	. 8152	58
3	. 9166	. 0833	.2174	. 9529	.1207	.0189	. 1854	. 8146	57
4 5	.9195 .19224	. 0805 .80776	.2097 5.2019	. 9559 .19589	$.1128 \\ 5.1049$.0189 1.0190	. 1859	. 8140 .98135	56 55
6	9252	. 0748	.1942	. 9619	.0970	.0191	. 1871	. 8129	54
7	. 9281	. 0719	.1865	. 9649	.0892	.0191	1876	8124	53
8	9309	. 0691	.1788	9680	.0814	.0192	. 1882	. 8118	52
9	. 9338	. 0662	.1712	. 9710	.0736	.0192	. 1887	. 8112	51
10	.19366	.80634	5.1636	.19740	5.0658	1.0193	.01893	.98107	50
11	. 9395	. 0605	.1560	. 9770	.0581	.0193	. 1899	. 8101	49
12 13	. 9423 . 9452	. 0576 . 0548	.1484 .1409	. 9800 . 9831	.0504	.0194 .0195	. 1904	. 8095 . 8090	48
13	. 9452	. 0519	.1333	9861	.0350	.0195	. 1916	. 8084	46
15	.19509	.80491	5.1258	19891	5.0273	1.0196	.01921	.98078	45
16	. 9537	. 0462	.1183	. 9921	.0197	.0196	. 1927	. 8073	44
17	. 9566	. 0434	.1109	. 9952	.0121	.0197	. 1933	. 8067	43
18	. 9595	. 0405	.1034	. 9982	.0045	.0198	. 1938	. 8061	42
19	. 9623	. 0377	.0960	.20012	4.9969	.0198	. 1944	. 8056	41
20	.19652 .9680	.80348	5.0886	.20042	4.9894	1.0199	.01950	.98050 .8044	40
21 22	. 9709	. 0320	.0812 .0739	. 0103	.9819 .9744	.0199 .0200	. 1950	. 8039	38
23	. 9737	. 0263	.0666	. 0133	.9669	.0200	1967	. 8033	37
24	. 9766	. 0234	.0593	0163	.9594	.0201	1973	. 8027	36
25	.19794	.80206	5.0520	.20194	4.9520	1.0202	.01979	.98021	35
26 27	. 9823	. 0177	.0447	. 0224	.9446	.0202	. 1984	. 8016	34
27	. 9851	. 0149	.0375	. 0254	.9372	.0203	. 1990	. 8010	33
28 29	. 9880	. 0120	.0302	. 0285	.9298	.0204	. 1996	. 8004	32 31
30	. 9908 .19937	. 0092	.0230	.0315 .20345	.9225 4.9151	.0204 1.0205	. 2002	. 7998	30
31	. 9965	. 0035	.0087	. 0375	.9078	.0205	. 2013	7987	29
32	. 9994	. 0006	.0015	. 0406	.9006	.0206	2019	. 7981	28
33	.20022	.79978	4.9944	. 0436	.8933	.0207	. 2025	. 7975	28 27
34	. 0051	. 9949	.9873	. 0466	.8860	.0207	. 2031	. 7969	26
35	.20079	.79921	4.9802	.20497	4.8788	1.0208	.02037	.97963	25
36 37	. 0108	. 9892 . 9863	.9732	. 0527 . 0557	.8716	.0208	. 2042	. 7957	24 23
38	. 0165	. 9805	.9661 .9591	. 0588	.8644	.0209 .0210	2048	. 7946	20
39	. 0193	9807	.9521	. 0618	.8501	.0210	2060	. 7940	22 21
40	.20222	.79778	4,9452	.20648	4.8430	1.0211	.02066	97934	20
41	. 0250	. 9750	.9382	. 0679	.8359	.0211	. 2072	. 7928	19
42	. 0279	. 9721	.9313	. 0709	.8288	.0212	. 2078	. 7922	18
43	. 0307	. 9693	.9243	. 0739	.8217	.0213	. 2084	. 7916	17
44 45	. 0336 .20364	. 9664	.9175	. 0770	.8147	.0213 1.0214	. 2089	. 7910	16 15
46	. 0393	. 9607	4.9106	. 0830	.8007	.0214	. 2101	. 7899	14
47	. 0421	. 9579	.8969	. 0861	.7937	.0215	. 2107	. 7893	13
48	. 0450	. 9550	.8901	. 0891	.7867	.0216	. 2113	. 7887	12
49	. 0478	. 9522	.8833	. 0921	.7798	.0216	. 2119	. 7881	11
50	.20506	.79493	4.8765	.20952	4.7728	1.0217	.02125	.97875	10
51	. 0535	. 9465	.8697	. 0982	.7659	.0218	. 2131	. 7869	9
$\frac{52}{53}$. 0563 . 0592	. 9436	.8630	.1012 .1043	.7591 ,7522	.0218 .0219	. 2137	. 7857	87
54	. 0620	9379	.8563	. 1043	.7453	.0219	2143	7851	6
55	.20649	.79351	4.8429	.21104	4.7385	1.0220	.02155	.97845	65
56	. 0677	. 9323	.8362	. 1134	.7317	.0221	. 2161	. 7839	4
57	. 0706	. 9294	.8296	. 1164	.7249	.0221	. 2167	. 7833	3
58	. 0734	. 9266	.8229	. 1195	.7181	.0222	. 2173	. 7827	2
59	. 0763	. 9237	.8163	. 1225	.7114	.0223 .0223	. 2179	. 7821	1
60	. 0791	. 9209	.8097	. 1256	.7046				
М.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	V TS. COS.	Sine.	M.

12°

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Natural Trigonometrical Functions.

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12	-	INA	iturat 11	rigonom	erricai				
М.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	<u>M.</u>
0	.20791	.79209	4.8097	.21256	4.7046	1.0223	.02185	.97815	60
ĭ	. 0820	. 9180	.8032	, 1286	.6979	.0224	. 2191	. 7809	59
$\overline{2}$. 0848	. 9152	.7966	. 1316	.6912	.0225	. 2197	. 7803	58
3	. 0876	. 9123	.7901	. 1347	.6845	.0225	. 2203	. 7806	57
4	. 0905	. 9105	.7835	. 1377	.6778	.0226	. 2209	. 7790	56
5 6	.20933	.79066	4.7770	.21408	4.6712	1.0226	.02215	.97784	55
6	. 0962	. 9038	.7706	. 1438	.6646	.0227	. 2222	. 7778	54
7	. 0990	. 9010	.7641	. 1468	.6580	.0228	. 2228	. 7772	53
8	. 1019	. 8981	.7576	. 1499	.6514	.0228	· 2234 · 2240	. 7766	52
10	.1047 .21076	. 8953 .78924	.7512 4.7448	. 1529 .21560	$ \begin{array}{r} .6448 \\ 4.6382 \end{array} $	1.0230	.02240	. 7760	51 50
10 11	. 1104	. 8896	7384	, 1590	.6317	.0230	. 2252	. 7748	49
12^{11}	. 1132	. 8867	.7320	1621	.6252	.0231	2258	. 7741	48
13	. 1161	. 8839	7257	1651	.6187	.0232	. 2264	. 7735	47
14	. 1189	. 8811	7193	. 1682	.6122	.0232	2271	7729	46
15	.21218	78782	4.7130	.21712	4.6057	1.0233	.02277	.97723	45
16	. 1246	. 8754	.7067	. 1742	.5993	.0234	. 2283	. 7717	44
17	. 1275	. 8725	.7004	. 1773	.5928	.0234	. 2289	. 7711	43
18	. 1303	. 8697	.6942	. 1803	.5864	.0235	. 2295	. 7704	42
1 9	. 1331	. 8668	.6879	. 1834	.5800	.0235	. 2302	7698	41
20	.21360	.78640	4.6817	.21864	4.5736	1.0236	.02308	.97692	40
21	. 1388	. 8612	.6754	. 1895	.5673	.0237	. 2314	. 7686	39
22	. 1417	. 8583	.6692	. 1925	.5609 .5546	.0237	· 2320 · 2326	. 7680	38
23	. 1445	. 8555 . 8526	.6631 .6569	. 1956 . 1986	.5483	.0238	· 2320 · 2333	. 7673	37
24	.1473 .21502	.78508	4,6507	.22017	4,5420	1.0239	.02339	.7667 .97661	36 35
$\frac{1}{25}$ 26	. 1530	. 8470	.6446	2047	.5357	.0240	. 2345	. 7655	34
27	. 1559	. 8441	.6385	2078	.5294	.0241	2351	7648	33
28	. 1587	. 8413	.6324	. 2108	.5232	.0241	2358	. 7642	32
29	. 1615	. 8384	.6263	. 2139	.5169	.0242	. 2364	7636	31
30	.21644	.78356	4.6202	.22169	4.5107	1.0243	.02370	.97630	30
31	. 1672	 8328 	.6142	. 2200	.5045	.0243	. 2377	. 7623	29
32	. 1701	. 8299	.6081	. 2230	.4983	.0244	. 2383	. 7617	28
33	. 1729	. 8271	.6021	. 2261	.4921	.0245	. 2389	. 7611	27
34	. 1757	. 8242	.5961	. 2291	.4860	.0245	. 2396	. 7604	26
35	.21786 . 1814	.78214 .8186	4.5901	.22322	4.4799 .4737	1.0246 .0247	.02402	.97598	25
$\frac{36}{37}$. 1814	. 8154	.5782	2383	.4676	.0247	2408 2415	. 7592 . 7585	24 23
38	. 1871	. 8129	.5722	2414	.4615	.0248	2421	7579	$\frac{23}{22}$
39	. 1899	. 8100	.5663	2444	.4555	.0249	2427	. 7573	$\tilde{21}$
40	.21928	78072	4.5604	22475	4.4494	1.0249	.02434	.97566	$\tilde{20}$
41	. 1956	. 8043	.5545	. 2505	.4434	.0250	. 2440	. 7560	19
42	. 1985	. 8015	.5486	. 2536	.4373	.0251	. 2446	. 7553	18
43	. 2013	. 7987	.5428	. 2566	.4313	.0251	. 2453	. 7547	17
44	. 2041	. 7959	.5369	. 2597	.4253	.0252	. 2459	. 7541	16
45	.22070	.77930	4.5311	.22628	4.4194	1.0253	.02466	.97534	15
46	. 2098	. 7902	.5253	. 2658	.4134	.0253	. 2472	. 7528	14
47 48	· 2126 · 2155	. 7873 . 7845	.5195 .5137	. 2689 . 2719	.4074 .4015	.0254 .0255	. 2479 . 2485	. 7521	13
49	. 2183	. 7817	.5079	2750	.3956	.0255	2480 2491	· 7515 7508	12
50	. 2185	77788	4.5021	22781	4.3897	1.0256	.02498	.97502	11 10
51	. 2240	. 7760	.4964	. 2811	.3838	.0257	. 2504	. 7495	9
52	2268	7732	.4907	2842	.3779	.0257	. 2511	7489	8
53	. 2297	. 7703	.4850	. 2872	.3721	.0258	. 2517	7483	8 7
54	 2325 	. 7675	.4793	. 2903	.3662	.0259	. 2524	. 7476	6
55	.22353	.77647	4.4736	.22934	4.3604	1.0260	.02530	.97470	5
56	. 2382	. 7618	.4679	. 2964	.3546	.0260	. 2537	. 7463	4
57	. 2410	7590	.4623	. 2995	.3488	.0261	. 2543	. 7457	3
58	2438	. 7561	.4566	. 3025	.3430	.0262	. 2550	. 7450	2
59	2467	. 7533	.4510	. 3056	.3372	.0262	. 2556	. 7443	1
60	. 2495	. 7505	.4454	. 3087	.3315	.0263	. 2563	. 7437	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	Μ.

102°

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-7

NATURAL FUNCTIONS.

13°		Na	tural Tr	igonom	etrical I	Punction	ıs.	10	66°
M .	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.22495	.77505	4.4454	.23087	4.3315	1.0263	.02563	.97437	60
i	2523	. 7476	.4398	. 3117	.3257	.0264	. 2569	. 7430	59
2	2552	. 7448	.4342	. 3148	.3200	.0264	. 2576	. 7424	58
234567	. 2580	. 7420	.4287	. 3179	.3143	.0265	. 2583	. 7417	57
4	. 2608	. 7391	.4231	. 3209	.3086	.0266	. 2589	. 7411	56
5	.22637	.77363	4.4176	.23240	4.3029	1.0266	.02596	.97404	55
6	. 2665	. 7335	.4121	. 3270	.2972	.0267	. 2602	. 7398	54
7	. 2693	. 7306	.4065	. 3301	.2916	.0268	. 2609	. 7391	53
8	. 2722	. 7278	.4011	. 3332	.2859	.0268	.2616 .2622	. 7384	52 51
9 10	.2750 .22778	. 7250	.3956 4.3901	. 3363 .23393	.2803	.0269 1.0270	.02629	. 7378	50
11	. 2807	. 7193	.3847	. 3424	.2691	.0271	. 2835	. 7364	49
12	2835	7165	.3792	. 3455	.2635	.0271	2642	7358	48
13	2863	7136	.3738	. 3485	.2579	.0272	. 2649	. 7351	47
14	2892	. 7108	.3684	. 3516	.2524	.0273	. 2655	. 7344	46
15	.22920	.77080	4.3630	.23547	4.2468	1.0273	.02662	.97338	45
16	. 2948	. 7052	.3576	. 3577	.2413	.0274	. 2669	. 7331	44
17	. 2977	. 7023	.3522	. 3608	.2358	.0275	. 2675	. 7324	43
18	. 3005	. 6995	.3469	. 3639	.2303	.0276	. 2682	. 7318	42
19	. 3033	. 6967	.3415	. 3670	.2248	.0276	. 2689	. 7311	41
20	.23061	.76938	4.3362	.23700	4.2193	1.0277	.02695	.97304	40
21	. 3090	. 6910	.3309	. 3731	.2139	.0278	. 2702	. 7298	39
22 23	3118 3146	. 6882	.3256	3762 3793	.2084	.0278	. 2709 . 2716	. 7291 . 7284	38 37
23 24	3175	. 6853 . 6825	.3150	. 3793	.1976	.0279	2710	7277	36
24	.23203	.76797	4.3098	.23854	4,1921	1,0280	.02729	.97271	35
26	. 3231	6769	.3045	. 3885	.1867	.0281	. 2736	7264	34
27	. 3260	6740	.2993	3916	.1814	.0282	2743	. 7257	33
28	3288	. 6712	.2941	. 3946	.1760	.0283	. 2749	. 7250	32
29	. 3316	. 6684	.2888	. 3977	.1706	.0283	. 2756	. 7244	31
30	.23344	.76655	4.2836	.24008	4.1653	1.0284	.02763	.97237	30
31	. 3373	. 6627	.2785	. 4039	.1600	.0285	. 2770	. 7230	29
3 2	. 3401	. 6599	.2733	. 4069	.1546	.0285	. 2777	. 7223	28
33	. 3429	. 6571	.2681	. 4100	.1493	.0286	. 2783	. 7216	27
34	. 3458	. 6542	.2630 4.2579	. 4131	.1440 4.1388	.0287 1.0288	. 2790	7210 .97203	26 25
35	. 3514	.76514	2527	.24162	1335	.0288	2804	. 7196	24
36 37	. 3542	. 6457	.2327	. 4192	.1282	.0289	2811	7189	23
38	3571	6429	.2425	4254	.1230	.0290	2818	. 7182	22
39	3599	. 6401	.2375	4285	.1178	.0291	. 2824	. 7175	21
40	.23627	.76373	4.2324	.24316	4.1126	1.0291	.02831	.97169	20
41	. 3655	. 6344	.2273	. 4346	.1073	.0292	. 2838	. 7162	19
4 2	. 3684	. 6316	.2223	. 4377	.1022	.0293	. 2845	. 7155	18
43	. 3712	. 6288	.2173	. 4408	.0970	.0293	. 2852	. 7148	17
44	. 3740	. 6260	.2122	. 4439	.0918	.0294	. 2859	. 7141	16
45	.23768	.76231	4.2072	.24470	4.0867	1.0295	.02866	.97134	15
46	. 3797	. 6203	.2022	4501	.0815	.0296	2873	. 7127	13
47 48	. 3825 . 3853	6175	.1972	4562	.0713	.0290	2886	7113	12
49	. 3881	6118	.1873	4593	.0662	.0298	2893	7106	iĩ
50	.23910	.76090	4.1824	24624	4.0611	1.0299	.02900	.97099	10
51	. 3938	. 6062	.1774	. 4655	.0560	.0299	. 2907	. 7092	9
$\tilde{52}$. 3966	. 6034	.1725	. 4686	.0509	.0300	. 2914	. 7086	8
53	. 3994	. 6005	.1676	. 4717	.0458	.0301	. 2921	. 7079	7
54	. 4023	. 5977	.1627	. 4747	.0408	.0302	. 2928	. 7072	6
55	.24051	.75949	4.1578	.24778	4.0358	1.0302	.02935	.97065	5
56	. 4079	. 5921	.1529	. 4809	.0307	.0303	. 2942	. 7058	4
57	. 4107	. 5892	1481	. 4840	.0257	.0304	. 2949	. 7051	3
58	. 4136	. 5864	.1432	. 4871	.0207	.0305	. 2956	. 7044	2
59	4164	. 5836	.1384	4902	.0157	.0305	. 2963	. 7037	
60	. 4192	. 5808							
<u>M.</u>	Cosine.	Vrs. sin.	Secant.	Cotang.	Taug.	Cosec'nt	Vrs. cos.	Sine.	M .

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14°

Natural Trigonometrical Functions.

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140)	Natural Trigonom			etrical	Functio	165°		
M.	Siu <i>e</i> .	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. siu.	Cosine.	<u>M</u> .
0	.24192	.75808	4.1336	.24933	4.0108	1.0306	.02970	.97029	60
1	. 4220	. 5779	.1287	. 4964	.0058	.0307	. 2977	. 7022	59
$\frac{2}{3}$. 4249	. 5751	.1239	. 4995	.0009	.0308	. 2984	. 7015	58 57
3	.4277 .4305	. 5723 . 5695	.1191 .1144	. 5025 . 5056	3.9959	.0308	. 2991	. 7008	56
$\frac{4}{5}$. 24333	.75667	4.1096	.25087	3,9861	1.0310	.03006	.96994	55
6	. 4361	. 5638	.1048	. 5118	.9812	.0311	. 3013	. 6987	54
7	. 4390	. 5610	.1001	. 5149	.9763	.0311	. 3020	. 6980	53
8	. 4418	. 5582	.0953	. 5180	.9714	.0312	. 3027	. 6973	52
9 10	. 4446 .24474	. 5554 .75526	.0906 4.0859	.5211 .25242	.9665 3.9616	.0313 1.0314	. 3034 .03041	. 6966 .96959	51 50
11	. 4502	. 5497	.0812	5273	.9568	.0314	. 3048	. 6952	49
12	. 4531	5469	.0765	. 5304	.9520	.0315	. 3055	. 6944	48
13	. 4559	. 5441	.0718	. 5335	.9471	.0316	. 3063	. 6937	47
14	. 4587	. 5413	.0672	. 5366	.9423	.0317	. 3070	. 6930	46
15 16	.24615 . 4643	.75385 . 5356	4.0625	.25397 .5428	3.9375 .9327	1.0317 .0318	.03077	.96923 . 6916	45 44
17	. 4643 . 4672	5328	.0579	. 5459	.9327	.0319	. 3091	. 6909	43
18	4700	5300	.0486	. 5490	.9231	.0320	. 3098	6901	42
19	. 4728	. 5272	.0440	. 5521	.9184	.0320	. 3106	. 6894	41
20	.24756	.75244	4.0394	.25552	3.9136	1.0321	.03113	.96887	40
21	. 4784 . 4813	. 5215	.0348	. 5583	.9089	.0322	. 3120	. 6880	39
21 22 23 24 25	. 4813	. 5187 . 5159	.0302	. 5614 . 5645	.9042 .8994	.0323	3127 3134	.6873 .6865	38 37
24	. 4869	. 5133	.0256 .0211	. 5676	.8947	.0324	3142	. 6858	36
25	.24897	.75103	4.0165	.25707	3.8900	1.0325	.03149	.96851	35
26	. 4925	. 5075	.0120	. 5738	.8853	.0326	. 3156	. 6844	34
26 27 28 29	. 4953	. 5046	.0074	. 5769	.8807	.0327	. 3163	. 6836	33
28	4982 . 5010	. 5018 . 4990	.0029 3.9984	. 5800 . 5831	.8760 .8713	.0327 .0328	$ \begin{array}{c} 3171 \\ 3178 \end{array} $. 6829 . 6822	$\frac{32}{31}$
30	.25038	.74962	3.9939	.25862	3.8667	1.0329	.03185	.96815	30
31	5066	. 4934	.9894	. 5893	.8621	.0330	. 3192	. 6807	29
32	. 5094	. 4906	.9850	5924	.8574	.0330	. 3200	. 6800	28 27
33	. 5122	. 4877	.9805	. 5955	.8528	.0331	. 3207	. 6793	27
34 35	. 5151 .25179	. 4849 .74821	.9760 3.9716	.5986 .26017	.8482 3.8436	.0332 1.0333	. 3214 .03222	.6785 .96778	26 25
36	. 5207	. 4793	.9672	. 6048	.8390	.0334	. 3229	. 6771	24
37	. 5235	. 4765	.9627	. 6079	.8345	.0334	. 3236	. 6763	23 22
38	 5263 	. 4737	.9583	. 6110	.8299	.0335	. 3244	. 6756	22
39	. 5291	. 4709	.9539	. 6141	.8254	.0336	. 3251	. 6749	21
40 41	.25319 .5348	.74680 .4652	3.9495 .9451	.26172	3.8208 .8163	1.0337 .0338	.03258 . 3266	.96741 . 6734	20 19
42	. 5376	4624	.9408	. 6234	.8118	.0338	3273	. 6727	18
43	. 5404	. 4596	.9364	. 6266	.8073	.0339	. 3281	. 6719	17
44	. 5432	. 4568	.9320	. 6297	.8027	.0340	. 3288	. 6712	16
45	.25460	.74540	3.9277	.26328	3.7983	1.0341	.03295	.96704	15
46 47	. 5488 . 5516	. 4512 . 4483	.9234 .9190	. 6359 . 6390	.7938 .7893	.0341 .0342	. 3303 . 3310	. 6697	14 13
48	. 5544	. 4455	.9147	. 6421	.7848	.0343	. 3318	. 6690 . 6682	13
49	. 5573	4427	.9104	6452	.7804	.0344	. 3325	. 6675	11
50 51	.25601	.74399	3.9061	.26483	3.7759	1.0345	.03332	.96667	10
51	. 5629	. 4371	.9018	. 6514	.7715	.0345	. 3340	. 6660	9
52	. 5657 . 5685	. 4344	.8976	. 6546	.7671	.0346	. 3347	. 6652	8 7
53 54	. 2080 . 5713	.4315 .4287	.8933 .8890	. 6577	.7627 .7583	.0347 .0348	.3355 .3362	. 6645 . 6638	6
55	.25741	.74259	3.8848	.26639	3.7539	1.0349	.03370	. 96630	6 5
56	. 5769	. 4230	.8805	. 6670	.7495	.0349	. 3377	. 6623	4
57	. 5798	. 4202	.8763	. 6701	.7451	.0350	. 3385	. 6615	3
58	. 5826	. 4174	.8721	. 6732	.7407	.0351	. 3392	. 6608	2
59 60	. 5854 . 5882	.4146 .4118	.8679 .8637	. 6764 . 6795	.7364 .7320	.0352 .0353	. 3400	. 6600 . 6592	$1 \\ 0$
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М.	Cosine.	Vrs. siu.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	м.

NATURAL FUNCTIONS.

154)	Na	tural Tr	igonom	etrical	Function	15.	1	64°
M.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.25882	.74118	3.8637	.26795	3.7320	1.0353	.03407	.96592	60
$\frac{1}{2}$. 5910	. 4090	.8595	. 6826	.7277	.0353	. 3415	. 6585	59
2	5938	. 4062	.8553	. 6857	.7234	.0354	. 3422	. 6577	58
3 4	. 5966	. 4034	.8512	. 6888	.7191	.0355	. 3430	. 6570	57
5	.5994 .26022	. 4006	.8470 3.8428	.6920 .26951	.7147	.0356 1.0357	. 3438	. 6562 .96555	56 55
6	. 6050	. 3949	.8387	. 6982	.7062	.0358	. 3453	. 6547	54
7	. 6078	. 3921	.8346	. 7013	.7019	.0358	. 3460	. 6540	53
8	. 6107	. 3893	.8304	. 7044	.6976	.0359	. 3468	. 6532	52
9	. 6135	. 3865	.8263	. 7076	.6933	.0360	. 3475	. 6524	51
10	.26163	.73837	3.8222	.27107	3.6891	1.0361	.03483	.96517	50
11 12	. 6191	. 3809	.8181	. 7138	.6848	.0362	. 3491	. 6509	49
13	. 6219 . 6247	.3781 .3753	.8140	.7169 .7201	.6806	.0362	. 3498	. 6502 . 6494	48
14	6275	. 3725	.8059	7232	.6722	.0364	. 3514	. 6486	46
15	.26303	.73697	3.8018	.27263	3.6679	1.0365	.03521	.96479	45
16	. 6331	. 3669	.7978	. 7294	.6637	.0366	. 3529	. 6471	44
17	. 6359	. 3641	.7937	. 7326	.6596	.0367	. 3536	. 6463	43
18	. 6387	. 3613	.7897	. 7357	.6554	.0367	. 3544	. 6456	42
19	. 6415	. 3585	.7857	. 7388	.6512	.0368	. 3552	. 6448	41
20 21	.26443 .6471	.73556	3.7816	.27419 .7451	3.6470	1.0369	.03560 . 3567	.96440	40 39
2 2	. 6499	. 3500	.7736	. 7482	.6387	.0371	. 3575	. 6425	38
23	6527	3472	.7697	7513	.6346	.0371	3583	. 6417	37
24	. 6556	. 3444	.7657	7544	.6305	.0372	. 3590	. 6409	36
25	.26584	.73416	3.7617	.27576	3.6263	1.0373	.03598	.96402	35
2 6	. 6612	. 3388	.7577	. 7607	.6222	.0374	. 3606	. 6394	34
27	. 6640	. 3360	.7538	. 7638	.6181	.0375	. 3614	. 6386	33
28 29	. 6668	. 3332 . 3304	.7498	. 7670 . 7701	.6140	.0376	. 3621 . 3629	.6378 .6371	32
30	. 26724	.73276	3.7420	.27732	.6100 3.6059	1.0377	. 3629	.96363	31 30
31	. 6752	. 3248	.7380	. 7764	.6018	.0378	. 3645	. 6355	29
32	. 6780	. 3220	.7341	. 7795	.5977	.0379	. 3652	. 6347	28
3 3	. 6808	. 3192	.7302	. 7826	.5937	.0380	. 3660	. 6340	27
34	. 6836	. 3164	.7263	. 7858	.5896	.0381	. 3668	. 6332	26
35	.26864	.73136	3.7224	.27889	3.5856	1.0382	.03676	.96324	25
36 37	. 6892 . 6920	. 3108 . 3080	.7186	. 7920 . 7952	.5816 .5776	.0382 .0383	. 3684 . 3691	. 6316 . 6308	24 23
38	. 6948	3052	.7108	7983	.5736	.0384	. 3699	. 6301	22
39	6976	. 3024	7070	8014	.5696	0385	3707	. 6293	21
40	27004	.72996	3.7031	.28046	3.5656	1.0386	.03715	.96285	20
41	. 7032	. 2968	.6993	. 8077	.5616	.0387	. 3723	. 6277	19
42	. 7060	. 2940	.6955	. 8109	.5576	.0387	. 3731	. 6269	18
43	. 7088	. 2912	.6917	. 8140	.5536	.0388	. 3739	. 6261	17
44 45	.7116 .27144	. 2884 .72856	.6878 3.6840	. 8171 .28203	.5497 3.5457	.0389 1.0390	. 3746	.6253 .96245	16 15
40	. 7172	. 2828	.6802	. 8234	.5418	.0391	. 3762	. 6238	14
47	7200	2800	.6765	. 8266	.5378	.0392	3770	. 6230	13
48	7228	. 2772	.6727	. 8297	.5339	.0393	. 3778	. 6222	12
49	. 7256	. 2744	.6689	. 8328	.5300	.0393	. 3786	. 6214	11
50	.27284	.72716	3.6651	.28360	3.5261	1.0394	.03794	.96206	10
51	. 7312	. 2688	.6614	. 8391	.5222	.0395	. 3802	. 6198	9
52 53	. 7340	. 2660 . 2632	.6576	. 8423 . 8454	.5183	.0396	$. 3810 \\ . 3818 $. 6190	8 7
54	7368 7396	. 2632	.6539 .6502	. 8486	.5144	.0397	. 3826	. 6182 . 6174	6
55	27424	.72576	3.6464	.28517	3.5066	1.0399	.03834	.96166	5
56	. 7452	. 2548	.6427	. 8549	.5028	.0399	. 3842	. 6158	4
57	. 7480	. 2520	.6390	. 8580	.4989	.0400	. 3850	. 6150	32
58	. 7508	. 2492	.6353	. 8611	.4951	.0401	. 3858	. 6142	
59	. 7536	. 2464	.6316	. 8643	.4912	.0402	. 3866	. 6134	1
60	. 7564	. 2436	.6279	. 8674	.4874	.0403	. 3874	. 6126	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec 'nt	Vrs. cos.	Sine.	M.

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Natural Trigonometrical Functions

160)	Na	tural Ti	rigonom	etrical	Functio	ns.	1	63°
Μ.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	М.
0	.27564	.72436	3.6279	.28674	3.4874	1.0403	.03874	.96126	60
1	. 7592	. 2408	.6243	. 8706	.4836	.0404	. 3882	. 6118	59
2	. 7620	. 2380	.6206	. 8737	.4798	.0405	. 3890	. 6110	58
3	. 7648	. 2352	.6169	. 8769	.4760	.0406	. 3898	. 6102	57
4	. 7675	. 2324 .72296	.6133	. 8800 .28832	4722	.0406	. 3906	. 6094 .96086	56
5 6	.27703 .7731	. 2268	3.6096	.28852 .8863	3.4684	1.0407	. 3922	. 6078	55 54
7	. 7759	2240	.6024	. 8895	.4608	.0409	3930	. 6070	53
8	. 7787	2213	.5987	. 8926	.4570	.0410	3938	. 6062	152
ğ	. 7815	2185	.5951	8958	.4533	.0411	. 3946	. 6054	51
10	.27843	72157	3.5915	.28990	3,4495	1.0112	.03954	.96045	50
11	. 7871	. 2129	.5879	. 9021	.4458	.0413	. 3962	. 6037	49
12	. 7899	. 2101	.5843	. 9053	.4420	.0413	. 3971	. 6029	48
13	. 7927	. 2073	.5807	. 9084	.4383	.0414	. 3979	. 6021	47
14	. 7955	. 2045	.5772	. 9116	.4346	.0115	. 3987	. 6013	46
15	.27983	72017	3.5736	.29147	3.4308	1.0416	.03995	.96005	45
$\frac{16}{17}$. 8011	. 1989	.5700	. 9179	.4271	.0417	. 4003	. 5997	44
17 18	8039 8067	. 1961 . 1933	.5665	.9210 .9242	.4234	.0418	.4011 .4019	. 5989 . 5980	43 42
19	. 8094	. 1955	.5594	9242	.4197	.0419	. 4028	5972	41
20	.28122	71877	3.5559	.29305	3.4124	1.0420	.04036	.95964	40
21	. 8150	1849	.5523	. 9337	.4087	.0421	. 4044	. 5956	39
22	. 8178	. 1822	.5488	9368	.4050	.0422	. 4052	. 5948	38
23	. 8206	. 1794	.5453	. 9400	.4014	.0423	. 4060	. 5940	37
24	 8234 	, 1766	.5418	. 9432	.3977	.0424	. 4069	. 5931	36
25	.28262	.71738	3.5383	.29463	3.3941	1.0425	.04077	.95923	35
26	. 8290	. 1710	.5348	. 9495	.3904	.0426	. 4085	. 5915	34
27	. 8318	1682	.5313	. 9526	.3868	.0427	. 4093	. 5907	33
$\frac{28}{29}$	 8346 8374 	. 1654 . 1626	.5279 .5244	9558 9590	.3832	.0428 .0428	. 4101 . 4110	5898 5890	32 31
29 30	.28401	.71608	3.5294	29621	3,3795 3,3759	1.0428	.04118	.95882	30
31	. 8429	. 1570	.5175	9653	.3723	.0430	. 4126	5874	29
32	. 8457	1543	.5140	9685	.3687	.0431	4134	5865	28
33	. 8485	. 1515	.5106	. 9716	.3651	.0432	. 4143	5857	27
34	 8513 	. 1487	.5072	. 97 48	.3616	.0433	. 4151	. 5849	26
35	.28541	.71459	3.5037	.29780	3.3580	1.0434	.04159	.95840	25
36	. 8569	. 1431	.5003	. 9811	.3544	.0435	. 4168	. 5832	24
37	• 8597 8697	. 1403	.4969	· 9843	.3509	.0436	.4176 .4184	. 5824	23 22
38	. 8624 . 8652	.1375 .1347	.4935 .4901	9875 9906	.3473 .3438	.0437 .0438	.4184 .4193	. 5816 . 5807	22 21
39 40	.28680	.71320	3.4867	.29938	3.3402	1.0438	.04201	.95799	20
41	. 8708	. 1292	.4833	9970	.3367	.0439	. 4209	. 5791	19
42	. 8736	1264	.4799	30001	.3332	.0440	. 4218	5782	18
43	. 8764	. 1236	.4766	. 0033	.3296	.0441	. 4226	. 5774	17
44	8792	. 1208	.4732	. 0065	.3261	.0442	. 4234	. 5765	16
45	.28820	.71180	3.4698	.30096	3.3226	1.0443	.04243	.95757	15
46	. 8847	.1152	.4665	. 0128	.3191	.0144	. 4251	. 5749	14
47	. 8875	1125 1097	.4632	. 0160	.3156 .3121	.0445	.4260 .4268	. 5740	$\frac{13}{12}$
48	. 8903 . 8931	. 1097	.4598 .4565	. 0192	.3121	.0446	.4208 .4276	. 5732 . 5723	11
49 50	28959	.71041	3.4532	30255	3.3052	1.0448	.04285	.95715	10
51	. 8987	. 1013	.4498	0287	.3017	.0448	4293	. 5707	9
52	9014	. 0985	.4465	0319	.2983	.0449	4302	. 5698	8
53	9042	. 0958	.4432	0350	.2948	.0450	. 4310	. 5690	7
54	9070	. 0930	.4399	. 0382	.2914	.0451	. 4319	. 5681	6
55	.29098	.70902	3.4366	.30414	3.2879	1.0452	.04327	95673	5
56	. 9126	. 0874	.4334	0446	.2845	.0453	. 4335	. 5664	4
57	. 9154	. 0846	.4301	. 0478	.2811	.0454	. 4344	. 5656	3
58	. 9181	. 0818	.4268	0509	.2777	.0455	. 4352	. 5647	$\frac{2}{1}$
59 60	. 9209 . 9237	. 0791 . 0763	.4236 .4203	0541 0573	.2742	.0456 .0457	. 4361 . 4369	. 5639 . 5630	i 0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M .

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NATURAL FUNCTIONS.

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$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	$\begin{array}{c} .04369\\ .4378\\ .4386\\ .4395\\ .4404\\ .04412\\ .4421\\ .4426\\ .4438\\ .4446\\ .04455\\ .4463\\ .4472\\ .4481\\ .4489\\ .04498\\ .4507\end{array}$	$\begin{array}{r} .95630\\ .5622\\ .5613\\ .5605\\ .5596\\ .95588\\ .5579\\ .5579\\ .5571\\ .5562\\ .5554\\ .95545\\ .5536\\ .5528\\ .5519\end{array}$	M. 60 59 58 57 56 55 54 53 52 51 50 49 48
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} . 4378 \\ . 4386 \\ . 4395 \\ . 4404 \\ . 04412 \\ . 4421 \\ . 4426 \\ . 4438 \\ . 4146 \\ . 04455 \\ . 4463 \\ . 4472 \\ . 4481 \\ . 4489 \\ . 04498 \\ . 4507 \end{array}$. 5622 . 5613 . 5605 . 5596 . 95588 . 5579 . 5571 . 5562 . 5554 . 5556 . 5536 . 5536 . 5528 . 5519	59 58 57 56 55 54 53 52 51 50 49
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} . 4378 \\ . 4386 \\ . 4395 \\ . 4404 \\ . 04412 \\ . 4421 \\ . 4426 \\ . 4438 \\ . 4146 \\ . 04455 \\ . 4463 \\ . 4472 \\ . 4481 \\ . 4489 \\ . 04498 \\ . 4507 \end{array}$. 5622 . 5613 . 5605 . 5596 . 95588 . 5579 . 5571 . 5562 . 5554 . 5556 . 5536 . 5536 . 5528 . 5519	59 58 57 56 55 54 53 52 51 50 49
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} . \ 4386\\ . \ 4395\\ . \ 4404\\ .04412\\ . \ 4421\\ . \ 4426\\ . \ 4438\\ . \ 4446\\ .04455\\ . \ 4463\\ . \ 4472\\ . \ 4481\\ . \ 4489\\ .04498\\ . \ 4507\end{array}$. 5613 . 5605 . 5596 .95588 . 5579 . 5571 . 5552 . 5554 . 5554 . 5536 . 5528 . 5519	58 57 56 55 54 53 52 51 50 49
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} . 4404 \\ .04412 \\ .4421 \\ .4426 \\ .4438 \\ .4438 \\ .4436 \\ .4435 \\ .4463 \\ .4472 \\ .4481 \\ .4489 \\ .04498 \\ .04498 \\ .4507 \end{array}$. 5596 .95588 . 5579 . 5571 . 5562 . 5554 . 95545 . 5536 . 5528 . 5519	56 55 54 53 52 51 50 49
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} .04412 \\ .4421 \\ .4426 \\ .4438 \\ .4146 \\ .04455 \\ .4463 \\ .4472 \\ .4481 \\ .4489 \\ .04498 \\ .4507 \end{array}$.95588 .5579 .5571 .5562 .5554 .95545 .5536 .5536 .5528 .5519	55 54 53 52 51 50 49
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} . \ 4421 \\ . \ 4426 \\ . \ 4438 \\ . \ 4146 \\ .04455 \\ . \ 4463 \\ . \ 4472 \\ . \ 4481 \\ . \ 4489 \\ . \ 4489 \\ . \ 4507 \end{array}$. 5579 . 5571 . 5562 . 5554 . 95545 . 5536 . 5528 . 5519	54 53 52 51 50 49
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4426 . 4438 . 4446 .04455 . 4463 . 4463 . 4472 . 4481 . 4489 .04498 . 4507	. 5571 . 5562 . 5554 .95545 . 5536 . 5528 . 5519	53 52 51 50 49
$\begin{array}{c c c c c c c c c c c c c c c c c c c $. 4438 . 4146 .01455 . 4463 . 4472 . 4481 . 4489 .04498 . 4507	. 5562 . 5554 .95545 . 5536 . 5528 . 5519	52 51 50 49
$\begin{array}{c c c c c c c c c c c c c c c c c c c $. 4146 .04455 . 4463 . 4472 . 4481 . 4489 .04498 . 4507	. 5554 .95545 . 5536 . 5528 . 5519	51 50 49
$\begin{array}{c c c c c c c c c c c c c c c c c c c $.04455 .4463 .4472 .4481 .4489 .04498 .4507	.95545 .5536 .5528 .5519	50 49
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4463 . 4472 . 4481 . 4489 .04498 . 4507	. 5536 . 5528 . 5519	49
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4472 . 4481 . 4489 .04498 . 4507	. 5528 . 5519	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4481 . 4489 .04498 . 4507	. 5519	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.04498 .4507		47
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4507	. 5511	46
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.95502	45
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	11 1000	. 5493	44
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4515	. 5485	43
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4524	. 5476 . 5467	42 41
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.04541	.95459	41
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4550	. 5450	39
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4558	. 5441	38
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4567	. 5433	37
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4576	. 5424	36
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.04585	.95415	35
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4593	. 5407	34
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4602	• 5398	33
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4611	. 5389 . 5380	32
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4619	.95372	31
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4637	. 5363	29
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4646	. 5354	28
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 4654	. 5345	27
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 4663	. 5337	26
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$.04672	.95328	25
38 . 0292 . 9707 . 3011 . 1786 . 1460 .0493	. 4681	. 5319	24
	. 4690 . 4698	. 5310 . 5301	23
39 . 0320 . 9680 . 2981 . 1818 . 1429 .0494	4098	. 5293	22 21
40 .30348 .69652 3.2951 .31850 3.1397 1.0495	.04716	.95284	20
41 . 0375 . 9624 . 2921 . 1882 . 1366 .0496	. 4725	. 5275	19
42 . 0403 . 9597	. 4734	 5266 	18
43 . 0431 . 9569	. 4743	 5257 	17
44 . 0459 . 9541 .2831 . 1978 .1271 .0499	. 4751	. 5248	16
45 .30486 .69513 3.2801 .32010 3.1240 1.0500	.04760	.95239	15
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	4769	5231 5222	14
47 . 0542 . 9458 .2742 . 2074 .1177 .0502 48 . 0569 . 9430 .2712 .2106 .1146 .0503	4778	5213	13 12
49 . 0597 . 9403 . 2683 . 2138 . 1115 .0504	4796	. 5204	11
50 .30625 .69375 3.2653 .32171 3.1084 1.0505	04805	.95195	10
51 . 0653 . 9347	. 4814	. 5186	9
52 . 0680 . 9320 . 2594 . 2235 . 1022 .0507	4823	. 5177	87
53 . 0708 . 9292 .2565 . 2267 .0991 .0508	. 4832	. 5168	17
54 . 0736 . 9264 . 2535 . 2299 .0960 .0509	. 4840	. 5159	6
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$.04849	.95150	5
	4858	. 5141 . 5132	4 2
$\begin{array}{c c c c c c c c c c c c c c c c c c c $. 4807	. 5152	2
59 . 0874 . 9126 . 2390 . 2423 . 0807 . 0513	4885	. 5115	6 5 4 3 2 1
60 . 0902 . 9098 . 2361 . 2492 .0777 .0515	4894	. 5106	ō
M. Cosine. Vrs. sin. Secant. Cotang. Tang. Cosec'in	Vrs. cos.	Sine.	м.

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18	0	N	atural T	rigonor	netrical	Function	o ns.	1	61°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang	Secant	Vrs. sin.	Cosine.	M.
0	.30902	.69098	3.2361	.32492	3.0777	1.0515	.04894	.95106	60
$ \begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{array} $. 0929	. 9071	3.2361 .2332	.32492 . 2524	8.0777 .0746	.0516	. 4903	. 5097	59 58
2	. 0957	. 9043 . 9015	.2303	. 2556	.0716	.0517	4912	. 5088	58
3	. 0985	. 9015	.2274	. 2588	.0686	.0518	. 4921	. 5079	67
4	. 1012	. 8988	.2245	. 2621	.0655 3.0625 .0595	.0519 1.0520	. 4930	. 5070	56 55
- 0 6	1068	.68960 .8932 .8905 .8877	3.2216 .2188	.32653 .2685	0505	1.0520	. 4948	. 5051	54
7	. 1068 . 1095 . 1123	. 8905	.2159	2085	.0565	.0521 .0522 .0523	. 4957	5042	53
7 8	. 1123	8877	.2131	. 2749	.0535	.0523	. 4966	. 5042 . 5033	52
9	1150	1.8849	.2102	. 2782	.0505	1 .0524	. 4975	. 5024	51
10	.31178 .1206 .1233	.68822	3.2074	.32814	3.0475	1.0525 .0526	.04985	.95015	50
11	. 1206	. 8794	.2045	2846	.0445	.0526	. 4994	. 5006	49
12	. 1233	. 8766	.2017	. 2878	.0415 .0385 .0356 3.0326	.0527	. 5003	. 4997	48
13	. 1261	. 8739 . 8711	.1989 .1960	. 2910	.0385	.0527 .0528 .0529 1.0530 .0531 .0532 .0533	. 5012	. 4988	47
$\frac{14}{15}$	$\begin{array}{r} . 1289 \\ .31316 \\ . 1344 \end{array}$. 68684	3.1950	. 2943 .32975	.0356	.0529	. 5021	. 4979 .94970	46
$16 \\ 16$	1214	.08084 8656	.1932	.32970	.0296	1.0030	100030	.94970	45 44
17	1372	. 8656 . 8628	.1876	. 3007 . 3039	.0290	.0531	. 5039 . 5048	. 4961 . 4952	44
18	. 1372 . 1399	. 8601	.1848	. 3072	.0237	0533	11 5057	4942	42
19	1427	. 8573	.1820	. 3104	.0208	.0534	. 5066	4933	41
20	.31454 . 1482	.68545 . 8518	$.1820 \\ 3.1792$.33136	3.0178	1.0535	. 5066 .05076 . 5085 . 5094	.94924	40
21	. 1482	. 8518	.1764	. 3169	.0149	.0536	. 5085	. 4915	39
22	. 1510	. 8490	.1736	. 3201	.0120 .0090	.0537 .0538	. 5094	. 4906	38 37
23	.1537 .1565 .31592	. 8463	.1708	. 3233	.0090	.0538	11 5103	. 4897	37
24	1560	. 8435	.1681	. 3265	.0061 3.0032	.0539	. 5112	. 4888 .94878	136
20	1690	.68407 .8380	3.1653 .1625 .1598 .1570	.33298 . 3330	3.0032	$.0539 \\ 1.0540 \\ .0541 $.05121 .5131	.94878	35
20	1648	8250	.1020	• 333U 9960	.0003 2.9974	.0541	· 5131	. 4869	34
28	1675	. 8352 . 8325 . 8297	1570	. 3362 . 3395	.9945	.0542	. 5140	. 4860 . 4851	33 32
29	1703	8297	1543	3427	9916	0544	. 5149 . 5158	. 4841	31
20 21 22 23 24 25 26 27 28 29 30 31 32 33	.31592 .1620 .1648 .1675 .1703 .31730 .1758 .1758	1.68269 I	$.1543 \\ 3.1515$. 3427 .33459	.9916 2.9887	$.0544 \\ 1.0545$.05168	.94832	30
31	. 1758	. 8242	$.1488 \\ .1461 \\ .1433$. 3492	.9858	.0546	. 5177	. 4823	29
32	• 1700	. 8214	.1461	. 3524	.9829	05.17	5186	. 4814	28
33	. 1813	. 8187	.1433	. 3557	.9800	.0548 .0549 1.0550 .0551	. 5195 . 5205	. 4805	27
34 35	. 1841	. 8159	.1406 3.1379 .1352	. 3589	.9772 2.9743	.0549	. 5205	. 4795	26
36	. 1841 .31868 . 1896 . 1923 . 1951 . 1978 .32006	.68132 . 8104	3.1379	.33621 . 3654	2.9743	1.0550	.05214	.94786	25
37	1923	8076	.1325	2696	.9714	.0551	. 5223 . 5232	. 4777	24
37 38	1951	. 8076 . 8049	1968	.3686 .3718	.9686 .9657	.0552	. 0252	. 4767 . 4758	23
39	. 1978	1, 8021	$\begin{array}{c} .1271 \\ 3.1244 \\ .1217 \end{array}$	3751	9629	.0553 .0554 1.0555	.5242 .5251	. 4758	22 21
40	.32006	.67994	3.1244	.33783	.9629 2.9600	1.0555	.05260	.94740	20
41	+ 200 9	. 7966 . 7939	.1217	. 3816	.9572	0556	5270	. 4730	19
42	2061	• 7939	$.1190 \\ .1163$. 3848	.9544	.0557	. 5279	4721	18
43	2089 2116	. 7911	.1163	. 3880	.9515	.0557 .0558 .0559 1.0560 .0561	. 5279 . 5288	4721 4712	18 17
4 4 45	• 2110	.7884 .67856	.1137	. 3913	.9487 2.9459	.0559	. 5297 .05307	. 4702 .94693	16
46	.32144 2171	-07800	3.1110	.33945 . 3978	2.9459	1.0560	.05307	.94693	$\tilde{15}$
47	2199	. 7828 . 7801 . 7773	.1083 .1057 .1030	. 4010	.9431	.0561	. 5316	. 4684	14
48	. 2226	7773	1030	. 4043	.9403	.0002	. 5326 . 5335	. 4674	13
49 50	. 2254	. 7746	.1004	. 4075	9347	.0563 .0565	. 5344	. 4665 . 4655	$\frac{12}{11}$
50	.32282	.67718	3.0977	.34108	.9347 2.9319	1.0566	.05354	.94646	10
$\frac{51}{52}$ $\frac{53}{53}$	 2309 	. 7691 . 7663	.0951	. 4140	.9291	.0567	. 5363	. 4637	
52	2337	. 7663	.0925	. 4173	.9263	0560	. 5373	4627	8
53	. 2364	. 7636	.0898	. 4205	.9235	.0569 .0569 .0570 1.0571 .0572 .0573	. 5373 . 5382	. 4627 . 4618	9 8 7 6 5
54 55	. 2392 .32419	. 7608	.0872	. 4205 . 4238 .34270 . 4303	.9208 2.9180	.0570	. 5391	. 4608	6
56	-02419 -0445	.67581	3.0846 .0820	.34270	2.9180	1.0571	.05401	.94599	5
57	. 2447 . 2474	. 7553 . 7526	.0820	. 4303	.9152 .9125	.0572	. 5410	. 4590	4
57 58	2502	. 74 <u>98</u>	.0767	. 4368	.9125	.0573 .0574	. 5420	. 4580	3
59	2529	7471	.0741	. 4400	.9069	.0574	5429	. 4571	2
60	. 2557	. 7443	.0715	4433	.9042	.0576	5448	. 4561 . 4552	$1 \\ 0$
-	~ .						0110	. 4004	0
M .	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	М.
108	0								

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Natural Trigonometrical Functions

Natural Trigonometrical Functions.

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19-		118	culai II	Igonom	cuicai i	unction	13.	10	J0-
М.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.32557	.67443	3.0715	.34433	2,9042	1.0576	.05448	.94552	60
1	. 2584	. 7416	.0690	. 4465	.9015	.0577	. 5458	. 4542	59
2	.2612	. 7388	.0664	. 4498	.8987	.0578	. 5467	. 4533	58
3	. 2639	. 7361	.0638	. 4530	.8960	.0579	. 5476	4523	57
4 5 6	. 2667	. 7333	.0612	. 4563	.8933	.0580	. 5486	. 4514	56
ð	.32694 . 2722	.67306	3.0586	.34595	2.8905	1.0581	.05495	.94504	55
7	2749	. 7278 . 7251	.0561 .0535	.4628 .4661	.8878	.0582 .0584	. 5505 . 5515	.4495 .4485	54
8	2777	7223	.0509	4693	.8824	.0585	5524	. 4476	52
ğ	. 2804	7196	.0484	4726	.8797	.0586	5534	4466	51
10	.32832	.67168	3.0458	.34758	2.8770	1.0587	.05543	.94457	50
11	. 2859	. 7141	.0433	. 4791	.8743	.0588	. 5553	. 4447	49
12	. 2887	. 7113	.0407	. 4824	.8716	.0589	. 5562	. 4438	48
13	. 2914	. 7086	.0382	. 4856	.8689	.0590	. 5572	. 4428	47
$\frac{14}{15}$. 2942 .32969	. 7058	.0357 3.0331	. 4889 .34921	.8662 2.8636	.0591 1.0592	. 5581	. 4418	46
16	. 2996	. 7003	.0306	. 4954	.8609	.0593	. 5601	. 4399	40
17	. 3024	6976	.0281	4987	.8582	.0594	. 5610	. 4390	43
18	. 3051	. 6948	.0256	. 5019	.8555	.0595	. 5620	4380	42
19	. 3079	. 6921	.0231	. 5052	.8529	.0596	. 5629	. 4370	41
$\frac{1}{20}$.33106	.66894	3.0206	.35085	2.8502	1.0598	.05639	.94361	40
21	. 3134	. 6866	.0181	. 5117	.8476	.0599	. 5649	. 4351	39
$\frac{22}{23}$. 3161	. 6839	.0156	. 5150	.8449	.0600	. 5658	. 4341	38
23	. 3189 . 3216	. 6811	.0131	. 5183	.8423	.0601	. 5668	4332	37
$\frac{1}{24}$.33243	. 6784 .66756	.0106	. 5215 .35248	.8396 2.8370	.0602 1.0603	. 5678	. 4322	36 35
26	. 3271	. 6729	.0056	. 5281	.8344	.0604	. 5697	. 4303	34
27	3298	6701	.0031	. 5314	.8318	.0605	. 5707	4293	33
27 28 29	. 3326	. 6674	.0007	. 5346	.8291	.0606	. 5716	. 4283	32
29	. 3353	. 6647	2.9982	. 5379	.8265	.0607	. 5726	. 4274	31
30	.33381	.66619	2.9957	.35412	2.8239	1.0608	.05736	.94264	30
31	. 3408	. 6592	.9933	. 5445	.8213	.0609	. 5745	. 4254	29 28 27
$\frac{32}{33}$. 3435	. 6564	.9908	5477	.8187 .8161	.0611	5755 5765	. 4245 . 4235	28
33 34	· 3463 · 3490	. 6537 . 6510	.9859	. 5510 . 5543	.8135	.0612	. 5775	4235	26
35	.33518	.66482	2.9835	.35576	2.8109	1.0614	.05784	.94215	25
36	. 3545	. 6455	.9810	. 5608	.8083	.0615	. 5794	. 4206	24
37	. 3572	. 6427	.9786	. 5641	.8057	.0616	. 5804	. 4196	23
38	. 3600	. 6400	.9762	. 5674	.8032	.0617	. 5814	. 4186	22
39	. 3627	. 6373	.9738	. 5707	.8006	.0618	. 5823	. 4176	21
40	.33655	.66345	2.9713	.35739	2.7980	1.0619	.05833	.94167	20
41 42	. 3682 . 3709	. 6318 . 6290	.9689	. 5772 . 5805	.7954	.0620 .0622	. 5843 . 5853	. 4157	19 18
43	3737	. 6263	.9641	. 5838	.7903	.0623	5863	4137	17
44	3764	6236	.9617	. 5871	.7878	.0624	. 5872	4127	16
$\overline{45}$	33792	.66208	2,9593	.35904	2.7852	1.0625	.05882	.94118	15
46	. 3819	. 6181	.9569	. 5936	.7827	.0626 .0627	. 5892	. 4108	14
47	. 3846	. 6153	.9545	. 5969	.7801	.0627	. 5902	. 4098	13
48	. 3874	. 6126	.9521	. 6002	.7776	.0628	. 5912	. 4088	12
49	. 3901 .33928	. 6099	.9497	. 6035	.7751 2.7725	.0629	. 5922	. 4078	11
$\frac{50}{51}$. 3956	.66071 .6044	2.9474	.36068	.7700	1.0630 .0632	. 5941	. 4058	10
52	3983	6017	.9426	. 6134	.7675	.0633	. 5951	. 4049	8
53	. 4011	. 5989	.9402	. 6167	.7650	.0634	. 5961	4039	17
54	. 4038	. 5962	.9379	. 6199	.7625	.0635	. 5971	. 4029	9 8 7 6 5
55	.34065	.65935	2.9355	.36232	2.7600	1.0636	.05981	.94019	
56	. 4093	. 5907	.9332	. 6265	.7574	.0637	. 5991	. 4009	4
57	. 4120	. 5880	.9308	. 6298	.7549	.0638	. 6001	. 3999	3
58	. 4147	. 5853	.9285	. 6331	.7524	.0639	. 6011	. 3989	3 2 1
59 60	.4175 .4202	5825	.9261	. 6364 . 6397	.7500	.0641	. 6021	. 3979 . 3969	
00	. 4202	. 0100	.9400	. 0057	.1410	.0014	. 0031	. 0 00 9	<u> </u>
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.
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o	4	:4

20°

Natural Trigonometrical Functions.

1590

20	Adular Higonometrical Functions.								
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.34202	.65798	2.9238	.36397	2.7475	1.0642	.06031	.93969	60
1	. 4229	. 5771	.9215	. 6430	.7450	.0643	. 6041	. 3959	159
$\frac{1}{2}$. 4257	. 5743	.9191	. 6463	.7425	.0644	. 6051	. 3949	58 57
3	. 4284	. 5716	.9168	. 6496	.7400	.0645	. 6061	. 3939	57
4	. 4311	. 5689	.9145	. 6529	.7376	.0646	. 6071	. 3929	56
4 5 6 7	.34339	.65661	2.9122	.36562	2.7351	1.0647	.06080	.93919	55
6	. 4366	. 5634	.9098	. 6595	.7326	.0648	. 6090	. 3909	54
	. 4393	. 5607	.9075	. 6628	.7302	.0650	. 6100	. 3899	53
8	. 4421	. 5579	.9052	. 6661	.7277	.0651	. 6110	. 3889	52
.9	. 4448	. 5552	.9029	. 6694	.7252	.0652	. 6121	. 3879	51
10	.34475	.65525	2.9006	.36727	2.7228	1.0653	.06131	.93869	50
$\frac{11}{12}$. 4502 . 4530	. 5497	.8983	. 6760	.7204	.0654	6141	. 3859	49
	. 4030	. 5470	.8960	. 6793	.7179	.0655	. 6151	. 3849	48
$\frac{13}{14}$. 4557 . 4584	. 5443	.8937	. 6826	.7155	.0656	6161	. 3839	47
14	. 4564	. 5415	.8915 2.8892	. 6859 .36892	.7130	.0658	. 6171	. 3829 .93819	46
16	. 4639	. 5361	.8869	. 6925	$2.7106 \\ .7082$	1.0659	.06181		45
17	. 4666	. 5334	.8846	6958	.7053	.0660	. 6191	. 3809 . 3799	44
18	. 4693	. 5306	.8824	. 6991	.7033	.0661 .0662	.6201 .6211 .6221	3789	42
19	. 4721	. 5279	.8801	. 7024	.7009	.0663	6991	3779	41
20	.34748	65252	2.8778	.37057	2.6985	1.0664	.06231	.93769	40
$\overline{21}$. 4775	65252 5225	.8756	. 7090	.6961	.0666	. 6241	3758	39
22	. 4803	. 5197	.8733	. 7123	.6937	.0667	. 6251	3748	38
23	. 4830	. 5170	.8711	7156	.6913	.0668	6262	3738	37
24	. 4857	. 5143	.8688	7190	.6889	.0669	. 6272	3728	36
$\frac{25}{26}$.34884	.65115	2.8666	.37223	2.6865	1.0670	.06282	.93718	35
26	. 4912	. 5088	.8644	. 7256	.6841	.0671	. 6292	. 3708	34
27	. 4939	. 5061	.8621	. 7289	.6817	.0673	. 6302	. 3698	33
28	. 4966	. 5034	.8599	. 7322	.6794	.0674	. 6312	. 3687	32
29	. 4993	. 5006	.8577	. 7355	.6770	.0675	. 6323	. 3677	31
30	,35021	.64979	2.8554	.37388	2.6746	1.0676	.06333	.93667	30
31	. 5048	. 4952 . 4925	.8532	. 7422	.6722	.0677	. 6343	. 3657	29 28
$\frac{32}{33}$.5075 .5102	. 4925	.8510	. 7455	.6699	.0678	. 6353	. 3647	28
34	. 5130	. 4870	.8488 .8466	. 7488 . 7521	.6675	.0679	. 6363	. 3637	27
35	.35157	.64843	2.8444	. 7521	$.6652 \\ 2.6628$.0681	. 6373	. 3626	26
36	. 5184	. 4816	.8422	7587	.6604	1.0682 .0683	.06384	.93616	26 25 24
37	. 5211	. 4789	.8400	7621	.6581	.0684	. 6394 . 6404	. 3606 . 3596	24 23
38	. 5239	. 4761	.8378	. 7654	.6558	.0685	6414	. 3585	20
39	. 5266	. 4734	.8356	7687	.6534	.0686	6495	3575	22 21
40	.35293	.64707	2.8334	.37720	2.6511	1.0688	.6425 .06435	.93565	20
41	. 5320	. 4680	.8312	7754	.6487	.0689	. 6445	. 3555	19
42	. 5347	. 4652	.8290	. 7787	.6464	.0690	. 6456	. 3544	18
43	. 5375	. 4625	.8269	. 7820	.6441	.0691	. 6466	3534	17
44	. 5402	. 4598	.8247	. 7853	.6418	.0692	. 6476	3524	16
45	.35429	.64571	2.8225	.37887	2.6394	1.0694	.06486	.93513	$\overline{15}$
46 47	. 5456	. 4544	.8204	. 7920	.6371	.0695	. 6497	. 3503	14
48	.5483 .5511	. 4516	.8182	. 7953	.6348	.0696	. 6507	. 3493	13
49	. 5538	. 4489 . 4462	.8160 .8139	. 7986	.6325	.0697	. 6517	. 3482	12
50	.35565	.64435	2.8117	. 8020	.6302	.0698	. 6528	. 3472	11
51	. 5592	. 4408	.8096	.38053	2.6279	1.0699	.06538	.93462	10
52	. 5619	. 4380	.8090	. 8086 . 8120	.6256	.0701	. 6548	. 3451	9
53	. 5647	4353	.8053	. 8153	.6233 .6210	.0702	. 6559	. 3441	8
54	. 5674	4326	.8032	8186	.6187	.0703	. 6569	. 3431	$\frac{7}{6}$
55	.35701	.64299	2.8010	.38220	2.6167	1.0705	. 6579	. 3420	6
56	. 5728	. 4272	.7989	. 8253	.6142	.0707	. 6600	.93410	5 4 3 2
57	. 5755	4245	.7968	8286	.6119	.0708	.6611	. 3400	2
58	. 5782	4217	.7947	8320	.6096	.0709	.6621	3379	0
59	. 5810	. 4190	.7925	8353	.6073	.0710	. 6631	3368	ī
60	. 5837	. 4163	.7904	. 8386	.6051	.0711	. 6642	3358	õ
M.	Corine	Van air							_
<u>m.</u>	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	м.

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210 Natural Trigonometrical Functions. 158° M Sine. Cosec'nt Tang. Cotang. Secant. Vrs. sin. Cosine. M Vrs. cos. .35837 .64163 2.7904.38386 2 6051 1.0711 06642 .93358 60 0 . 5864 . 4136 . 8420 .0713 . 6652 . 3348 1 .7883 .6028 59 . 5891 . 8453 .6006 6663 3337 4109 .7862 .0714 58 2 3 5918 4082 .7841 . 8486 .5983 .0715 . 6673 . 3327 57 3316 4 5945 4055 7820 8520 .5960 .0716 6684 56 2.5938 .06694 .93306 .35972 .64027 2.7799.38553 1.0717 5 55 .5916 . 6705 3295 6 . 6000 4000 .7778 8587 .0719 $\overline{54}$. 3285 ž . 6027 3973 .7757 8620 .5893 .0720 6715 53 . . 6054 3946 7786 8654 .5871 .0721 6726 3274 528 0722 3264 6736 51 ğ 6081 3919 .77158687 .584893253 .36108 2.7694.38720 2.58261.0723 .06747 50 .63892 10 . 6757 6135 3865 7674 . 8754 .5804.0725 3243 49 11 3232 7653 12 6162 3837 8787 5781 .07266768 48 . .0727 3222 8821 .5759 6778 13 6189 3810 .763247• • .0728 3211 14 6217 3783 7611 8854 5737 6789 $\bar{4}6$.93201 36244 .38888 1.0729 15 .63756 2.75912.5715.06799 45 6271 3729 .7570 8921 .5693 .0731 6810 3190 $\overline{44}$ 16 . 0732 6820 3180 6298 8955 17 3702 .7550.5671 43 . 7529 3169 3158 6325 8988 5640 .0733 6831 42 3675 18 . 19 6352 3648 .7509 2.7488 9022 .5627 .0734 6841 41 .93148 20 21 22 36379 .63621 .39055 2.5605.068521.073640 3593 7468 .5583 6863 3137 30 6406 9089 .0737 . • 3566 .7447 5561 6873 3127 6433 9122 .073838 23 24 25 6884 3116 6460 3539 .7427 9156 .5539.0739 37 6488 3512 .7406 9189 .5517 .07406894 3105 36 .39223 .93095 .36515 .63485 2.7386 2.54951.074206905 35 .7366 266542 3458 9257 .5473 .07436916 3084 34 27 28 29 .0744 6926 3074 6569 3431 7346 9290 .5451 33 6937 6596 7325 9324 .5430 .0745 3063 $\tilde{32}$ 3404 . • . . 6623 3377 .7305 9357 5408 .0747 6947 3052 31 2.53861.0748 93042 30 36650 .63350 2.7285.39391 .06958<u>30</u> 6969 3031 2**9** 3323 7265 9425 .5365 .0749 31 6677 . . • .7245 53433020 32 6704 3296 9458 0750 6979 $2\dot{8}$.7225 33 6731 3269 9492 .5322.0751 6990 3010 27• .7205 .0753 7001 2999 $\dot{3}\dot{4}$ 6758 324295255300 26.07012 .36785 2.71852.527892988 .6321439559 1.0754 2535 . 6812 2978 3187 .7165 9593 5257 .07557022 $2\overline{4}$ 36 2967 . 6839 7033 37 3160 .7145 9626 .5236 .0756 23 . .5214 .0758 7044 2956 $\tilde{2}\tilde{2}$ 6866 3133 .71259660 38 . 6893 3106 .71052.7085 9694 5193 .0759 7054 2945 $2\overline{1}$ 39 .36921 92935 .63079 .39727 2.51711.0760 .07065 $\overline{20}$ $\overline{40}$ 7076 2924 .7065 9761 19 41 6948 3052.5150.0761• 2913 6975 3025 .7045 9795 5129 .0763 7087 18 42 . 7002 ,7026 2998 9828 .5108 .0764 7097 290217 43 . 2971 .7006 .5086 7108 2892 44 7029 9862.076516 37056 2,5065 07119 .92881 45 .629442.6986.39896 1.0766 15 7130 5044.0768 2870 7083 2917 .6967 9930 46 14 . 7110 2890 .6947 9963 5023.0769 7141 $\bar{2}859$ 13 47 2848 7137 2863 .6927 9997 5002 .0770 7151 1248 7164 2836 2838 .6908 .40031 .4981 .0771716211 49 37191 2.6888.40065 2.4960 .07173 92827 .62809 1.0773 10 50 7218 2782 .6869 0098 .4939 .0774 7184 2816 51 a 7245 2755 .49187195 2805 8 52.6849 0132 .0775• . 7205 7272 2728 .6830 .4897 27947 53 0166 .0776 ٠ 7299 2701 .6810 0200 4876 0778 7216 27846 54.37326 .40233 92773 55.62674 2.6791 2.48551.0779.07227 5 2762 7238 56 7353 2647 0267 .4834 .07804 .6772. • .4813 .0781 7249 2751 ŝ 57 7380 2620.6752 0301• 2593 .6733 0335 .4792 .0783 7260 2740 58 7407 21 . . 2729 7271 7434 2566.6714 0369 .4772 .078459. • 2539 .0785 7282. 2718 ō 60 7461 .6695 0403 .4751. M. Cosine. Vrs. sin. Secant. Cotang. Tang. Cosec'nt Vrs. cos. Sine. Μ.

344 22°

Natural Trigonometrical Functions.

157°

229	,	Natural Trigonom			etrical	1570			
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosino.	М.
0	.37461	.62539	2,6695	.40403	2.4751	1.0785	.07282	.92718	60
1	. 7488	. 2512	.6675	. 0436	.4730	.0787	. 7292	. 2707	59
2	. 7514	, 2485	.6656	. 0470	.4709	.0788	. 7303	. 2696	58
3	. 7541	. 2458	.6637	. 0504	.4689	.0789	. 7314	. 2686	57
234567	. 7568 .37595	. 2431	.6618	. 0538	.4668	.0790	. 7325	. 2675 .92664	56 55
e G	. 7622	.62404	2.6599 .6580	.40572	2.4647	1.0792 .0793	.07336	. 2653	54
7	. 7649	2351	.6561	. 0640	.4606	.0794	. 7358	2642	53
8	. 7676	2324	.6542	. 0673	.4586	.0795	. 7369	2631	52
8	. 7703	. 2297	.6523	. 0707	.4565	.0797	. 7380	. 2620	51
10	.37730	.62270	2.6504	.40741	2.4545	1.0798	.07391	.92609	50
11	. 7757	. 2243	.6485	. 0775	.4525	.0799	. 7402	. 2598	49
12	. 7784	. 2216	.6466	. 0809	.4504	.0801	. 7413	. 2587	48
13	. 7811	. 2189	.6447	. 0843	.4484	.0802	. 7424	. 2576 . 2565	47
14 15	. 7838 .37865	.2162 .62135	2.6410	. 0877	.4463 2.4443	1.0803	. 7435	. 2000	46
16	. 7892	. 2108	.6391	. 0945	.4423	.0806	. 7457	. 2543	44
17	. 7919	2081	.6372	. 0979	.4403	.0807	. 7468	2532	43
18	. 7946	. 2054	.6353	. 1013	.4382	.0808	. 7479	2521	42
19	. 7972	. 2027	.6335	. 1047	.4362	.0810	. 7490	.2510	41
20	.37999	.62000	2.6316	.41081	2.4342	1.0811	.07501	.92499	40
21	. 8026	. 1974	.6297	. 1115	.4322	.0812	. 7512	. 2488	39
22	. 8053	. 1947	.6279	. 1149	.4302	.0813	. 7523	. 2477	38
23	. 8080 . 8107	.1920 .1893	.6260 .6242	.1183 .1217	.4282 .4262	.0815 .0816	. 7534 . 7545	. 2466 . 2455	37 36
$\frac{24}{25}$.38134	.61866	2.6223	.41251	2.4242	1.0817	.07556	.92443	35
-26	. 8161	. 1839	.6205	. 1285	.4222	.0819	. 7567	. 2432	34
27 28 29	. 8188	. 1812	.6186	1319	.4202	.0820	. 7579	. 2421	33
28	. 8214	. 1785	.6168	. 1353	.4182	.0821	. 7590	. 2410	33 32
29	. 8241	. 1758	.6150	. 1387	.4162	.0823	. 7601	. 2399	31
30	.38268	.61732	2.6131	.41421	2.4142	1.0824	.07612	.92388	30
31	. 8295	. 1705	.6113	. 1455	.4122	.0825	. 7623	. 2377	29
32 33	• 8322 • 8349	.1678 .1651	.6095	.1489 .1524	.4102	.0826 .0828	7634	. 2366 . 2354	28 27
33 34	. 8376	. 1624	.6058	1524	.4063	.0828	7657	· 2343	26
35	.38403	.61597	2.6040	.41592	2.4043	1.0830	.07668	.92332	$\frac{26}{25}$
36	. 8429	. 1570	.6022	. 1626	.4023	.0832	. 7679	. 2321	$\tilde{24}$
37	 8456 	. 1544	.6003	. 1660	.4004	.0833	. 7690	. 2310	23
38	. 8483	. 1517	.5985	. 1694	.3984	.0834	. 7701	2299	$\frac{23}{22}$
39	. 8510	. 1490	.5967	. 1728	.3964	.0836	. 7712	. 2287	21
40	.38537	.61463	2.5949	.41762	2.3945	1.0837	.07724	.92276	20
41 42	. 8564 . 8591	. 1436 . 1409	.5931 .5913	• 1797 • 1831	.3925 .3906	.0838	. 7735 . 7746	. 2265 . 2254	19 18
$\frac{12}{43}$. 8617	. 1382	.5895	. 1865	.3886	.0841	. 7757	2242	17
44	. 8644	. 1356	.5877	. 1899	.3867	.0842	. 7769	2231	16
45	.38671	.61329	2.5859	.41933	2.3847	1.0844	.07780	.92220	$\tilde{15}$
46	. 8698	. 1302	.5841	. 1968	.3828	.0845	7791	. 2209	14
47	. 8725	. 1275	.5823	. 2002	.3808	.0846	. 7802	. 2197	13
48	. 8751	. 1248	.5805	. 2036	.3789	.0847	. 7814	. 2186	12
49	.8778 .38805	.1222 .61195	.5787	. 2070	.3770	.0849	. 7825	. 2175	11
50 51	. 8832	. 1168	2.5770 .5752	.42105 . 2139	2.3750 .3731	1.0850 .0851	.07836 .7847	.92164 . 2152	10
$\frac{51}{52}$	8859	: 1141	.5734	2173	.3712	.0853	. 7859	2132	8
53	. 8886	. 1114	.5716	2207	.3692	.0854	7870	2130	7
54	. 8912	. 1088	.5699	2242	.3673	.0855	7881	2118	6
55	.38939	.61061	2.5681	.42276	2.3654	1.0857	.07893	.92107	9 8 7 6 5 4
56	. 8966	. 1034	.5663	, 2310	.3635	.0858	7904	. 2096	4
57	. 8993	. 1007	.5646	. 2344	.3616	.0859	. 7915	. 2084	3 2
58 59	. 9019	. 0980	.5628	. 2379	.3597	.0861	. 7927	. 2073	2
59 60	. 9046 . 9073	• 0954 • 0927	.5610 .5593	.2413 .2447	.3577	.0862	. 7938	. 2062 . 2050	$1 \\ 0$
-						.0864			
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

112°

Natural Trigonometrical Functions.

156°

23	Natural Trigonom			etrical Functions.			190-		
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.39073	.60927	2.5593	.42447	2.3558	1.0864	.07949	.92050	60
1	. 9100	. 0900	.5575	2482 2516	.3539	.0865	. 7961	. 2039	59
2 3	· 9126	. 0873	.5558		.3520	.0866	. 7972	. 2028	58 57
	. 9153	. 0846	.5540	. 2550	.3501	.0868	. 7984	. 2016	57
4 5	. 9180	. 0820	.5523	. 2585	.3482	.0869	. 7995	. 2005	56
5	.39207	.60793	2.5506	.42619	2.3463	1.0870	.08006	.91993	55
6 7	. 9234	. 0766	.5488	. 2654	.3445	.0872	. 8018	. 1982	54
7	. 9260	. 0739	.5471	. 2688	.3426	.0873	. 8029	. 1971	53
8	. 9287 . 9314	. 0713	.5453	. 2722	.3407	.0874	. 8041	. 1959	52
9	. 9314	. 0686	.5436	. 2757 .42791	.3388	.0876 1.0877	. 8052	. 1948	51 50
$\frac{10}{11}$. 9367	. 0632	2.5419	. 2826	2.3369	.0878	. 8075	. 1925	49
12	9394	. 0606	.5384	2860	.3332	.0880	. 8086	. 1913	48
13	9421	. 0579	.5367	2894	.3313	.0881	. 8098	1902	47
14	. 9448	. 0552	.5350	2929	.3294	.0882	. 8109	1891	46
15	.39474	.60526	2.5333	.42963	2.3276	1.0884	.08121	91879	45
16	. 9501	. 0499	.5316	. 2998	* .3257	.0885	. 8132	. 1868	44
17	. 9528	. 0472	.5299	. 3032	.3238	.0886	. 8144	. 1856	43
18	. 9554	. 0445	.5281	. 3067	.3220	.0888	. 8155	. 1845	42
19	. 9581	. 0419	.5264	. 3101	.3201	.0889	. 8167	. 1833	41
20	.39608	.60392	2.5247	.43136	2.3183	1.0891	.08178	.91822	40
21	. 9635	. 0365	.5230	. 3170	.3164	.0892	. 8190	. 1810	39
22	. 9661	. 0339	.5213	. 3205	.3145	.0893	. 8201	. 1798	38
23	. 9688	. 0312	.5196	. 3239	.3127	.0895	. 8213	. 1787	37
24 25	. 9715	. 0285	.5179	. 3274	.3109	.0896	. 8224	. 1775	36
25 26	.39741	.60258 .0232	2.5163	.43308	2.3090	1.0897	.08236	.91764 . 1752	35
$\frac{20}{27}$. 9795	. 0205	.5140	. 3377	.3053	.0899	· 8248 · 8259	. 1752	33
28	. 9821	. 0178	.5125	. 3412	.3035	.0900	. 8259	. 1729	32
29	9848	. 0152	.5095	. 3447	.3017	.0903	. 8282	1718	31
30	.39875	.60125	2.5078	.43481	2.2998	1.0904	.08294	.91706	30
31	. 9901	. 0098	.5062	. 3516	.2980	.0906	. 8306	. 1694	29
32	. 9928	. 0072	.5045	. 3550	.2962	.0907	. 8317	. 1683	28
33	. 9955	. 0045	.5028	. 3585	.2944	.0908	. 8329	. 1671	27
34	. 9981	. 0018	.5011	. 3620	.2925	.0910	. 8340	. 1659	26
35	40008	.59992	2.4995	.43654	2.2907	1.0911	.08352	.91648	25
36	. 0035	. 9965	.4978	. 3689	.2889	.0913	. 8364	. 1636	24
37	. 0061	• 9938	.4961	. 3723	.2871	.0914	. 8375	. 1625	23
38 39	. 0088	. 9912 . 9885	.4945	. 3758	.2853	.0915	. 8387	. 1613	22
39 40	. 0115	. 9885	.4928 2.4912	.3793 .43827	.2835 2.2817	.0917 1.0918	. 8399 .08410	.1601 .91590	21 20
41	. 0168	, 9832	.4895	. 3862	.2799	.0920	. 8422	.1578	19
42	. 0195	. 9805	.4879	. 3897	.2781	.0921	. 8434	. 1566	18
43	. 0221	. 9778	.4862	3932	.2763	.0922	. 8445	. 1554	17
44	. 0248	. 9752	.4846	. 3966	.2745	.0924	. 8457	. 1543	16
45	.40275	.59725	2.4829	.44001	2.2727	1.0925	.08469	.91531	15
4 6	. 0301	. 9699	.4813	. 4036	·2709	.0927	. 8480	. 1519	14
47	. 0328	. 9672	.4797	. 4070	.2691	.0928	. 8492	. 1508	13
48	. 0354	. 9645	.4780	. 4105	.2673	.0929	. 8504	. 149 6	12
49	. 0381	. 9619	.4764	. 4140	.2655	.0931	. 8516	. 1484	11
50	.40408	.59592	2.4748	.44175	2.2637	1.0932	.08527	.91472	10
51	. 0434	. 9566	.4731	. 4209 . 4244	.2619	.0934	. 8539	. 1461	9
52	. 0461	. 9539	.4715		.2602	.0935	. 8551	. 1449	8
53 54	. 0487 . 0514	. 9512 . 9486	.4699 .4683	.4279 .4314	.2584	.0936 .0938	. 8563 . 8575	. 1437 . 1425	76
55	.40541	.59459	2.4666	.44349	2.2548	1.0939	.08586	. 1425	5
56	. 0567	. 9433	.4650	. 4383	.2531	.0941	. 8598	. 1402	4
57	. 0594	. 9406	.4634	4418	.2513	.0942	. 8610	1390	3
58	. 0620	9379	.4618	4453	.2495	.0943	8622	1378	
59	. 0647	9353	.4602	. 4488	.2478	.0945	. 8634	. 1366	2
60	. 0674	. 9326	.4586	4523	.2460	.0946	. 8645	. 1354	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	м.

113°

66°

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346 24°

Natural Trigonometrical Functions.

155°

24	,	Na	tural II	rigonom	etricai	Function	ns.	1	55
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang,	Secant.	Vrs. sin.	Cosine.	M.
0	.40674	,59326	2.4586	.44523	2.2460	1.0946	.08645	.91354	60
1	. 0700	. 9300	.4570	. 4558	.2443	.0948	. 8657	. 1343	59
2	. 0727	. 9273	.4554	. 4593	.2425	.0949	. 8669	. 1331	58
34	. 0753	. 9247	.4538	. 4627	.2408	.0951	. 8681	. 1319	57
4	. 0780	. 9220	.4522	. 4662	.2390	.0952	. 8693	. 1307	56
5 6 7	.40806	.59193	2.4506	.44697	2.2373	1.0953	.08705	.91295	55
6	. 0833	. 9167	.4490	. 4732	.2355	.0955	. 8716	. 1283	54
8	. 0860 . 0886	.9140 .9114	.4474 .4458	. 4767 . 4802	.2338	.0956 .0958	. 8728 . 8740	.1271 .1260	53 52
9	.0000	. 9087	.4442	4802	.2303	.0959	8752	. 1248	51
10	.40939	.59061	2.4426	.44872	2.2286	1.0961	.08764	.91236	50
11	. 0966	. 9034	.4411	. 4907	,2268	.0962	. 8776	. 1224	49
12	0992	9008	.4395	. 4942	.2251	.0963	8788	1212	48
13	1019	. 8981	4379	. 4977	.2234	.0965	. 8800	. 1200	47
14	. 1045	. 8955	.4363	. 5012	.2216	.0966	. 8812	. 1188	46
15	.41072	.58928	2.4347	.45047	2.2199	1.0968	.08824	.91176	45
16	. 1098	. 8901	.4332	. 5082	.2182	.0969	. 8836	. 1164	44
17	. 1125	. 8875	.4316	. 5117	.2165	.0971	. 8848	. 1152	43 42
18	. 1151	. 8848	.4300	. 5152	.2147	.0972	. 8860	. 1140	42
19	.1178 .41204	. 8822 .58795	2,4285 2,4269	.5187 .45222	2.2130 2.2113	.0973 1.0975	.8872 .08884	.1128 .91116	40
$\frac{20}{21}$. 1231	. 8769	.4254	. 5257	.2096	.0976	. 8896	. 1104	39
22	. 1257	. 8742	.4238	5292	.2030	.0978	. 8908	1092	38
23	1284	. 8716	4222	5327	.2062	.0979	. 8920	: 1080	37
24	, 1310	. 8689	4207	. 5362	.2045	,0981	. 8932	. 1068	36
25	.41337	.58663	2,4191	.45397	2.2028	1.0982	.08944	.91056	35
26	. 1363	. 8636	.4176	. 5432	.2011	.0984	. 8956	. 1044	34
27	. 1390	. 8610	.4160	. 5467	.1994	.0985	. 8968	. 1032	33
28	. 1416	. 8584	.4145	. 5502	.1977	.0986	. 8980	1020	32
29	. 1443	. 8557 .58531	.4130	. 5537	.1960	.0988	. 8992	. 1008	31 30
$\frac{30}{31}$.41469 . 1496	. 8504	2.4114 .4099	.45573	2.1943 .1926	1.0989 .0991	.09004	.90996 . 0984	29
$\frac{31}{32}$. 1450	. 8478	.4083	. 5643	.1920	.0992	9028	. 0972	28
33	1549	. 8451	.4068	. 5678	1892	.0994	9040	0960	27
34	1575	. 8425	.4053	5713	1875	.0995	. 9052	. 0948	26
35	41602	.58398	2.4037	.45748	2.1859	1.0997	.09064	.90936	25
36	. 1628	. 8372	.4022	. 5783	.1842	.0998	. 9076	. 0924	24
37	. 1654	. 8345	.4007	. 5819	.1825	.1000	. 9088	. 0911	23
38	. 1681	. 8319	.3992	. 5854	.1808	.1001	. 9101	. 0899	22 21
39 40	.1707 .41734	. 8292 .58266	.3976 2.3961	. 5889 .45924	$.1792 \\ 2.1775$	1003 1.1004	. 9113 .09125	.0887 .90875	20
41	. 1760	. 8240	.3946	. 5960	.1758	.1004	. 9137	. 0863	19
42	. 1787	8213	.3931	. 5995	.1741	.1005	. 9149	. 0851	18
43	1813	8187	.3916	. 6030	.1725	.1008	9161	. 0839	17
44	. 1839	. 8160	.3901	. 6065	.1708	.1010	. 9173	. 0826	16
45	.41866	.58134	2.3886	.46101	2.1692	1.1011	.09186	.90814	15
46	. 1892	. 8108	.3871	. 6136	.1675	.1013	. 9198	. 0802	14
47	. 1919	. 8081	.3856	. 6171	.1658	.1014	. 9210	. 0790	13
48 49	. 1945 . 1972	. 8055 . 8028	.3841	. 6206	.1642	.1016	. 9222	. 0778	12 11
50	.41998	.58002	$.3826 \\ 2.3811$.6242 .46277	.1625 2.1609	.1017 1.1019	.9234 .09247	. 0765 .90753	10
51	2024	. 7975	.3796	. 6312	.1592	.1020	. 9259	. 0741	10
52	2051	7949	.3781	. 6348	.1576	.1022	9271	. 0729	l š
53	. 2077	. 7923	.3766	6383	.1559	.1023	. 9283	. 0717	8
54	. 2103	, 7896	.3751	. 6418	.1543	.1025	. 9296	0704	6
55	.42130	.57870	2.3736	.46454	2.1527	1.1026	.09308	.90692	5
56	. 2156	. 7844	.3721	. 6489	.1510	.1028	. 9320	. 0680	4
57	. 2183	. 7817	.3706	. 6524	.1494	.1029	. 9332	. 0668	3
58	. 2209	· 7791	.3691	. 6560	.1478	.1031	. 9345	. 0655	2
59	2235 2262	. 7764	.3677 .3662	. 6595 . 6631	.1461	.1032	. 9357	. 0643	$\begin{vmatrix} 1\\0 \end{vmatrix}$
60 —						1!	. 9369	. 0631	_
<u>M,</u>	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec 'nt	Vrs. cos.	Sine.	M.

1140

Table 3.

NATURAL FUNCTIONS.

Natural Trigonometrical Functions. 25° 1540 M. Sine. Vrs. cos. Cosec'nt Tang. Cotang. Secant. Vrs. sin. Cosine. M. 42262 .57738 2.3662.90631 n .46631 2.1445 1.103409369 60 . 2288 . 7712 .1429 . 9381 . 0618 i .3647 . 6666 .1035 59 $\overline{2}$ 2314 7685 .3632 . 6702 .1412 9394 .10370606 58 3 2341 7659 .3618 . 6737 .1396 .1038 9406 57 0594 . 2367 .1380 2,1364 .1040 $\overline{4}$ 7633 3603 6772 9418 0581 56 90569 .46808 5 .42394.576062.35881.1041 .09431 55 Ğ 2420 7580 .3574 6843 .1348 .1043 9443 0557 54. ž 2446 7554 .3559 . 6879 .1331 .1044 9455 0544 $5\bar{3}$. ŝ 2473 7527 .1046 .3544 6914 .1315 9468 0532 $\overline{52}$. • <u>9</u> 2499 7501 .3530 6950 .12991047 9480 0520 $\overline{51}$ 90507 10 .42525 .57475 2.351546985 2,1283 50 1.1049.094922552 .3501 .1267 .1050 9505 0495 $\tilde{49}$ 11 7448 7021 2578 7056 1251 12 7422 .3486 1052 9517 0483 $\bar{48}$ • 13 1235 1053 2604 7396 .34727092 9530 0470 47 2630 14 15 7369 3457 7127 .1219 .1055 9542 0458 46 .42657 2.3443 .57343 .47163 2.1203 1.1056.09554 90445 45 16 . 2683 7317 .1187 .1058 . 0433 .3428 7199 9567 $\overline{44}$ 2709 . 0421 17 7290 .3414 7234 .1171 .1059 9579 43 2736 7264 7270 . 0408 18 .3399 9592 $\overline{42}$.1155.1061 . 7238 19 2762.3385 7305 .1139 .1062 9604 0396 41 .90383 20 21 22 23 24 25 42788 .57212 2.3371.47341 2.11231.1064 .09617 $\overline{40}$.3356 .1107 .1065 . 0371 . 2815 7185 7376 9629 39 . . 7159 2841 .3342 7412 .1092 .1067 9641 0358 38 . . 2867 7133 .3328 7448 .1076 .1068 9654 . 0346 37 • . 2893 7106 .3313 7483 9666 0333 .1060 1070 36 .42920 .57080 2.3299 2.1044.475191.1072.09679 .9032135 26 27 28 29 30 2946 7054 .3285 7555 $\tilde{34}$.1028 .10739691 0308 . 2972 7028 .32717590 $.\bar{1}013$.1075 9704 0296 33 2998 0283 7001 .32567626 .0997.1076 9716 32 3025 3242 7662 0271 6975 .0981 9729 31 .1078.56949 2.3228 .43051 .47697 .90258 2.09651.1079 .09741 30 . 3077 7733 .1081 . 0246 31 6923 .3214.0950 9754 29 $\overline{32}$ 3104 6896 .3200 7769 .0934 .1082 9766 . 0233 28 33 . 3130 6870 3186 7805 9779 . 0221 $\tilde{27}$ 0918 .1084 . 3156 7840 .1085 34 6844 3172.0903 9792 0208 26 .43182 .90196 35 .56818 2.3158.47876 2.08871.1087 .09804 25 36 3208 6791 . 0183 .3143 7912 0872 .1088 24 9817 . 37 3235 6765 .31297948 .0856 1090 9829 . 0171 23 . 3261 . 0158 38 6739 .3115 7983 .0840 .1092 9842 $\overline{22}$ 39 3287 1093 $\overline{21}$ 6713 .3101 8019 .082598540145 .43313 .56686 .48055 46 2.30872.08091.1095 .09867 90133 $\overline{20}$ 41 42 .1096 . 0120 3340 6660 .3073 8091 .07949880 19 3366 6634 .30598127 .0778.109898926168 18 . . 43 3392 6608 3046 8162 .1099 9905 . .0763• 0095 17 1101 44 3418 6582 3032 8198 .0747 9917 0082 16 .48234 45 43444 .56555 2.30182.07321.1102.09930 .90070 15 46 6529 . 8270 3471 .3004 $.110\bar{4}$. 0057 .07179943 14 . 47 3497 6503 2990 8306 .0761 .1106 9955 0044 13 48 3523 . 6477 2976 8342 .1107 . 0032 12.0686 9968 2962 $\overline{49}$ 3549 8378 .1109 1.1110 . 0019 6451 .0671 9981 11 ŝŏ 43575 56424 2,2949 .48414 2.0655.09993 90006 10 51 . 3602 6398 2935 8449 .0640 .1112 10006 89994 9 $\tilde{5}\bar{2}$ 2921 3628 63728485 .0625 .1113 0019 9981 8 53 3654 6346 2907 8521 .0609 .1115 0031 9968 7 54 3680 6320 2894 8557 .0594 .1116 0044 9956 6 55.43706 .56294 2.2880 .48593 2.05791.1118 10057 89943 5 563732 6267 .2866 8629 .0564 .1120 ā 6070 9930 6241 2853 .1121 57 8665 .0548 3 3759 00829918 . 6215 .1123 ž 58 3785 2839 8701 .0533 0095 9905 . . • . .112459 3811 6189 .2825 .0518 1 8737 0108 9892٠ • • .1126 . 9879 60 3837 6163 .28128773 .65030121 0 M. Cosine. Vrs. sin. Secant. Cotang. Tang. Cosec'nt Vrs. cos. Sine. М.

115°

26°

Natural Trigonometrical Functions.

153°

20		144		igonom	cericar,	unction	10.		
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.43837	.56163	2,2812	.48773	2.0503	1.1126	.10121	.89879	60
ī	. 3863	. 6137	.2798	. 8809	.0488	.1127	. 0133	. 9867	59
	. 3889	. 6111	.2784	. 8845	.0473	.1129	. 0146	. 9854	58
2 8 4	. 3915	. 6084	.2771	. 8881	.0458	.1131	. 0159	. 9841	57
4	. 3942	. 6058	.2757	. 8917	.0443	.1132	. 0172	. 9828	56
5 6	.43968	.56032	2.2744	.48953	2.0427	1.1134	.10184	.89815	55
6	. 3994	. 6006	.2730	. 8989	.0412	.1135	. 0197	. 9803	54
7	. 4020	. 5980	.2717	. 9025	.0397	.1137	. 0210	. 9790	53
8	. 4046	. 5954	.2703	. 9062	.0382	.1139	. 0223	. 9777	52
9	. 4072	. 5928	.2690	. 9098	.0367	.1140	. 0236	. 9764	51
10	.44098	.55902	2.2676	.49134	2.0352	1.1142	.10248	.89751	50
11	. 4124	. 5875	.2663 .2650	. 9170	.0338	.1143	. 0261	. 9739 . 9726	49
12	. 4150	. 5849	.2650	. 9206	.0323	.1145	. 0274	. 9720 . 9713	48
13	. 4177	. 5823	.2636	. 9242	.0308	.1147	. 0287	. 9713	47 46
14	. 4203 .44229	5797	2.2623 2.2610	.9278 .49314	.0293 2.0278	.1148 1.1150	.10313	.89687	40
15	.44225	.55771 . 5745	.2596	. 9351	.0263	.1151	. 0326	. 9674	40
16 17	• 4200 • 4281	. 5745	.2583	. 9387	.0203	.1153	. 0338	. 9661	43
18	. 4307	. 5693	.2570	9423	.0240	.1155	. 0351	9619	42
19	. 4333	. 5667	.2556	9459	.0219	.1156	. 0364	9636	41
20	.44359	.55641	2,2543	.49495	2.0204	1.1158	.10377	.89623	40
21	. 4385	. 5615	.2530	9532	.0189	.1159	. 0390	. 9610	39
22	. 4411	5589	.2517	9568	.0174	.1161	. 0403	9597	38
$\frac{1}{22}$ 23	. 4437	5562	.2503	. 9604	.0159	.1163	. 0416	9584	37
24	. 4463	. 5536	.2490	. 9640	.0145	.1164	. 0429	9571	36
25	.44489	.55510	2.2477	.49677	2.0130	1.1166	.10442	.89558	35
26	. 4516	. 5484	.2464	. 9713	.0115	.1167	. 0455	. 9515	34
27	. 4542	. 5458	.2451	. 9749	.0101	.1169	. 0468	. 9532	33
28	 4568 	. 5432	.2438	. 9785	.0086	.1171	. 0481	. 9519	32
29	. 4594	. 5406	.2425	. 9822	.0071	.1172	. 0493	. 9506	31
30	-14620	.55380	2.2411	.49858	2.0058	1.1174	.10506	.89493	30
31	. 4646	. 5354	.2398	. 9894	.0042	.1176	. 0519	. 9480	29
32	. 4672	. 5328	.2385	. 9931	.0028	.1177 .1179	. 0532	. 9467	28
83	. 4698	. 5302	.2372	. 9967	.0013	.1179	. 0545	. 9454	27
34	. 4724	. 5276	.2359	.50003	1.9998	.1180	. 0558	. 9441 .	26
35	.44750	.55250 .5224	2.2346	.50040	1.9984	1.1182	.10571	.89428	25
36 37	. 4776 . 4802	. 5198	.2333 .2320	. 0076	.9969 .9955	.1184 .1185	. 0584 . 0598	. 9415 . 9402	24 23
38	4802	. 5198	.2307	. 0113	.9955	.1185	. 0611	. 9389	23
39	. 4854	5146	.2294	. 0185	.9926	.1189	. 0624	. 9376	21
40	.44880	.55120	2,2282	.50222	1,9912	1.1190	.10637	.89363	20
41	. 4906	. 5094	.2269	. 0258	.9897	.1192	. 0650	. 9350	19
42	. 4932	. 5068	.2256	0295	.9883	.1193	. 0663	9337	18
43.	. 4958	. 5042	.2243	. 0331	.9868	.1195	. 0676	9324	17
44	. 4984	. 5016	,2230	. 0368	.9854	.1197	. 0689	9311	16
45	.45010	.54990	2.2217	.50404	1.9840	1.1198	.10702	.89298	15
46	5036	. 4964	.2204	. 0441	.9825	.1200	. 0715	. 9285	14
47	. 5062	. 4938	.2192	. 0477	.9811	.1202	. 0728	. 9272	13
48	5088	4912	.2179	. 0514	.9797	.1203	. 0741	. 9258	12
49	. 5114	. 4886	.2166	. 0550	.9782	.1205	. 0754	. 9245	11
50	.45140	.54860	2.2153	.50587	1.9768	1.1207	.10768	.89232	10
51	. 5166	. 4834	.2141	. 0623	.9754	.1208	. 0781	. 9219	9
52	. 5191	. 4808	.2128	. 0660	.9739	.1210	. 0794	. 9206	8 7
53	. 5217	. 4782	.2115	. 0696	.9725 .9711	.1212	. 0807	. 9193	7
54	. 5243	. 4756	.2103	. 0733	.9711	.1213	. 0820	. 9180	6 5 4
$\frac{55}{56}$.45269	.54730	2.2090	.50769	1.9697	1.1215	.10833	.89166	D
50 57	5295 5321	. 4705	.2077	. 0806 . 0843	.9683	.1217	. 0846	. 9153	4
58	5347	. 4653	.2055	. 0843	.9668	.1218 .1220	. 0860	. 9140	32
59	. 5373	4627	.2032	. 0879	.9654	.1220	. 0873	. 9127 . 9114	
60	5399	4601	.2033	. 0952	.9626	.1223	. 0899	. 9101	0
						.12	. 0033	. 5101	_
M .	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos	Sine.	M.

Natural Trigonometrical Functions.

152°

21-		148	turai ir	igonom	etrical	Function	15.	1.	520
<u>M.</u>	Sine.	Vrs. cos.	Cosec'nt	Taug.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.45399	.54601	2.2027	.50952	1.9626	1.1223	.10899	.89101	60
11	. 5425	. 4575	.2014	. 0989	.9612	.1225	. 0912	. 9087	59
$\frac{\overline{2}}{3}$	 5451 	. 4549	.2002	. 1026	.9598	.1226	. 0926	. 9074	58
3	. 5477	. 4523	.1989	. 1062	.9584	.1228	. 0939	. 9061	57
4	5503	. 4497	.1977	. 1099	.9570	.1230	. 0952	. 9048	56
5	45528	.54471	2.1964	.51136	1.9556	1.1231	.10965	.89034	55
7	. 5554 . 5580	. 4445 . 4420	.1952 .1939	.1172 .1209	.9542 .9528	.1233 .1235	. 0979 . 0992	. 9021 . 9008	54
8	. 5606	. 4394	.1909	. 1246	.9514	.1235	. 1005	. 8995	52
9	. 5632	. 4368	.1914	1283	.9500	.1238	1018	. 8981	51
10	45658	.54342	2,1902	.51319	1.9486	1.1240	.11032	.88968	50
11	. 5684	. 4316	.1889	. 1356	.9472	.1242	. 1045	. 8955	49
12	. 5710	. 4290	.1877	. 1393	.9458	.1243	. 1058	. 8942	48
13	. 5736	. 4264	.1865	. 1430	.9444	.1245	. 1072	. 8928	47
14	. 5761	. 4238	.1852	. 1466	.9430	.1247	. 1085	. 8915	46
15	.45787	.54213	2.1840 .1828	.51503	1.9416	1.1248 .1250	.11098	.88902 .8888	45
16 17	. 5813 . 5839	. 4187	.1815	. 1540 . 1577	.9402	.1250	.1112 .1125	. 8875	44 43
18	. 5865	. 4135	.1803	1614	.9375	.1253	. 1138	8862	42
19	. 5891	4109	.1791	. 1651	.9361	.1255	1152	. 8848	41
20	.45917	.54083	2.1778	.51687	1.9347	1.1257	.11165	.88835	40
21	. 5942	. 4057	.1766	. 1724	.9333	.1258	. 1178	, 8822	39
22	. 5968	. 4032	.1754	. 1761	.9319	.1260	. 1192	. 8808	38
23	. 5994	. 4006	.1742	. 1798	.9306	.1262	. 1205	. 8795	37
24	. 6020	. 3980	.1730	. 1835	.9292	.1264	. 1218	. 8781	36
25	.46046	.53954	2.1717	.51872	1.9278	1.1265 .1267	.11232 .1245	.88768 .8755	35 34
$\frac{26}{27}$. 6072 . 6097	· 3928 · 3902	.1705	. 1909 . 1946	.9264 .9251	.1267	1245	. 8741	33
28	. 6123	. 3877	.1681	. 1983	.9237	.1270	1272	. 8728	32
28 29	. 6149	. 3851	.1669	2020	.9223	,1272	1285	. 8714	31
30	.46175	.53825	2,1657	.52057	1.9210	1,1274	.11299	.88701	30
31	. 6201	. 3799	.1645	. 2094	.9196	.1275	. 1312	. 8688	29
32	 6226 	. 3773	.1633	. 2131	.9182	.1277	. 1326	. 8674	28
33	. 6252	. 3748	.1620	. 2168	.9169	.1279	. 1339	. 8661	27
34	. 6278	. 3722	.1608	. 2205	.9155	.1281	. 1353	. 8647	26 25
35 36	.46304	.53696	2.1596	.52242 .2279	1.9142 .9128	1.1282 .1284	.11366 . 1380	.88634 .8620	25
30 37	. 6330 . 6355	. 3645	.1572	. 2316	.9115	.1284	. 1393	. 8607	23
38	. 6381	. 3619	.1560	2353	.9101	.1287	1407	8593	22
39	6407	3593	.1548	2390	.9088	1289	1420	. 8580	21
40	.46433	.53567	2.1536	.52427	1.9074	1.1291	.11434	.88566	20
41	. 6458	. 3541	.1525	. 2464	.9061	.1293	. 1447	. 8553	19
42	. 6484	. 3516	.1513	. 2501	.9047	.1294	. 1461	. 8539	18
43	. 6510	. 3490	.1501	. 2538	.9034	.1296	. 1474	. 8526	17
44	. 6536	. 3464	.1489	.2575 .52612	.9020	.1298 1.1299	. 1488	. 8512 .88499	16 15
$\frac{45}{46}$. 46561	. 3413	.1465	. 2650	.8993	.1301	. 1515	. 8485	14
47	. 6613	3387	.1453	2687	.8980	.1303	1528	. 8472	13
48	. 6639	3361	.1441	2724	.8967	.1305	1542	. 8458	12
49	. 6664	. 3336	.1430	. 2761	.8953	.1306	. 1555	. 8444	11
50	.46690	.53310	2.1418	.52798	1.8940	1.1308	.11569	.88431	10
51	. 6716	. 3284	.1406	. 2836	.8927	.1310	. 1583	. 8417	9
52	. 6741	. 3258	.1394	. 2873	.8913	.1312	. 1596	. 8404	8
53	. 6767	. 3233	.1382	. 2910	.8900	.1313	. 1610	. 8390	
$\frac{54}{55}$. 6793	. 3207 .53181	.1371 2.1359	. 2947	.8887 1.8873	1.1315 1.1317	.1623 .11637	. 8376	6 5 4 3 2 1
ээ 56	. 6844	. 3156	1347	3022	.8860	.1319	. 1651	. 8349	4
57	6870	. 3130	,1335	. 3059	.8847	1320	1664	. 8336	1 3
58	. 6896	. 3104	.1324	. 3096	.8834	.1322	1678	. 8322	2
59	. 6921	3078	.1312	. 3134	.8820	.1324	. 1691	. 8308	
60	. 6947	. 3053	.1300	. 3171	.8807	.1326	. 1705	. 8295	0
M.	Cosine.	Vrs. sio.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	М.

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28°	

Natural Trigonometrical Functions.

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			curar m	igonom	centear	unction	13.		
М.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.46947	.53053	2,1300	.53171	1.8807	1.1326	.11705	,88295	60
1	. 6973	. 3027	.1289	. 3208	.8794	.1327	. 1719	. 8281	59
$\frac{2}{3}$. 6998	. 3001	.1277	. 3245	.8781	.1329	. 1732	. 8267	58
3	. 7024	. 2976	.1266	. 3283	.8768	.1331	. 1746	. 8254	57
4 5	. 7050	. 2950	.1254	. 3320	.8754	.1333	. 1760	. 8240	56
5	.47075	.52924	2.1242	.53358	1.8741	1.1334	.11774	.88226	55
6 7	. 7101	. 2899	.1231	. 3395	.8728	.1336	. 1787	. 8213	54
7	. 7127	. 2873	.1219	. 3432	.8715	.1338	. 1801	. 8199	55
8	. 7152	. 2847	.1208	. 3470	.8702	.1340	. 1815	. 8185	52
9	. 7178	. 2822	.1196	. 3507	.8689	.1341	. 1828	. 8171	51
10 11	.47204	.52796 . 2770	2.1185 .1173	.53545 . 3582	1.8676 .8663	1.1343 .1345	.11842	. 8144	50 49
12	. 7255	2745	.1173	. 3619	.8650	.1345	. 1870	. 8130	49
$\widehat{12}$ 13	. 7281	2719	.1150	. 3657	.8637	.1349	1883	. 8117	47
14	7306	2694	.1139	. 3694	.8624	.1350	1897	8103	46
15	.47332	.52668	2.1127	.53732	1.8611	1.1352	.11911	·88089	45
16	. 7357	. 2642	.1116	. 3769	.8598	.1354	. 1925	. 8075	44
17	. 7383	. 2617	.1104	. 3807	.8585	.1356	1938	. 8061	43
18	. 7409	2591	.1093	. 3844	.8572	.1357	. 1952	. 8048	42
19	. 7434	. 2565	.1082	, 3882	.8559	.1359	. 1966	. 8034	41
$\frac{20}{21}$.47460	.52540	2,1070	.53919	1.8546	1.1361	.11980	.88020	40
21	. 7486	. 2514	.1059	. 3957	.8533	.1363	. 1994	. 8006	39
22	. 7511	. 2489	.1048	. 3995	.8520	.1365	. 2007	. 7992	3 8 37
23	. 7537	. 2463	.1036	. 4032	.8507	.1366	. 2021	. 7979	37
24	. 7562	. 2437	.1025	. 4070	.8495	.1368	. 2035	. 7965	36
2 5	.47588	.52412	2.1014	.54107	1.8482	1.1370	.12049	.87951	35
26	. 7613	. 2386	.1002	. 4145	.8469	.1372	. 2063	. 7937	34
$\frac{1}{27}$ 28	. 7639	. 2361	.0991	4183	.8456	.1373	. 2077	. 7923	33
28 29	. 7665	. 2335	.0980	. 4220	.8443	.1375	. 2090	. 7909	32
29 30	.7690 .47716	. 2310 .52284	.0969	4258	.8430	.1377	. 2104	. 7895	31
30 31	. 7741	. 2258	2.0957	.54295 . 4333	1.8418	1.1379	.12118	.87882	30
32	. 7767	2233	.0940	. 4353	.8405 .8392	.1381 .1382	. 2132 . 2146	. 7868 . 7854	29 28
33	7792	2207	.0924	. 4409	.8379	.1384	2140	. 7840	27
34	. 7818	2182	.0912		.8367	.1386	2174	7826	26
35	.47844	.52156	2.0901	.54484	1.8354	1.1388	.12188	.87812	25
36	. 7869	. 2131	.0890	. 4522	.8341	,1390	. 2202	. 7798	24
37	. 7895	. 2105 . 2080	.0879	4559	.8329	.1391	. 2216	7784	23
38	. 7920	. 2080	.0868	. 4597	.8316	.1393	. 2229	. 7770	$\frac{23}{22}$
39	. 7946	. 2054	.0857	. 4635	.8303	.1395	. 2243	. 7756	21
40	.47971	.52029	2.0846	.54673	1.8291	1.1397	.12257	.87742	20
41	. 7997	. 2003	.0835	. 4711	.8278	.1399	. 2271	. 7728	19
42	. 8022	. 1978	.0824	. 4748	.8265	.1401	. 2285	. 7715	18
43	. 8048	. 1952	.0812	. 4786	.8253	.1402	. 2299	. 7701	17
44	. 8073	. 1927	.0801	. 4824	.8240	.1404	. 2313	. 7687	16
45	.48099	.51901	2.0790	.54862	1.8227	1.1406	.12327	.87673	15
46 47	. 8124 . 8150	. 1876 . 1850	.0779 .0768	. 4900 . 4937	.8215	.1408	. 2341	. 7659	14
48	. 8175	. 1825	.0757	. 4957	.8202 .8190	.1410	. 2355	. 7645	13
49	. 8201	1799	.0746	. 5013	.8190	.1411 .1413	. 2369 . 2383	. 7631 . 7617	12 11
50	.48226	.51774	2.0735	.55051	1.8165	1.1415	.12397	.87603	10
51	. 8252	. 1748	.0725	5089	.8152	.1417	. 2411	. 7588	9
52	. 8277	1723	.0714	, 5127	.8140	.1419	2425	. 7574	8.
53	8303	. 1697	.0703	5165	.8127	.1415	2420	. 7560	7
54	. 8328	. 1672	.0692	5203	.8115	.1422	2453	. 7546	6
55	.48354	.51646	2,0681	.55241	1.8102	1,1424	.12468	.87532	5
56	. 8379	. 1621	.0670	5279	.8090	,1426	. 2482	. 7518	14
57	. 8405	. 1 595	.0659	. 5317	.8078	.1428	. 2496	7504	3
58	. 8430	. 1570	.0648	. 5355	.8065	.1430	. 2510	. 7504 . 7490	3
59	. 8455	. 1544	.0637	. 5393	.8053	.1432	. 2524	. 7476	1
60	. 8481	. 1519	.0627	. 5431	.8040	.1 433	. 2538	. 7462	0
M.	Cosine,	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos	Sine.	M.
446						0000 10	. 101 000.	ono.	-a.

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Table 3. NATURAL FUNCTIONS.

M. 0 1 2 3 4 5	Sine.	Vrs. cos.	Cosec'nt	-	1				
$\frac{1}{2}$			COSCC III	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
$\frac{2}{3}$	0500	.51519	2.0627	.55431	1.8040	1.1433	.12538	.87462	60
234	. 8506	. 1493	.0616	. 5469	.8028	.1435	. 2552	. 7448	59
34	. 8532	. 1468	.0605	. 5507	.8016	.1437	. 2566	. 7434	58
4	. 8557	. 1443	.0594	. 5545	.8003	.1439	. 2580	. 7420	57
	. 8583	. 1417	.0583	. 5583	.7991	.1441	. 2594	. 7405	56
5	.48608	.51392	2.0573	.5562 1	1.7979	1.1443	.12609	.87391	55
6 7	 8633 	. 1366	.0562	. 5659	.7966	.1445	. 2623	. 7377	54
	. 8659	. 1341	.0551	. 5697	.7954	.1446	. 2637	. 7363	53
8 9	. 8684	. 1316	.0540	. 5735	.7942	.1448	. 2651	. 7349	52
9 10	. 8710	. 1290	.0530	. 5774	.7930	.1450 1.1452	. 2665	. 7335 .87320	51
10	.48735	.51265	2.0519	.55812	1.7917	1.1402	.12679		50
	. 8760	1239	.0508	. 5850 . 5888	.7905	.1454	. 2694	. 7306 . 7292	49
13	. 8786 . 8811	. 1214 . 1189	.0498	. 5926	.7893	.1456 .1458	2708 2722	7278	47
14	. 8837	. 1163	.0487	. 5964	.7868	.1459	2736	7264	46
15	.48862	.51138	2.0466	.56003	1.7856	1.1461	.12750	87250	45
16	. 8887	. 1112	.0455	. 6041	.7844	.1463	. 2765	. 7235	44
17	. 8913	. 1087	.0444	. 6079	.7832	.1465	2779	. 7221	43
18	8938	. 1062	.0434	. 6117	.7820	.1467	2793	. 7207	42
19	. 8964	1036	.0423	. 6156	.7808	.1469	. 2807	7193	41
20	48989	.51011	2.0413	.56194	1.7795	1.1471	12821	.87178	40
20 21 22 23 24 25 26 27 28 29	. 9014	. 0986	.0402	. 6232	.7783	.1473	. 2836	. 7164	39
22	. 9040	. 0960	.0392	. 6270	.7771	.1474	. 2850	. 7150	38
23	. 9065	. 0935	.0381	. 6309	.7759	.1476	. 2864	. 7136	37
24	. 9090	. 0910	.0370	. 6347	.7747	.1478	. 2879	. 7121	36
25	.49116	.50884	2.0360	.56385	1.7735	1.1480	.12893	.87107	35
26	. 9141	. 0859	.0349	. 6424	.7723	.1482	. 2907	. 7093	34
27	. 9166	. 0834	.0339	. 6462	.7711	.1484	. 2921	. 7078	33
28	. 9192	. 0808	.0329	. 6500	.7699	.1486	. 2936	. 7064	32
29	. 9217	. 0783	.0318	. 6539	.7687	.1488	. 2950	. 7050	31
30 -	.49242	.50758	2.0308	.56577	1.7675	1.1489	.12964	.87035	30
31	. 9268	. 0732	.0297	. 6616	7663	.1491	. 2979	. 7021	29
32	. 9293	• 0707	.0287	. 6654	.7651	.1493	. 2993	. 7007	28
33 34	. 9318 . 9343	. 0682 . 0656	.0276	. 6692	.7639	.1495	. 3007	. 6992	27
35	.49369	. 50631	.0266 2.0256	. 6731	.7627	.1497	. 3022	. 6978	26
36 36	. 9394	. 0606	.0245	.56769	1.7615	1.1499	.13036	.86964 . 6949	25 24
27	. 9419	. 0580	.0245	. 6846	.7603	.1501 .1503	. 3050 . 3065	. 6935	23
37 38 39	. 9445	. 0555	.0235	. 6885	.7579	.1505	. 3079	. 6921	20
39	9470	. 0530	.0214	6923	.7567	.1507	3094	. 6906	$ \frac{22}{21} $
40	.49495		2.0204	.56962	1.7555	1.1508	.13108	.86892	20
41	. 9521	. 0479	.0194	. 7000	.7544	.1510	. 3122	. 6877	19
42	. 9546	. 0454	.0183	. 7039	.7532	.1512	. 3137	. 6863	18
43	. 9571	. 0429	.0173	. 7077	.7520	.1514	. 3151	. 6849	17
44	. 9596	. 0404	.0163	. 7116	.7508	.1516	. 3166	. 6834	16
45	.49622	.50378	2.0152	.57155	1.7496	1 .1518	.13180	.86820	15
46	. 9647	. 0353	.0142	. 7193	.7484	.1520	. 3194	. 6805	14
47	. 9672	. 0328	.0132	. 7232	.7473	.1522	. 3209	. 6791	13
48	. 9697	. 0303	.0122	.7270	.7461	.1524	. 3223	. 6776	12
49	. 9723	. 0277	.0111	. 7309	.7449	1526	. 3238	. 6762	11
50 51 52 53	.49748	.50252	2.0101	.57348	1.7437	1.1528	.13252	.86748	10
51	. 9773	. 0227	.0091	. 7386	.7426	.1530	. 3267	. 6733	9
DZ	. 9798	. 0202	.0081	. 7425	.7414	.1531	. 3281	. 6719	l 8
53 54	. 9823 . 9849	. 0176	.0071	. 7464 . 7502	.7402	.1533	. 3296	. 6704	
55.	. 9849	.0151	$.0061 \\ 2.0050$.7502 .57541	.7390 1.7379	.1535 1.1537	. 3310 .13325	. 6690 .86675	
56	. 9899	. 0101	.0040	. 7580	.7367	.1539	.13325	. 6661	
57	. 9899	. 0076	.0040	. 7619	.7355	.1539	. 3354	. 6646	4
58	. 9950	. 0050	.0030	. 7657	.7344	.1543	. 3368	. 6632	0
59	. 9975	. 0025	.0020	7696	.7344	.1545	. 3383	. 6617	1 1
50 I	.50000	. 00000	.0000	. 7735	.7320	.1547	. 3397	. 6602	9 8 7 6 5 4 3 2 1 0
								. 0002	<u> </u>
М.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

119°

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Natural Trigonometrical Functions.

149°

304	1	Natural Trigono			netrical Functions.			149°	
M.	Sinc.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.50000	.50000	2.0000	.57735	1.7320	1.1547	.13397	.86602	60
1	. 0025	.49975	1.9990	. 7774	.7309	.1549	. 3412	. 6588	59
2 3	. 0050	. 9950	.9980	. 7813	.7297	.1551	. 3426	. 6573	58
3	. 0075	. 9924	.9970	. 7851	.7286	.1553	. 3441	. 6559	57
4 5 6 7	. 0101	. 9899	.9960	. 7890	.7274	.1555	. 3456	. 6544	56
5	.50126	.49874	1.9950	.57929	1.7262	1.1557	.13470	.86530	55
6	. 0151	. 9849	.9940	. 7968	.7251	1559	. 3485	. 6515	54 53
- 6	. 0176	. 9824 . 9799	.9930 .9920	. 8007 . 8046	.7239	.1561 .1562	. 3499	. 6486	52
8 9	. 0201	9773	.9910	. 8085	.7216	.1564	3529	. 6471	51
10	.50252	49748	1.9900	.58123	1.7205	1.1566	.13543	.86457	50
11	. 0277	. 9723	.9890	. 8162	.7193	.1568	. 3558	. 6442	49
12	0302	. 9698	.9880	. 8201	.7182	.1570	. 3572	. 6427	48
13	. 0327	. 9673	.9870	. 8240	.7170	.1572	. 3587	. 6413	47
14	. 0352	. 9648	.9860	. 8279	.7159	.1574	. 3602	. 6398	46
15	.50377	.49623	1.9850	.58318	1.7147	1.1576	.13616	.86383	45
16	. 0402	. 9597	.9840	. 8357	.7136	.1578	. 3631	. 6369	44
17	. 0428	. 9572	.9830	. 8396	.7124	.1580	. 3646	. 6354	43
18	. 0453 . 0478	. 9547 . 9522	.9820 .9811	8435 . 8474	.7113 .7101	.1582 .1584	. 3660 . 3675	. 6339 . 6325	42
19 20	.50503	.49497	1.9801	.58513	1.7090	1.1586	.13690	.86310	40
21	. 0528	. 9472	.9791	, 8552	.7079	.1588	. 3704	. 6295	39
22	0553	. 9447	.9781	8591	.7067	.1590	3719	6281	38
23	0578	9422	.9771	. 8630	.7056	.1592	. 3734	6266	37
24	. 0603	. 9397	.9761	. 8670	.7044	.1594	. 3749	. 6251	36
25	.50628	.49371	1.9752	.58709	1.7033	1.1596	.13763	.86237	35
26	. 0653	. 9346	.9742	. 8748	.7022	.1598	. 3778	. 6222	34
24 25 26 27 28 29 30	. 0679	. 9321	.9732	. 8787	.7010	.1600	. 3793	. 6207	33
28	. 0704	. 9296	.9722	. 8826	.6999	.1602	. 3807	. 6192	32
29	. 0729 .50754	.9271 .49246	.9713 1.9703	. 8865 .58904	.6988	.1604 1.1606	. 3822 .13837	.6178 .86163	31 30
31	. 0779	. 9221	.9693	. 8944	1.6977 .6965	.1608	, 3852	. 6148	29
32	. 0804	. 9196	.9683	8983	.6954	.1610	3867	. 6133	28
33	. 0829	. 9171	.9674	9022	.6943	.1612	3881	6118	$\tilde{27}$
34	. 0854	. 9146	.9664	. 9061	.6931	.1614	. 3896	. 6104	27 26
35	50879	.49121	1.9654	.59100	1.6920	1.1616	.13911	.86089	25
36	. 0904	. 9096	.9645	. 9140	.6909	.1618	. 3926	. 6074	24
37	. 0929	. 9071	.9635	. 9179	.6898	.1620	. 3941	. 6059	23
38	. 0954	. 9046	.9625	. 9218	.6887	.1622	. 3955	. 6044	22
39 40	.0979 .51004	. 9021 .48996	.9616 1.9606	. 9258 .59297	.6875	.1624 1.1626	. 3970 .13985	. 6030 .86015	$\frac{21}{20}$
41	.1029	. 8971	.9596	. 9336	1.6864 .6853	.1628	. 4000	. 6000	19
42	. 1054	. 8946	.9587	9376	.6842	.1630	4015	. 5985	18
$\overline{43}$. 1079	. 8921	.9577	. 9415	.6831	.1632	4030	. 5970	17
44	. 1104	. 8896	.9568	. 9454	.6820	.1634	. 4044	5955	16
45	.51129	.48871	1.9558	.59494	1.6808	1.1636	.14059	.85941	15
46	. 1154	. 8846	.9549	. 9533	.6797	.1638	. 4074	. 5926	14
47	. 1179	. 8821	.9539	. 9572	.6786	.1640	. 4089	. 5911	13
48	. 1204 . 1229	. 8796 . 8771	.9530 .9520	. 9612	.6775	.1642	. 4104	5896	12
49 50	.1229 .51254	. 48746	1.9510	. 9651 .59691	.6764 1.6753	.1644 1.1646	.4119 .14134	. 5881 .85866	11 10
51	. 1279	. 8721	.9501	. 9730	.6742	.1648	. 4149	. 5851	9
52	1304	8696	.9491	. 9770	.6731	.1650	4164	. 5836	
53	1329	. 8671	.9482	. 9809	.6720	.1652	4178	5821	8 7
54	. 1354	. 8646	.9473	. 9849	.6709	.1654	. 4193	. 5806	6
55	.51379	.48621	1.9463	.59888	1.6698	1.1656	.14208	.85791	5
56	. 1404	. 8596	.9454	. 9928	.6687	.1658	. 4223	. 5777	4
57	. 1429	. 8571	.9444	. 9967	.6676	.1660	4238	. 5762	3
58 59	.1454 .1479	. 8546 . 8521	.9435 .9425	.60007	.6665	.1662	. 4253	. 5747	3 2 1
60 60	. 1479	. 8521 . 8496	.9425	. 0046	.6654 .6643	.1664	· 4268 · 4283	.5732 .5717	0
_									_
M.	Cosine.	Vrs. sin.	Secant,	Cotang.	Tang.	Cosec'nt	vrs. cos.	Sine.	М.

120°

Table 3.

NATURAL FUNCTIONS.

310		Na	tural Tr	igonom	etricai I	148°			
М.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.51504	.48496	1.9416	.60086	1.6643	1.1666	.14283	.85717	60
1	. 1529	. 8471	.9407	. 0126	.6632	.1668	. 4298	. 5702	59
2	. 1554	. 8446	.9397	. 0165	.6621	.1670	. 4313	. 5687	58
3	. 1578	. 8421	.9388	. 0205	.6610	.1672	. 4328	. 5672	57
4	. 1603	. 8396	.9378	. 0244	.6599	.1674	. 4343	. 5657	56
5	.51628	.48371	1.9369	.60284	1.6588	1.1676	.14358	.85642	55
7	. 1653	. 8347 . 8322	.9360 .9350	. 0324	.6577	.1678	. 4373 . 4388	. 5627	54
8	. 1678 . 1703	. 8297	.9550 .9341	. 0363 . 0403	.6566 .6555	.1681 .1683	. 4388	.5612 .5597	53 52
9	. 1728	8272	.9332	. 0443	.6544	.1685	. 4418	. 5582	51
10	.51753	48247	1.9322	.60483	1.6534	1.1687	.14433	.85566	50
11	. 1778	. 8222	.9313	. 0522	.6523	.1689	. 4448	. 5551	49
12	. 1803	. 8197	.9304	. 0562	.6512	.1691	. 4463	. 5536	48
13	 1827 	. 8172	.9295	. 0602	.6501	.1693	. 4479	. 5521	47
14	. 1852	. 8147	.9285	. 0642	.6490	.1695	. 4494	. 5506	46
15	.51877	.48123	1.9276	.60681	1.6479	1.1697	.14509	.85491	45
16	. 1902	. 8098	.9267	. 0721	.6469	.1699	. 4524	. 5476	44
17	. 1927	. 8073	.9258	. 0761	.6458	.1701	. 4539	. 5461	43
18 19	. 1952 . 1977	. 8048	.9248	. 0801	.6447 .6436	.1703 .1705	. 4554 . 4569	. 5446	42
20	.52002	.47998	1.9230	.60881	1.6425	1.1707	.14581	.5431 .85416	41 40
21	. 2026	. 7973	.9221	. 0920	.6415	.1709	4599	. 5400	39
	. 2051	7949	.9212	. 0960	.6404	.1712	4615	. 5385	38
23	. 2076	. 7924	.9203	, 1000	.6393	.1714	. 4630	5370	37
24 25	. 2101	. 7899	.9193	. 1040	.6383	.1716	. 4645	. 5355	36
25	.52126	.47874	1.9184	.61080 -	1.6372	1.1718	.14660	.85340	35
26	. 2151	. 7849	.9175	. 1120	.6361	.1720	. 4675	. 5325	34
27 28 29	. 2175	. 7824	.9166	. 1160	.6350	.1722	. 4690	. 5309	33
28	· 2200	. 7800	.9157	. 1200 . 1240	.6340	.1724	. 4706	. 5294	32
29 30	.52250	.47750	1.9139	.61280	.6329 1.6318	$.1726 \\ 1.1728$. 4721 .14736	. 5279 .85264	31 30
31	. 2275	. 7725	.9130	. 1320	.6308	.1730	. 4751	. 5249	29
$3\overline{2}$	2299	7700	.9121	. 1360	.6297	.1732	4766	. 5234	28
33	. 2324	. 7676	.9112	. 1400	.6286	.1734	. 4782	. 5218	27
34	. 2349	. 7651	.9102	. 1440	.6276	.1737	. 4797	. 5203	26
35	.52374	.47626	1.9093	.61480	1.6265	1.1739	.14812	.85188	25
36	. 2398	. 7601	.9084	. 1520	.6255	.1741	. 4827	. 5173	24
37	. 2423	. 7577	.9075	1560	.6244	.1743	. 4842	. 5157	23
38 39	· 2448 · 2473	. 7552	.9066	.1601 .1641	.6233 .6223	.1745	. 4858 . 4873	.5142 .5127	22 21
40	.52498	.47502	1.9048	.61681	1.6212	1.1749	.14888	.85112	$\frac{21}{20}$
41	. 2522	. 7477	.9039	. 1721	.6202	.1751	. 4904	. 5096	19
42	. 2547	. 7453	.9030	. 1761	.6191	.1753	. 4919	. 5081	18
43	. 2572	. 7428	.9021	. 1801	.6181	.1756	. 4934	. 5066	17
44	. 2597	. 7403	.9013	. 1842	.6170	.1758	. 4949	. 5050	16
45	.52621	.47379	1.9004	.61882	1.6160	1.1760	.14965	.85035	15
46	. 2646	. 7354	.8995	. 1922	.6149	.1762	. 4980	. 5020	14
47 48	. 2671	. 7329	.8986	. 1962 . 2004	.6139 .6128	.1764 .1766	. 4995	. 5004	$13 \\ 12$
49	2720	. 7280	.8968	. 2043	.6118	.1768	5026	4974	11
50	.52745	.47255	1.8959	.62083	1.6107	1.1770	15041	.84959	10
51	. 2770	. 7230	.8950	. 2123	.6097	.1772	. 5057	. 4943	10
52	. 2794	. 7205	.8941	. 2164	.6086	.1775	. 5072	. 4928	8
53	. 2819	. 7181	.8932	. 2204	.6076	.1777	. 5087	. 4912	17
54	. 2844	. 7156	.8924	. 2244	.6066	.1779	. 5103	. 4897	6
55	.52868	.47131	1.8915	.62285	1.6055	1.1781	.15118	.84882	5
56	. 2893	. 7107	.8906	. 2325	.6045	.1783	. 5133	. 4866	4
57 58	. 2918 . 2942	. 7082	.8897	· 2366 · 2406	.6034	.1785	. 5149	. 4851	32
08 59	. 2942	. 7033	.8888	. 2406	.6024	.1787	. 5164	. 4836 . 4820	1
6 0	2992	. 7008	.8871	2487	.6003	.1790	5195	. 4805	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	V rs. cos.	Sine.	M.

354 32°

Natural Trigonometrical Functions.

147°

320		Natural Trigo			onometrical Function		ns. 147°		
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.52992	.47008	1.8871	.62487	1.6003	1.1792	.15195	.84805	60
1	, 3016	. 6983	.8862	. 2527	.5993	.1794	. 5211	4789	59
$\hat{2}$. 3041	. 6959	.8853	. 2568	.5983	.1796	. 5226	. 4774	58
$\hat{2} \\ 3$. 3066	. 6934	.8844	. 2608	.5972	.1798	. 5241	. 4758	57
4 5 6	. 3090	. 6909	.8836	. 2649	.5962	.1800	.5257 .15272	. 4743	56
5	.53115	.46885	1.8827	.62689	1.5952	1.1802	.15272	.84728	55
6	. 3140	. 6860	.8818	. 2730	.5941	.1805	. 5288	. 4712	54
7	. 3164	. 6835	.8809	. 2770	.5931	.1807	. 5303	. 4697	53
8	. 3189	. 6811	.8801	. 2811	.5921	.1809	. 5319	. 4681	52
9	. 3214	. 6786	.8792	. 2851	.5910	.1811	. 5334	. 4666	51
10	.53238	.46762	1.8783	.62892	1.5900	1.1813	.15350	.84650	50
$\frac{11}{12}$	 3263 3288 	.6737 .6712	.8775	. 2933 . 2973	.5890	.1815 .1818	.5365 .5381	.4635 .4619	49
$\frac{12}{13}$. 3200	6688	.8757	. 3014	.5869	.1820	. 5396	. 4604	40
14	. 3337	. 6663	.8749	. 3055	.5859	.1822	. 5412	4588	46
15	53361	.46638	1.8740	.63095	1.5849	1.1824	.15427	.84573	45
16	. 3386	. 6614	.8731	. 3136	.5839	.1826	. 5443	. 4557	44
17	. 3411	. 6589	.8723	. 3177	.5829	.1828	. 5458	4542	43
18	. 3435	. 6565	.8714	. 3217	.5818	.1831	. 5474	. 4526	42
19	. 3460	. 6540	.8706	. 3258	.5808	.1833	. 5489	. 4511	41
20	.53484	.46516	1.8697	.63299	1.5798	1.1835	.15505	.84495	40
21	. 3509	. 6491	.8688	. 3339	.5788	.1837	. 5520	. 4479	39
22	. 3533	. 6466	.8680	. 3380	.5778	.1839	. 5536	. 4464	38
23	. 3558	. 6442	.8671	. 3421	.5768	.1841	. 5552	. 4448	37
24	. 3583	. 6417	.8663	. 3462	.5757	.1844	. 5567	. 4433	36
25	.53607	.46393	1.8654	.63503	1.5747	1.1846	.15583	.84417	35
26	. 3632	• 6368	.8646 .8637	. 3543 . 3584	.5737	.1848 .1850	5598 5614	$\frac{4402}{4386}$	34
27 28	.3656 .3681	. 6319	.8629	. 3625	.5717	.1852	. 5630	4380	33 32
29	. 3705	. 6294	.8620	3666	.5707	.1855	. 5645	. 4355	31
30	.53730	.46270	1.8611	.63707	1.5697	1.1857	.15661	. 84339	30
31	. 3754	. 6245	.8603	. 3748	.5687	.1859	. 5676	. 4323	29
32	. 3779	. 6221	.8595	. 3789	.5677	.1861	. 5692	. 4308	28
33	. 3803	. 6196	.8586	. 3830	.5667	.1863	. 5708	. 4292	27
34	. 3828	. 6172	.8578	. 3871	.5657	.1866	. 5723	. 4276	26
35	.53852	.46147	1.8569	.63912	1.5646	1.1868	.15739	.84261	25
36	. 3877	. 6123	.8561	. 3953	.5636	.1870	. 5755	. 4245	24
37	. 3901	. 6098	.8552	. 3994	.5626	.1872	. 5770	. 4229	23
38	. 3926	. 6074	.8544	. 4035	.5616	.1874	. 5786	. 4214	22
39	. 3950 .53975	. 6049	.8535 1.8527	. 4076 .64117	.5606	.1877 1.1879	.5802 .15817	.4198	$\frac{21}{20}$
40 41	. 3999	.46025 .6000	.8519	. 4158	1.5596 .5586	.1881	. 5833	.84182 . 4167	19
41 42	. 4024	. 5976	.8510	. 4199	.5577	.1883	. 5849	. 4151	18
43	. 4048	. 5951	.8502	4240	.5567	.1886	. 5865	. 4135	17
44	4073	. 5927	.8493	. 4281	.5557	.1888	5880	4120	16
45	.54097	.45902	1.8485	.64322	1.5547	1.1890	.15896	.84104	15
46	. 4122	. 5878	.8477	. 4363	.5537	.1892	. 5912	. 4088	14
47	. 4146	. 5854	.8468	. 4404	.5527	.1894	. 5927	. 4072	13
48	. 4171	. 5829	.8460	. 4446	.5517	.1897	. 5943	. 4057	12
49	. 4195	. 5805	.8452	. 4487	.5507	.1899	. 5959	. 4041	11
50	.54220	.45780	1.8443	.64528	1.5497	1.1901	.15975	.84025	10
51	. 4244	. 5756	.8435	. 4569	.5487	.1903	. 5991	. 4009	9
52	. 4268 . 4293	. 5731	.8427	4610	.5477	.1906	. 6006	. 3993	8
53	. 4293	. 5707 . 5682	.8418 .8410	. 4652 . 4693	.5467	.1908 .1910	. 6022 . 6038	. 3978	
54 55	. 4317	. 5652	1.8410	. 4693	.5458 1.5448	1,1910	. 6058	.3962 .83946	6 5
55 56	. 4366	. 5634	.8394	. 4775	.5438	.1912	. 6070	. 3930	
57	. 4391	. 5609	.8385	4817	.5428	.1917	. 6085	. 3914	13
58	. 4415	. 5585	.8377	4858	.5418	.1919	6101	3899	1 g
59	4439	. 5560	.8369	4899	.5408	.1921	. 6117	. 3883	$\frac{2}{1}$
60	4464	. 5536	.8361	. 4941	.5399	.1922	. 6133	. 3867	ō
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine,	M.

1220

Table 3.

NATURAL FUNCTIONS.

33°		Na	tural Tr	igonom	etrical I	unction	IS.	14	46°
М.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.54464	.45536	1.8361	.64941	1.5399	1.1924	.16133	.83867	60
1	. 4488	. 5512	.8352	. 4 982	.5389	.1926	. 6149	. 3851	59
2	. 4513	. 5487	.8344	. 5023	.5379	.1928	. 6165	. 3835	58
2 3 4 5	. 4537	. 5463	-8336	. 5065	.5369	.1930	. 6180	. 3819 . 3804	57 56
- 2	. 4561 .54586	. 5438 .45414	.8328 1.8320	. 5106 .65148	.5359 1.5350	.1933 1.1935	. 6196 .16212	83788	55
6	. 4610	. 5390	.8311	. 5189	.5340	.1937	. 6228	. 3772	54
7	4634	. 5365	.8303	5231	.5330	.1939	. 6244	3756	53
8	. 4659	. 5341	.8295	. 5272	.5320	.1942	. 6260	. 3740	52
9	. 4683	. 5317	.8287	. 5314	.5311	.1944	. 6276	. 3724	51
10	.54708	.45292	1.8279	.65355	1.5301	1.1946	.16292	.83708	50
$\begin{array}{c c} 11 \\ 12 \end{array}$. 4732 . 4756	. 5268	.8271	. 5397	.5291	.1948	. 6308	. 3692	49 48
13	. 4781	. 5244 . 5219	.8263 .8255	.5438 .5480	.5282 .5272	.1951 .1953	. 6323	3676 3660	40
14	4805	5195	.8246	5521	.5262	.1955	6355	3644	46
15	54829	.45171	1.8238	.65563	1.5252	1.1958	.16371	83629	45
16	. 4854	. 5146	.8230	. 5604	.5243	.1960	. 6387	3613	44
17	. 4878	. 5122	.8222	. 5646	.5233	.1962	. 6403	. 3597	43
18	. 4902	. 5098	.8214	. 5688	.5223	.1964	. 6419	. 3581	42
19	. 4926	. 5073	.8206	. 5729	.5214	.1967	6435	. 3565	41
$\frac{20}{21}$.54951	.45049	1.8198	.65771	1.5204	1.1969	.16451	.83549	40
$\frac{21}{22}$. 4975 . 4999	. 5025	.8190	. 5813	.5195	.1971	. 6467	. 3533 . 3517	39
23	. 5024	. 4976	.8182	. 5854 . 5896	.5185	.1974 .1976	• 6483	. 3501	38 37
24	. 5048	4952	.8166	5938	.5166	.1978	6515	. 3485	36
$\overline{25}$.55072	.44928	1.8158	.65980	1,5156	1.1980	.16531	.83469	35
26	. 5097	. 4903	.8150	. 6021	.5147	.1983	. 6547	. 3453	34
27	. 5121	. 4879	.8142	. 6063	.5137	.1985	. 6563	. 3437	33
28	. 5145	. 4855	.8134	. 6105	.5127	.1987	. 6579	. 3421	32
29	. 5169	. 4830	.8126	. 6147	.5118	.1990	. 6595	. 3405	31
$\frac{30}{31}$.55194	.44806	1.8118	.66188 . 6230	1. 5108	1.1992 .1994	. 16611	.83388 .3372	30 29
32	. 5242	4758	.8102	6272	.5089	.1994	. 6643	. 3356	28
33	5266	4733	.8094	6314	.5080	.1999	6660	3340	27
34	. 5291	. 4709	.8086	6356	.5070	.2001	. 6676	. 3324	26
35	.55315	.44685	1.8078	.66398	1.5061	1.2004	.16692	.83308	25
36	. 5339	. 4661	.8070	. 6440	.5051	.2006	. 6708	. 3292	24
37	. 5363	. 4637	.8062	. 6482	.5042	.2008	. 6724	. 3276	23 22
38 39	. 5388	. 4612 . 4588	.8054	. 6524	.5032	.2010	6740	.3260 .3244	22
40	.55436	.44564	1.8039	6566	1.5013	1.2015	16772	.83228	20
41	. 5460	. 4540	.8031	. 6650	.5004	.2013	. 6788	. 3211	19
42	. 5484	. 4515	.8023	6692	.4994	.2020	6804	3195	18
43	5509	. 4491	.8015	. 6734	.4985	.2022	. 6821	. 3179	17
44	. 5533	. 4467	.8007	. 6776	.4975	.2024	. 6837	. 3163	16
45	.555557	.44443	1.7999	.66818	1.4966	1.2027	.16853	.83147	15
46	. 5581	. 4419	.7992	. 6860	.4957	.2029	. 6869	. 3131	14
47 48	. 5605	. 4395 . 4370	.7984	6902	.4947	.2031 .2034	6885	3115	13
49	5654	. 4346	.7968	6986	.4928	,2034	6918	. 3082	111
5 0	.55678	.44322	1.7960	.67028	1.4919	1.2039	.16934	.83066	10
51	. 5702	. 4298	.7953	. 7071	.4910	.2041	. 6950	. 3050	9
52	. 5726	. 4274	.7945	. 7113	.4900	.2043	. 6966	. 3034	87
53	. 5750	. 4250	.7937	. 7155	.4891	.2046	. 6982	. 3017	
54	. 5774	. 4225	.7929	. 7197	.4881	.2048	. 6999	. 3001	65
55	.55799	.44201	1.7921	.67239	1.4872	1.2050	.17015	.82985	4
56 57	. 5823	. 4177	.7914	. 7282	.4863	.2053	. 7031	2969	3
58	. 5871	4135	.7898	. 7366	.4844	.2055	7047	2936	3 2 1
59	5895	4105	7891	. 7408	.4835	.2060	7080	2920	Ιĩ
60	. 5919	4081	.7883	. 7451	.4826	.2062	. 7096	2904	Ô
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.
		1	II	1.0000081	1 1000	1.0000 11			

356 34°

Natural Trigonometrical Functions.

145°

34 ⁰		Natural Trigonor			netrical Functions.			145		
М.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	М.	
0	.55919	.44081	1.7883	.67451	1.4826	1.2062	.17096	.82904	60	
1	. 5943	. 4057	.7875	. 7493	.4816	.2064	. 7112	. 2887	59	
$\frac{2}{3}$. 5967	. 4032	.7867	. 7535	.4807	.2067	. 7129	. 2871	58	
3	. 5992	. 4008	.7860	. 7578	.4798	.2069	. 7145	. 2855	57	
4	. 6016	. 3984	.7852	. 7620	.4788	.2072	. 7161	. 2839	56	
5	.56040	.43960	1.7844 .7837	.67663	1.4779 .4770	1.2074	.17178	.82822 . 2806	55 54	
$\frac{6}{7}$	• 6064 • 6088	.3936 .3912	.7829	.7705 .7747	.4761	.2079	7210	2790	53	
8	. 6112	. 3888	7821	. 7790	.4751	.2081	7227	2773	52	
9	. 6136	. 3864	.7814	7832	.4742	.2083	. 7243	2757	51	
10	.56160	.43840	1.7806	.67875	1.4733	1.2086	.17259	.82741	50	
11	. 6184	. 3816	.7798	. 7917	.4724	.2088	. 7276	. 2724	49	
$\frac{12}{13}$. 6208	. 3792	.7791	. 7960	.4714	.2091	. 7292	. 2708	48	
14	• 6232 • 6256	.3768 .3743	.7783	. 8002 . 8045	.4705	.2093	. 7308 . 7325	. 2692 . 2675	47	
$15 \\ 15 \\ 15 \\ 15 \\ 15 \\ 15 \\ 15 \\ 15 \\$.56280	.43719	1.7768	.68087	1.4687	1,2098	.17341	.82659	45	
16	. 6304	. 3695	.7760	. 8130	.4678	.2100	. 7357	. 2643	44	
17	6328	. 3671	.7753	. 8173	.4669	.2103	7374	2626	43	
18	. 6353	. 3647	.7745	. 8215	.4659	.2105	. 7390	. 2610	42	
19	. 637 7	. 3623	.7738	. 8258	.4650	.2107	. 7406	. 2593	41	
20 21 22	.56401	.43599	1.7730	.68301	1.4641	1.2110	.17423	.82577	40	
21	. 6425 . 6449	. 3575 . 3551	.7723	. 8343 . 8386	.4632	.2112	. 7439	. 2561 . 2544	39	
$\frac{22}{23}$. 6473	. 3527	.7715	. 8429	.4623 .4614	.2115 .2117	. 7450	2528	38 37	
24	6497	. 3503	.7700	8471	.4605	.2119	7489	2511	36	
$\frac{24}{25}$.56521	.43479	1.7693	.68514	1.4595	1.2122	.17505	82495	35	
26	. 6545	. 3455	.7685	. 8557	.4586	.2124	. 7521	, 2478	34	
27	. 6569	. 3431	.7678	. 8600	.4577	.2127	. 7538	. 2462	33	
28	. 6593	. 3407	.7670	. 8642	.4568	.2129	. 7554	. 2445	32	
29 30	. 6617 .56641	. 3383 .43359	.7663 1.7655	. 8685 .68728	.4559	.2132 1.2134	. 7571 .17587	. 2429 .82413	31	
31	. 6664	. 3335	.7648	. 8771	1.4550 .4541	.2134	. 7604	. 2396	30 29	
32	6688	3311	.7640	. 8814	.4532	.2139	7620	2380	28	
33	. 6712	3287	.7633	8857	.4523	.2141	7637	2363	27	
34	. 6736	. 3263	.7625	. 8899	.4514	.2144	. 7653	. 2347	26	
35	.56760	.43239	1.7618	.68942	1.4505	1.2146	.17670	.82330	25	
36 37	. 6784	. 3216	.7610	. 8985	.4496	.2149	. 7686	. 2314	24	
37	. 6808 . 6832	.3192 .3168	.7603 .7596	. 9028 . 9071	.4487 .4478	.2151 .2153	. 7703 . 7719	. 2297 . 2280	$\frac{23}{22}$	
39	. 6856	3144	.7588	9114	.4469	.2156	7736	2260	$\tilde{21}$	
40	.56880	43120	1.7581	.69157	1.4460	1.2158	.17752	82247	$\overline{20}$	
41	. 6904	. 3096	.7573	. 9200	.4451	.2161	. 7769	. 2231	19	
42	. 6928	. 3072	7566	. 9243	.4442	.2163	. 7786	. 2214	18	
43	. 6952	. 3048	.7559	. 9286	.4433	.2166	. 7802	. 2198	17	
44 45	. 6976 .57000	. 3024 .43000	1.7551 1.7544	. 9329 .69372	.4424 1.4415	$\begin{array}{c} .2168 \\ 1.2171 \end{array}$. 7819 .17835	. 2181 .82165	$\frac{16}{15}$	
46	. 7023	. 2976	.7537	. 9415	.4406	.2173	. 7852	. 2148	10	
47	7047	2952	.7529	9459	4397	.2175	7868	2131	13	
48	7071	. 2929	.7522	9502	.4388	.2178	. 7885	2115	$\hat{1}\hat{2}$	
49	. 7095	. 2905	.7514	. 9545	.4379	.2180	. 7902	. 2098	11	
50	.57119	.42881	1.7507	.69588	1.4370	1.2183	.17918	.82082	10	
51	. 7143	. 2857	.7500	• 9631	.4361	.2185	. 7935	. 2065	9	
52 53	. 7167 . 7191	. 2833 . 2809	.7493 .7485	. 9674 . 9718	.4352	.2188 .2190	. 7951 . 7968	. 2048 . 2032	8	
54	. 7214	2785	.7478	9761	.4345	.2190	. 7900	. 2032 . 2015	7 6	
55	57238	.42761	1.7471	69804	1.4326	1.2195	.18001	81998	5	
56	. 7262	. 2738	.7463	. 9847	.4317	.2198	. 8018	. 1982	4	
57	. 7286	. 2714	.7456	. 9891	.4308	.2200	. 8035	. 1965	3	
58	. 7310	. 2690	.7449	. 9934	.4299	.2203	. 8051	. 1948	2	
59	. 7334	. 2666	.7442	. 9977	.4290	.2205	. 8068	. 1932	1	
60	. 7358	. 2642	.7434	.70021	.4281	.2208	. 8085	. 1915	0	
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.	

Natural Trigonometrical Functions.

144°

						anotio		-	
<u>M.</u>	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	<u>M</u> .
0	.57358	.42642	1.7434	.70021	1.4281	1.2208	.18085	.81915	60
1	. 7381	. 2618	.7427	. 0064	.4273	.2210	. 8101	. 1898	59
2	. 7405	. 2595	.7420	. 0107	.4264	.2213	. 8118	. 1882	58
3	. 7429	. 2571	.7413	. 0151	.4255	.2215	. 8135	. 1865	57
4 5	. 7453	. 2547	.7405	. 0194	.4246	.2218	. 8151	. 1848	56
5	.57477	.42523	1.7398	.70238	1.4237	1.2220	.18168	.81832	55
6	. 7500	. 2499	.7391	. 0281	.4228	.2223	. 8185	. 1815	54
7	. 7524	. 2476	.7384	. 0325	.4220	.2225	. 8202	. 1798	53
8	. 7548	. 2452	.7377	. 0368	.4211	.2228	. 8218	. 1781	52
.9	. 7572	. 2428	.7369	. 0412	.4202	.2230	. 8235	. 1765	51
10	.57596	.42404	1.7362	.70455	1.4193	1.2233	.18252	.81748	50
$\frac{11}{12}$	• 7619 • 7643	2380 2357	.7355	. 0499	.4185	.2235	. 8269 . 8285	.1731	49
12	. 7667	2333	.7348	. 0542	.4176	.2238		. 1714	48
13	7691	2309	.7341 .7334	. 0629	.4167	.2240	. 8302 . 8319	. 1698	47
15	57714	42285	1.7327	.70673	.4158	1.2245	.18336	.1681 .81664	46
16	. 7738	2262	7319	. 0717	1.4150 .4141	.2248	. 8353	. 1647	45 44
17	7762	2238	.7312	0760	.4132	.2240	. 8369	. 1630	43
18	7786	2214	.7305	. 0804	.4123	.2253	. 8386	. 1614	42
19	7809	2190	7298	. 0848	.4115	.2255	. 8403	1597	41
20	57833	.42167	1.7291	.70891	1.4106	1.2258	.18420	.81580	40
21	. 7857	. 2143	.7284	. 0935	.4097	.2260	. 8437	. 1563	39
22	. 7881	. 2119	7277	. 0979	.4089	.2263	. 8453	1546	38
$\tilde{23}$. 7904	. 2096	.7270	1022	.4080	.2265	. 8470	1530	37
24	. 7928	. 2072	,7263	. 1066	.4071	.2268	8487	. 1513	36
25	57952	.42048	1.7256	.71110	1.4063	1.2270	.18504	.81496	35
26	. 7975	. 2024	.7249	. 1154	.4054	.2273	. 8521	. 1479	34
27	. 7999	. 2001	.7242	. 1198	.4045	.2276	. 8538	. 1462	33
28	 8023 	. 1977	.7234	. 1241	.4037	.2278	. 8555	. 1445	32
29	. 8047	. 1953	.7227	. 1285	.4028	.2281	. 8571	. 1428	31
30	.58070	.41930	1.7220	.71329	1.4019	1.2283	.18588	.81411	30
31	. 8094	. 1906	.7213	. 1373	.4011	.2286	. 8605	. 1395	29
32	. 8118	. 1882	.7206	. 1417	.4002	.2288	. 8622	. 1378	28
33	. 8141	. 1859	.7199	. 1461	.3994	.2291	. 8639	. 1361	27
34	· 8165	. 1835	.7192	. 1505	.3985	.2293	. 8656	. 1344	26
25	.58189	.41811	1.7185	.71549	1.3976	1.2296	.18673	.81327	25
36	- 8212	1788	.7178	. 1593	.3968	.2298	. 8690	. 1310	24
37	 8236 8259 	. 1764	.7171 .7164	. 1637 . 1681	.3959 .3951	.2301 .2304	. 8707 . 8724	. 1293	23
88 39	8259 8283	1717	.7157	. 1725	.3942	.2304	. 8741	.1276 .1259	22 21
40	.58307	.41693	1.7151	.71769	1.3933	1.2309	.18758	.81242	20
41	. 8330	. 1669	.7144	. 1813	.3925	.2311	. 8775	. 1225	19
42	8354	. 1646	.7137	. 1857	.3916	.2314	8792	1208	18
43	8378	1622	.7130	1901	.3908	.2316	8809	. 1191	17
44	. 8401	1599	.7123	1945	.3899	.2319	. 8826	. 1174	16
45	.58425	41575	1.7116	71990	1.3891	1.2322	18843	.81157	15
46	. 8448	. 1551	.7109	. 2034	.3882	.2324	. 8860	. 1140	14
47	. 8472	. 1528	.7102	. 2078	.3874	.2327	. 8877	. 1123	13
48	. 8496	. 1504	.7095	. 2122	.3865	.2329	. 8894	. 1106	12
49	. 8519	. 1481	.7088	. 2166	.3857	.2332	. 8911	. 1089	11
50	.58543	.41457	1.7081	.72211	1.3848	1.2335	.18928	.81072	10
51	 8566 	. 1433	.7075	. 2255	.3840	.2337	. 8945	. 1055	9
52	. 8590	. 1410	.7068	. 2299	.3831	.2340	. 8962	. 1038	8
53	. 8614	. 1386	.7061	. 2344	.3823	.2342	. 8979	. 1021	7
54	. 8637	. 1363	.7054	. 2388	.3814	.2345	. 8996	. 1004	6
55	.58661	.41339	1.7047	.72432	1.3806	1.2348	.19013	.80987	5
56	. 8684	. 1316	.7040	. 2477	.3797	.2350	. 9030	. 0970	4
57	. 8708	. 1292	.7033	. 2521	.3789	.2353	. 9047	. 0953	3
58	. 8731	. 1268	.7027	. 2565	.3781	.2355	. 9064	. 0936	2
59	. 8755	. 1245	.7020	. 2610	.3772	.2358	. 9081	. 0919	1
60	. 8778	. 1221	.7013	. 2654	.3764	.2361	. 9098	. 0902	0
NT	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vra con	Sine.	M.
<u>M.</u>	Cosme.	1 1 18, 811.	becant.	onang.	Taug.	COBEC IL	7 FB, COB, (one.	111

Natural Trigonometrical Functions.

143°

	30		118	urai ii	rigonom	errical	runctio	15.	1	43°
	M.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine,	M.
	0	.58778	.41221	1.7013	.72654	1.3764	1.2361	.19098	.80902	60
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1									59
$ \begin{array}{ccccccccccccccccccccccccccccccccccc$	$\overline{2}$. 2743		.2366			58
$ \begin{array}{ccccccccccccccccccccccccccccccccccc$	3	. 8849	. 1151	.6993		.3738		. 9150		57
	4									56
	5				.72877					55
	6									54
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	7									53
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	8									52
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $. 3055			. 9252		51
					.73100					50
	11									
					3078					46
					73323	1 3638				45
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										44
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										43
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $										42
$\begin{array}{c c c c c c c c c c c c c c c c c c c $										41
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.40752	1.6878	.73547			.19442	.80558	40
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	21	. 9272	. 0728	.6871		.3588	.2416		. 0541	39
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	22			.6865		.3580	.2419		. 0524	38
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	23	. 9318				.3572	.2421	. 9493	. 0507	37
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	24 1					.3564				36
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	25									35
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	26									34
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	27									33
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	28									32
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										31
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	30									30
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										29
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	22									28
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										20
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	36									24
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	37				4312					23
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	38									22
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	39			.6752	. 4402		.2464			21
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.59716					1.2467	.19788	.80212	20
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$.3424		. 9805	. 0195	19
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$										18
$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$										17
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$.6720			.2478			16
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										15
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$										14
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$										13
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$.0094						
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$.0009				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										9
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	53									97
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										6
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	55						1 2508			5
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										4
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										3
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										2
<u>60</u> . 0181 . 9818 .6616 . 5355 .3270 .2521 . 0136 . 9863 (ĩ
M. Cosine. Vrs. sin. Secant. Cotang. Tang. Cosec'nt Vrs. cos. Sine. M.		. 0181	. 9818	.6616						Ô
	M.	Cosine.	Vrs. sin.	Secant.	Cotang,	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

126°

Natural Trigonometrical Functions.

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310		INB	tural II	rigonom	etrical	Function	ns.	1.	4 <i>2</i> °
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	М.
0	.60181	.39818	1.6616	.75355	1.3270	1.2521	.20136	.79863	60
0	. 0205	. 9795	.6610	. 5401	.3262	.25?4	. 0154	. 9846	59
23	. 0228	. 9772	.6603	. 5447	.3254	.2527	. 0171	. 9828	58
3	. 0251	. 9749	.6597	. 5492	.3246	.2530	. 0189	. 9811	57
4 5 6 7	. 0274	. 9726	.6591	. 5538	.3238	.2532	. 0206	. 9793	56
ð	.60298	.39702	1.6584	.75584	1.3230	1.2535	.20224	.79776	55
5	. 0320	. 9679	.6578	. 5629	.3222	.2538	. 0242	. 9758	54
6	. 0344 . 0367	• 9656 • 9633	.6572	.5675 .5721	.3214 .3206	.2541 .2543	. 0259	9741	53 52
8 9	. 0390	. 9610	.6565	5767	.3198	.2546	. 0294	. 9706	51
10	.60413	39586	1.6552	75812	1.3190	1.2549	.20312	.79688	50
ĨĬ.	. 0437	. 9563	.6546	5858	.3182	.2552	. 0329	. 9670	49
$\overline{12}$. 0460	. 9540	.6540	. 5904	.3174	.2554	. 0347	. 9653	48
13	. 0483	. 9517	.6533	. 5950	.3166	.2557	. 0365	. 9635	47
14	. 0506	. 9494	.6527	. 5996	.3159	.2560	. 0382	. 9618	46
15	.60529	.39471	1.6521	.76042	1.3151	1.2563	.20400	.79600	45
16	. 0552	• 9447	.6514	. 6088	.3143	.2565	. 0417	• 9582	44
17	. 0576	. 9424	.6508	. 6134	.3135	.2568	. 0435	• 9565	43
18 19	. 0599 . 0622	9401	.6502 .6496	• 6179 • 6225	.3127 .3119	.2571	. 0453	. 9547 . 9530	42
20	.60645	.39355	1.6489	.76271	1.3111	1.2577	.20488	.79512	40
20 21 22 23 24	. 0668	. 9332	.6483	. 6317	.3103	.2579	. 0505	. 9494	39
22	. 0691	. 9309	.6477	. 6364	.3095	.2582	. 0523	. 9477	38
23	0714	. 9285	.6470	. 6410	.3087	.2585	. 0541	. 9459	37
24	. 0737	. 9262	.6464	. 6456	.3079	.2588	. 0558	. 9441	36
25	.6076 1	.39239	1.6458	.76502	1.3071	1.2591	.20576	.79424	35
25 26 27 28 29	. 0784	. 9216	.6452	 6548 	.3064	.2593	. 0594	. 9406	34
27	. 0807	. 9193	.6445	. 6594	.3056	.2596	. 0611	. 9388	33
28	. 0830	. 9170	.6439	. 6640	.3048	.2599	. 0629	. 9371	32 31
29	. 0853 .60876	. 9147	.6433 1.6427	. 6686 .76733	.3040 1.3032	.2602 1.2605	. 0647	. 9353 .79335	30
30 81	. 0899	. 9101	.6420	. 6779	.3024	.2607	. 0682	. 9318	29
32	. 0922	9078	.6414	6825	.3016	.2610	0700	. 9300	28
33	. 0945	9055	.6408	. 6871	.3009	.2613	. 0718	9282	28 27
34	. 0963	. 9031	.6402	. 6918	.3001	.2616	. 0735	. 9264	26
35	.60991	.39008	1.6396	.76964	1.2993	1.2619	.20753	.79247	25
36	. 1014	. 8985	.6389	. 7010	.2985	.2622 .2624	. 0771	. 9229	24
37 38	. 1037 . 1061	. 8962 . 8939	.6383 .6377	. 7057 . 7103	.2977 .2970	.2624	. 0789	. 921 1 . 9193	23 22
39	. 1084	. 8939	.6371	. 7149	.2962	.2630	. 0824	. 9195	21
40	.61107	.38893	1.6365	.77196	1.2954	1.2633	.20842	.79158	20
41	. 1130	. 8870	.6359	7242	.2946	.2636	. 0860	. 9140	19
$\overline{42}$. 1153	. 8847	.6352	. 7289	.2938	.2639	. 0878	. 9122	18
43	. 1176	. 8824	.6346	. 7335	.2931	.2641	. 0895	. 9104	17
44	. 1199	. 8801	.6340	. 7382	.2923	.2644	. 0913	. 9087	16
45	.61222	.38778	1.6334	.77428	1.2915	1.2647	.20931	.79069	15
46	. 1245	· 8755	6328	. 7475	.2907	.2650	. 0949	. 9051	14
47 48	. 1268 . 1290	. 8732 . 8709	.6322 .6316	. 7521 . 7568	.2900	.2653 .2656	. 0967	. 9033 . 9015	13 12
49	. 1314	. 8686	.6309	7614	.2884	.2659	1002	. 8998	11
50	.61337	.38663	1.6303	.77661	1.2876	1.2661	.21020	.78980	10
51	. 1360	. 8640	.6297	7708	.2869	.2664	. 1038	. 8962	9
52	. 1383	. 8617	.6291	. 7754	.2861	.2667	. 1056	. 8944	87
53	. 1405	. 8594	.6285	. 7801	.2853	.2670	. 1074	. 8926	7
54	. 1428	. 8571	.6279	. 7848	.2845	.2673	. 1091	. 8908	6
55	.61451	.38548	1.6273	.77895	1.2838	1.2676	.21109	.78890	5
56	. 1474	. 8525	6267	. 7941	.2830	.2679	. 1127	. 8873	4
57	. 1497 . 1520	. 8503 . 8480	.6261	. 7988 . 8035	.2822	.2681 .2684	.1145 .1163	. 8855 . 8837	0
58 59	. 1520 . 1543	. 8457	.6235	. 8082	.2815	2687	. 1103	. 8819	3 2 1
60	. 1566	8434	.6243	. 8128	2799	.2690	1199	. 8801	ō
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М.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

Natural Trigonometrical Functions.

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30-		148	turai ir	igonom	etricar	unction	13.		
Μ.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.61566	.38434	1.6243	.78128	1.2799	1.2690	.21199	.78801	60
ĭ	, 1589	. 8411	.6237	. 8175	.2792	.2693	. 1217	. 8783	59
$\overline{2}$. 1612	. 8388	.6231	, 8222	.2784	.2696	. 1235	8765	58
3	. 1635	. 8365	.6224	. 8269	.2776	.2699	. 1253	. 8747	57
4	. 1658	. 8342	.6218	. 8316	.2769	.2702	. 1271	. 8729	56
5	.61681	.38319	1.6212	.78363	1.2761	1.2705	.21288	.78711	55
6	. 1703	. 8296	.6206	. 8410	.2753	.2707	. 1306	. 8693	54
7	. 1726	. 8273	.6200	. 8457	.2746	.2710	. 1324 . 1342	8675 8657	53 52
8	· 1749 · 1772	8251 8228	.6194 .6188	. 8504 . 8551	.2738	.2713 .2716	1360	. 8640	51
10	.61795	38205	1.6182	.78598	1.2723	1.2719	.21378	78622	50
11	. 1818	. 8182	.6176	. 8645	.2715	.2722	. 1396	. 8604	49
12	1841	8159	.6170	. 8692	2708	.2725	. 1414	. 8586	48
13	1864	. 8136	.6164	8739	.2700	2728	. 1432	. 8568	47
14	. 1886	. 8113	.6159	. 8786	.2692	.2731	. 1450	. 8550	46
15	.61909	.38091	1.6153	.78834	1.2685	1.2734	.21468	.78532	45
1 6	1932	. 8068	.6147	. 8881	.2677	.2737	. 1486	. 8514	44
17	. 1955	. 8045	.6141	· 8928	.2670	.2739	. 1504	. 8496	43
18	1978	. 8022	.6135	. 8975	.2662	.2742	. 1522	. 8478	42
19	. 2001	. 7999	.6129	. 9022 .79070	.2655 1.2647	.2745 1.2748	. 1540	. 8460 .78441	41 40
$\frac{20}{21}$.62023 . 2046	.37976 .7954	1.6123 .6117	. 9117	.2639	.2751	. 1576	. 8423	39
$\frac{21}{22}$	2040	7931	.6111	9164	.2632	2754	1594	. 8405	38
23	2003	7908	.6105	9212	2624	2757	1612	. 8387	37
$\tilde{2}\tilde{4}$. 2115	7885	.6099	9259	.2617	.2760	. 1631	. 8369	36
25	.62137	.37862	1.6093	.79306	1.2609	1.2763	.21649	.78351	35
26 27	. 2160	. 7840	.6087	. 9354	.2602	.2766	. 1667	. 8333	34
27	. 2183	. 7817	.6081	. 9401	.2594	.2769	. 1685	. 8315	33
28	. 2206	. 7794	.6077	. 9449	.2587	2772	. 1703	. 8297	32
29	. 2229	. 7771	.6070	. 9496	.2579	.2775	. 1721	. 8279	31
30	.62251 .2274	.37748 .7726	1.6064	.79543 . 9591	1.2572 .2564	1.2778 .2781	.21739 . 1757	.78261 . 8243	$\frac{30}{29}$
$\frac{31}{32}$	22/4	7703	.6058 .6052	· 9591	.2557	.2784	1757	. 8224	29
33	2320	. 7680	.6046	. 9686	.2549	.2787	1793	. 8206	27
34	2342	7657	.6040	9734	.2542	2790	1812	. 8188	$\tilde{26}$
35	62365	.37635	1.6034	79781	1.2534	1.2793	.21830	.78170	25
36	. 2388	. 7612	.6029	. 9829	.2527	.2795	. 1848	. 8152	24
37	. 2411	. 7589	.6023	. 9876	.2519	.2798	. 1866	 8134 	23
38	. 2433	. 7566	.6017	. 9924	.2512	.2801	. 1884	. 8116	22
39	. 2456	. 7544	.6011	. 9972	.2504	.2804	. 1902	. 8097	21
40	.62479 . 2501	.37521	1.6005	.80020 .0067	1.2497 .2489	1.2807	.21921	.78079	20
41 42	2501	. 7498 . 7476	.6000	. 0115	.2489	.2810 .2813	. 1939 . 1957	. 8061 . 8043	19 18
43	2547	. 7453	5988	. 0163	.2475	.2816	1975	. 8025	17
44	2570	7430	.5982	. 0211	.2467	.2819	1993	8007	16
45	.6 2592	.37408	1.5976	80258	1.2460	1.2822	.22011	.77988	15
46	2615	. 7385	.5971	. 0306	.2452	.2825	. 2030	. 7970	14
47	 2638 	. 7362	.5965	. 0354	.2445	.2828	. 2048	. 7952	13
48	 2660 	. 7340	.5959	. 0402	.2437	.2831	 2066 	. 7934	12
49	. 2683	. 7317	.5953	. 0450	.2430	.2834	. 2084	. 7915	11
50	62706	.37294	1.5947	.80498	1.2423	1.2837	.22103	.77897	10
51 52	2728 2751	. 7272 . 7249	.5942 .5936	. 0546 . 0594	.2415	.2840 .2843	· 2121 · 2139	. 7879 . 7861	9
53	2774	7226	.5930	0642	.2400	.2846	. 2159	. 7842	87
54	2796	7204	5924	. 0690	.2393	.2849	2176	7824	6
55	.62819	.37181	1.5919	.80738	1.2386	1.2852	.22194	77806	5
56	2841	. 7158	.5913	. 0786	.2378	.2855	. 2212	. 7788	4
57	. 2864	. 7136	.5907	. 0834	.2371	.2858	. 2230	. 7769	3
58	. 2887	. 7113	.5901	. 0882	.2364	.2861	. 2249	. 7751	2
59	. 2909	. 7090	.5896	. 0930	.2356	.2864	. 2267	. 7733	1
60	. 2932	. 7068	.5890	. 0978	.2349	.2867	. 2285	. 7715	_0
М.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec 'nt	Vrs. cos.	Sine.	м.

Natural Trigonometrical Functions.

				Bourou	ett teat				
<u>M.</u>	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.62932	.37068	1.5890	.80978	1.2349	1.2867	.22285	.77715	60
1	. 2955	. 7045	.5884	. 1026	.2342	.2871	. 2304	. 7696	59
$^{2}_{3}$. 2977 . 3000	. 7023 . 7000	.5879	. 1075	.2334	.2874	. 2322	. 7678	58
4	. 3022	. 6977	.5873 .5867	.1123 .1171	.2320	.2877 .2880	· 2340 · 2359	7660 7641	57 56
4 5	.63045	.36955	1.5862	.81219	1.2312	1.2883	.22377	77623	55
6 7	. 3067	. 6932	.5856	. 1268	.2305 .2297	.2886	. 2395	. 7605	54
	. 3090	. 6910	.5850	. 1316	.2297	.2889	. 2414	 7586 	53
8 9	. 3113 . 3135	. 6887	.5845	. 1364	.2290	.2892	. 2432	. 7568	52
10	.63155	. 6865 .36842	.5839 1.5833	. 1413 .81461	.2283 1.2276	.2895 1.2898	. 2450 .22469	. 7549 .77531	51 50
11	. 3180	. 6820	.5828	. 1509	.2268	.2901	. 2487	7513	49
12	 3203 	. 6797	.5822	. 1558	.2261	.2904	. 2505	. 7494	48
13	. 3225	. 6774	.5816	. 1606	.2254	.2907	 2524 	. 7476	47
14	. 3248	. 6752	.5811	. 1655	.2247	.2910	. 2542	. 7458	46
15 16	.63270 . 3293	.36729	1.5805 .5799	.81703 . 1752	1.2239	1.2913 .2916	.22561	.77439 .7421	45
17	. 3315	6684	.5794	1800	.2232 .2225	.2919	2597	7402	43
18	3338	. 6662	.5788	1849	.2218	.2922	2616	7384	42
19	. 3360	. 6639	.5783	. 1898	.2210	.2926	. 2634	7365	41
20	.63383	.36617	1.5777	.81946	1.2203	1.2929	.22653	.77347	40
21 22	 3405 3428 	. 6594 . 6572	5771	. 1995	.2196 .2189	.2932 .2935	. 2671 . 2690	. 7329 . 7310	39
22	. 3450	. 6549	.5766 .5760	· 2043 · 2092	.2189	.2935	2708	. 7292	38 37
24	. 3473	6527	.5755	. 2141	.2174	.2941	2727	7273	36
25	.63495	.36504	1.5749	.82190	1.2167	1.2944	.22745	77255	35
26 27	. 3518	. 6482	.5743	. 2238	.2160 .2152	.2947	. 2763	. 7236	34
27 28	. 3540 . 3563	. 6459 . 6437	.5738 .5732	2287 2336	.2152	.2950 .2953	. 2782 . 2800	. 7218 . 7199	33
28 29	. 3585	. 6415	.5732	2385	.2140	.2955	2819	. 7181	32
30	.63608	.36392	1.5721	.82434	1.2131	1.2960	.22837	77162	30
31	. 3630	. 6370	.5716	. 2482	.2124	.2963	2856	. 7144	29
$\frac{32}{2}$. 3653	. 6347	.5710	. 2531	.2117	.2966	. 2874	. 7125	28
$\frac{33}{34}$. 3675 . 3697	6325 6302	.5705 .5699	. 2580 . 2629	.2109	.2969 .2972	. 2893 . 2912	. 7107 . 7088	27 26
35	.63720	.36280	1.5694	.82678	1.2095	1.2975	.22930	77070	25
36	. 3742	. 6258	.5688	. 2727	.2088	.2978	. 2949	. 7051	24
37	. 3765	. 6235	.5683	. 2776	.2081	.2981	. 2967	. 7033	23 22
38 39	. 3787 . 3810	. 6213 . 6190	.5677 .5672	. 2825 . 2874	.2074	.2985 .2988	. 2986 . 3004	. 7014 . 6996	22
40	.63832	.36168	1,5666	.82923	1.2059	1.2991	.23023	.76977	20
41	. 3854	. 6146	.5661	. 2972	.2052	.2994	. 3041	6958	19
42	. 3877	. 6123	.5655	. 3022	.2045	.2997	. 3060	. 6940	18
43	. 3899	. 6101	.5650	. 3071	.2038 .2031	.3000	. 3079	. 6921	17
44 45	. 3921 .63944	. 6078	.5644 1.5639	. 3120 .83169	1.2031	.3003 1.3006	. 3097 .23116	. 6903 76884	16 15
46	. 3966	. 6034	.5633	. 3218	.2016	.3010	. 3134	. 6865	14
47	. 3989	. 6011	.5628	3267	.2009	.3013	. 3153	. 6847	13
48	. 4011	. 5989	.5622	. 3317	.2002	.3016	. 3172	. 6828	12
49 50	. 4033	. 5967 .35944	.5617 1.5611	. 3366 .83415	.1995 1.1988	.3019 1.3022	.3190 .23209	. 6810 .76791	11 10
51	. 4078	. 5922	.5606	. 3465	.1981	.3025	3227	. 6772	9
52	4100	. 5900	.5600	. 3514	.1974	.3029	3246	6754	8
53	. 4123	. 5877	.5595	. 3563	.1967	.3032	. 3265	. 6735	7
54	. 4145	. 5855	.5590	. 3613	.1960	.3035	. 3283	. 6716	ę
55 56	.64167 . 4189	.35833	1.5584 .5579	.83662 . 3712	1.1953 .1946	1.3038 .3041	.23302 .3321	.76698 .6679	5 4
57	. 4212	. 5788	.5573	3761	1939	.3044	3339	6660	3
58	4234	. 5766	.5568	. 3811	.1932	.3048	3358	. 6642	2
59	. 4256	. 5743	.5563	. 3860	.1924	.3051	. 3377	. 6623	1
60	. 4279	. 5721	.5557	. 3910	.1917	.3054	. 3395	. 6604	0
M.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.
129	0							·,	50°
								•	

40°

Natural Trigonometrical Functions.

139°

40	•	INE	iturai I	rigonon	errical	Functio	ns.	1	39-
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.64279	.35721	1.5557	.83910	1.1917	1,3054	.23395	.76604	60
1	. 4301	. 5699	.5552	. 3959	.1910	.3057	, 3414	. 6586	59
2	. 4323	. 5677	.5546	. 4009	.1903	.3060	. 3433	. 6567	58
2 3 4 5 6 7	. 4345	. 5654	,5541	. 4059	.1896	.3064	. 3452	. 6548	57
4	. 4368	. 5632	.5536	. 4108	.1889	.3067	. 3470	. 6530	56
5	.64390	.35610	1.5530	.84158	1.1882	1.3070	.23489	.76511	55
6	. 4412	. 5588	.5525	. 4208	.1875	.3073	. 3508	. 6492	54
7	. 4435	. 5565	.5520	. 4257	.1868	.3076	. 3527	. 6473	53
8	. 4457	. 5543	.5514	. 4307	.1861	.3080	. 3545	. 6455	52
9	. 4479	. 5521	.5509	. 4357	.1854	.3083	. 3564	. 6436	51
10	.64501	.35499	1.5503	.81107	1.1847	1.3086	.23583	.76417	50
11	. 4523	. 5476	.5498	. 4457	.1840	.3089	. 3602	. 6398 . 6380	49
12	. 4546	.5454 .5432	.5493	. 4506	.1833	.3092	. 3620	, 6361	47
$\frac{13}{14}$. 4568 . 4590	5410	.5487 .5482	. 4556 . 4606	.1826 .1819	.3096	. 3658	6342	46
15	.64612	.35388	1.5477	.84656	1.1812	1.3102	.23677	.76323	45
16	. 4635	. 5365	.5471	. 4706	.1805	.3105	. 3695	. 6304	44
17	. 4657	5343	.5466	4756	.1798	.3109	. 3714	. 6286	43
18	4679	. 5321	.5461	. 4806	.1791	.3112	. 3733	6267	42
19	4701	5299	.5456	4856	.1785	.3115	3752	6248	41
20	.64723	.35277	1.5450	.84906	1.1778	1.3118	.23771	.76229	40
21	. 4745	. 5254	.5445	. 4956	.1771	.3121	. 3790	. 6210	39
22	4768	. 5232	.5440	. 5006	.1764	.3125	. 3808	. 6191	38
23	. 4790	. 5210	.5434	. 5056	.1757	.3128	3827	. 6173	37
24	. 4812	5188	.5429	, 5107	.1750	.3131	. 3846	, 6154	36
25	.64834	.35166	1.5424	.85157	1.1743	1.3134	.23865	.76135	35
26	. 4856	. 5144	.5419	. 5207	.1736	.3138	. 3884	. 6116	34
27	. 4878	. 5121	.5413	. 5257	.1729	.3141	. 3903	. 6097	33
20 21 22 23 24 25 26 27 28 29 30 31	. 4900	. 5099	.5408	. 5307	.1722	.3144	. 3922	. 6078	32
29	. 4923	. 5077	.5403	. 5358	.1715	.3148	. 3940	. 6059	31
30	.64945	.35055	1.5398	.85408	1.1708	1.3151	.23959	.76041	30
31	. 4967	. 5033	.5392	. 5458	.1702	.3154	. 3978	. 6022	29
32	. 4989	. 5011	.5387	. 5509	.1695	.3157	. 3997	. 6003	28
33	. 5011	. 4989	.5382	. 5559	.1688	.3161	. 4016	. 5984	27
$\frac{34}{35}$. 5033 .65055	.4967 .34945	.5377 1.5371	. 5609 .85660	$.1681 \\ 1.1674$.3164	.4035 .24054	5965 75946	26 25
36	. 5077	. 4922	.5366	. 5710	.1667	$1.3167 \\ .3170$. 4073	, 5927	20
37	5099	4900	.5361	. 5761	.1660	.3174	. 4092	5908	23
38	5121	4878	.5356	. 5811	.1653	.3177	. 4111	. 5889	22
39	. 5144	4856	.5351	5862	1647	.3180	4130	5870	21
40	.65166	.34834	1.5345	.85912	$.1647 \\ 1.1640$	1.3184	.24149	75851	20
41	. 5188	, 4812	.5340	. 5963	.1633	.3187	. 4168	5832	19
42	. 5210	. 4790	.5335	. 6013	.1626	.3190	. 4186	5813	18
43	. 5232	. 4768	.5330	. 6064	.1619	.3193	4205	. 5794	17
44	. 5254	. 4746	.5325	. 6115	.1612	.3197	. 4224	. 5775	16
45	.65276	.34724	1.5319	.86165	-1.1605	1.3200	.24243	.75756	15
46	. 5298	. 4702	.5314	. 6216	.1599	.3203	. 4262	. 5737	14
47	. 5320	. 4680	.5309	. 6267	.1592	.3207	. 4281	. 5718	13
48	. 5342	· . 4658	.5304	. 6318	.1585	.3210	. 4300	. 5699	12
49	. 5364	. 4636	.5299	. 6368	.1578	.3213	. 4319	. 5680	11
50	.65386	.34614	1.5294	.86419	1.1571	1.3217	.24338	.75661	10
51	. 5408	. 4592 . 4570	.5289 .5283	. 6470	.1565	.3220	. 4357	. 5642	9
52	. 5430 . 5452	. 4570	.5283	. 6521	.1558	.3223	. 4376	. 5623	8 7 6
53 54	. 5474	. 4546	.5278	. 6572	.1551	.3227	. 4396	. 5604	17
55	.65496	.34504	1.5273 1.5268	.6623 .86674	.1544 1.1537	.3230 1.3233	.4415 .24434	. 5585	0
56	. 5518	. 4482	.5263	. 6725				.75566	5
56 57	. 5540	4460	.5258	6775	.1531 .1524	.3237 .3240	$\begin{array}{c} . 4453 \\ . 4472 \end{array}$	5547	4
58	5562	4438	.5253	. 6826	.1517	.3240	. 4472	. 5528 . 5509	3
59	. 5584	. 4416	.5248	. 6878	.1510	.3243	. 4510	. 5490	
60	5606	. 4394	.5242	6929	.1504	.3250	4529	. 5471	0
М.	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec 'nt	Vrs. cos.	Sine,	M.
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Table 3.

41°

Natural Trigonometrical Functions.

410		Na	tural Tr	igonom	etrical	Function	15.	1.	38°
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.65606	.34394	1.5242	.86929	1.1504	1.3250	.24529	.75471	60
1	. 5628	. 4372	.5237	. 6980	.1497 .1490	.3253 .3257	. 4548	. 5452	59
2	. 5650	. 4350	.5232	. 7031	.1490	.3257	. 4567	. 5433	58 57
34 56 7	. 5672	. 4328	.5227	. 7082	.1483	.3260	. 4586	. 5414	57
4	. 5694	. 4306 .34284	.5222 1.5217	. 7133 .87184	.1477 1,1470	.3263 1.3267	. 4605	. 5394 .75375	56 55
8	.657 16 .5737	. 4262	.5212	. 7235	.1463	.3270	. 4644	. 5356	54
7	5759	4240	5207	7287	.1456	3274	4663	5337	53
8	. 5781	. 4219	.5202	7338	.1450	.3277	. 4682	. 5318	52
9	. 5803	. 4197	.5197	. 7389	.1443	.3280	. 4701	. 5299	51
10	.65825	.34175	1.5192	.87441	1.1436	1.3284	.24720	.75280	50
$\frac{11}{12}$	· 5847	. 4153	.5187	. 7492	.1430	.3287 .3290	. 4739 . 4758	.5261 .5241	49 48
13	. 5869 . 5891	. 4131 . 4109	.5182	. 7543 . 7595	.1423	.3290	. 4758	. 5222	47
14	. 5913	4087	.5171	7646	.1409	,3297	4797	5203	46
15	.65934	.34065	1.5166	87698	1.1403	1.3301	.24816	.75184	45
16	. 5956	. 4043	.5161	. 7749	.1396	.3304	. 4835	. 5165	44
17	. 5978	. 4022	.5156	. 7801	.1389	.3307	. 4854	. 5146	43
18 19	. 6000	. 4000	.5151	. 7852	.1383	.3311	. 4873	. 5126	42
19 20	.6022 .66044	. 3978 .33956	.5146 1.5141	. 7904 .87955	.1376 1.1369	.3314 1.3318	. 4893	. 5107	41 40
20	. 6066	. 3934	.5136	. 8007	.1363	.3321	. 4931	5069	39
21 22 23 24	. 6087	3912	.5131	8058	.1356	.3324	4950	. 5049	38
23	. 6109	. 3892	.5126	. 8110	.1349	.3328	. 4970	. 5030	37
24	. 6131	. 3869	.5121	. 8162	.1343	.3331	. 4989	. 5011	36
25	.66153	.33847	1.5116	.88213	1.1336	1.3335	.25008	.74992	35
26 27	. 6175	. 3825 . 3803	.5111	. 8265 . 8317	.1329 .1323	.3338	. 5027	. 4973	34
27 99	.6197 .6218	. 3803 . 3781	.5106	. 8369	.1325	.3345	. 5047	4933	32
29	6240	3760	.5096	. 8421	.1309	.3348	. 5085	4915	31
28 29 30	.66262	33738	1.5092	.88172	1.1303	1.3352	.25104	.74895	30
31	. 6284	. 3716	.5087	. 8524	.1296	.3355	. 5124	. 4876	29 28 27 26 25 24 23 22 21
32	. 6305	. 3694	.5082	. 8576	.1290	.3359	. 5143	. 4857	28
33	. 6327 . 6349	. 3673	.5077	. 8628	.1283 .1276	.3362	. 5162	. 4838 . 4818	21
34 35	.66371	. 3651 .33629	.5072 1.5067	. 8680	1.1270	.3366 1.3369	. 5181 .25201	74799	25
36	. 6393	. 3607	.5062	. 8784	.1263	.3372	. 5220	4780	24
37	. 6414	. 3586	.5057	. 8836	.1257 .1250	.3376	5239	4760	23
38	. 6436	. 3564	.5052	. 8888	.1250	.3379	. 5259	. 4741	22
39	. 6458	. 3542	.5047	. 8940	.1243	.3383	. 5278	. 4722	21
40	.66479	.33520	1.5042	.88992	1.1237 .1230	1.3386 .3390	.25297	.74702	20 19
41 42	. 6523	. 3499	.5032	9097	.1230	.3393	, 5336	. 4664	18
43	. 6545	3455	.5027	9149	.1217	3397	5355	4644	17
44	. 6566	. 3433	.5022	. 9201	.1211	.3400	. 5375	. 4625	16
45	.66588	.33412	1.5018	.89253	1.1204	1.3404	.25394	.74606	15
46	. 6610	. 3390	.5013	. 9306	.1197	.3407	. 5414	. 4586	14
47	. 6631	. 3368	.5008	. 9358	.1191	.3411	. 5433	. 4567	13 12
48 49	. 6653 . 6675	. 3347 . 3325	.5003	9410	.1184 .1178	.3414 .3418	5452 5472	. 4548 . 4528	11
50	.66697	.33303	1.4993	.89515	1.1171	1.3421	.25491	.74509	10
51	. 6718	. 3282	.4988	. 9567	.1165	.3425	. 5510	. 4489	
52	. 6740	. 3260	.4983	. 9620	.1158	.3428	. 5530	. 4470	8
53	6762	. 3238	.4979	. 9672	.1152	.3432	. 5549	. 4450	17
54	. 6783	. 3217	.4974	. 9725	.1145	.3435	. 5569	. 4431	9 8 7 6 5 4
- 00 56	.66805 .6826	.33195 .3173	1.4969 .4964	.89777 .9830	1.1139	1.3439 .3442	.25588	.74412	10
55 56 57	. 6848	. 3152	.4959	. 9882	.1132	.3442	. 5627	4392	3
58	. 6870	. 3130	.4954	, 9935	.1119	.3449	5647	4353	32
59	· 6891	. 3108	.4949	. 9988	.1113	.3453	. 5666	. 4334	1
60	. 6913	. 3087	.4945	.90040	.1106	.3456	. 5685	. 4314	0
M.	Cosine.	Vrs. sin.	Secant,	Cotang.	Tang.	Cosec'nt	Vrs. cos	Sine.	M.
	0					1.0000 10			100

364

42°

Natural Trigonometrical Functions.

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	44		114	turar ri	igonom	cuitari	MACTIO			
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	M.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	<u>M.</u>
$ \begin{array}{ccccccccccccccccccccccccccccccccccc$	0	.66913	.33087	1.4945	.90040	1.1106	1.3456	.25685		60
	1			.4940	. 0093	.1100	.3460		. 4295	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2									
	3				. 0198	.1086	.3467	. 5744		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4				. 0251	.1080			. 4236	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	5									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	6									
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $										
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$.1034				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$						1028				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										47
								. 5959		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$.25978		45
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$. 7258		.4868		.1003		. 5998	. 4002	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	17	. 7280	. 2720	.4863	. 0940					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.73924	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	21			.4844						
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	22									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	23		. 2591							
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	24									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	20									34
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	20									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	28									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	29									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.32441						73728	30
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$. 2419			.0907	.3567	. 6292	. 3708	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$\begin{array}{cccccccccccccccccccccccccccccccccccc$. 7623	. 2377				.3574			27
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.0888				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			• 2312							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$. 2291		. 2008					20
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										21
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			32227						73531	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	44		. 2141	,4736			.3614	. 6548	. 3452	16
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$. 2098		. 2493		.3622			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$										
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		0.200					.3040			8
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	52	0.051								1 %
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										6
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	55				92980				73234	5
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										4
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$										2
60 . 8200 . 1800 .4663 . 3251 .0724 .3673 . 6865 . 3135 0						.0730				1
M. Cosine. Vrs. sin. Secant. Cotang. Tang. Cosee 'nt Vrs. cos. Sine. M.	60		. 1800	.4663	. 3251	.0724	.3673	. 6865	. 3135	0
m, cosine, vis. sin, becant. cotang. Tang. cosec nt vis. cos. Sine. M.	7.1	Covine	Vra eir	Secont	Cotone	Tang	(losesiet	Vrs no-	Sine	M
	<u>M.</u>	Cosme.	v rs. s. n.	Becant.	cotang.	Tang.	JOOBCC IL	1 TB. COB.	oine.	101.

Table 3.

43°

Natural Trigonometrical Functions.

43°		Na	tural Tr	igonom	etrical	if Functions. 13		30°	
M.	Sine.	Vrs. cos.	Cosec 'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.68200	.31800	1.4663	.93251	1.0724	1.3673	.26865	.73135	60
1	8221	. 1779	.4658	3306	.0717	.3677	. 6884	. 3115	59
2	. 8242	. 1758	.4654	. 3360	.0711	.3681	. 6904	. 3096	58
3	. 8264	. 1736	.4649	. 3415	.0705	.3684	. 6924	. 3076	57
3 4 5	. 8285	. 1715	.4644	. 3469	.0699	.3688	. 6944	. 3056 .73036	56 55
D e	.68306 . 8327	.31694 . 1673	1.4640 .4635	.93524 .3578	1.0692 .0686	1.3692 .3695	.26964	. 3016	54
67	8349	1651	.4631	3633	.0680	.3699	. 7004	2996	53
8	8370	1630	.4626	3687	.0674	3703	7023	2976	52
8 9	8391	. 1609	.4622	. 3742	.0667	.3707	. 7043	. 2956	51
10	.68412	.31588	1.4617	.93797	1.0661	1.3710	.27063	.72937	50
11	. 8433	. 1566	.4613	. 3851	.0655	.3714	. 7083	. 2917	49
12	. 8455	. 1545	.4608	. 3906 . 3961	.0649	.3718	. 7103 . 7123	2897 2877	48
$13 \\ 14$. 8476 . 8497	. 1524 . 1503	.4604	. 4016	.0643 .0636	.3725	. 7123	2857	46
15	.68518	.31482	1,4595	94071	1.0630	1.3729	.27163	72837	45
16	. 8539	1460	4590	4125	.0624	.3733	. 7183	. 2817	44
17	8561	. 1439	.4586	. 4180	.0618	.3737	. 7203	. 2797	43
18	. 8582	. 1418	.4581	. 4235	.0612	.3740	. 7223	. 2777	42
19	. 8603	. 1397	.4577	. 4290	.0605	.3744	. 7243	. 2757	41
20	.68624	.31376	1.4572	.94345 .4400	1.0599	1.3748	.27263 .7283	.72737 . 2717	40 39
21 22	. 8645 . 8666	. 1355 . 1333	.4568 .4563	4400	.0595	.3752 .3756	. 7302	2697	38
23	. 8688	13312	.4559	4510	.0581	.3759	7322	2677	37
24	. 8709	1291	.4554	4565	.0575	3763	7342	2657	36
25	.68730	.31270	1.4550	.94620	1.0568	1.3767	.27362	72637	35
26	. 8751	. 1249	.4545	. 4675	.0562	.3771	. 7382	. 2617	34
27 28 29	. 8772	 1228 	.4541	. 4731	.0556	.3774	. 7402	. 2597	33
28	. 8793	. 1207	.4536	. 4786	.0550	.3778	. 7422	2577	32 31
29 80	. 8814	. 1186	.4532 1.4527	. 4841 .94896	.0544 1.0538	1,3782 1,3786	. 7442	72537	30
$\frac{50}{31}$.68835 .8856	.31164 . 1143	4523	. 4952	.0532	.3790	7482	2517	29
32	8878	11122	4518	5007	.0525	.3794	7503	2497	28
33	. 8899	1101	.4514	5062	.0519	.3797	. 7523	. 2477	27
34	. 8920	. 1080	.4510	. 5118	.0513	.3801	. 7543	. 2457	26
35	.68941	.31059	1,4505	.95173	1.0507	1.3805	.27563	.72437	25 24
36	. 8962	. 1038	.4501	. 5229 . 5284	.0501	.3809	. 7583	. 2417 . 2397	24 23
$\frac{37}{38}$	8983	. 1017	.4496	. 5340	.0493	.3816	7623	2377	22
39	9004	. 0975	.4487	. 5395	.0483	3820	7043	2357	$\tilde{21}$
40	.69046	.30954	1,4483	.95451	1.0476	1.3824	.27663	.72337	20
Ĩ	9067	. 0933	.4479	. 5506	.0470	.3828	. 7683	. 2317	19
42	. 9088	. 0912	.4474	. 5562	.0464	.3832	. 7703	. 2297	18
43	. 9109	. 0891	.4470	. 5618	.0458	.3836	. 7723	. 2277	17 16
44	. 9130	. 0870	.4465 1.4461	. 5673	.0452 1.0446	.3839 1.3843	. 7743 .	.72236	15
45 46	69151 9172	. 0828	.4457	. 5785	.0440	.3847	. 7784	2216	14
47	9193	. 0807	4452	. 5841	.0434	.3851	7804	. 2196	13
48	. 9214	. 0786	.4448	. 5896	.0428	.3855	. 7824	. 2176	12
49	9235	. 0765	.4443	. 5952	.0422	.3859	. 7844	. 2156	11
50	.69256	.30744	1.4439	.96008	1.0416	1.3863	.27864	.72136	10
51	. 9277	. 0728	.4435	. 6064	.0410	.3867 .3870	. 7884	. 2115 . 2095	9
52	. 9298 . 9319	. 0702	.4426	. 6176	.0397	.3874	7925	2035	87
53 54	. 9340	. 0660	.4422	6232	.0391	.3878	7045	2055	
55	.69361	.30639	1.4417	.96288	1.0385	1.3882	27965	.72035	65
56	. 9382	. 0618	.4413	. 6344	,0379	.3886	. 7985	. 2015	4
57	. 9403	. 0597	.4408	. 6400	.0373	.3890	. 8005	. 1994	3
58	. 9424	. 0576	.4404	. 6456	.0367	.3894	. 8026	. 1974	321
59	. 9445	. 0555	.4400	. 6513	.0361	.3898	. 8046	. 1954 . 1934	
60	. 9466	. 0534	.4395	. 6569	.0355	.3902			
<u>M.</u>	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

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Natural Trigonometrical Functions.

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44	,	Na	itural T	rigonom	etrical	Function	ns.	1	350
M.	Sine.	Vrs. cos.	Cosec'nt	Tang.	Cotang.	Secant.	Vrs. sin.	Cosine.	M.
0	.69466	.30534	1.4395	.96569	1.0355	1.3902	.28066	.71934	60
1	. 9487	. 0513	.4391	. 6625	.0349	.3905	. 8086	. 1914	59
2	. 9508	. 0492	.4387	. 6681	.0343	.3909	. 8106	. 1893	58
3	 9528 	. 0471	.4382	. 6738	.0337	.3913	. 8127	. 1873	57
4	. 9549	. 0450	.4378	. 6794	.0331	.3917	. 8147	. 1853	56
2	.69570 . 9591	.30430	1.4374 .4370	.96850 .6907	1.0325 .0319	1.3921 .3925	.28167	.71833 . 1813	55
- 2	. 9612	. 0388	.4365	6963	.0313	.3929	. 8208	. 1792	53
3456789	9633	. 0367	.4361	. 7020	.0307	.3933	8228	. 1772	52
ğ	9654	. 0346	.4357	. 7076	.0301	.3937	. 8248	. 1752	51
10	.69675	.30325	1.4352	.97133	1.0295	1.3941	.28268	.71732	50
11	9696	. 0304	.4348	. 7189	.0289	.3945	. 8289	. 1711	49
12	. 9716	. 0283	.4344	. 7246 . 7302	.0283	.3949	. 8309	1691	48
$\frac{13}{14}$	9737 9758	.0263 .0242	.4339	. 7359	.0277 .0271	.3953 .3957	8329 8349	.1671 .1650	47
15	.69779	.30221	1.4331	.97416	1.0265	1.3960	28370	.71630	45
16	. 9800	. 0200	.4327	. 7472	.0259	.3964	. 8390	. 1610	14
17	. 9821	. 0179	.4322	, 7529	.0253	.3968	. 8410	. 1589	43
18	. 9841	. 0158	.4318	. 7586	.0247	.3972	. 8431	. 1569	42
19	. 9862	. 0138	.4314	. 7643	.0241	.3976	. 8451	. 1549	41
20	.69883	.30117	1.4310	.97699	1.0235 .0229	1.3980	.28471	.71529	40
$\frac{21}{22}$. 9904 . 9925	. 0096	.4305 .4301	. 7756 . 7813	.0229	.3984	.8492 .8512	. 1508 . 1488	3 9 38
$\frac{22}{23}$. 9925	. 0073	.4301	. 7870	.0218	.3992	. 8532	. 1468	37
24	9966	. 0034	4292	. 7927	.0212	.3096	. 8553	. 1447	36
$\frac{24}{25}$.69987	.30013	1.4288	.97984	1.0206	1.4000	.28573	.71427	35
26 i	.70008	.29992	.4284	. 8041	.0200	.4004	. 8593	. 1406	34
27	. 0029	. 9971	.4280	. 8098	.0194	.4008	. 8614	. 1386	33
$\frac{28}{29}$. 0049	. 9950	.4276 .4271	. 8155	.0188	.4012	. 8634	. 1366	32
$\frac{29}{30}$.0070 .70091	. 9930 .29909	4271 1.4267	. 8212 .98270	$.0182 \\ 1.0176$.4016 1.4020	. 8654	. 1345 .71325	31 30
31	. 0112	. 9888	4263	. 8327	.0170	.4024	. 8695	. 1305	29
32	. 0132	9867	4259	8384	.0164	.4028	. 8716	. 1284	28
33	. 0153	9847	.4254	. 8441	.0158	.4032	8736	1264	27
34	. 0174	. 9826	.4250	. 8499	.0152	.4036	, 8756	. 1243	26
35	.70194	.29805	1.4246	.98556	1.0146	1.4040	.28777	.71223	25
36	. 0215	. 9785	.4242	. 8613	.0141	.4044	. 8797	· 1203	24
37 38	. 0236 . 0257	. 9764 . 9743	.4238	. 8671 . 8728	.0135 .0129	.4048 .4052	. 8818 . 8838	.1182 .1162	23 22
39	. 0277	9722	.4229	. 8786	.0123	.4056	. 8859	. 1141	21
40	70298	.29702	1,4225	.98843	1.0117	1.4060	.28879	.71121	20
41	. 0319	. 9681	.4221	. 8901	.0111	.4065	. 8899	. 1100	19
42	. 0339	. 9660	.4217	. 8958	.0105	.4069	. 8920	. 1080	18
43	. 0360	. 9640	.4212	. 9016	.0099	.4073	. 8940	. 1059	17
44 45	.0381 .70401	. 9619 .29598	.4208 1.4204	. 9073 .99131	.0093 1.0088	.4077 1.4081	.8961 .28981	. 1039 .71018	16 15
40	. 0422	. 9578	.4200	. 9189	.0082	.4085	9002	. 0998	14
47	. 0443	. 9557	.4196	. 9246	.0076	.4089	9022	. 0977	13
48	0463	. 9536	.4192	. 9304	.0070	,4093	9043	. 0957	12
49	. 0484	. 9516	.4188	. 9362	.0064	.4097	, 9063	. 0936	11
50	.70505	.29495	1.4183	.99420	1.0058	1.4101	.29084	.70916	10
51	. 0525	. 9475	.4179	. 9478	.0052	.4105	. 9104	. 0895	9
$\frac{52}{53}$. 0546 . 0566	. 9454 . 9433	.4175 .4171	. 9536 . 9593	.0047 .0041	.4109 .4113	. 9125 . 9145	. 0875 . 0854	8 7
54	. 0587	. 9413	.4167	. 9651	.0035	.4113	. 9145	. 0834	6
55	70608	.29392	1.4163	.99709	1.0029	1.4122	.29186	.70813	5
56	. 0628	. 9372	.4159	. 9767	.0023	.4126	. 9207	. 0793	4
57	. 0649	. 9351	.4154	. 9826	.0017	.4130	. 9228	. 0772	32
58	. 0669	. 9330	.4150	. 9884	.0012	.4134	. 9248	. 0752	2
59 60	.0690 .0711	. 9310 . 9289	.4146 .4142	. 9942 1.0000	.0006	.4138	. 9269	. 0731	1
						.4142	. 9289	. 0711	0
M .	Cosine.	Vrs. sin.	Secant.	Cotang.	Tang.	Cosec'nt	Vrs. cos.	Sine.	M.

	AND CI	RCULAR A	AREAS OF	INUS. FRO	M I TO 52	0
No.	Square	Cube	Sq. Root	Cube Root	Cir	CLE
10.	Square	Cube	Sq. Kool	Cube Root	Circum.	Area
Ι	I	I	1.0000	1.0000	3.142	0.7854
2	4	8	1.4142	1.2599	ŏ.283	3.1416
3	9	27	1.7321	I.4422	9.425	7.0686
4	16	64	2.0000	1.5874	12.566	12.5664
5	25	125	2.2361	1.7100	15.708	19.6350
	(0.0	
6	36	216	2.4495	1.8171	18.850	28.2743
7 8	49	343	2.6458	1.9129	21.991	38.4845
	64	512	2.8284	2.0000	25.133	50.2655
9	81	729	3.0000	2.0801	28.274	63.6173
10	100	1000	3.1623	2.1544	31.416	78.5398
11	121	1331	3.3166	2.2240	34.558	95.033
11	144	1728	3.4641	2.2894	37.699	113.097
	169	2197	3.6056	2.3513	40.841	132.732
13	109		3.7417	2.4101	43.982	153.938
14		2744	3.8730	2.4662	43.902	176.715
15	225	3375	3.0730	2.4002	4/.124	1/0./15
16	256	4096	4.0000	2.5198	50.265	201.062
17	289	4913	4.1231	2.5713	53.407	226.980
18	324	5832	4.2426	2.6207	56.549	254.469
19	361	6859	4.3589	2.6684	59.690	283.529
20	400	8000	4.4721	2.7144	62.832	314.159
					<i>.</i>	
21	441	9261	4.5826	2.7589	65.973	346.361
22	484	10648	4.6904	2.8020	69.115	380.133
23	529	12167	4.7958	2.8439	72.257	415.476
24	576	13824	4.8990	2.8845	75.398	452.389
25	625	15625	5.0000	2.9240	78.540	490.874
26	676	17576	5.0990	2.9625	81.681	530.929
27	729	19683	5.1962	3.0000	84.823	572.555
28	784	21952	5.2915	3.0366	87.965	615.752
	841	24389	5.3852	3.0723	91.106	660.520
2 9	900	24309	5.4772	3.1072	94.248	706.858
30	900	2,000		3.10/2	94-240	1,00,00,0
31	961	29791	5.5678	3.1414	90.389	754.768
32	1024	32768	5.6569	3.1748	100.531	804.248
33	1089	35937	5.7446	3.2075	103.673	855.299
34	1156	39304	5.8310	3.2396	106.814	907.920
35	1225	42875	5.9161	3.2711	109.956	962.113
		1				00
36	1296	46656	6.0000	3.3019	113.097	1017.88
37	1369	50653	6.0828	3.3322	116.239	1075.21
38	I444	54872	6.1644	3.3620	119.381	1134.11
39	1521	59319	6.2450	3.3912	122.522	1194.59
40	1600	64000	6.3246	3.4200	125.660	1256.64
	۱ <u>ـــــ</u>	l		<u> </u>		<u> </u>

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM ¹ TO 520

SQUARES, CUBES, SQU.	are Roots, Cube	ROOTS, CIR	CUMFERENCES
AND CIRCULA	AR AREAS OF NOS	. FROM I TO	520
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AND CIRCULAR AREAS OF NOS. FROM 1 10 520							
No.	Square	Cube	Sq. Root	Cube Root	CIR		
					Circum.	Area	
		60	6				
41	1681	68921	6.4031	3.4482	128.81	1320.25	
42	1764	74088	6.4807	3.4760	131.95	1 385.44	
43	1849	795 <u>0</u> 7	6.5574	3.5034	135.09	1452.20	
44	1936	85184	6.6332	3.5303	138.23	1520.53	
45	2025	91125	6.7082	3.5569	141.37	1590.43	
46	2116	97336	6.7823	3.5830	144.51	1661.90	
47	2200	103823	6.8557	3.6088	147.65	1734.94	
48	2304	110592	6.9282	3.6342	150.80	1809.56	
49	2401	117649	7.0000	3.6593	153.94	1885.74	
50	2500	125000	7.0711	3.6840	157.08	1963.50	
30	2300	12,000	7.0711	ļ ° .	197.00		
51	2601	132651	7. 1414	3.7084	160.22	2042.82	
52	2704	140608	7.2111	3.7325	163.36	2123.72	
53	2809	148877	7.2801	3.7563	166.50	2206.18	
54	2916	157464	7.3485	3.7798	169.65	2290.22	
55	3025	166375	7.4162	3.8030	172.79	2375.83	
56	3136	175616	7.4833	3.8259	175.93	2463.01	
57	3249	185193	7.5498	3.8485	179.07	2551.76	
58	3364	195112	7.6158	3.8700	182.21	2642.08	
59	3481	205379	7.6811	3.8930	185.35	2733.97	
60	3600	216000	7.7460	3.9149	188.50	2827.43	
	3000				100.90	2027.43	
61	3721	226981	7.8102	3.9365	191.64	2922.47	
62	3844	238328	7.8740	3.9579	194.78	3019.07	
63	3969	250047	7.9373	3.9791	197.92	3117.25	
64	4096	262144	8.0000	4.0000	201.06	3216.99	
65	4225	274625	8.0623	4.0207	204.20	3318.31	
66	4356	287496	8.1240	4.0412	207.35	3421.19	
67	4489	300763	8.1854	4.0615	207.35	3525.65	
68	4624	314432	8.2462	4.0817	213.63	3631.68	
60	4761	328500	8.3066	4.1016	215.03	3739.28	
70	4000	343000	8.3666	4.1213	210.77	3848.45	
70	4900	343000	0.3000	4.1213	219.91	3040.45	
71	5041	357911	8.4261	4.1408	223.05	3959.19	
72	5184	373248	8.4853	4.1602	226.19	4071.50	
73	5329	389017	8.5440	4.1793	229.34	4185.39	
74	5476	405224	8.6023	4.1983	232.48	4300.84	
75	5625	421875	8.6603	4.2172	235.62	4417.86	
76	1776	438976	8.7178	4 2258	238.76	4526 46	
70	5776			4.2358	230.70	4536.46	
77 78	5929 6084	456533	8.7750 8.8318	4.2543	241.90	4656.63	
		474552	8.8882	4.2727 4.2908	245.04	4778.36	
79 80	6241	493039	1	4.2908		4901.67	
00	6400	512000	8.9443	4.3009	251.33	5026.55	
			· · · · · · · · · · · · · · · · · · ·				

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Table 4.

	ANDC	IRCULAR P	KEAS OF 1	NUS. FRUI		
No.	Square	Cube	Sq. Root	Cube Root	Cir	
	oquare		oq: noor		Circum.	Area
e	6.6.			1		
81	. 6561	531441	9.0000	4.3267	254.47	5153.00
82	6724	551368	9.0554	4.3445	257.61	5281.02
83	6889	571787	9.1104	4.3621	260.75	5410.61
84	•7056	592704	9.1652	4.3795	263.89	5541.77
85	7225	614125	9.2195	4.3968	267.04	5674.50
86	7396	636056	9.2736	4.4140	270.18	5808.80
87	7569	658503	9.3274	4.4310	273.32	5944.68
88	7744	681472	9.3808	4.4480	276.46	6082.12
89	7921	704969	9.4340	4.4647	279.60	6221.14
90	8100	720000	9.4868	4.4814	282.74	6361.73
90	0100	729000	9.4000	4.4014	202.74	0301.73
91	8281	753571	9.5394	4.4979	285.88	6503.88
92	8464	778688	9.5917	4.5144	289.03	6647.61
93	8649	804357	9.6437	4.5307	292.17	6792.91
94	8836	830584	9.6954	4.5468	295.31	6939.78
95	9025	857375	9.7468	4.5629	298.45	7088.22
96	9216	884736	9.7980	4.5789	301.59	7238.23
90 97		912673	9.8489	4.5947	304.73	7389.81
97 98	9409	912073	9.8995	4.6104	307.88	7542.96
-	9801			4.6261	311.02	7697.69
99		970299	9.9499	4.6416	314.16	7853.98
100	10000	1000000	10.0000	4.0410	314.10	7353.98
101	10201	1030301	10.0499	4.6570	317.30	8011.85
102	10404	1061208	10.0005	4.6723	320.44	8171.28
103	10609	1002727	10.1489	4.6875	323.58	8332.29
104	10816	1124864	10.1980	4.7027	326.73	8494.87
105	11025	1157625	10.2470	4.7177	329.87	8659.01
106	11236	1101016	10.2956	4.7326	333.01	8824.73
100	11230	1225043	10.2950	4.7320	336.15	8992.02
107	11664	1259712	10.3923	4.7622	339.29	9160.88
	11881		10.3923	4.7769	342.43	9331.32
109 110	12100	1295029 1331000	10.4403	4.7914	342.43	9503.32
110	12100	1331000	10.4001	4.7914	343.30	9503.32
111	12321	1367631	10.5357	4.8059	348.72	9676.89
112	12544	1404928	10.5830	4.8203	351.86	9852.03
113	12769	1442897	10.6301	4.8346	355.00	10028.7
τ14	12996	1481544	10.6771	4.8488	358.14	10207.0
115	13225	1520875	10.7238	4.8629	361.28	10386.9
116	13456	1560896	10.7703	4.8770	364.42	10568.3
117	13689	1601613	10.8167	4.8910	367.57	10751.3
117		1643032	10.8628	4.9049	370.71	10935.9
	13924		10.0020	4.9187	373.85	11122.0
119	14161	1685159				11309.7
120	14400	1728000	10.9545	4.9324	376.99	11309.7

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

	AND (CIRCULAR A	REAS OF	NOS. FROM	M I TO 52	0
27				las n.	Cir	CLE
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
121	14641	1771561	11.0000	4.9461	380.13	11499.0
122	14884	1815848	11.0454	4.9597	383.27	11689.9
123	15129	1860867	11.0905	4.9732	386.42	11882.3
124	15376	1906624	11.1355	4.9866	389.56	12076.3
125	15625	1953125	11.1803	5.0000	392.70	12271.8
. 5		00000		5	• •	
126	15876	2000376	11.2250	5.0133	395.84	12469.0
127	16129	2048383	11.2694	5.0265	398.98	12667.7
128	16384	2097152	11.3137	5.0397	402.12	12868.0
129	16641	2146689	11.3578	5.0528	405.27	13069.8
130	16900	2197000	11.4018	5.0658	408.41	13273.2
Ŭ						
131	1716 1	2248091	11:4455	5.0788	411.55	13478.2
132	17424	2299968	11.4891	5.0916	414.69	13684.8
133	17689	2352637	11.5326	5.1045	417.83	13892.9
134	17956	2406104	11.5758	5.1172	420.97	14102.6
135	18225	2460375	11.6190	5.1299	424.12	14313.9
	0 (
136	18496	2515456	11.6619	5.1426	427.26	14526.7
137	18769	2571353	11.7047	5.1551	430.40	14741.1
138	19044	2628072	11.7473	5.1676	433.54	14957.1
139	19321	2685619	11.7898	5.1801	436.68	15174.7
140	19600	2744000	11.8322	5.1925	439.82	15393.8
141	19881	2803221	11.8743	5.2048	442.96	15614.5
141	20164	2863288	11.9164	5.2171	442.90	15836.8
142	20104	2003200	11.9583			16060.6
143	20449 20736	2985984	12.0000	5.2293	449.25	16286.0
		3048625		5.2415	452.39	
145	21025	3040025	12.0416	5.2536	455.53	16513.0
146	21316	3112136	12.0830	5.2656	458.67	16741.5
147	21609	3176523	12.1244	5.2776	461.81	16971.7
148	21904	3241792	12.1655	5.2896	464.96	17203.4
149	22201	3307949	12.2066	5.3015	468.10	17436.6
150	22500	3375000	12.2474	5.3133	471.24	17671.5
- 5 -		5575		5.5-55	4/1124	-1012.3
151	22801	3442951	12.2882	5.3251	474.38	17907.9
152	23104	3511808	12.3288	5.3368	477.52	18145.8
153	23409	3581577	12.3693	5.3485	480.66	18385.4
154	23716	3652264	12.4097	5.3601	483.81	18626.5
155	24025	3723875	12.4499	5.3717	486.95	18869.2
			,/			
156	24336	3796416	12.4900	5.3832	490.09	19113.4
157	24649	3869893	12.5300	5.3947	493.23	19359.3
158	24964	3944312	12.5698	5.4061	496.37	19606.7
159	25281	4019679	12.6095	5.4175	499.51	19855.7
160	25600	4096000	12.6491	5.4288	502.65	20106.2
		l		1		

Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520

Table 4.

		IRCULAR A	indiano or	INUS. FROM		
No.	Square	Cube	Sq. Root	Cube Root		CLE
140.	oquare	Cube		Cube Root	Circum.	Area
		_			-	
161	25921	4173281	12.6886	5.4401	505.80	20358.3
162	26244	4251528	12.7279	5.4514	508.94	20612.0
163	26569	4330747	12.7671	5.4626	512.08	20867.2
164	26896	4410944	12.8062	5.4737	515.22	21124.1
165	27225		12.8452	5.4848	518.36	21382.5
105	27225	4492125	12.0452	3.4040	510.30	21302.5
166	27556	4574296	12.8841	5.4959	521.50	21642.4
167	27889	4657463	12.0228	5.5069	524.65	21904.0
168	23224	4741632	12.9615	5.5178	527.79	22167.1
		4826800				
169	28561		13.0000	5.5288	530.93	22431.8
170	28900	4913000	13.0384	5.5397	534.07	22698.0
T /2 T	00047	5000211	13.0767	5.5505	537.21	22965.8
171	29241					
172	29584	5088448	13.1149	5.5613	540.35	23235.2
173	29929	5177717	13.1529	5.5721	543.50	23506.2
174	30276	5268024	13.1909	5.5828	546.64	23778.7
175	30625	5359375	13.2288	5.5934	549.78	24052.8
						0
176	30976	5451776	13.2665	5.6041	552.92	24328.5
177	31329	5545233	13.3041	5.6147	556.06	24605.7
178	31684	5639752	13.3417	5.6252	559.20	24884.6
179	32041	5735339	13.3791	5.6357	562.35	25164.9
180	32400	5832000	13.4164	5.6462	565.49	25446.9
	-					
181	32761	5929741	13.4530	5.6567	568.63	25730.4
182	33124	6028568	13.4907	5.6671	571.77	26015.5
183	33489	6128487	13.5277	5.6774	574.91	26302.2
184	33856	6229504	13.5647	5.6877	578.05	26590.4
185	34225	6331625	13.6015	5.6980	581.19	26880.3
-	545	-333				5
186	34596	6434856	13.6382	5.7083	584.34	27171.6
187	34969	6539203	13.6748	5.7185	587.48	27464.6
188	35344	6644672	13.7113	5.7287	500.62	27759.1
189	35721	6751269	13.7477	5.7388	593.76	28055.2
		6850000	15.7840	5.7489	596.90	28352.9
190	36100	0059000	1 3.7040	3.1409	390.90	
101	36481	6967871	13.8203	5.7590	600.04	28652.1
191	36864	7077888	13.8564	5.7690	603.19	28952.9
			13.8024	5.7790	606.33	20932.9
193	37249	7189057	13.0924		600.33	
194	37636	7301384	13.9284	5.7890		29559.2
195	38025	7414875	13.9642	5.7989	612.61	29864.8
196	38416	7529536	14.0000	5.8088	615.75	30171.9
				5.8186	618.89	30171.9
197	38809	7645373	14.0357	5.0100		
198	39204	7762392	14.0712	5.8285	622.04	30790.7
199	39601	7880599	14.1067	5.8383	625.18	31102.6
200	40000	8000000	14.1421	5.8480	628.32	31415.9
	l			1		

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

	AND C	IRCULAR F	REAS OF .	NUS. FROM	<u>4 1 10 52</u>	
-	-				CIR	CLE
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Атеа
						~
201	40401	8120601	14.1774	5.8578	631.46	31730.9
		8242408		5.8675	634.60	32047.4
202	40804		14.2127		637.74	32365.5
203	41209	8365427	14.2478	5.8771		32685.1
204	41616	8489664	14.2829	5.8868	640.89	
205	42025	8615125	14.3178	5.8964	644.03	33006.4
206	42436	8741816	14.3527	5.9059	647.17	33329.2
207	42849	8869743	14.3875	5.9155	650.31	33653.5
208	43264	8998912	14.4222	5.9250	653.45	33979.5
	43681	0120320	14.4568	5.9345	656.59	34307.0
209					659.73	34636.1
210	44100	9261000	14.4914	5.9439	039.73	34030.1
211	44521	9393931	14.5258	5-9533	662.88	34966.7
212	44944	0528128	14.5602	5.9627	666.02	35298.9
213	45369	9663597	14-5945	5.9721	669.1 6	35632.7
214	45796	9800344	14.6287	5.9814	672.30	35968.1
215	46225	9938375	14.6629	5.9907	675.44	36305.0
5	j					
216	46656	10077696	14.6969	6,0000	678.58	36643.5
217	47089	10218313	14.7309	6.0092	681.73	36983.6
218	47524	10360232	14.7648	6.0185	684.87	37325.3
219	47961	10503459	14.7986	6.0277	688.01	37668.5
220	48400	10648000	14.8324	6.0368	691.15	38013.3
	.00		066-	6	604.00	a8ara 6
22I	48841	10793861	14.8661	6.0459	694.29	38359.6
222	49284	10941048	14.8997	6.0550	697.43	38707.6
223	49729	11089567	14.9332	6.0641	700.58	39057.1
224	50176	11239424	14.9666	6.0732	703.72	39408.1
225	50625	11390625	15.0000	6.0822	706.86	39760.8
226	51076	11543176	15.0333	6.0912	710.00	40115.0
227	51529	11697083	15.0665	6.1002	713.14	40470.8
228	51984	11852352	15.0997	6.1091	716.28	40828.1
229	52441	12008989	15.1327	6.1180	719.42	41187.1
230	52900	12167000	15.1658	6.1260	722.57	41547.6
230	• •	1210/000	*3.1030		122.21	4-34/10
231	53361	12326391	15.1987	6.1358	725.71	41909.6
232	53824	12487168	15.2315	6.1446	728.85	42273.3
233	54289	12649337	15.2643	6.1534	731.99	42638.5
234	54756	12812904	15.2971	6.1622	735-13	43005.3
235	55225	12977875	15.3297	6.1710	738.27	43373.6
					151	
236	55696	13144256	15.3623	6.1797	741.42	43743.5
237	56169	13312053	15.3948	6.1885	744.56	44115.0
238	56644	13481272	15.4272	6.1972	747. <u>7</u> 0	44488.1
239	57121	13651919	15.4596	6.2058	750.84	44862.7
240	57600	13824000	15.4919	6.2145	753.98	45238.9
				1		1

Table 4. SQUARES, CUBES AND ROOTS.

Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520

					CIR	CLE
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
				(
241	58081	13997521	15.5242	6.2231	757.12	45616.7
242	58564	14172488	15.5563	6.2317	760.27	45996.1
243	59049	14348907	15.5885	6.2403	763.41	46377.0
244	59536	14526784	15.6205	6.2488	766.55	46759.5
245	60025	14706125	15.6525	6.2573	769.69	47143-5
246	60516	14886936	15.6844	6.2658	772.83	47529.2
247	61009	15069223	15.7162	6.2743	775.97	47916.4
248	61504	15252992	15.7480	6.2828	779.12	48305.1
		13232992		6.2012	782.26	48695.5
249	62001	15438249	15.7797			49087.4
250	62500	15625000	15,8114	6.2996	785.40	49087.4
251	63001	15813251	15.8430	6.3080	788.54	49480.9
252	63504	16003008	15.8745	6.3164	791.68	49875.9
253	64009	16194277	15.9060	6.3247	794.82	50272.6
254	64516	16387064	15.9374	6.3330	797.96	50670.7
255	65025	16581375	15.9687	6.3413	801.11	51070.5
256	65536	16777216	16.0000	6.3496	804.25	51471.9
257	66049	16974593	16.0312	6.3579	807.39	51874.8
258	66564	17173512	16.0624	6.3661	810.53	52279.2
				6.3743	813.67	52685.3
259	67081	17373979	16.0935		816.81	53092.9
260	67600	17576000	16.1245	6.3825	010.01	
261	68121	17779581	16.1555	6.3907	819.96	53502.1
262	68644	17984728	16.1864	6.3988	823.10	53912.9
263	60160	18101447	16.2173	6.4070	826.24	54325.2
264	69696	18399744	16.2481	6.4151	829.38	54739.1
265	70225	18609625	16.2788	6.4232	832.52	55154.6
Ť.			-6 0007	6 1010	835.66	55571.6
266	70756	18821096	16.3095	6.4312	838.81	55990.3
267	71289	19034163	16.3401	6.4393	841.05	56410.4
268	71824	19248832	16.3707	6.4473	841.95	56832.2
269	72361	19465109	16.4012	6.4553	845.09	
270	72900	19683000	16.4317	6.4633	848.23	57255.5
271	73441	19902511	16.4621	6.4713	851.37	57680.4
272	73984	20123648	16.4924	6.4792	854.51	58106.9
273	74529	20346417	16.5227	6.4872	857.66	58534.9
274	75076	20570824	16.5529	6.4951	860.80	58964.6
275	75625	20796875	16.5831	6.5030	863.94	59395.7
276	76176	21024576	16.6132	6.5108	867.08	59828.5
277	76729	21253933	16.6433	6.5187	870.22	60262.8
278	77284	21484952	16.6733	6.5265	873.36	60698.7
-/-		1	1 +6 2022	6.5343	876.50	61136.2
279	77841	21717639	16.7033 16.7332	6.5421	879.65	61575.2

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SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

-		JIRCULAR F	ICEAS OF	100. 1 10		
No.	Square	Cube	Sq. Root	Cube Root		CLE
	bquare				Circum.	Area
281	-8-6-	00799017	-6-6	6	00. 50	600000
	78961	22188041	16.7631	6.5499	882.79	62015.8
282	79524	22425768	16.7929	6.5577	885.93	62458.0
283	80089	22665187	16.8226	6.5654	889.07	62901.8
284	80656	22906304	16.8523	6.5731	892.21	63347.1
285	81225	23149125	16.8819	6.5808	895.35	63794.0
286	81796	23393656	16.9115	6.5885	898.50	64242.4
287	82369	23639903	16.9411	6.5962	901.64	64692.5
288	82944	23887872	16.9706	6.6039	904.78	65144.1
289	83521	24137569	17.0000	6.6115	907.92	65597.2
290	84100	24380000	17.0204	6.6191	011.06	66052.0
	84681			-	-	
291		24642171	17.0587	6.6267	914.20	66508.3
292	85264	24897088	17.0880	6.6343	917.35	66966.2
293	85849	25153757	17.1172	6.6419	920.49	67425.6
294	86436	25412184	17.1464	6.6494	923.63	67886.7
295	87025	25672375	17.1756	6.6569	926.77	68349.3
296	87616	25934336	17.2047	6.6644	929.91	68813.5
297	88209	26198073	17.2337	6.6719	933.05	69279.2
298	88804	26463592	17.2627	6.6794	936.19	69746.5
299	89401	26730800	17.2016	6.6860	939.34	70215.4
300	90000	27000000	17.3205	6.6943	942.48	70685.8
301	90601	27270001	17.3494	6.7018	945.62	
302	91204	27543608	17.3781	6.7092	945.02 948.76	71157.9
303	91809	27818127	17.4069			71631.5
	92416	28094464		6.7166	951.90	72106.6
304			17.4356	6.7240	955.04	72583.4
305	93025	28372625	17.4642	6.7313	958.19	73061.7
306	93636	28652616	17.4929	6.7387	961.33	73541.5
307	94249	28934443	17.5214	6.7460	964.47	74023.0
308	94864	29218112	17.5499	6.7533	967.61	74506.0
309	95481	29503629	17.5784	6.7606	970.75	74990.6
310	96100	29791000	17.6068	6.7679	973.89	75476.8
311	96721	30080231	17.6352	6.7752	977.04	75964.5
312	97344	30371328	17.6635	6.7824	980.18	75904.5
313	97969	30664297	17.6018	6.7897	983.32	
314	98596	30959144	17.7200	6.7969	986.46	76944.7
315	99225	31255875	17.7482	6.8041	900.40	77437.1
			1/0/402	. 1	989 . 60	77931.1
316	99856	31554496	17.7764	6.8113	992.74	78426.7
317	100489	31855013	17.8045	6.8185	995.88	78923.9
318	101124	32157432	17.8326	6.8256	999.03	79422.6
319	101761	32461759	17.8606	6.8328	1002.20	79922.9
320	102400	32768000	17.8885	6.8399	1005.30	80424.8
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Table 4.SQUARES, CUBES AND ROOTS.375

	and C	IRCULAR A	REAS OF	Nos. from	4 I TO 52	0
			0. 0		CIR	CLE
No.	Square	Cube	Sq. Root	Cube Root	Circum.	Area
			-			
321	103041	33076161	17.9165	6.8470	1008.5	80928.2
322	103684	33386248	17.9444	6.8541	ð.1101	81433.2
323	104329	33698267	17.9722	6.8612	1014.7	81939.8
324.	104976	34012224	18.0000	6.8683	1017.9	82448.0
325	105625	34328125	18.0278	6.8753	1021.0	82957.7
	66		- 9	6 00		80,600
326	106276	34645976	18.0555	6.8824	1024.2	83469.0
327	106929	34965783	18.0831	6.8894	1027.3	83981.8
328	107584	35287552	18.1108	6.8964	1030.4	84496.3
329	108241	35611289	18.1384	6.9034	1033.6	85012.3
330	108900	35937000	18.1659	6.9104	1036.7	85529.9
331	109561	36264691	18.1934	6.9174	1039.9	86049.0
332	110224	36594368	18.2200	6.9244	1043.0	86569.7
333	110889	36926037	18.2483	6.9313	1046.2	87092.0
334	111556	37259704	18.2757	6.9382	1049.3	87615.9
335	112225	37595375	18.3030	6.9451	1052.4	88141.3
	-					00000
336	112896	37933056	.18.3303	6.9521	1055.6	88668.3
337	113569	38272753	18.3576	6.9589	1058.7	89196.9
338	114244	38614472	18.3848	6.9658	1061.9	89727.0
339	114921	38958219	18.4120	6.9727	1065.0	90258.7
340	115600	39304000	18.4391	6.9795	1068.1	90792.0
341	116281	39651821	18.4662	6.9864	1071.3	91326.9
342	116964	40001688	18.4932	6.9932	1074.4	91863.3
343	117649	40353607	18.5203	7.0000	1077.6	92401.3
344	118336	40707584	18.5472	7.0068	1080.7	92940.9
345	119025	41063625	18.5742	7.0136	1083.8	93482.0
346	119716	41421736	18.6011	7.0203	1087.0	94024.7
347	120409	41781923	18.6279	7.0271	1090.1	94569.0
348	121104	42144192	18.6548	7.0338	1093.3	95114.9
349	121801	42508549	18.6815	7.0406	1006.4	95662.3
349	122500	42875000	18.7083	7.0473	1099.6	96211.3
330	122300	420,3000		1.04/3	109910	
351	123201	43243551	18.7350	7.0540	1102.7	96761.8
352	123904	43614208	18.7617	7.0607	1105.8	97314.0
353	124609	43986977	18.7883	7.0674	1109.0	97867.7
354	125316	44361864	18.8149	7.0740	III2.I	98423.0
355	126025	44738875	18.8414	7.0807	1115.3	98979.8
356	126736	45118016	18,8680	7.0873	1118.4	99538.2
357	127449	45499293	18.8944	7.0940	1121.5	100098
358	128164	45882712	18.9209	7.1006	1124.7	100660
359	128881	46268279	18.9473	7.1072	1127.8	101223
360	129600	46656000	18.9737	7.1138	1131.0	101788
0		1.	1 2101	1, 1,	U	

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES

Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520

AND CIRCULAR AREAS OF INOS. FROM 1 10 520							
No.	Square	Cube	Sq. Root	Cube Root		CLE	
					Circum.	Area	
~							
361	130321	47045881	19.0000	7.1204	1134.1	102354	
362	131044	47437928	19.0263	7.1269	1137.3	102922	
363	131769	47832147	19.0526	7.1335	1140.4	103491	
364	1 32496	48228544	19.0788	7.1400	1143.5	104062	
365	133225	48627125	19.1050	7.1466	1146.7	104635	
366	133956	49027896	19.1311	7.1531	1149.8	105209	
367	133950	49430863	19.1311	7.1596			
368	134009	49430003	19.1572	7.1661	1153.0 1156.1	105785 106362	
			/ 00		ç		
369	136161	50243409	19.2094	7.1726	1159.2	106941	
370	136900	50653000	19.2354	7.1791	1162.4	107521	
371	137641	51064811	19.2614	7.1855	1165.5	108103	
372	1 38 384	51478848	19.2873	7.1920	1168.7	108687	
373	139129	51895117	19.3132	7.1984	1171.8	109272	
374	1 39876	52313624	19.3391	7.2048	1175.0	109858	
375	140625	52734375	19.3649	7.2112	1178.1	110447	
			-9-3-49	/		110447	
376	141376	53157376	19.3907	7.2177	1181.2	111036	
377	142129	53582633	19.4165	7.2240	1184.4	111628	
378	142884	54010152	19.4422	7.2304	1187.5	112221	
379	143641	54439939	19.4679	7.2368	1190.7	112815	
380	144400	54872000	19.4936	7.2432	1193.8	113411	
381	146161	## a06a.47	TO 5700	-			
382	145161	55306341	19.5192	7.2495	1196.9	114000	
382 383	145924	55742968 56181887	19.5448	7.2558	1200.1	114608	
303	146689		19.5704	7.2622	1203.2	115209	
384	147456	56623104	19.5959	7.2685	1206.4	115812	
385	148225	57066625	19.6214	7.2748	1209.5	116416	
386	148006	57512456	19.6469	7.2811	1212.7	117021	
387	149769	57960603	19.6723	7.2874	1215.8	117628	
388	150544	58411072	19.6977	7.29.36	1218.0	118237	
389	151321	58863869	19.7231	7.2999	1222.1	118847	
390	152100	59319000	19.7484	7.3061	1225.2	119459	
57	-			1.3001	1223.2	119459	
391	152881	59776471	19.7737	7.3124	1228.4	120072	
392	153664	60236288	19.7990	7.3186	1231.5	120687	
393	154449	60698457	19.8242	7.3248	1234.6	121304	
394	155236	61162984	19.8494	7.3310	1237.8	121922	
395	156025	61629875	19.8746	7.3372	1240.9	122542	
206	60 - 6	6					
396	156816	62099136	19.8997	7.3434	1244.1	123163	
397	157609	62570773	19.9249	7.3496	1247.2	123786	
398	158404	63044792	19.9499	7.3558	1250.4	124410	
399	159201	63521199	19.9750	7.3619	1253.5	125036	
400	160000	64000000	20.0000	7.3684	1256.6	125664	
	·						

Table 4.SQUARES, CUBES AND ROOTS.377

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		AND C	IRCULAR A	REAS OF I	VOS. FROM	4 I TO 520	2
No.SquareCureSq. KootCure KootCircum.Area4011608016448120120.0250 7.3742 1259.8126234021616046496480820.0499 7.3803 1262.9126923403162256643012520.1740 7.3925 1269.2128190405164256643012520.1740 7.3925 1273.31288254061648366692341620.1742 7.4047 1275.51294624071656496741914320.1742 7.4047 1275.51294624071664646791731220.1900 7.4169 1281.81307414091672816841792920.2237 7.4229 1288.1132025411168006892100020.2485 7.4290 1288.11332674121607446993452820.2978 7.4470 1297.51339654141713967095794420.3470 7.4530 1300.61346144151722257147337520.3715 7.4590 1303.813526541617305677199129620.3961 7.4650 1306.91399184171738897251171320.4266 7.4770 131.213257418174724735605920.4605 7.5077 1325.8139867422178084751544820.5163 7.5077 1325.8139867423178929756860720.50767.507 <td></td> <td></td> <td>0.1</td> <td>a p i</td> <td></td> <td>CIR</td> <td>CLE</td>			0.1	a p i		CIR	CLE
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	No.	Square	Cube	Sq. Koot	Cube Root	Circum.	
402 161604 64964808 20.0499 7.3803 1262.9 126923 403 162409 65450827 20.0749 7.3864 1266.1 127556 404 163216 65939264 20.0998 7.3925 1269.2 128825 405 164025 66430125 20.1246 7.3986 1272.3 128825 406 164836 66923416 20.1494 7.4047 1275.5 129462 407 165649 67419143 20.1494 7.4047 1275.5 129462 407 16781 68417929 20.2237 7.4229 1288.1 130741 409 167281 68417929 20.22485 7.4290 1288.1 132025 411 168100 68921000 20.2485 7.4290 1288.1 132025 411 176569 70944997 20.3224 7.4410 1294.3 13317 413 170569 70944997 20.3247 7.4530 1300.6 134614 415 172225 71473375 20.3715 7.4590 1303.8 135265 416 173056 71991296 20.3961 7.4650 1306.9 135918 417 173889 72511713 20.4206 7.4770 131.2 137228 419 175561 756567 20.6398 7.5007 1322.6 139265 420 176400 74688000 20.4939 7.4829 1316.3 137228 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	401	160801		20.0250	7.3742	1259.8	126293
404 163216 65939264 20.0998 7.3925 1269.2 128120 405 164025 66430125 20.1246 7.3986 1272.3 128825 406 164836 66923416 20.1494 7.4047 1275.5 129462 407 165649 67419143 20.1742 7.4108 1278.6 130100 408 166464 67917312 20.1990 7.4109 1281.8 130741 409 167816 68417929 20.2237 7.4290 1288.1 132025 411 168100 68921000 20.2485 7.4290 1288.1 132025 411 169744 69934528 20.2978 7.4410 1291.2 132670 112 169744 69934528 20.2978 7.4410 1297.5 13395 412 169744 69934528 20.2978 7.4470 1297.5 13395 413 170569 7044997 20.3224 7.4470 1297.5 13395 414 171306 70957944 20.3961 7.4650 1306.9 135918 417 173889 72511713 20.4206 7.4710 1310.0 135265 416 177926 73056059 20.3961 7.4650 1306.9 135918 417 173889 751713 20.4625 7.4770 1313.2 137228 419 175561 7356059 20.5426 7.5007 1325.8 130651 <	402			20.0499	7.3803	1262.9	126923
405 164025 66430125 20.1246 7.3986 1272.3 128825 406 164836 66923416 20.1494 7.4047 1275.5 129462 407 165649 67419143 20.1742 7.4108 1278.6 130100 408 166464 67917312 20.1900 7.4169 1281.8 130741 409 167281 68417929 20.2237 7.4229 1284.9 131382 410 16800 68921000 20.2485 7.4290 1288.1 132025 411 168921 69426531 20.2731 7.4350 1291.2 133965 412 169744 69934528 20.2978 7.4410 1294.3 133317 413 170569 7044997 20.3224 7.4470 1297.5 133965 414 171396 70957944 20.32747 7.4590 1300.6 134614 415 17225 71473375 20.3961 7.4650 1306.9 135918 417 173889 72511713 20.4206 7.4770 1313.2 137285 420 176400 74688000 20.4957 7.4829 1310.5 139265 416 177241 74618461 20.5183 7.4948 1322.6 139205 421 177241 74618461 20.5183 7.507 1325.8 139867 422 178929 75686967 20.5670 7.507 1325.8 139867 <td>403</td> <td></td> <td>65450827</td> <td>20.0749</td> <td> 7.3864 </td> <td>1266.1</td> <td>127556</td>	403		65450827	20.0749	7.3864	1266.1	127556
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	404		65939264	20.0998	7.3925	1269.2	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	405	164025	66430125	20.1246	7.3986	1272.3	128825
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	106	-6.0.6	660001-6				
408 166464 67917312 20.1990 7.4169 1281.8 130741 409 167281 68417929 20.2237 7.4229 1284.9 131382 410 168100 68921000 20.2485 7.4290 1288.1 132025 411 168921 69426531 20.2731 7.4350 1291.2 132670 412 169744 69934528 20.2978 7.4410 1294.3 133317 413 170569 7044997 20.3224 7.4470 1297.5 133965 414 171396 70957944 20.3470 7.4530 1300.6 134614 415 172225 71473375 20.3715 7.4590 1306.9 135918 417 173889 72511713 20.4206 7.4770 1313.2 137228 419 175561 7356059 20.4695 7.4829 1316.3 137885 420 176400 7468800 20.4939 7.4889 1319.5 138544 421 177241 74618461 20.5183 7.4948 1322.6 139205 423 178929 75686967 20.5970 7.5067 1328.9 140531 424 179776 76225024 20.5163 7.5185 1335.2 141863 425 180625 7675625 20.6155 7.5185 1335.2 141863 426 181476 77308776 20.6398 7.5244 1338.3 142531 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$							
410 168100 68921000 20.2485 7.4290 1288.1 132025 411 168921 69426531 20.2731 7.4350 1291.2 132670 412 169744 69934528 20.2978 7.4410 1294.3 133317 413 170569 70444997 20.3224 7.4470 1297.5 133065 414 171396 70957944 20.3224 7.4470 1297.5 133065 414 177366 70957944 20.3274 7.4450 130.6 134614 415 172225 71473375 20.3715 7.4590 130.3 135918 416 173056 71991296 20.3961 7.4650 1306.9 135918 417 173889 72511713 20.4266 7.4710 1313.2 137288 419 175561 7356059 20.4450 7.4700 1313.2 137288 420 176400 74088000 20.4939 7.4889 1310.5 138544 421 177241 74618461 20.5183 7.4948 1322.6 139205 422 178024 755572024 20.5970 7.5067 1332.9 140531 424 170776 76225024 20.5973 7.5126 1332.0 141196 425 180625 76765625 20.6398 7.5244 1338.3 142531 426 181476 77308776 20.6398 7.5420 1341.6 143872 423 18							
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4121697446993452820.29787.44101294.3133317413170569704499720.32247.44701297.51339654141713967095794420.32247.44701297.51339654151722257147337520.37157.45301300.61365724161730567199129620.39617.46501306.91359184171738897251171320.42067.47101310.01365724181747247303463220.44507.47701313.21372884201764007408800020.49397.48891310.3137885420176400746860720.51837.49481322.6139205422178847515144820.54207.50071325.81398674231789297568696720.56707.50671328.9140531424179776762502420.50137.51261332.01411664251806257676562520.61557.51851335.21418634261814767730877620.63987.52441338.31425314271823297785448320.64007.53021341.5143201428183184780275220.68827.53611344.61438724301849007950700020.73647.54781350.91452204311857618062156820.7237.55371354.014586 </td <td>410</td> <td>103100</td> <td>00921000</td> <td>20.2405</td> <td>7.4290</td> <td>1200.1</td> <td>132025</td>	410	103100	00921000	20.2405	7.4290	1200.1	132025
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	413	170569					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	414	171396		-			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	415	172225	71473375		7.4590	1303.8	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$							
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	420	170400	74088000	20.4939	7.4889	1319.5	138544
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	421	177241	74618461	20.5183	7.4048	1322.6	130205
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			75686067				
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	430	184900	79507000	20.7304	7.5478	1350.9	145220
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	121	185761	80062001	20.7605	7.5527	1254.0	145806
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437 190969 83453453 20.9045 7.5886 1372.9 149987 438 191844 84027672 20.9284 7.5944 1376.0 150674 439 192721 84604519 20.9523 7.6001 1379.2 151363	-55	1				1,000,0	
438 191844 84027672 20.9284 7.5944 1376.0 150674 439 192721 84604519 20.9523 7.6001 1379.2 151363				20.8806	7.5828		
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439 192721 84604519 20.9523 7.6001 1379.2 151363	438						
<u>440 193600 85184000 20.9762 7.6059 1382.3 152053</u>	439		84604519	20.9523			
	440	193600	85184000	20.9762	7.6059	1382.3	152053
		1	<u> </u>	1	1	<u> </u>	!

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES, AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

SQUARES, CUBES, SQUARE ROOTS, CUBE ROOTS, CIRCUMFERENCES AND CIRCULAR AREAS OF NOS. FROM 1 TO 520

			ALAS OF	NOS. FROM	······································	
No.	Square	Cube	Sq. Root	Cube Root		RCLE
					Circum.	Area
		8				
441	194481	85766121	21.0000	7.6117	1385.4	152745
442	195364	86350888	21.0238	7.6174	1388.6	153439
443	196249	86938307	21.0476	7.6232	1391.7	154134
444	197136	87528384	21.0713	7.6289	1394.9	154830
445	198025	88121125	21.0950	7.6346	1398.0	155528
4 46	198916	88716536	21.1187	7.6403	1401.2	156228
447	199809	89314623	21.1424	7.6460	1404.3	156930
448	200704	89915392	21.1660	7.6517	1407.4	157633
449	201601	90518849	21.1896	7.6574	1410.6	158337
450	202500	91125000	21.2132	7.6631	1413.7	159043
451	203401	91733851	21.2368	7.6688	1416.9	またの方だす
452	204304	92345408	21.2503	7.6744	1410.9	159751 160460
453	204304	92959677	21.2838	7.6801	1420.0	100400
454	200110	93576664	21.2030	7.6857	1423.1	101171
455	207025	93570004				161883
			21.3307	7.6914	1429.4	162597
€56	207936	94818816	21.3542	7.6970	1432.6	163313
457	208849	95443993	21.3776	7.7026	1435.7	164030
45 ⁸	209764	96071912	21.4009	7.7082	1438.9	164748
459	210681	96702579	21.4243	7.7138	1442.0	165468
460	211600	97336000	21.4476	7.7194	1445.1	166190
461	212521	97972181	21.4709	7.7250	1448.3	166914
462	213444	98611128	21.4042	7.7306	1451.4	167639
463	214369	99252847	21.5174	7.7362	1454.6	168365
464	215296	99897344	21.5407	7.7418	1457.7	169093
465	216225	100544625	21.5639	7.7473	1457.7	169823
					1400.0	109823
466	217156	101194696	21.5870	7.7529	1464.0	170554
467	218089	101847563	21.6102	7.7584	1467.1	171287
468	219024	102503232	21.6333	7.7639	1470.3	172021
469	219961	103161709	21.6564	7.7695	1473.4	172757
470	220900	103823000	21.6795	7.7750	1476.5	173494
471	221841	104487111	21.7025	7.7805	1479.7	174234
472	222784	105154048	21.7256	7.7860	1482.8	174234
473	223729	105823817	21.7486	7.7915	1486.0	175716
474	224676	106496424	21.7715	7.7970	1489.1	176460
475	225625	107171875	21.7945	7.8025	1409.1	
					1492.3	177205
476	226576	107850176	21.8174	7.8079	1495.4	177952
477	227529	108531333	21.8403	7.8134	1498.5	178701
478	228484	109215352	21.8632	7.8188	1501.7	179451
479	229441	109902239	21.8861	7.8243	1504.8	180203
480	230400	110592000	21.9089	7.8297	1508.0	180956
				<u> </u>		

Table 4.SQUARES, CUBES AND ROOTS.379

Squares, Cubes, Square Roots, Cube Roots, Circumferences and Circular Areas of Nos. from 1 to 520 =

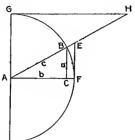
	AND C	IRCULAR A	REAS OF 1	NOS. FROM	4 1 10 52	<u> </u>
No.	Square	Cube	Sq. Root	Cube Root	Cir	CLE
140.	oquare	Cube	54. 1001	Cube Root	Circum.	Area
481	231361	111284641	21.9317	7.8352	1511.1	181711
482	232324	111980168	21.9545	7.8406	1514.3	182467
483	233289	112678587	21.9773	7.8460	1517.4	183225
484	234256	113379904	22.0000	7.8514	1520.5	183984
485	235225	114084125	22.0227 -	7.8568	1523.7	184745
-						- 0 0
486	236196	114791256	22.0454	7.8622	1526.8	185508
487	237169	115501303	22.0681	7.8676	1530.0	186272
488	238144	116214272	22.0907	7.8730	1533.1	187038
489	239121	116930169	22.1133	7.8784	1536.2	187805
490	240100	117649000	22.1359	7.8837	1539.4	188574
491	241081	118370771	22.1585	7.8801	1542.5	189345
492	242064	110005488	22.1811	7.8944	1545.7	190117
492	243049	119823157	22.2036	7.8998	1548.8	190890
	243049	120553784	22.2261	7.9051	1551.9	191665
494		121287375	22.2486	7.9105	1555.1	192442
495	245025	12120/3/3	22.2400	1.9103	193311	-9-44-
496	246016	122023936	22.2711	7.9158	1558.2	193221
497	247009	122763473	22.2935	7.9211	1561.4	194000
498	248004	123505992	22.3159	7.9264	1564.5	194782
499	240001	124251499	22.3383	7.9317	1567.7	195565
500	250000	125000000		7.9370	1570.8	196350
•		1				107126
501	251001	125751501		7.9423	1573.9	197136
502	252004	1 26506008		7.9476	1577.1	197923
503	253009	1 27 263 5 27		7.9528	1580.2	198713
504	254016	128024064		7.9581	1583.4	199504
5 °5	255025	128787625	22.4722	7.9634	1586.5	200290
506	256036	1 29554216	22.4944	7.9686	1589.7	201090
507	257049	130323843		7.9739	1592.8	201886
508	258064			7.9791	1595.9	202683
509	259081	131872229		7.9843	1599.1	203482
510	260100			7.9896	1602.2	204282
5		1		1		
511	261121	133432831	22.6053	7.9948	1605.4	205084
512	262144			8.0000	1608.5	205887
513	263169			8.0052	1611.6	206692
514	264196		22.6716	8.0104	1614.8	207499
515	265225	136590875	22.6936	8.0156	1617.9	208307
516	266256	137388096	22.7156	8.0208	1621.1	209117
517	267 289		22.7376	8.0260	1624.2	209928
518	268324			8.0311	1627.3	210741
510	260324			8.0363	1630.5	211556
520	270400		22.8035	8.0415	1633.6	212372
520	1 2/0400	1-4000000				}

380 TRIGONOMETRIC FUNCTIONS.

TABLE 5. TRIGONOMETRIC FUNCTIONS AND THE SOLUTION OF TRIANGLES

In the accompanying figure the trigonometric functions of the angle Abetween the lines B A and A C are as follows;

> $\sin A = B C$ $\cos A = A C$ $\tan A = E F$ $\cot A = G H$ $\sec A = A E$ $\csc A = A H$ ex-sec A = B E



In the right-angled triangle A B Clet a equal the side B C opposite the

angle A; let b equal the side A C opposite the angle B; let c equal A B, the side opposite the angle C.

Let $C = 90^{\circ}$

The following formulæ apply to right-angled triangles:

Angles.
$$A + B + C = 180^{\circ} \qquad Sides. \qquad a = c \sin A = b \tan A$$
$$A + B = 90^{\circ} \qquad a = \sqrt{(c+b)(c-b)}$$
$$A = 90^{\circ} - B$$
$$B = 90^{\circ} - A \qquad b = c \cos A = \frac{a}{\tan A}$$
$$\sin A = \frac{a}{c} \qquad Area \qquad area = \frac{a}{b} \qquad c = \frac{a}{\sin A} = \frac{b}{\cos A}$$
$$c = \sqrt{a^2 + b^2}$$

Oblique Triangles.

Note. Where an angle is more than 90° its sine, cosine, and tangent are equal to that of the angle (180° - the angle in question); that is, if the sine of 120° is desired take the sine of ($180^{\circ} - 120^{\circ}$) = 60° .

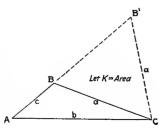


Table 5.TRIGONOMETRIC TABLES.

Given	Desired	Formulæ
A, B, a	С, в	$C = 180 - (A + B); \ b = \frac{a}{\sin A} \sin B$
	c, K	$c = \frac{a}{\sin A} \sin (A + B); K = \frac{a^2 \sin B \sin C}{2 \sin A}$
A, a, b	В, С	$\sin B = \frac{\sin A}{a} b; C = 180^{\circ} - (A + B)$
	с	$c=\frac{a}{\sin A}\sin C$
		Two solutions are possible with B' as an acute angle and B as an obtuse angle
C, a, b	$\frac{1}{2}(A+B)$	$\frac{1}{2}(A+B) = 90^\circ - \frac{1}{2}C$
	$\frac{1}{2}(A-B)$	$\tan \frac{1}{2}(A-B) = \frac{a-b}{a+b} \tan \frac{1}{2}(A+B)$
	A B	$A = \frac{1}{2} (A + B) + \frac{1}{2} (A - B)$
		$B = \frac{1}{2} (A + B) - \frac{1}{2} (A - B)$ sin $\frac{1}{2} (A + B)$
	с	$c = (a - b) \frac{\sin \frac{1}{2} (A + B)}{\sin \frac{1}{2} (A - B)}$
	K	$K = \frac{1}{2} ab \sin C$
a, b , c	В	In the following formula $s = \frac{1}{2} (a + b + c)$
		$\sin \frac{1}{2} B = \sqrt{\frac{(s-a)(s-c)}{ac}}.$
		$\sin B = \frac{2\sqrt{s(s-a)(s-b)(s-c)}}{ac}$
	K	$K = \sqrt{s(s-a)(s-b)(s-c)}$

EXPLANATION OF TABLES.

TABLE I. LOGARITHMS OF NUMBERS.—The logarithm of any number to any base is the index of the power to which the base must be raised to equal the number. The logarithms given in Table I are Briggs or Common Logarithms in which the base is 10. Then $100 = 10^2$, and the logarithm of 100 = 2. Also $200 = 10^{2.30103}$, and the logarithm of 200 = 2.30103. The integer of a logarithm is called the *characteristic*, and is one less than the number of integers in the number. The decimal part of the logarithm is called the *mantissa* and is given in Table I.

The mantissae of the logarithms in Table I are given to five places; while the numbers are given to four significant figures. Where there are more than four significant figures in the number, the table of proportional parts may be used. The star opposite certain logarithms shows that the two figures at the left are to be taken from the line below.

The logarithm of 1 is 0, and the logarithm of any number less than unity will be negative. It is much more convenient to use positive mantissae, and logarithms of numbers less than unity are written as cologarithms or modified logarithms in which the negative logarithm is subtracted from a positive integer as 10, 20, etc., 100, 200, etc.; and the cologarithm or modified logarithm is written as a positive logarithm with the integer shown as subtracted from the logarithm. For example the logarithm of 0.2 =logarithm of $\frac{1}{5} = \log_{10} 1 - \log_{10} 5 = 0.00000 - 0.69893 =$ The cologarithm or modified logarithm will be ---0.69893. equal to the logarithm subtracted from 10 and is written 9.30103 - 10. The logarithm of $.00625 = \log 5_{000} = \log 5$ 800 = 0.69897 - 2.90309 = -2.20412, or as a colog- $-\log$. arithm or modified logarithm = 7.79588 - 10. The mantissae of the cologarithms of numbers less than unity are given in Table I.

The following rules should be kept in mind in using the table of logarithms. 1. The logarithm of a product is the sum of the logarithms of the factors.

2. The logarithm of a quotient is the difference of the logarithms of the dividend and divisor.

3. The logarithm of a power of a number is equal to the logarithm of the number multiplied by the index of the power.

4. The logarithm of a root of a number is equal to the logarithm of the number divided by the index of the root.

5. The logarithm of a fraction is equal to the logarithm of the numerator minus the logarithm of the denominator.

6. In dividing modified logarithms add a number to the positive and negative characteristics so that the resulting logarithm will have -10 following the logarithm. For example if 8.36748 - 10 is to be divided by 3, the logarithm should he written 29.36748 - 30; and dividing by 3 we have 9.45583 - 10.

Reverse the operation when multiplying modified logarithms.

7. The characteristic of the logarithm of an integer is always one less than the number of digits in the integral part of the number.

8. The characteristic of the cologarithm of a number less than unity (a decimal) is equal to 10 minus the number of the place to the right of the decimal point occupied by the first significant figure.

TABLE II. LOGARITHMIC FUNCTIONS OF ANGLES.

--To avoid the use of negative characteristics the logarithms of the functions of angles are written as cologarithms, 10 being added to the characteristic of each logarithm. In adding the logarithms of the functions of angles the correct number of tens should be subtracted from the result.

For angles from 0° to 45° and from 135° to 180° the headings at the tops of the columns are to be used; while from 45° to 90° and from 90° to 135° the headings at the bottoms of the columns are to be used; the minutes being read from the top down on the left of the page, and from the bottom up on the right of the page.

In using the logarithmic functions of angles in connection with logarithms of numbers it should be remembered that the logarithmic functions of angles are cologarithms and that 10 should be subtracted from each logarithmic function. TABLE III. NATURAL FUNCTIONS OF ANGLES.— For angles from 0° to 45° and from 135° to 180° the headings at the tops of the columns are to be used; while from 45° to 90° and from 90° to 135° the headings at the bottoms of the columns are to be used; the minutes being read from the top down on the left of the page and from the bottom up on the right of the page.

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Decorum, Field practice.	2
	$\overline{2}$
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Instructions, Familiarity	
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